

# TX Diversity with Array-Interference Gain

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# Abstract

- **The objective the transmit (TX) diversity with array interference gain is to provide better link reliability than conventional techniques such as orthogonal space-time block codes (O-STBCs) [1]. Such scheme could be used to improve coverage area of IEEE 802.22b.**
- **Improvement over O-STBCs [1] comes from exploiting the energy contained in the MIMO array-interference.**
- **This can be achieved by designing the transmit vector in a way that interference is always constructive at the decoder side.**
- **We provide simulation results indicating significant performance improvements as compared to existing techniques.**

# Alamouti [2] – 2TX

$$\mathbf{s} = \begin{bmatrix} s_1 \\ s_2 \end{bmatrix} \quad \mathcal{G}_2(\mathbf{s}) = \begin{bmatrix} s_1 & s_2 \\ -s_2^* & s_1^* \end{bmatrix} \quad \mathbf{h} = \begin{bmatrix} h_1 \\ h_2 \end{bmatrix} \quad \mathbf{w} = \begin{bmatrix} n_1 \\ n_2 \end{bmatrix}$$

$$\mathbf{r} = \begin{bmatrix} r_1 \\ r_2 \end{bmatrix} = \mathcal{G}_2 \cdot \mathbf{h} + \mathbf{w} \quad \text{(Received Open-Loop Alamouti signal)}$$

By doing the proper combination with “r” (skipped here for simplicity), the estimated symbol vector is:

$$\hat{\mathbf{s}} = \mathbf{D} \cdot \mathbf{s} + \bar{\mathbf{w}} = \begin{bmatrix} |h_1|^2 + |h_2|^2 & 0 \\ 0 & |h_1|^2 + |h_2|^2 \end{bmatrix} \cdot \begin{bmatrix} s_1 \\ s_2 \end{bmatrix} + \begin{bmatrix} \bar{w}_1 \\ \bar{w}_2 \end{bmatrix}$$

Diversity factor No Interference (Orthogonal)  
No Interference (Orthogonal) Diversity factor

# Generating Interference by Spanning Alamouti over 4 TX antennas

$$\mathcal{G}_4(\mathbf{s}) = \begin{bmatrix} \boxed{\begin{matrix} s_1 & s_2 \\ -s_2^* & s_1^* \\ \text{Alamouti} \end{matrix}} & \boxed{\begin{matrix} s_1 & s_2 \\ -s_2^* & s_1^* \\ \text{Alamouti} \end{matrix}} \end{bmatrix} \quad \mathbf{h} = \begin{bmatrix} h_1 \\ h_2 \\ h_3 \\ h_4 \end{bmatrix} \quad \mathbf{w} = \begin{bmatrix} w_1 \\ w_2 \end{bmatrix}$$

$$\mathbf{r} = \begin{bmatrix} r_1 \\ r_2 \end{bmatrix} = \mathcal{G}_4 \cdot \mathbf{h} + \mathbf{w}$$

By doing the proper combination with “r” (skipped here for simplicity), the estimated symbol vector is:

Same Diversity factor of 4TX STBC + generated interference

Orthogonal

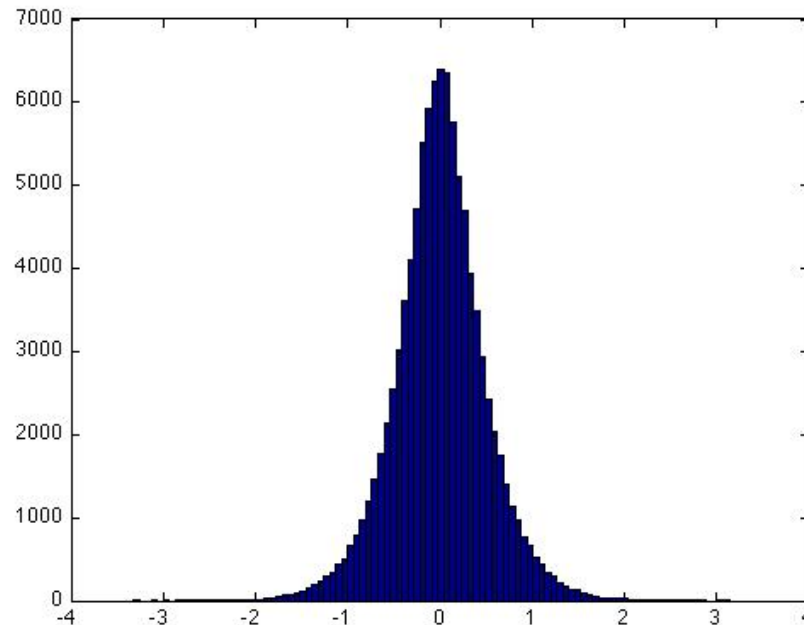
$$\hat{\mathbf{s}} = \mathbf{D} \cdot \mathbf{s} + \bar{\mathbf{w}} = \begin{bmatrix} \boxed{\begin{matrix} |h_1|^2 + |h_2|^2 + |h_3|^2 + |h_4|^2 \\ -(h_1^* h_3 + h_1 h_3^* + h_2^* h_4 + h_2 h_4^*) \end{matrix}} & \boxed{0} \\ \boxed{0} & \boxed{\begin{matrix} |h_1|^2 + |h_2|^2 + |h_3|^2 + |h_4|^2 \\ -(h_1^* h_3 + h_1 h_3^* + h_2^* h_4 + h_2 h_4^*) \end{matrix}} \end{bmatrix} \cdot \begin{bmatrix} s_1 \\ s_2 \end{bmatrix} + \begin{bmatrix} \bar{w}_1 \\ \bar{w}_2 \end{bmatrix}$$

Orthogonal

Same Diversity factor of 4TX STBC + generated interference

# Generating Interference by Spanning Alamouti over 4 TX antennas

- The problem is that the generated interference bellow  
 $-(h_1^* h_3 + h_1 h_3^* + h_2^* h_4 + h_2 h_4^*) = -(2\text{Re}\{h_1 h_3 + h_2 h_4\})$   
assumes “positives” and “negative” values with the same probability due  
to its pdf being:

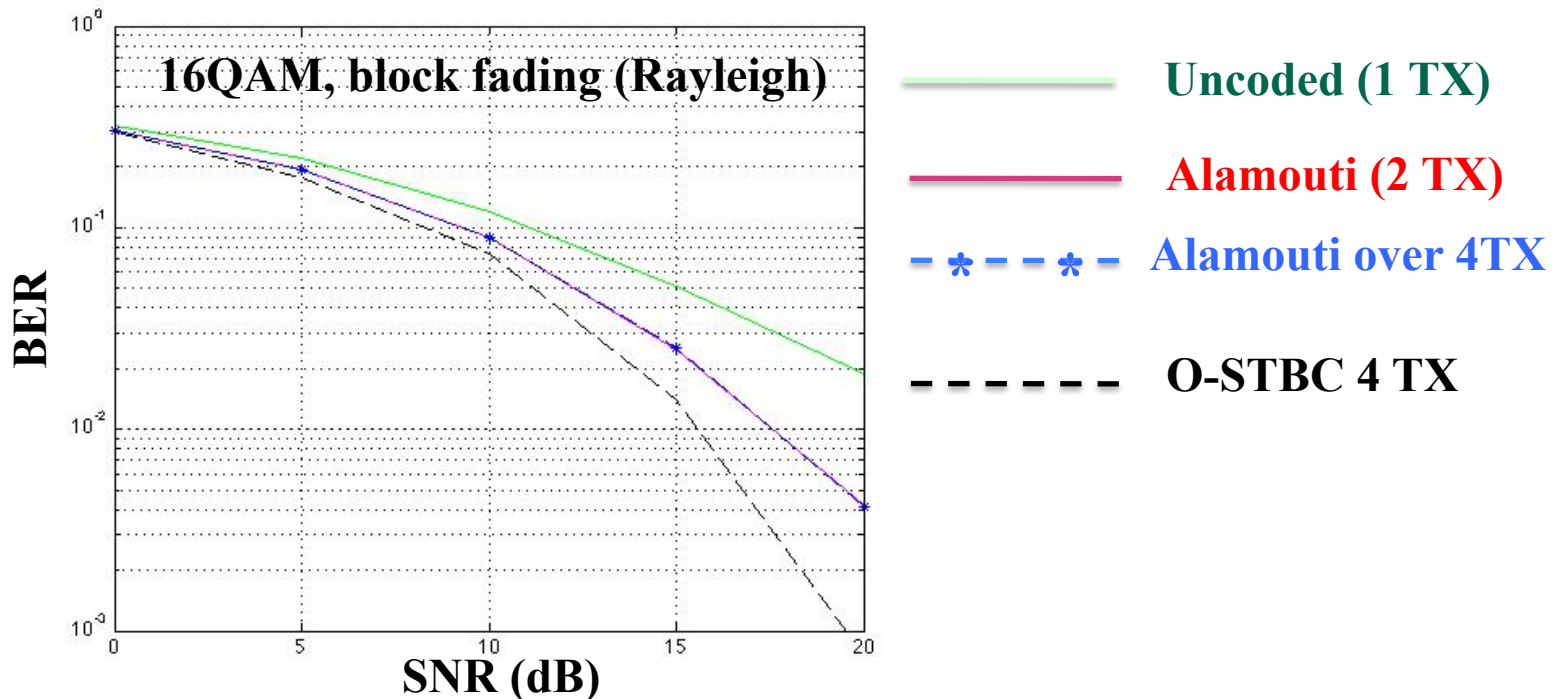


# Generating Interference by Spanning Alamouti over 4 TX antennas

- The interference causes the diversity gain bellow (which is always “positive”) to sometimes increase and reduce its value.

$$|h_1|^2 + |h_2|^2 + |h_3|^2 + |h_4|^2$$

- The resultant is a final diversity similar to open loop Alamouti.



# Alamouti with Array-Interference Gain (4 TX Antennas)

- Since the interference is composed by channel values, and the receiver (RX) can estimate the channel with a high precision, the receiver knows when the interference is being “constructive” or “destructive”.
- The idea is to make the interference **ALWAYS constructive** (positive). In order to do it, we have to manipulate the transmit scheme in the following manner:

$$\bar{\mathcal{G}}_4(\mathbf{s}) = \begin{bmatrix} s_1 & s_2 & s_1 & s_2 \\ -s_2^* & s_1^* & -s_2^* & s_1^* \end{bmatrix} \quad \text{Whenever interference is “+”}$$

$$\bar{\bar{\mathcal{G}}}_4(\mathbf{s}) = \begin{bmatrix} s_1 & s_2 & -s_1 & -s_2 \\ -s_2^* & s_1^* & s_2^* & -s_1^* \end{bmatrix} \quad \text{Whenever interference is “-”}$$

# Alamouti with Array-Interference Gain (4 TX Antennas)

- Since 802.22b system supports TDD, both TX and RX obtain CSI due to channel reciprocity.
- By doing the necessary manipulations with the received signal (skipped here for the sake of simplicity), the estimated symbol vector is given by:

**Diversity factor + absolute value of interference**

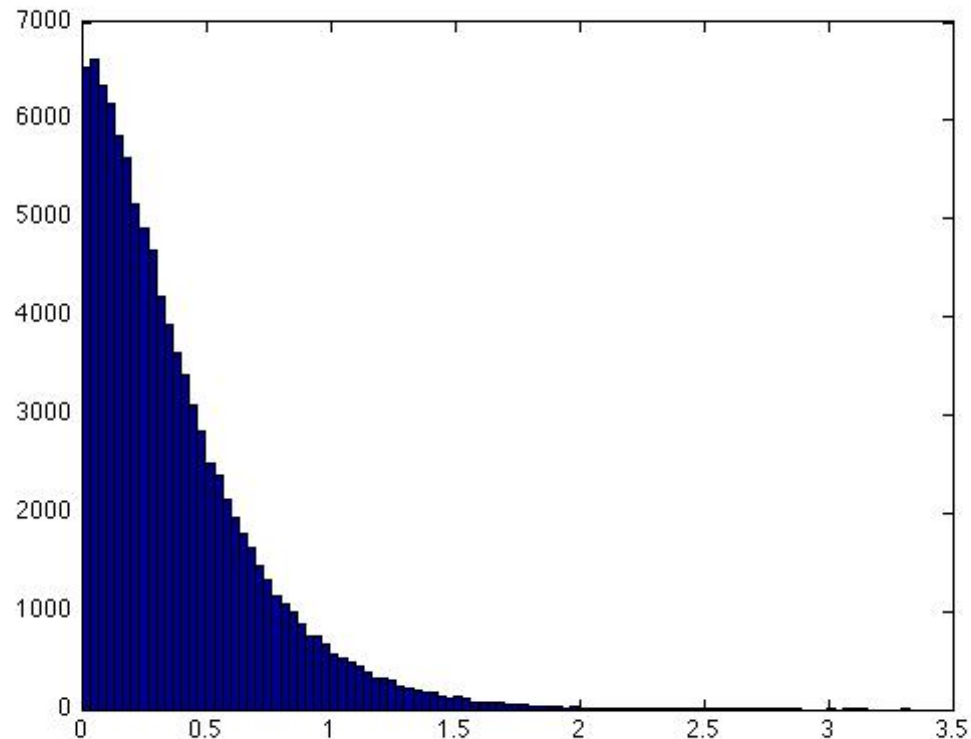
$$\hat{\mathbf{s}} = \mathbf{D} \cdot \mathbf{s} + \bar{\mathbf{w}} = \begin{bmatrix} |h_1|^2 + |h_2|^2 + |h_3|^2 + |h_4|^2 + \text{abs}(h_1^* h_3 + h_1 h_3^* + h_2^* h_4 + h_2 h_4^*) & 0 \\ 0 & |h_1|^2 + |h_2|^2 + |h_3|^2 + |h_4|^2 + \text{abs}(h_1^* h_3 + h_1 h_3^* + h_2^* h_4 + h_2 h_4^*) \end{bmatrix} \cdot \begin{bmatrix} s_1 \\ s_2 \end{bmatrix} + \begin{bmatrix} \bar{w}_1 \\ \bar{w}_2 \end{bmatrix}$$

**Diversity factor + absolute value of interference**



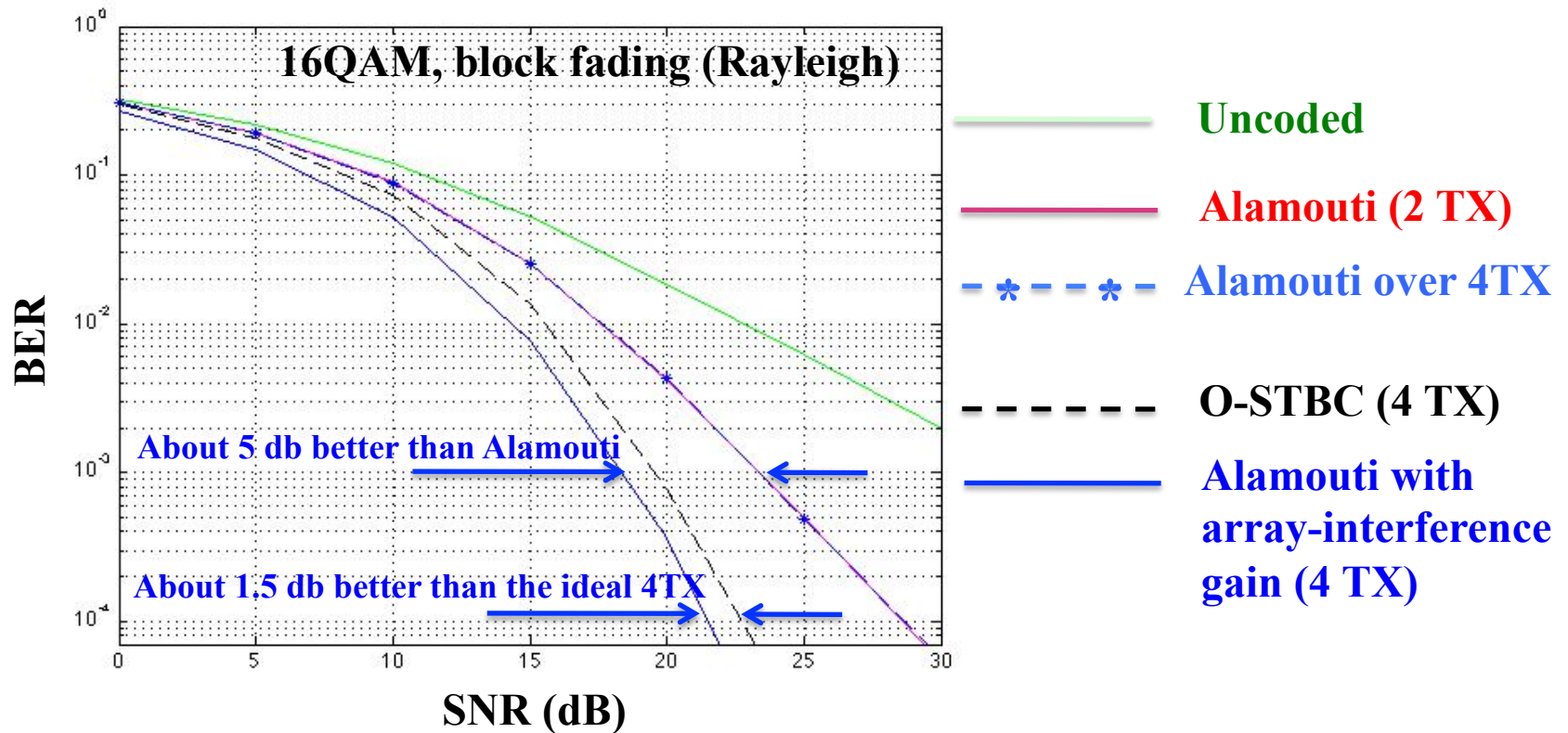
# Alamouti with Array-Interference Gain (4 TX Antennas)

- The interference is always constructive (positive) owing to the fact that choosing the proper transmit matrix, the interference pdf becomes:



# Alamouti with Array-Interference Gain

- BER performance



# Creating Further Interference Over 4TX Antennas

- In fact, Alamouti [2] is not the best scheme to span over TX antennas. The best scheme should be the one that generates more interference, so we can align then to increase the overall gain.
- In order to generate more interference, it is necessary to span a single symbol “s” over the TX antennas and do the proper received signal manipulation (skipped here for simplicity).
- Following the same line of thought, generate all possible dissimilar TX matrices:

$$\mathcal{G}_{4_1} = \begin{bmatrix} s & s & s & s \end{bmatrix}$$

$$\mathcal{G}_{4_2} = \begin{bmatrix} s & -s & s & -s \end{bmatrix}$$

$$\mathcal{G}_{4_3} = \begin{bmatrix} s & s & -s & -s \end{bmatrix}$$

$$\mathcal{G}_{4_4} = \begin{bmatrix} s & -s & -s & s \end{bmatrix}$$

$$\mathcal{G}_{4_5} = \begin{bmatrix} s & s & s & -s \end{bmatrix}$$

$$\mathcal{G}_{4_6} = \begin{bmatrix} s & s & -s & s \end{bmatrix}$$

$$\mathcal{G}_{4_7} = \begin{bmatrix} s & -s & s & s \end{bmatrix}$$

$$\mathcal{G}_{4_8} = \begin{bmatrix} -s & s & s & s \end{bmatrix}$$

# Creating Further Interference Over 4TX Antennas

- After doing the necessary manipulation (skipped for simplicity), each TX vector yields a specific estimated symbol:

$$\textcircled{1} \mathcal{G}_{4_1} = \begin{bmatrix} s & s & s & s \end{bmatrix}$$

$$\hat{s} = \begin{bmatrix} |h_1|^2 + |h_2|^2 + |h_3|^2 + |h_4|^2 \\ \underline{(h_1^*h_2 + h_1h_2^* + h_1^*h_3 + h_1h_3^* + h_1^*h_4 + h_1h_4^* + h_2^*h_3 + h_2h_3^* + h_2^*h_4 + h_2h_4^* + h_3^*h_4 + h_3h_4^*)} \end{bmatrix} \cdot [s] + [\bar{w}]$$

**Interference (I<sub>1</sub>)**

$$\textcircled{2} \mathcal{G}_{4_2} = \begin{bmatrix} s & -s & s & -s \end{bmatrix}$$

$$\hat{s} = \begin{bmatrix} |h_1|^2 + |h_2|^2 + |h_3|^2 + |h_4|^2 \\ \underline{(-h_1^*h_2 - h_1h_2^* + h_1^*h_3 + h_1h_3^* - h_1^*h_4 - h_1h_4^* - h_2^*h_3 - h_2h_3^* + h_2^*h_4 + h_2h_4^* - h_3^*h_4 - h_3h_4^*)} \end{bmatrix} \cdot [s] + [\bar{w}]$$

**Interference (I<sub>2</sub>)**

$$\textcircled{3} \mathcal{G}_{4_3} = \begin{bmatrix} s & s & -s & -s \end{bmatrix}$$

$$\hat{s} = \begin{bmatrix} |h_1|^2 + |h_2|^2 + |h_3|^2 + |h_4|^2 \\ \underline{(h_1^*h_2 + h_1h_2^* - h_1^*h_3 - h_1h_3^* - h_1^*h_4 - h_1h_4^* - h_2^*h_3 - h_2h_3^* - h_2^*h_4 - h_2h_4^* + h_3^*h_4 + h_3h_4^*)} \end{bmatrix} \cdot [s] + [\bar{w}]$$

**Interference (I<sub>3</sub>)**

# Creating Further Interference Over 4TX Antennas

$$\mathcal{G}_{44} = \begin{bmatrix} s & -s & -s & s \end{bmatrix}$$

$$\hat{\mathbf{s}} = \begin{bmatrix} |h_1|^2 + |h_2|^2 + |h_3|^2 + |h_4|^2 \\ \underline{(-h_1^*h_2 - h_1h_2^* - h_1^*h_3 - h_1h_3^* + h_1^*h_4 + h_1h_4^* + h_2^*h_3 + h_2h_3^* - h_2^*h_4 - h_2h_4^* - h_3^*h_4 - h_3h_4^*)} \end{bmatrix} \cdot [s] + [\bar{w}]$$

**Interference (I<sub>4</sub>)**

$$\mathcal{G}_{45} = \begin{bmatrix} s & s & s & -s \end{bmatrix}$$

$$\hat{\mathbf{s}} = \begin{bmatrix} |h_1|^2 + |h_2|^2 + |h_3|^2 + |h_4|^2 \\ \underline{(h_1^*h_2 + h_1h_2^* + h_1^*h_3 + h_1h_3^* - h_1^*h_4 - h_1h_4^* + h_2^*h_3 + h_2h_3^* - h_2^*h_4 - h_2h_4^* - h_3^*h_4 - h_3h_4^*)} \end{bmatrix} \cdot [s] + [\bar{w}]$$

**Interference (I<sub>5</sub>)**

$$\mathcal{G}_{46} = \begin{bmatrix} s & s & -s & s \end{bmatrix}$$

$$\hat{\mathbf{s}} = \begin{bmatrix} |h_1|^2 + |h_2|^2 + |h_3|^2 + |h_4|^2 \\ \underline{(h_1^*h_2 + h_1h_2^* - h_1^*h_3 - h_1h_3^* + h_1^*h_4 + h_1h_4^* - h_2^*h_3 - h_2h_3^* + h_2^*h_4 + h_2h_4^* - h_3^*h_4 - h_3h_4^*)} \end{bmatrix} \cdot [s] + [\bar{w}]$$

**Interference (I<sub>6</sub>)**

# Creating Further Interference Over 4TX Antennas

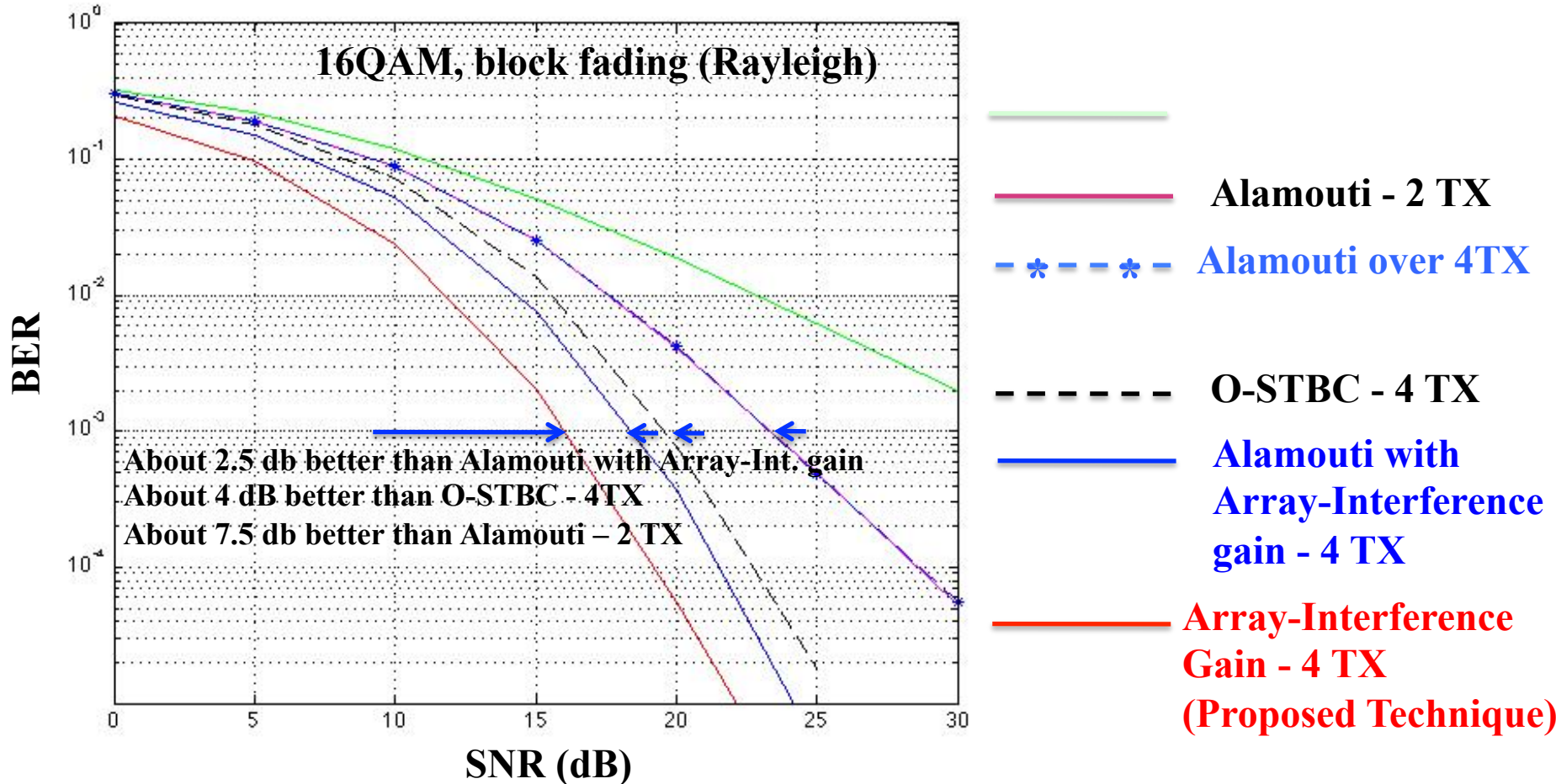
$$\hat{\mathbf{s}} = \begin{bmatrix} \mathcal{G}_{47} \\ |h_1|^2 + |h_2|^2 + |h_3|^2 + |h_4|^2 \\ \hline (-h_1^*h_2 - h_1h_2^* + h_1^*h_3 + h_1h_3^* + h_1^*h_4 + h_1h_4^* - h_2^*h_3 - h_2h_3^* - h_2^*h_4 - h_2h_4^* + h_3^*h_4 + h_3h_4^*) \end{bmatrix} \cdot [s] + [\bar{w}]$$

**Interference (I<sub>7</sub>)**

$$\hat{\mathbf{s}} = \begin{bmatrix} \mathcal{G}_{48} \\ |h_1|^2 + |h_2|^2 + |h_3|^2 + |h_4|^2 \\ \hline (-h_1^*h_2 - h_1h_2^* - h_1^*h_3 - h_1h_3^* - h_1^*h_4 - h_1h_4^* + h_2^*h_3 + h_2h_3^* + h_2^*h_4 + h_2h_4^* + h_3^*h_4 + h_3h_4^*) \end{bmatrix} \cdot [s] + [\bar{w}]$$

**Interference (I<sub>8</sub>)**

# Creating Further Interference Over 4TX Antennas



# Conclusions

- **Improved link reliability compared to the one of existing techniques can be earned by wisely exploiting the MIMO array interference. A natural consequence of utilizing such scheme is to increase of coverage area in IEEE 802.22b.**
- **The proposed scheme is full rate and full diversity + array interference gain, which results in improved link reliability even if compared to ideal 4TX antennas STBC.**
- **The proposed schemes makes use of the channel reciprocity inherent to TDD systems to as to estimate CSI and then design the transmit vector which yields the best constructive interference.**



# References

- [1] V. Tarok, H. Jafarkhani. and A.R. Calderbank, "Space-time block codes from orthogonal designs," *IEEE Trans. on Information Theory*, vol. 45. no. 5. pp. 1456-1467, July 1999
- [2] S.M. Alamouti. "A simple Transmitter diversity scheme for wireless communications," *IEEE Journal on Selected Areas in Communications*, vol. SAC-16, pp. 1451-1458, October 1998.