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# Starting Large AC Motors

For

IEEE Houston Section – CED Seminar

By:

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## **Synopsis:**

Review induction and synchronous motor operation and effect on starting method selection. Equivalent circuit for start and operation. Reviews starting techniques for AC motors: direct-on-line, captive transformer, autotransformer, capacitor start, wye-delta, solid-state soft start, Adjustable Drive System (ASD), "pony driver" starting, and adjustable V/f isolated bus starting. Starting method selection (limited power and other restrictions).

## Agenda

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- **Preliminaries**
- **Motor Fundamental**
- **Induction Motor**  
Construction, basics, characteristics, and modeling
- **Synchronous Motor**  
Construction, basics, characteristics, and modeling
- **Mechanical and Train Related Items**  
Load characteristics, Inertia, Torque Consideration, Train  
Acceleration Time, Process Consideration, Protection Consideration
- **Starting Techniques**  
Induction and Synchronous Motor, Synchronous Motor Only, Special
- **Calculations and Data Considerations**

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## Preliminaries

## Preliminaries

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During seminar, we will provide background and examples to answer following two questions:

How to start motor?

When motor is considered large for starting?

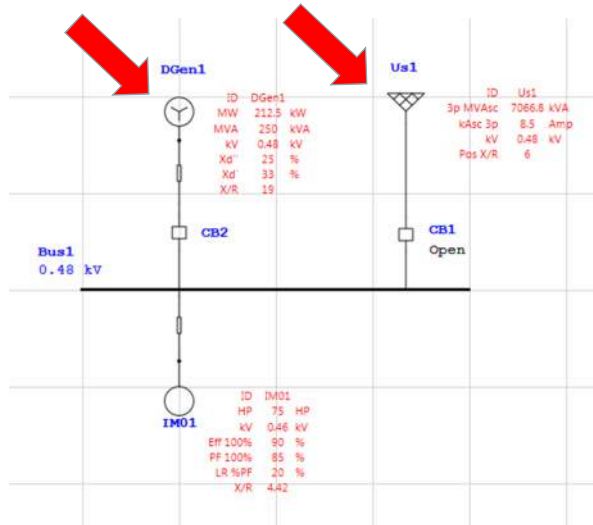
How to get data?

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**Something to think about...**

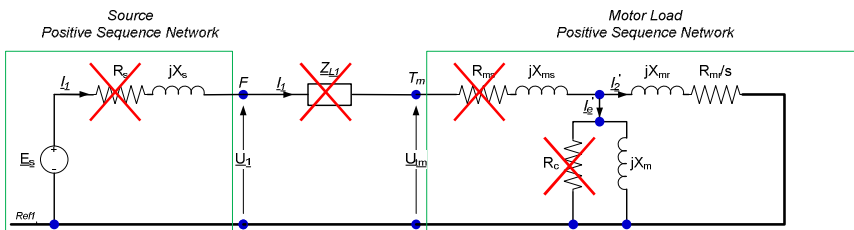
## Preliminaries

Typical motor starting circuit for IM.



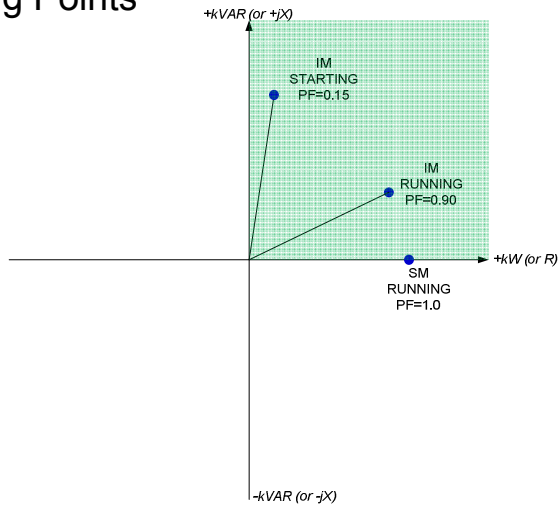
## Preliminaries

- Equivalent circuit for IM connected to Utility



## Preliminaries

### ■ Operating Points



## Preliminaries

### Condition 1:

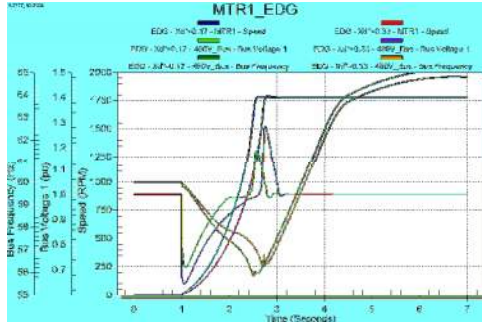
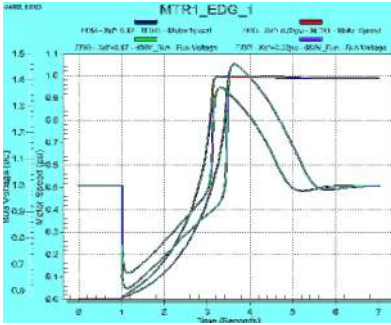
Typical diesel engine with “standard” synchronous generator (SG)  $X''$ ,  $X'$

### Condition 2:

SG is Low Voltage Transient (LVT) type with “adjusted”  $X'$

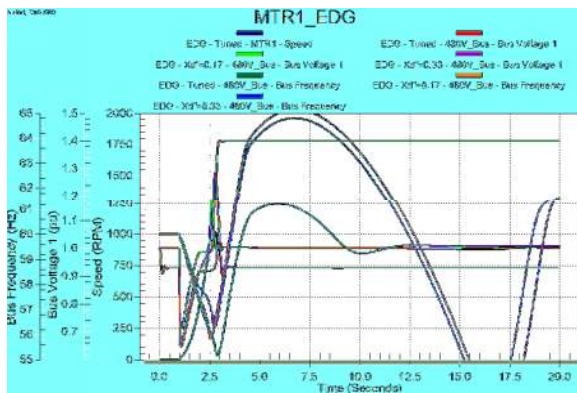
# Preliminaries

- Calculations



# Preliminaries

- Calculations



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## **Motor Fundamentals**

### **Motor Fundamentals**

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- Large motor definition
- Stator and Rotor Construction
- Insulation and Temperature Rise
- Mechanical/Torque Consideration
- Driver Selection IM/SM

## Motor Fundamentals

- Small Machine (Fractional) – in general for O&G, continues rating  $\leq 1$  Hp
  
- Medium Machine (Integral) - in general for O&G,  $< 500$ Hp ( $n_s=3600, 1800, 1200$ rpm) etc.
  
- Large Machine – Larger than Medium Machine size/synchronous speed

## Motor Fundamentals

- Insulation and Temperature Rise

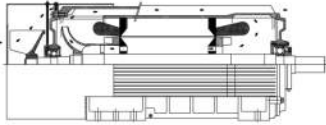
### Temperature Rise from 40°C

Machine Part	Method OF Temperature Determination	Temperature Rise [°C]							
		Class of Insulation System							
		A $T_{max}=105$		B $T_{max}=130$		F $T_{max}=155$		H $T_{max}=180$	
SF=1.0	SF=1.15	SF=1.0	SF=1.15	SF=1.0	SF=1.15	SF=1.0	SF=1.15		
Insulated Windings									
1. All power ratings	Resistance	60	70	80	90	105	115	125	135
2. 1500Hp or less	Embedded detector	70	80	90	100	115	125	140	150
3. Over 1500Hp (1120kW)									
3.a. $\leq 7000$ V	Embedded detector	65	75	85	95	110	120	135	145
3.b. $> 7000$ V	Embedded detector	60	70	80	90	105	115	125	135
Notes:									
1. Embedded detectors are located within the slot of the machine and can be either resistance elements or thermocouples. For machines equipped with embedded detectors, this method shall be used to demonstrate conformity with the standard.									
2. The temperatures attained by cores, squirrel-cage windings, collector rings, and miscellaneous parts (such as brushholders and brushes, etc.) shall not injure the insulation or the machine in any respect.									
3. For successful operation of induction machines in ambient temperatures higher than 40°C, the temperature rises of the machines given in above table shall be reduced by the number of degrees that the ambient temperature exceeds 40°C. Exceptions apply to TEWAC and TEAAC machines, see current MG-1.									
4. Table is based on assumption that well designed motor, the hot spot temperature is approximately 10°C higher than the average winding temperature.									
5. Class A insulation is obsolete. No longer used.									

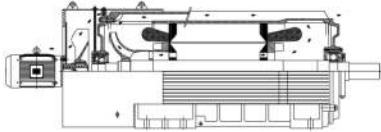


# Motor Fundamentals

## ■ Induction Motor - Cooling



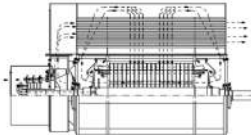
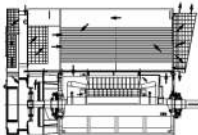
- Totally Enclosed
- Self-cooled
- IC411 (TEFC)
- IP55(W) / IP56(W) / IP65(W)



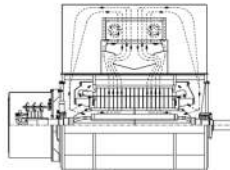
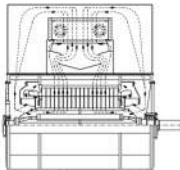
- Totally enclosed
- Forced cooling
- IC416 (TEBV)
- IP55(W) / IP56(W) / IP65(W)

# Motor Fundamentals

## ■ Induction Motor - Cooling



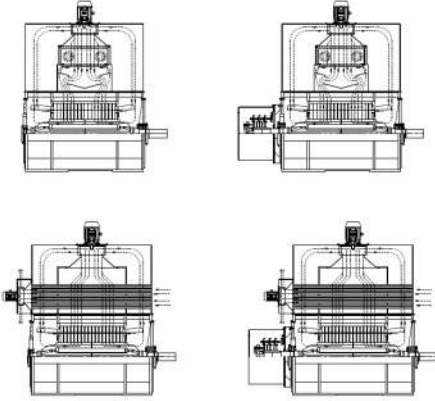
- Totally enclosed
- Air-to-air heat exchanger
- IC611 (TEAAC)
- IP55(W) / IP56(W) / IP65(W)
- MGF, MAF



- Totally enclosed
- Air-to-water heat exchanger
- IC81W (TEWAC)
- IP55(W) / IP56(W) / IP65(W)
- MGW, MAW

## Motor Fundamentals

### ■ Induction Motor - Cooling

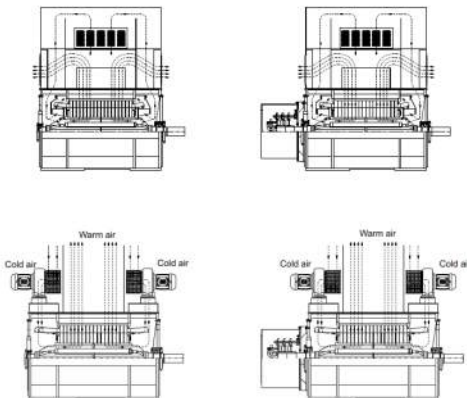


- Totally enclosed
- Independent cooling
- Air-to-water heat exchanger
- IC86W (TEWAC)
- IP55(W) / IP56(W) / IP65(W)
- MGL, MAL

- Totally enclosed
- Independent cooling
- Air-to-air heat exchanger
- IC666 (TEAAC)
- IP55(W) / IP56(W) / IP65(W)
- MGI, MAI

## Motor Fundamentals

### ■ Induction Motor - Cooling



- Open (Self-cooled)
- IC01 (ODP)
- IP23 (WP-I)
- IP24(W) (WP-II)
- MGA, MAA, MGP, MAP

- Open
- Independent cooling
- IC06 (OIV)
- IP23 without ducts
- IC26 (OIV)
- IP24(W) with ducts
- MGv, MAV



## Motor Fundamentals

### ▪ Code letters

In general it is accepted that small motors requires higher starting kVA than larger motors. Standard 3PH motors often have these locked rotor codes:

- <1 Hp: Locked Rotor Code L, 9.0-9.99 kVA
- 1 - 2 Hp: Locked Rotor Code L or M, 9.0-11.19
- 3 Hp : Locked Rotor Code K, 8.0-8.99
- 5 Hp : Locked Rotor Code J, 7.1-7.99
- 7.5 - 10 Hp : Locked Rotor Code H, 6.3-7.09
- >15 Hp : Locked Rotor Code G, 5.6-6.29

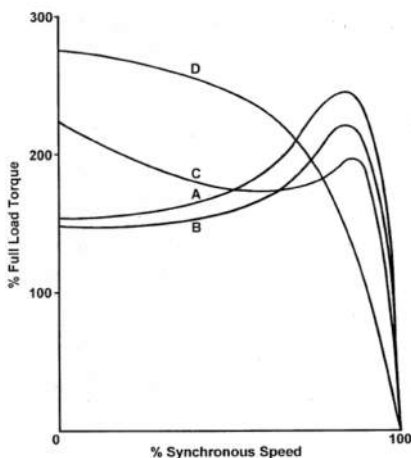
## Motor Fundamentals

### ▪ Design Type

Different motors of the same nominal horsepower can have varying starting current, torque curves, speeds, and other variables. Selection of a particular motor for an intended task must take all engineering parameters into account.

The four NEMA designs have unique speed-torque-slip relationships making them suitable to different type of applications:

- NEMA design A
- NEMA design B
- NEMA design C
- NEMA design D



## Motor Fundamentals

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### ▪ Design Type

- **NEMA design A**
  - o maximum 5% slip
  - o high to medium starting current
  - o normal starting torque (150-170% of rated)
  - o normal locked rotor torque
  - o high breakdown torque
  - o suited for a broad variety of applications - as **fans and pumps**
  
- **NEMA design B**
  - o maximum 5% slip
  - o low starting current
  - o high locked rotor torque
  - o normal breakdown torque
  - o suited for a broad variety of applications, normal starting torque - common in **HVAC application with fans, blowers and pumps**

## Motor Fundamentals

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### ▪ Design Type

- **NEMA design C**
  - o maximum 5% slip
  - o low starting current
  - o high locked rotor torque
  - o normal breakdown torque
  - o can't sustain overload as design A or B
  - o suited for equipment with high inertia starts - as **positive displacement pumps**
  
- **NEMA design D**
  - o maximum 5-13% slip
  - o low starting current
  - o very high locked rotor torque
  - o Usually special order
  - o suited for equipment with very high inertia starts - as **cranes, hoists** etc.

# Motor Fundamentals

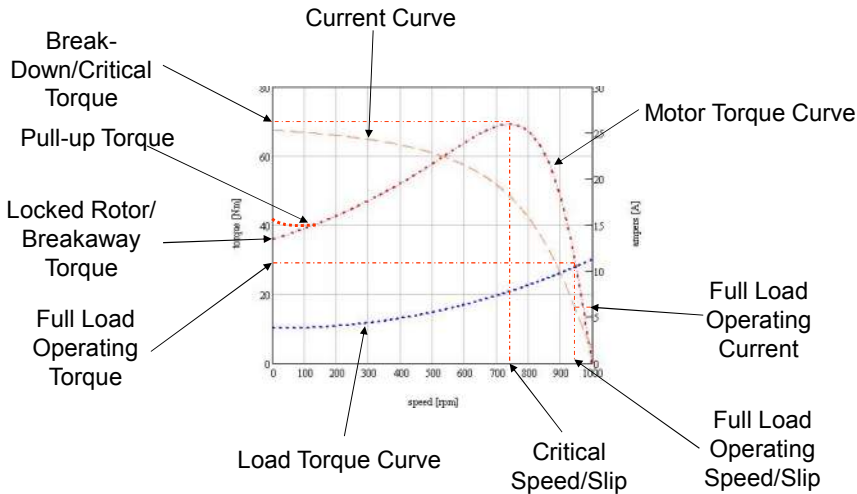
## NEMA Design Type - Comparison

NEMA Design	Starting Current	Lock Rotor Current of Full Load Current	Lock Rotor Torque of Full Load Torque	Breakdown Torque of Full Load Torque	% Nominal Slip	Example Application
A	Normal	600-1000%	70-275%	175-200%	0.5-5 %	Fans, blowers, pumps, and machine tools
B	Normal	600-700%	70-275%	175-300%	0.5-5 %	Fans, blowers, rotary pumps, unloaded compressors, conveyors, metal cutting, machine tools, miscellaneous machinery
C	Normal	600-700%	200-250%	190-225%	1-5%	Large centrifugal blowers, fly wheels, crusher drums, piston pumps, compressors and conveyors
D	Extra High	600-700%	275%	275%	1-5 %	Very high inertia and loaded starts. Choose slip range to match application
					5-8 %	Punch press, sheers, and forming machine tools
					8-13%	Cranes, hoists, elevators and oil well pumping jacks

Notes:  
 1. INSTANTANEOUS PEAK VALUE OF INRUSH CURRENT for 1/2 cycle in range (1.8 - 2.8) x Letter Designation Value (a function of the motor design and switching angle) is not included in above table.

# Motor Fundamentals

## Type of Torques



## Motor Fundamentals

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### Type of Torques (Both IM and SM)

- **Locked Rotor or Starting or Breakaway Torque (Static Torque)**

Lock Rotor or Starting Torque (LRT) is the minimum torque the electrical motor will develop at rest for all angular positions of the rotor, with rated voltage applied at rated frequency

- **Pull-up Torque**

The pull-up torque of an alternating-current motor is the minimum torque developed by the motor during the period of acceleration from rest to the speed at which breakdown torque occurs. For motors which do not have a definite breakdown torque, the pull-up torque is the minimum torque developed up to rated speed.

- **Break-down Torque**

The breakdown torque of a motor is the maximum torque which it will develop with rated voltage applied at rated frequency, without an abrupt drop in speed.

- **Full-load Torque or Braking Torque**

The full-load torque (FLT) of a motor is the torque necessary to produce its rated horsepower at full-load speed. In pounds at a foot radius, it is equal to the horsepower times 5252 divided by the full-load speed.

## Motor Fundamentals

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### Type of Torques (Only SM)

- **Pull-Out Torque**

The pull-out torque of a synchronous motor is the maximum sustained torque which the motor will develop at synchronous speed with rated voltage applied at rated frequency and with normal excitation

- **Pull-In Torque**

The pull-up torque of an alternating-current motor is the minimum torque developed by the motor during the period of acceleration from rest to the speed at which breakdown torque occurs. For motors which do not have a definite breakdown torque, the pull-up torque is the minimum torque developed up to rated speed.

## Motor Fundamentals

The **standard torque** (implied; do not have to be specified), with rated voltage and frequency applied, shall be not less than the following:

Torques	Percent of Rated Full-Load Torque
Locked-rotor*	60
Pull-up*	60
Breakdown*	175
Pushover**	175

\*Applies to squirrel-cage induction motors or induction generators when specified for self-starting

\*\*Applies to squirrel-cage induction generators

The **high torque** (when specified), with rated voltage and frequency applied, shall be not less than the following:

Torques	Percent of Rated Full-load Torque
Locked-rotor	200
Pull-up	150
Breakdown	190

## Motor Fundamentals

The **custom load curve** (when specified), with rated voltage and frequency applied, may be lower than Normal and High Torque requirements, but the motor developed torque exceeds the load torque by a minimum of 10% of the rated full-load torque and any speed up to that at breakdown torque occurs.

Note: Since the torque developed by the induction machine at any speed is approximately proportional to the square of the voltage and inversely proportional to the square of the frequency it is desirable to determine what voltage and frequency variations will actually occur at each installation, taking into account any voltage drop resulting from the starting current drawn by the machine. This information and the torque requirements of the driven (or driving) machine define the machine speed-torque curve, at rated voltage and frequency, which is adequate for the application.

Note: A torque margin of lower than 10% is subject to individual agreements between manufacturer and user.



## Motor Fundamentals

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For “**Low Inrush Motors**” i.e. motors with 4.5 pu and lower lock-rotor current above values do not apply. Break down torque shall be not less than 150% of rated full-load torque, and break away torque and pull-up torque do not have any restrictions.

## Motor Fundamentals

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- Operation of IM from Variable –Frequency or Variable-Voltage power supplies, or both

Induction machines to be operated from solid-state or other types of variable-frequency or variable-voltage power supplies, or both, for adjustable-speed applications may require individual consideration to provide satisfactory performance. Especially for operation below rated speed, it may be necessary to reduce the machine nameplate rating to avoid overheating. The **induction machine manufacturer should be consulted before selecting a machine for such applications!**

## Motor Fundamentals

- **Starting Conditions (MG-1).**  
IM with performance characteristics as described can accelerate load without damage or injurious temperature, for

- **Standard Torque** with load inertia ( $WK^2$ ) not exceeding

$$\text{Load } WK^2 = A \left[ \frac{\text{Hp}^{0.95}}{\left(\frac{\text{RPM}}{1000}\right)^{2.4}} \right] - 0.0685 \left[ \frac{\text{Hp}^{1.5}}{\left(\frac{\text{RPM}}{1000}\right)^{1.8}} \right]$$

Where:

A = 24 for 300 to 1800 rpm, inclusive, motors  
A = 27 for 3600 rpm motors

- **High Torque** with load inertia not exceeding 50% of above value.

## Motor Fundamentals

### ▪ Number of Starts

Squirrel-cage induction motors specified to start and accelerate a connected load shall be capable of making the following starts, providing the  $WK^2$  of the load, the load torque during acceleration, the applied voltage, and the method of starting are those for which the motor was designed.

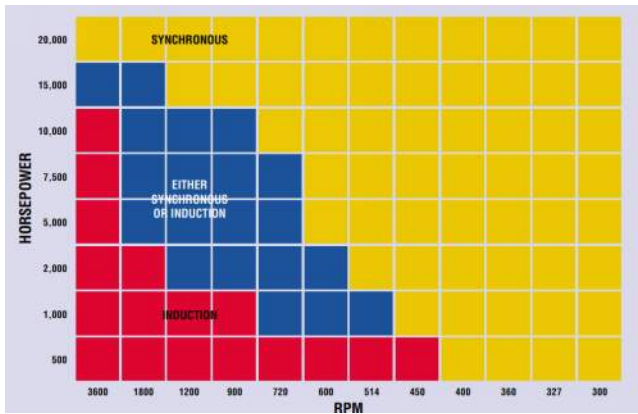
- Two starts in succession, coasting to rest between starts, with the motor initially at ambient temperature.
- One start with the motor initially at a temperature not exceeding its rated load operating temperature.

Note: If additional starts are required, it is recommended that none be made until all conditions affecting operation have been thoroughly investigated and the apparatus has been examined for evidence of excessive heating. It should be recognized that the number of starts should be kept to a minimum since the life of the motor is affected by the number of starts.

## Motor Fundamentals

- Selecting Driver

General areas of application of SM and IM



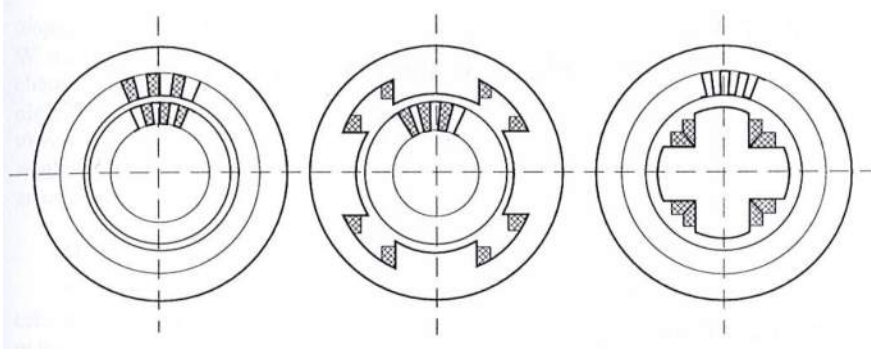
## Motor Fundamentals

- Selecting Driver - Other factors:

- VAR support for start and reacceleration
- Current pulsation (reciprocating compressors)
- Power supply size, type, connection etc.
- Grid vs. Island
- Stability (start, faults, other motor starts)
- Harmonics
- Sub-Synchronous Resonance (SSR) torque interactions

## Motor Fundamentals

- Stator (ST) and Rotor (RT) configurations



ST: Cylindrical  
RT: Cylindrical

ST: Silent Pole  
RT: Cylindrical

ST: Cylindrical  
RT: Silent Pole

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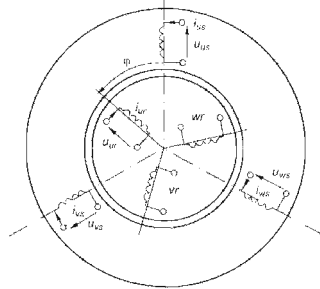
## Induction Motor

## Induction Motor

- Basics, type characteristics, load characteristics, and modeling
  - Motor modeling
  - General construction and Cooling
  - Induction motor - General data, principle of operation and nameplate information describing motor
  - Motor types and characteristics, application consideration
  - Equivalent motor parameters
  - Other consideration

## Induction Motor

- General-Non-linear Model – Squirrel-cage rotor IM



$$\begin{cases}
 \mathbf{u}_s^{abc} = \mathbf{r}_s^{abc} \mathbf{i}_s^{abc} + \frac{d}{dt} \mathbf{M}_{ss}^{abc} \mathbf{i}_s^{abc} + \frac{d}{dt} \mathbf{M}_{sr}^{abc} \mathbf{i}_r^{abc} \\
 \mathbf{0} = \mathbf{r}_r^{abc} \mathbf{i}_r^{abc} + \frac{d}{dt} \mathbf{M}_{rr}^{abc} \mathbf{i}_r^{abc} + \frac{d}{dt} \mathbf{M}_{rs}^{abc} \mathbf{i}_s^{abc} \\
 T_{em}(\mathbf{i}_s^{abc}, \mathbf{i}_r^{abc}, \omega) = \frac{1}{2} [\mathbf{i}_s^{abc} \quad \mathbf{i}_r^{abc}] \begin{bmatrix} \mathbf{0} & \frac{\partial}{\partial \omega} \mathbf{M}_{sr}^{abc} \\ \frac{\partial}{\partial \omega} \mathbf{M}_{rs}^{abc} & \mathbf{0} \end{bmatrix} \begin{bmatrix} \mathbf{i}_s^{abc} \\ \mathbf{i}_r^{abc} \end{bmatrix} \\
 T_{mech}(\omega) = a_0 + a_1 \omega + a_2 \omega^2 + \dots + a_n \omega^n \\
 J \frac{d^2 \omega}{dt^2} + k_d \frac{d\omega}{dt} = T_{em}(\mathbf{i}_s^{abc}, \mathbf{i}_r^{abc}, \omega) - T_{mech}(\omega) - T_{Loss} - B_r \omega
 \end{cases}$$

## Induction Motor

### After Arbitrary Reference Frame Transform

$$\begin{cases}
 u_{qs} = r_s i_{qs} + \frac{d}{dt} \lambda_{qs} + \omega \lambda_{ds} \\
 u_{ds} = r_s i_{ds} + \frac{d}{dt} \lambda_{ds} - \omega \lambda_{qs} \\
 u_{0s} = r_s i_{0s} + \frac{d}{dt} \lambda_{0s} \\
 u'_{qr} = r'_r i'_{qr} + \frac{d}{dt} \lambda'_{qr} + (\omega - \omega_r) \lambda'_{dr} \\
 u'_{dr} = r'_r i'_{dr} + \frac{d}{dt} \lambda'_{dr} - (\omega - \omega_r) \lambda'_{qr} \\
 u'_{0r} = r'_r i'_{0r} + \frac{d}{dt} \lambda'_{0r} \\
 T_{em}(i_s^{qd0}, i_r^{qd0}) = \frac{3P}{2} (\lambda_{ds} i_{qs} - \lambda_{qs} i_{ds}) \\
 \begin{bmatrix} \lambda_{qs} \\ \lambda_{ds} \\ \lambda_{0s} \\ \lambda'_{qr} \\ \lambda'_{dr} \\ \lambda'_{0r} \end{bmatrix} = \begin{bmatrix} L_{ls} + L_m & 0 & 0 & L_m & 0 & 0 \\ 0 & L_{ls} + L_m & 0 & 0 & L_m & 0 \\ 0 & 0 & L_{ls} & 0 & 0 & 0 \\ L_m & 0 & 0 & L'_{lr} + L_m & 0 & 0 \\ 0 & L_m & 0 & 0 & L'_{lr} + L_m & 0 \\ 0 & 0 & 0 & 0 & 0 & L'_{lr} \end{bmatrix} \begin{bmatrix} i_{qs} \\ i_{ds} \\ i_{0s} \\ i'_{qr} \\ i'_{dr} \\ i'_{0r} \end{bmatrix} \\
 T_{mech}(\omega) = a_0 + a_1 \omega + a_2 \omega^2 + \dots + a_n \omega^n \\
 \int \frac{d^2 \omega}{dt^2} + k_d \frac{d\omega}{dt} = T_{em}(i_s^{qd0}, i_r^{qd0}) - T_{mech}(\omega) - T_{Loss} - B_r \omega
 \end{cases}$$

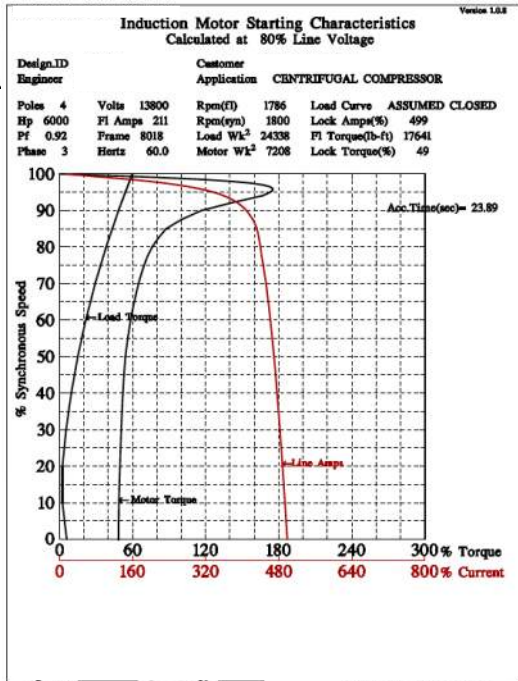
## Induction Motor

### Steady State $U_s = \text{const}$

$$\begin{cases}
 V_{as} = (r_s + j\omega_e L_{ls}) I_{as} + jL_m (I_{as} + I'_{ar}) \\
 V'_{ar} = (r'_r + js\omega_e L'_{lr}) I'_{ar} + js\omega_e L_m (I_{as} + I'_{ar}) \\
 T_{em} = 3 \frac{1}{\omega_{sm}} I'_{ar}{}^2 \frac{r'_r}{s} \\
 T_{mech}(\omega) = a_0 + a_1 \omega + a_2 \omega^2 + \dots + a_n \omega^n \\
 \int \frac{d^2 \omega}{dt^2} + k_d \frac{d\omega}{dt} = T_{em}(i_s^{qd0}, i_r^{qd0}) - T_{mech}(\omega) - T_{Loss} - B_r \omega
 \end{cases}$$

# Induction Motor

- Typical Starting Curves



# Induction Motor - Frames



## Induction Motor - Stator

- High Speed



- Low Speed



## Induction Motor - Rotor

- High  
Speed  
4-6 Pole



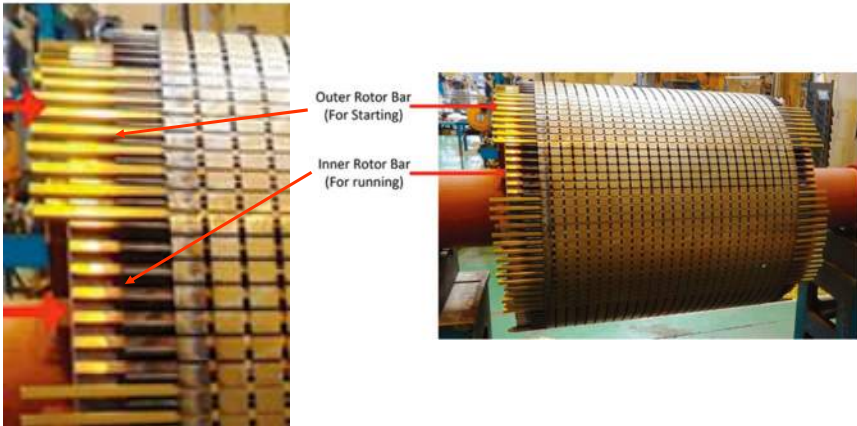
- Medium  
Speed  
8-14 Pole





## Induction Motor - Rotor

- Double-cage rotor bar construction for low inrush current motors



## Induction Motor


### General data

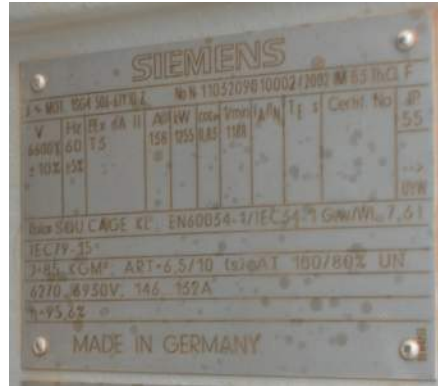
Motor electro-mechanical characteristics are described by:


- Nominal Voltage
- Nominal frequency
- Nominal Current
- Number of phases
- Number of poles
- Design class
- Code letter
- Moment of inertia
- All others (rated power factor, efficiency, excitation current etc.)

# Induction Motor

## General data


<b>ABB</b>  <b>II 3 G CE</b>		ABB Oy	
Type	HXR 500L P14	No	4570787
Year	2002	Phases	3~
Duty	S1	Output	470 kW
Connection	D	Voltage	3300 V
Insd. cl.	F	Frequency	50 Hz
Weight	7100 kg	Speed	425 rpm
IP	55	Current	145 A
IM	1001	Power factor	0.59
IEC	411		
IM	1001		
EEx nA II T3, EN 50021			
VTT 03 ATEX 011X			
IEC 60034-1			



<b>ABB</b>  <b>II 3 G CE</b>		ABB Oy	
Type	HXR 500L P14	No	4570787
Year	2002	Phases	3~
Duty	S1	Output	470 kW
Connection	D	Voltage	3300 V
Insd. cl.	F	Frequency	50 Hz
Weight	7100 kg	Speed	425 rpm
IP	55	Current	145 A
IM	1001	Power factor	0.59
IEC	411		
IM	1001		
EEx nA II T3, EN 50021			
VTT 03 ATEX 011X			
IEC 60034-1			

# Induction Motor

## General data

<b>ABB</b>  <b>II 3 G CE</b>		ABB Oy	
Type	HXR 450L B	No	4574367
Year	2003	Phases	3~
Duty	S1	Output	450 kW
Connection	D	Voltage	4500 V
Insd. cl.	F	Frequency	50 Hz
Weight	4095 kg	Speed	890 rpm
IP	55	Current	411 A
IM	1002		
SI_CONVERTER SUPPLY			
250	-	455	-
383	-	690	-
25	-	45.2	-
495.5	-	899.5	-
475	-	500	-
0.81	-	0.89	-
INVERTER PARAMETER SETTING:			
455 kW / 450 V / 45.2 Hz / 899.5 rpm / 475 A /			
0.83 PF / Tmax/Tmin 3.0			
OVERLOAD 1.8 x In, 60 s / 10 min			
455 - 800 - 950 rpm			
820 - 820 - 910 A			
IEC 60034-1			

<b>ABB</b>  <b>II 3 G CE</b>		ABB Oy	
SER	4564875	Year	2001
Type	AMA 450LW BAH	Weight	9810 lbs
Output	330 kW	HP/Phases	5
Voltage	4600 V	V/INS	F
Frequency	60 Hz	HZ/IMM	CONT
FL RPM	1790	RPM/ENCL	WPH
FLA	338 A	ALCODE	F
CONN	Y	IAMB	-40 °C, +40 °C
PF	0.89	ISTD	NEMA, CSA
SF	1.15	TEMP RISE	90°C, RES
CODE F, Amb. 40°C			
Class II, Div. 2, Group F			
IEC 60034-1			

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## Synchronous Motor

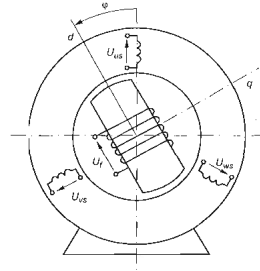
### Synchronous Motor

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## Synchronous Motor

- General-Non-linear Model



$$\begin{cases}
 \mathbf{u}_s^{abc} = \mathbf{r}_s^{abc} \mathbf{i}_s^{abc} + \frac{d}{dt} \mathbf{M}_{ss}^{abc} \mathbf{i}_s^{abc} + \frac{d}{dt} \mathbf{M}_{sf}^{abc} \mathbf{i}_f \\
 \mathbf{u}_f = r_f \mathbf{i}_f + \frac{d}{dt} \mathbf{M}_{ff} \mathbf{i}_f + \frac{d}{dt} \mathbf{M}_{fs}^{abc} \mathbf{i}_s^{abc} \\
 T_{em}(\mathbf{i}_s^{abc}, \mathbf{i}_f, \omega) = \frac{1}{2} \begin{bmatrix} \mathbf{i}_s^{abc} & \mathbf{i}_f \end{bmatrix} \begin{bmatrix} \mathbf{0} & \frac{\partial}{\partial \omega} \mathbf{M}_{sf}^{abc} \\ \frac{\partial}{\partial \omega} \mathbf{M}_{fs}^{abc} & \mathbf{0} \end{bmatrix} \begin{bmatrix} \mathbf{i}_s^{abc} \\ \mathbf{i}_f \end{bmatrix} \\
 T_{mech}(\omega) = a_0 + a_1 \omega + a_2 \omega^2 + \dots + a_n \omega^n \\
 J \frac{d^2 \omega}{dt^2} + k_d \frac{d\omega}{dt} = T_{em}(\mathbf{i}_s^{abc}, \mathbf{i}_f, \omega) - T_{mech}(\omega) - T_{Loss} - B_r \omega
 \end{cases}$$

## Synchronous Motor

- Park's Transform

$$\mathbf{T} = \sqrt{\frac{2}{3}} \begin{bmatrix} \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ \cos \varphi & \cos(\varphi - 120^\circ) & \cos(\varphi - 240^\circ) \\ -\sin \varphi & -\sin(\varphi - 120^\circ) & -\sin(\varphi - 240^\circ) \end{bmatrix}$$

$$u_d = R_s i_d + \frac{d}{dt} \psi_d - \dot{\varphi} \psi_q$$

$$u_q = R_s i_q + \frac{d}{dt} \psi_q + \dot{\varphi} \psi_d$$

$$u_f = R_f i_f + \frac{d}{dt} \psi_f$$

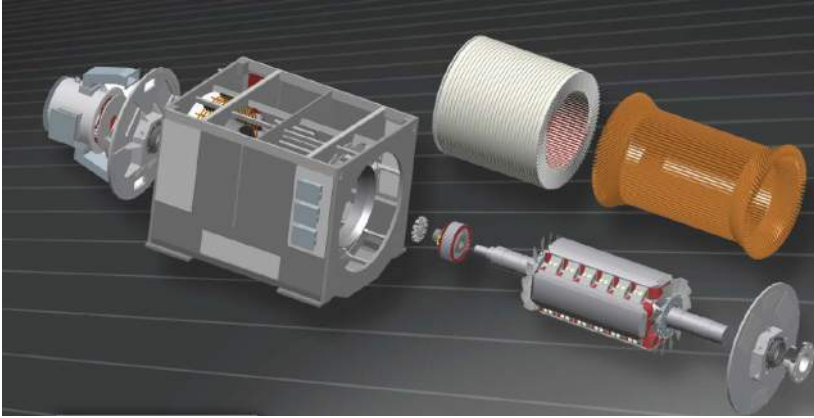
$$J \frac{d^2 \varphi}{dt^2} + k_d \frac{d\varphi}{dt} = T_e + T_m$$

$$T_e = \psi_d i_q - \psi_q i_d$$



## Synchronous Motor

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## Stator

---

- High Speed
- Low Speed



## Rotors

### High Speed

4-6 Pole Solid  
Rotors



### Medium Speed

8-14 Pole Stacked  
Rotors

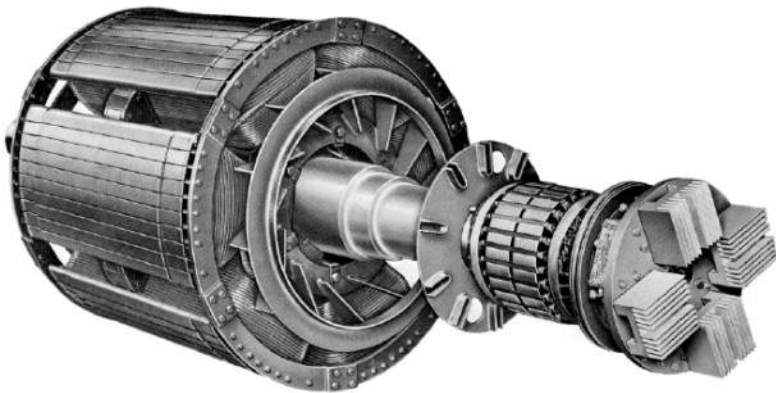


### Low Speed

>14 Pole Stacked  
Rotors



## Synchronous Motor

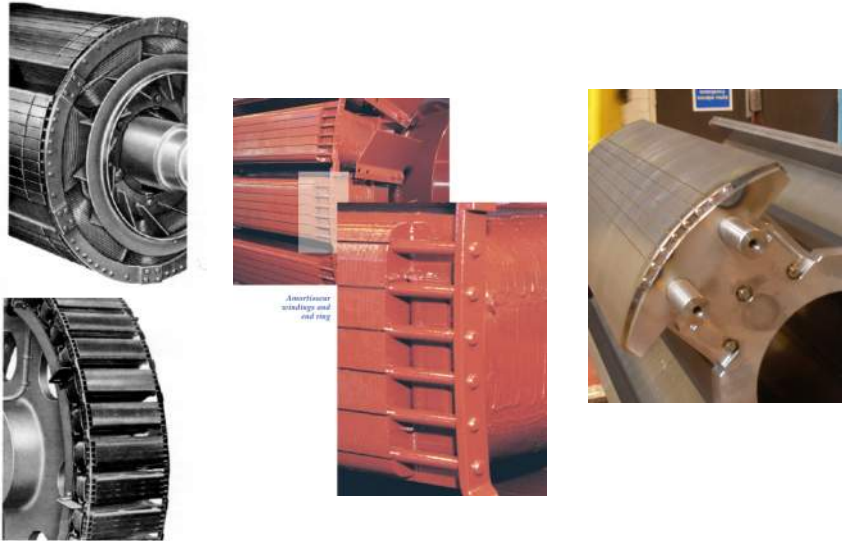




# Synchronous Motor



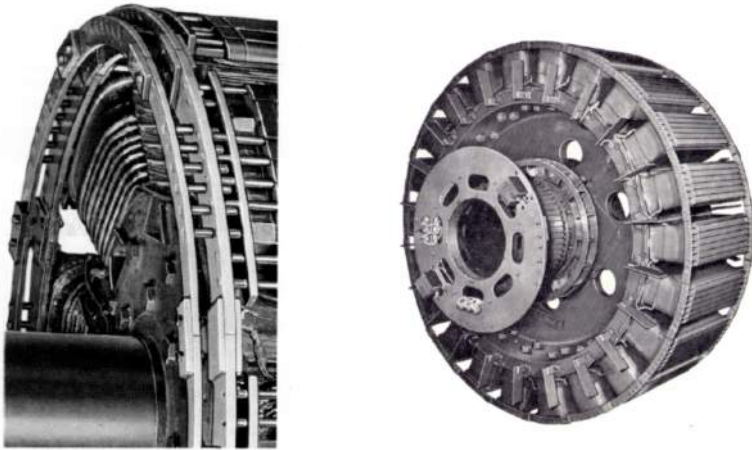
# Synchronous Motor





## Synchronous Motor

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## Synchronous Motor

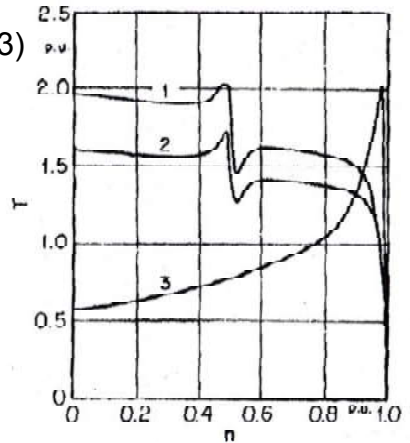
---

### General data

- Motor electro-mechanical characteristics are described by:
  - Nominal Voltage
  - Nominal frequency
  - Nominal Current
  - Number of phases
  - Number of poles
  - Design class
  - Code letter
  - Moment of inertia
  - All others (rated power factor, efficiency, excitation current etc.)

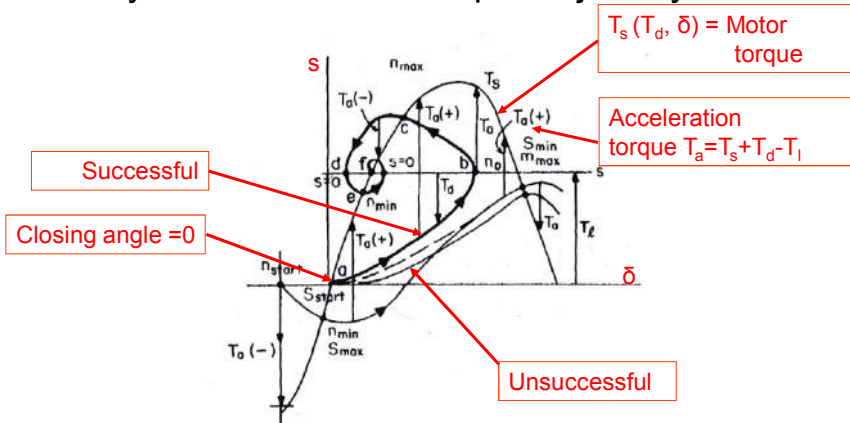
## Synchronous Motor

- Characteristic torque curves:
  - 5kHp SM (1-PF=1.0)
  - 5kHp SM (2-PF=0.80)
  - 5kHp IM / squirrel-cage (3)



## Synchronous Motor

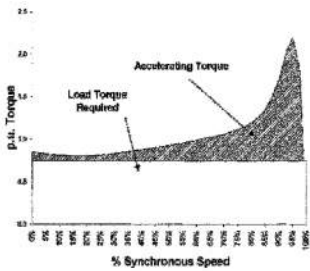
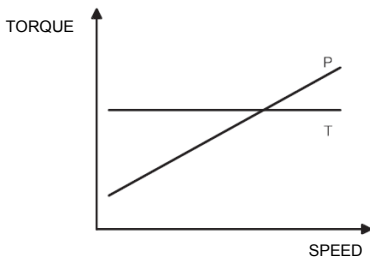
- SM Synchronization – Torque trajectory



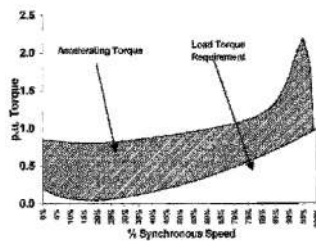
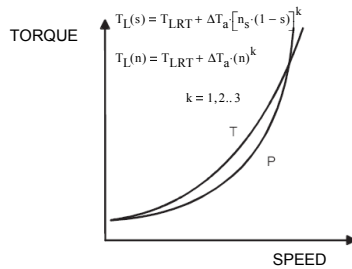
# Mechanical Load And Train System

## Load Types

### Constant Torque

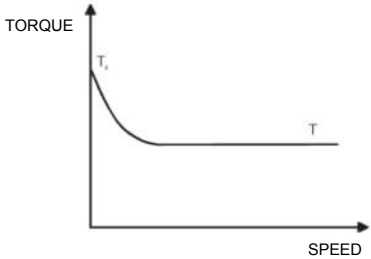
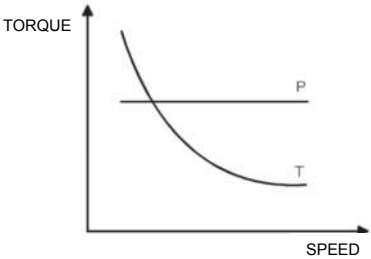


### Variable Torque



## Load Types

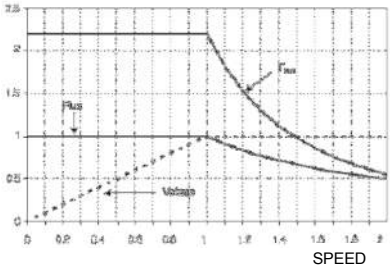
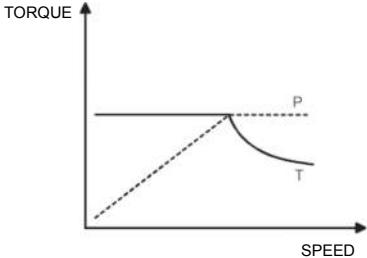
- Constant Power
- Constant Torque w/ High Brake-Away



$$T_L(n) = A_0 + B \cdot n + C \cdot n^2 + D \cdot n^3$$

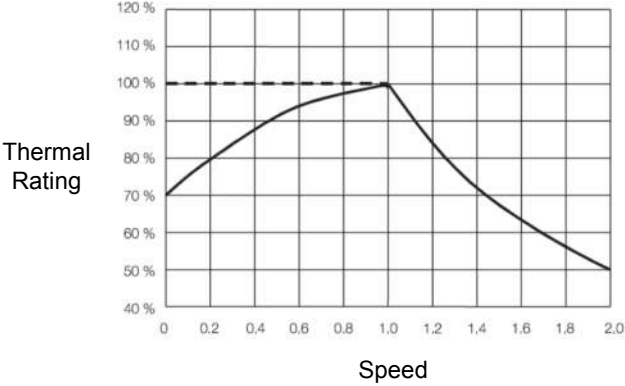
## Load Types

- Sub- and Super-Synchronous Applications



# Load Types

- ASD Application of Standard Motors



# Load Types

- Load Types

Application	Load Torque as a Minimum Percent Drive Torque		
	Breakaway	Accelerating	Peak Running
Blowers, centrifugal:			
Valve closed	30	50	40
Valve open	40	110	100
Blowers, positive displacement, rotary, bypass	40	40	100
Centrifuges	40	60	125
Compressors, axial-vane, loaded	40	100	100
Compressors, reciprocating, start unloaded	100	50	100
Conveyors, belt (loaded)	150	130	100
Conveyors, screw (loaded)	175	100	100
Conveyors, shaker-type (vibrating)	150	150	75
Fans, centrifugal, ambient:			
Valve closed	25	60	50
Valve open	25	110	100
Fans, centrifugal, hot:			
Valve closed	25	60	100
Valve open	25	200	175
Fans, propeller, axial-flow	40	110	100
Mixers, chemical	175	75	100
Mixers, slurry	150	125	100
Pumps, adjustable-blade, vertical	150	200	200
Pumps, centrifugal, discharge open	40	150	150
Pumps, oil-field, flywheel	40	150	150
Pumps, oil, lubricating	40	150	150
Pumps, oil, fuel	40	150	150
Pumps, propeller	40	100	100
Pumps, reciprocating, positive displacement	175	30	175
Pumps, screw-type, primed, discharge open	150	100	100
Pumps, slurry-handling, discharge open	150	100	100
Pumps, turbine, centrifugal, deep-well	50	100	100
Pumps, vacuum (paper mill service)	60	100	150
Pumps, vacuum (other applications)	40	60	100
Pumps, vane-type positive displacement	150	150	175

## Inertia

- Inertia

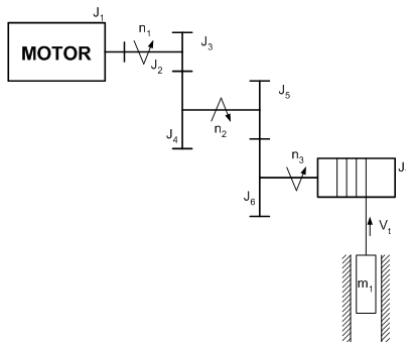
$$J_z = \sum_{i=1}^w J_i \left( \frac{n_i}{n_1} \right)^2 + \sum_{i=1}^p m_i \left( \frac{V_i}{n_1} \right)^2$$

w - numer rotating elements

p - number linera motion elements

## Inertia

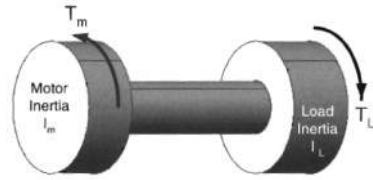
- Inertia



$$J_z = (J_1 + J_2 + J_3) \left( \frac{n_1}{n_1} \right)^2 + (J_4 + J_5) \left( \frac{n_2}{n_1} \right)^2 + (J_6 + J_7) \left( \frac{n_3}{n_1} \right)^2 + m_1 \left( \frac{V_1}{n_1} \right)^2$$

## Torsion

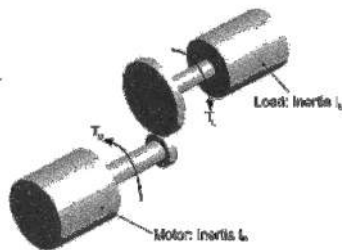
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$$T_m = T_L + (J_L + I_m) \cdot \left( \frac{d}{dt} n_m \right) + B \cdot n_m$$

## Torsion

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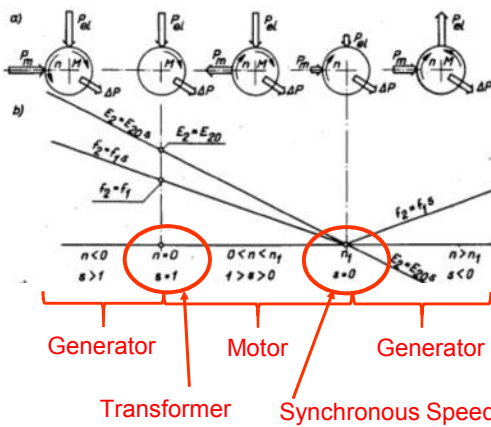
$$T_m = \frac{T_L}{N} + (J_L + I_m \cdot N^2) \cdot \left( \frac{d}{dt} n_m \right) + n_m \cdot (B_L + B_m \cdot N^2)$$

N - gear ratio  
J - inertia  
B - dumping

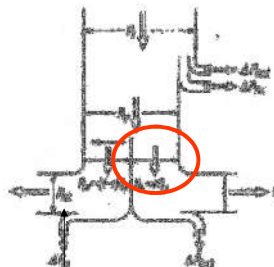
# Induction Motor

## Starting Methods

### Motor Starting – Induction Machine



▪ Motoring Operation



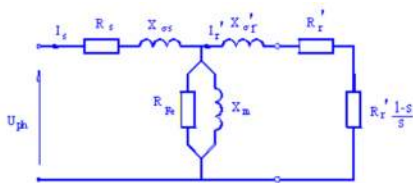


▪ Equivalent circuit of one phase of induction motor

$$Z_s(f) := R_s \cdot \frac{f}{f_n} \cdot j \cdot X_{\sigma s}$$

$$Z_r'(s, f) := \frac{R_r'}{s} \cdot \frac{f}{f_n} \cdot j \cdot X_{\sigma r}'$$

$$Z_m := \frac{R_{fe} \cdot X_m \cdot j}{R_{fe} + X_m \cdot j}$$



$$Z_m(f) := \frac{\left(\frac{f}{f_n}\right)^{0.7} \cdot R_{fe} \cdot \left(\frac{f}{f_n}\right) \cdot X_m \cdot j}{\left(\frac{f}{f_n}\right)^{0.7} \cdot R_{fe} + \left(\frac{f}{f_n}\right) \cdot X_m \cdot j}$$

$$Z(s, f) := Z_s(f) + \frac{Z_r'(s, f) \cdot Z_m(f)}{Z_r'(s, f) + Z_m(f)}$$

$$U(f) := U_n \cdot \frac{f}{f_n}$$

Modification for Variable Frequency

$$n(s, f) := \frac{60 \cdot f}{p} \cdot (1 - s)$$

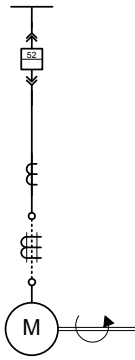
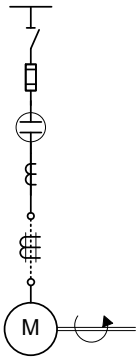
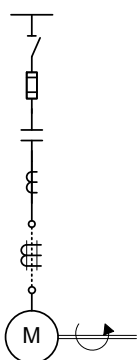
$$I_s(s, f) := \frac{U(f)}{\sqrt{3} \cdot Z(s, f)}$$

$$I_r'(s, f) := I_s(s, f) \cdot \frac{Z_m(f)}{Z_r'(s, f) + Z_m(f)}$$

$$T_e(s, f) := \frac{3 \cdot p}{2 \cdot \pi \cdot f} \cdot (|I_r'(s, f)|)^2 \cdot \text{Re}(Z_r'(s, f))$$

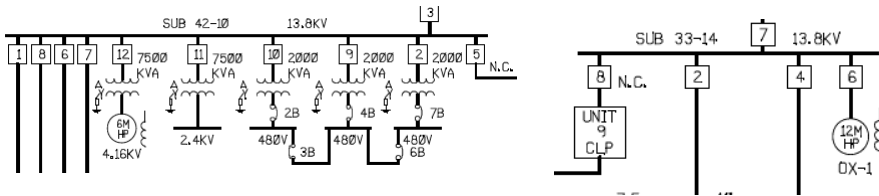
## Motor Starting

- Direct On Line Starter (or DOL or FVNR)
  - One Line Representation



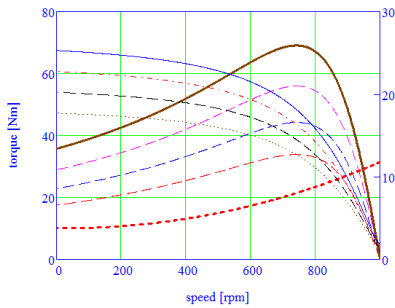
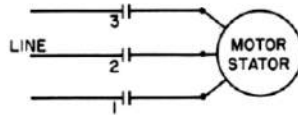
## Motor Starting

- Direct On Line Starter (or DOL or FVNR)
  - One Line Examples



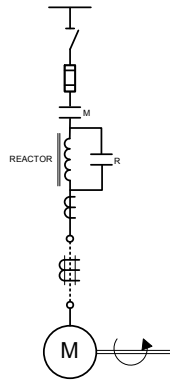
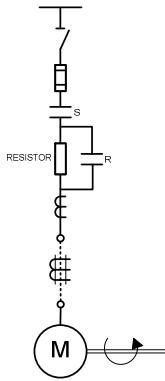
## Motor Starting

- Direct On Line Starter (or DOL or FVNR)
  - Characteristics



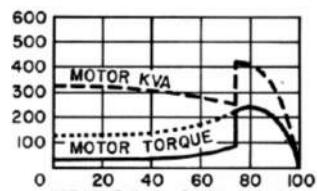
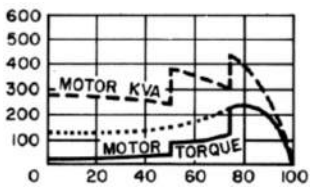
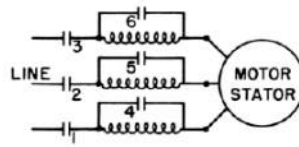
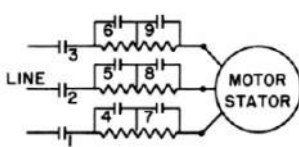
## Motor Starting

- Reduce Voltage Resistor/Reactor Starter
  - One Line Representation



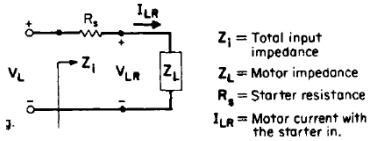
## Motor Starting

- Reduce Voltage Resistor/Reactor Starter
  - Characteristics



## Motor Starting

- Reduce Voltage Resistor/Reactor Starter
  - Equivalent Diag.



(b)

Motor Locked-Rotor Resistance Quantities with the Starter In

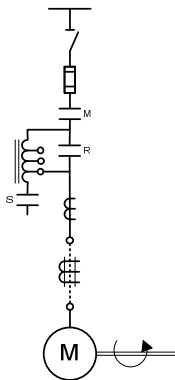
	Tap $\alpha$ value		
	0.50	0.65	0.80
in percent $I_{fl}$	269.5	350.4	431.2
percent $I_L$	50	65	80
in percent $T_{fl}$	32	54.1	81.9
percent $T_L$	2.5	42.5	64

**TABLE 5.3** Comparison of Resistance and Reactance Starting

No.	Feature	Resistance type	Reactor type
1	Starting pf	Higher	Lower
2	Developed torque around 75 to 85 percent $n_s$	Lower (15 to 20 percent $T_{fl}$ )	Higher (15 to 20 percent $T_{fl}$ )
3	Heat loss ( $I^2R$ )	Very high	Very small
4	Size	Larger	Smaller
5	Cost	Lower	Higher

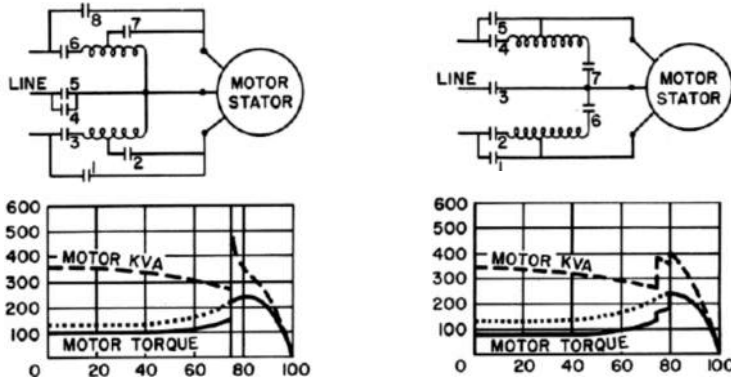
## Motor Starting

- Reduce Voltage Autotransformer Starter (RVAT or Korndörfer Starter)
  - One Line Representation



## Motor Starting

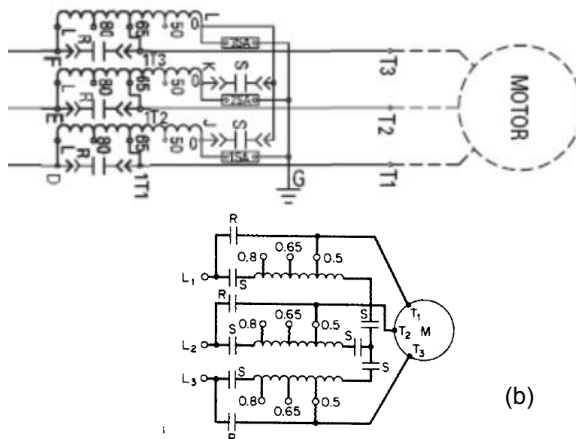
- Reduce Voltage Autotransformer Starter (RVAT or Korndörfer Starter) – 2-Winding XFMR
  - Characteristics



(a)

## Motor Starting

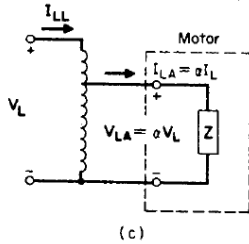
- Reduce Voltage Autotransformer Starter (RVAT or Korndörfer Starter) – 3-Winding XFMR



(b)

## Motor Starting

- Reduce Voltage Autotransformer Starter (RVAT or Korndörfer Starter)
  - Equivalent Diag.

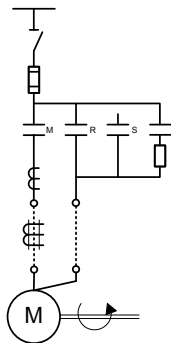
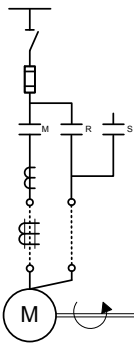


No.	Tap, $\alpha$	Line current, $I_{LL}$							
		Two transformers		Three transformers		Motor current, $I_{LA}$			
1	0.5	27.5	165	25	150	50	300	25	32.5
2	0.65	44.8	269	42.3	254	65	390	42.3	55
3	0.8	66.5	399	64	384	80	480	64	83.2
		$\sigma_d I_L$	$\sigma_d I_{fl}$	$\sigma_d I_L$	$\sigma_d I_{fl}$	$\sigma_d I_L$	$\sigma_d I_{fl}$	$\sigma_d T_L$	$\sigma_d T_{fl}$

- $\alpha =$  voltage tap  $= V_{LA} / V_f$
- $I_{LA} = \alpha I_L =$  motor current
- $I_{LL} = \alpha I_{LA} = \alpha^2 I_L =$  line current for (b)
- $= \alpha^2 I_L + 0.15 I_{fl}$  for (a)
- $T_A = \alpha^2 T =$  motor torque with autotransformer

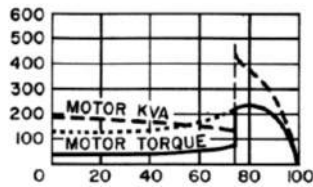
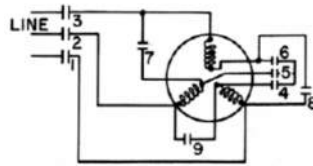
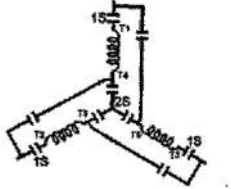
## Motor Starting

- Y /  $\Delta$  (or Delta / WYE) Starter
  - One Line Representation



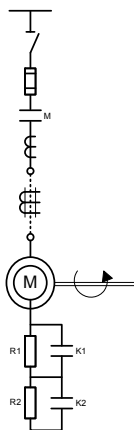
## Motor Starting

- Y /  $\Delta$  (or Delta / WYE) Starter
  - Characteristics



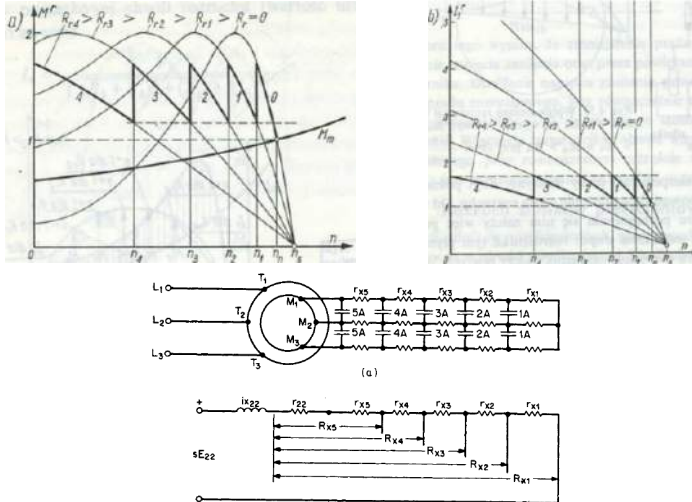
## Motor Starting

- Wound-rotor Resistance Starter (Slip-Ring Starter)
  - One Line Representation



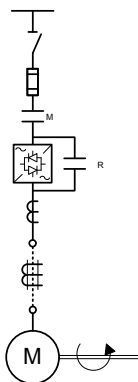
## Motor Starting

- Wound-rotor Resistance Starter (Slip-Ring Starter)
  - Principle



## Motor Starting

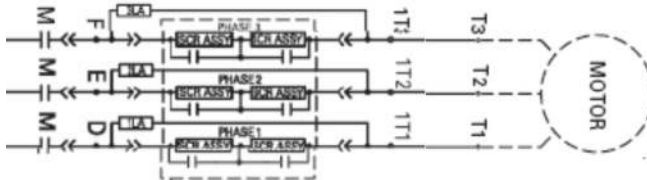
- Reduce Voltage Solid State Starter with  $V=var, f=const$  (or RVSS)





## Motor Starting

- Reduce Voltage Solid State Starter with  $V=\text{var}$ ,  $f=\text{const}$  (or RVSS)

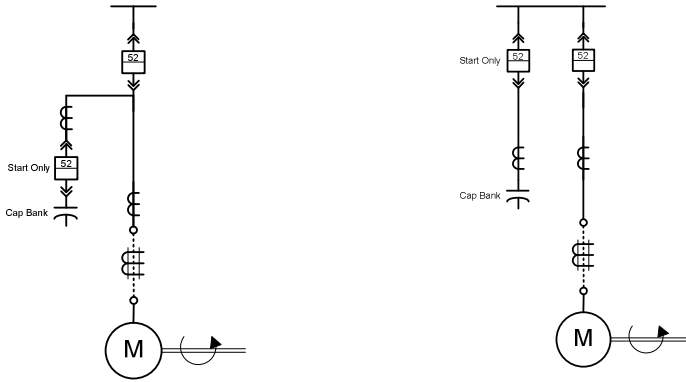


## Motor Starting

- Reduce Voltage Solid State Starter with  $V=\text{var}$ ,  $f=\text{const}$  (or RVSS)
  - Caution...

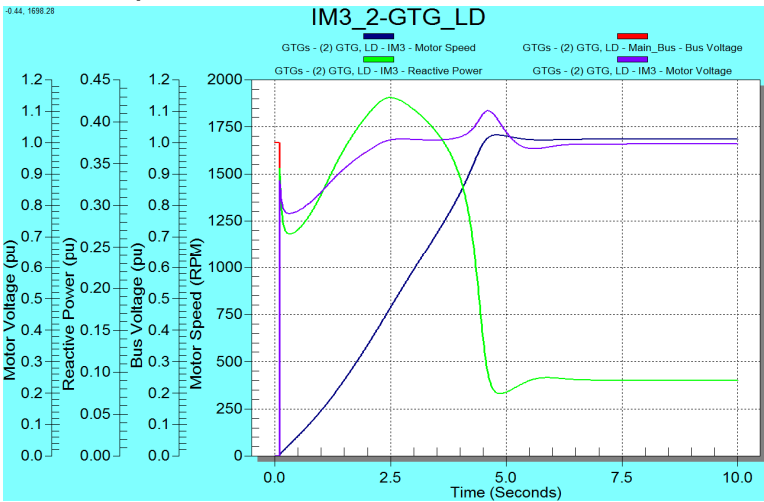
## Motor Starting

- Shunt Capacitor Starting
  - One Line Representation



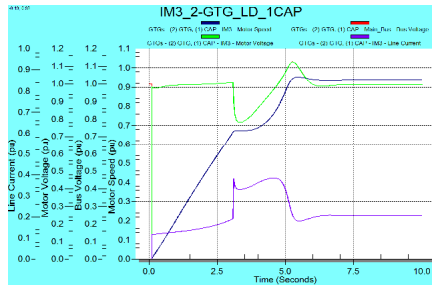
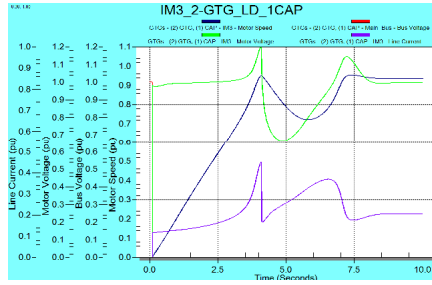
## Motor Starting

- Principle



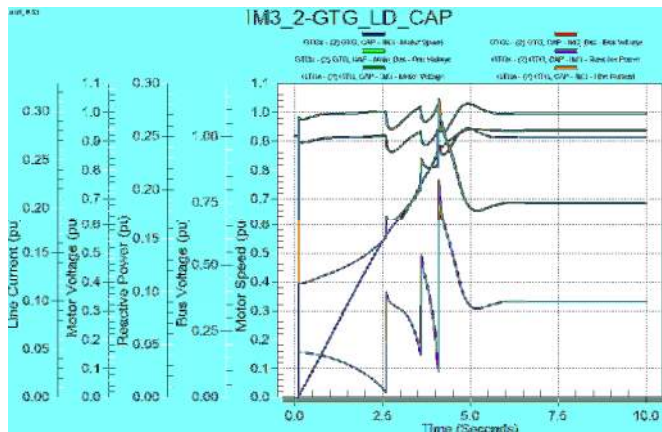
## Motor Starting

- Problems:
  - Multiple steps required
  - Overvoltages
  - Special control (motor speed)
  - Not suited for Islanded systems



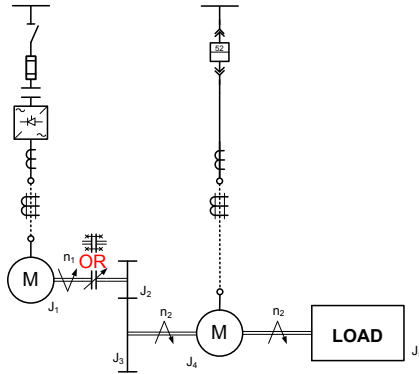
## Motor Starting

- Problems
  - (3) steps (i.e. 3x CB)



# Motor Starting

- Pony Motor (not Jacking Motor)
  - One Line Representation



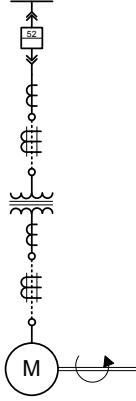
# Motor Starting - Comparison

Table - Motors Starting Methods / Comparison													
Item #	Train Starting Method	Stiff Network	Weak Network	Load with High Breakaway Torque	High Torsional Stresses Not Allowed - Fast Acceleration	System Issues	Locked Rotor		Maximum		Motor Starts Per Hour	Notes	
							Line Inrush [pu]	Voltage [pu]	Value [pu]	Duration [sec]	Cost [pu]		
1	FVNR/DDC	Preferred, if voltage drop excessive use 2,3,7,8	Results in unacceptable voltage drop	Preferable; otherwise use 4,5,6	Not recommended		6.0	0.8	6.0	3-10	10	1-2	
2	Reactor Resistor Start	Only if FVNR is not acceptable	Evaluate; if negative use 4,5,6	Not recommended	Preferred		3.5	.85	3.5	5-12	16	1-2	0.70 Tap
3	RVAT	Only if FVNR is not acceptable	Evaluate; if negative use 4,5,6	Not recommended	Preferred		2.5	0.9	2.5	5-12	14	1-2	0.70 Tap
4	Shunt Capacitor	Not recommended	Preferred on cost basis	Capacitors used as network support may allow a FVNR start	Not recommended	Resonance, back-to-back switching, overexcitation stability	2.2	0.89	4.5	1-2	2.5	1-2	50 %VAR Correction
5	Wound Rotor	If soft start required	Guaranteed start	No problems, guaranteed start	Preferred		10	0.97	3.0	1-2	2.0	1-2	100% LRT limit
6	Pony Motor	Not recommended	Use if capacitor start is unsuccessful	NO starting problem for unloaded driven eqp	Not recommended		12	0.96	2.0	10-300	18	Multiple	
7	RVSS	If soft start required	Evaluate; if negative use 4,5,6	Not recommended	Preferred		3.5	0.8	3.5	10-30	14	1-2	I(lim)=250%
8	Captive Transformer	If voltage drop in the utility network needs to be minimized	Evaluate; if negative use 4,5,6	Not recommended	Use if voltage stepdown function is required								
9	Frequency/Voltage Sirt PWM ASD	If soft start required	Guaranteed start	No problems, guaranteed start	Preferred	SSR Resonance	13	0.98	2.0	10-30	2.5	Multiple	24-48 pulses
10	Frequency/Voltage Sirt LQ ASD	If soft start required	Guaranteed start	No problems, guaranteed start	Preferred	SSR Resonance	13	0.98	2.0	10-30	2.5	Multiple	
11	Frequency/Voltage Sirt Isolated Bus	If soft start required	Guaranteed start	No problems, guaranteed start	Preferred	Special							W=const, Special Consideration
12	Synchronous Motor					Stability	4.5	0.9	2.1	2-5	16	1-2	Brushless Type

**Notes:**  
Cost and system parameters based on 10kHp motor selection needed for mechanical train.

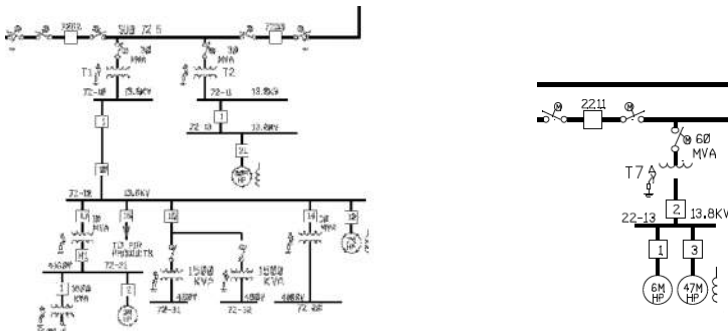
## Motor Starting

- Captive Transformer Starter
  - One Line Representation



## Motor Starting

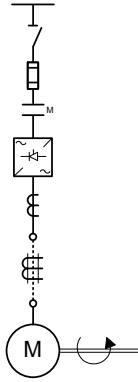
- Captive Transformer Starter
  - Actual One Lines



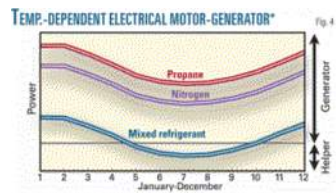
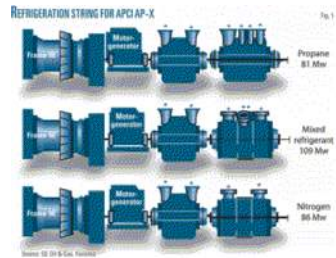
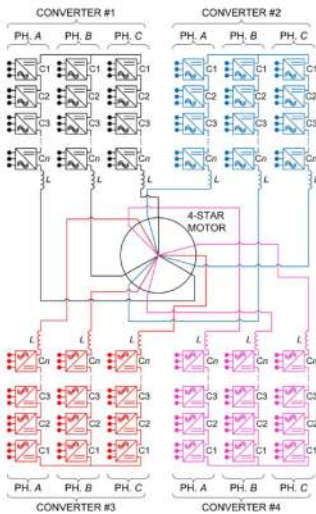


# Motor Starting

- Variable Frequency Drive Starting and Control



# Motor Starting – Special Methods



## **Motor Starting**

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- **Variable Generator / Isolated Bus Motor Starting**
  - Principle: use turbine/engine together with generator as a “VFD” starter.

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# **Starting Large AC Motors Day 2**

For

IEEE Houston Section – CED Seminar

By:

Roy Cosse, P.E.  
Robert Spiewak, P.E.

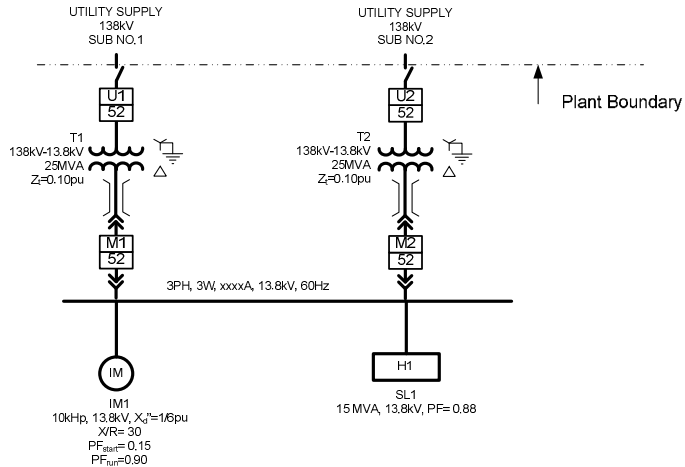
Presentation Code: 214

March 22-23, 2016



## Motor Starting

### ▪ Typical Application - DOL



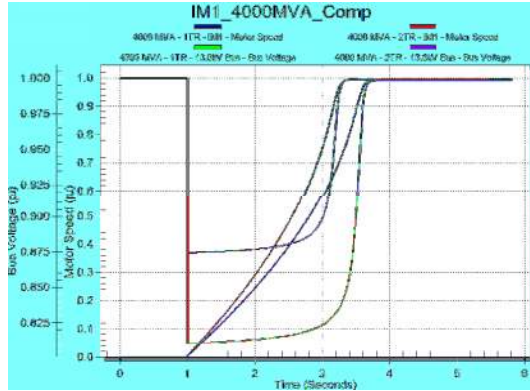
## Motor Starting

### ▪ Typical Application – Cont.

- Condition 1 –  $S_{sc}=4000$  MVA, X/R=5
  - o Both T's On-Line
  - o One T On-Line
- Condition 2 –  $S_{sc}=1000$  MVA, X/R=5
  - o Both T's On-Line
  - o One T On-Line

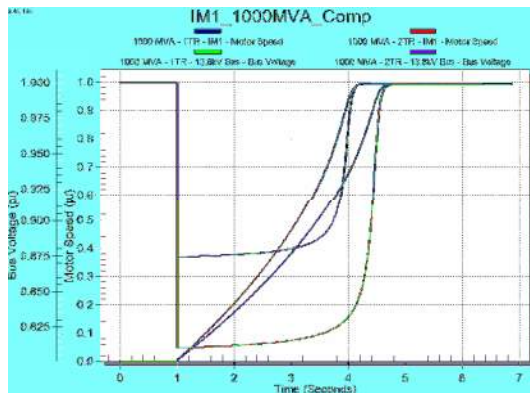
## Motor Starting

- Typical Application – Cont.
  - Condition 1 –  $S_{sc}=4000$  MVA,  $X/R=5$ 
    - o Both TRs On-Line
    - o One TR On-Line



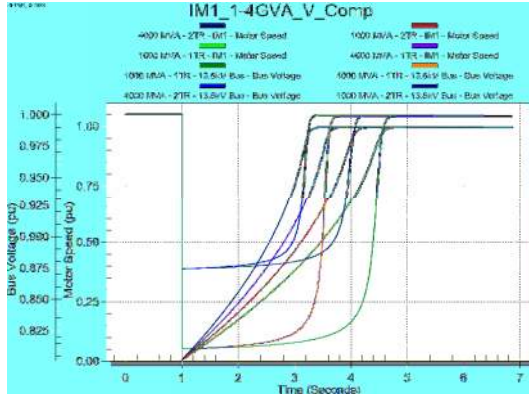
## Motor Starting

- Typical Application – Cont.
  - Condition 2 –  $S_{sc}=1000$  MVA,  $X/R=5$ 
    - o Both TR's On-Line
    - o One TR On-Line



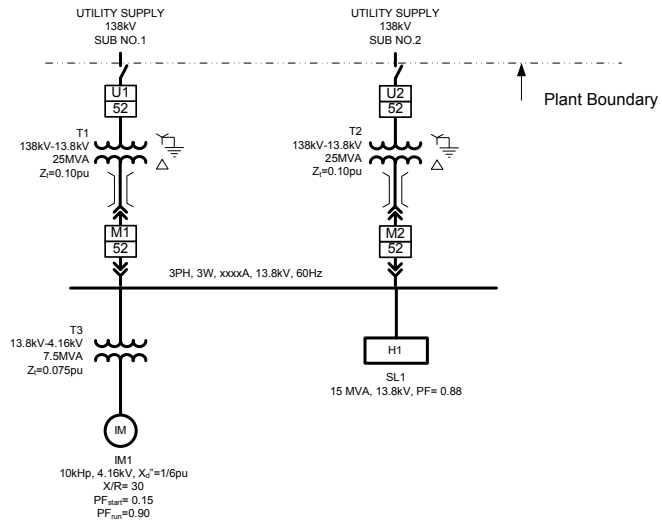
# Motor Starting

- Typical Application – Comparison



# Motor Starting

- Captive Transformer

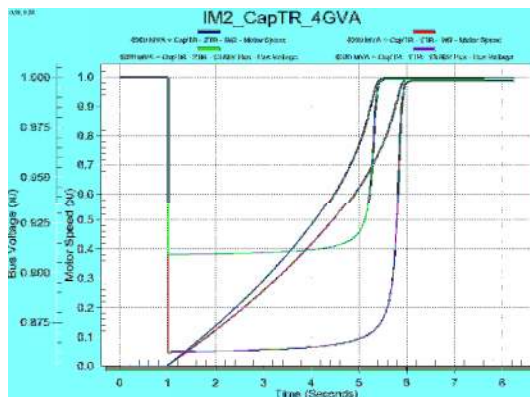


## Motor Starting

- Captive Transformer – Cont.
  - Condition 1 –  $S_{sc}=4000$  MVA,  $X/R=5$ 
    - Both T's On-Line
    - One T On-Line
  - Condition 2 –  $S_{sc}=1000$  MVA,  $X/R=5$ 
    - Both T's On-Line
    - One T On-Line
  - Condition 3 - Change voltage from 13.8 kV to 13.2 kV

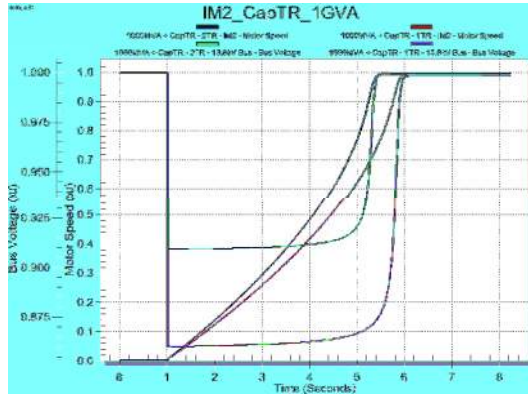
## Motor Starting

- Captive Transformer – Cont.
  - Condition 1 –  $S_{sc}=4000$  MVA,  $X/R=5$ 
    - Both T's On-Line
    - One T On-Line



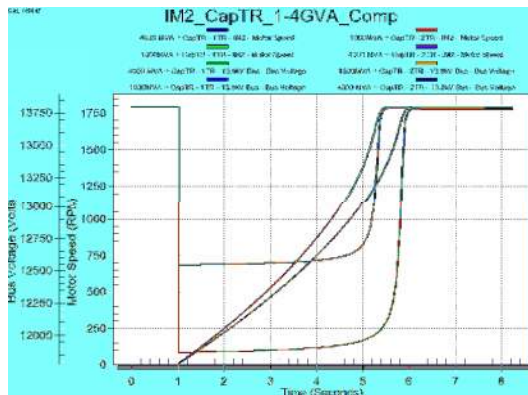
## Motor Starting

- Captive Transformer – Cont.
  - Condition 2 –  $S_{sc}=1000$  MVA,  $X/R=5$ 
    - o Both T's On-Line
    - o One T On-Line



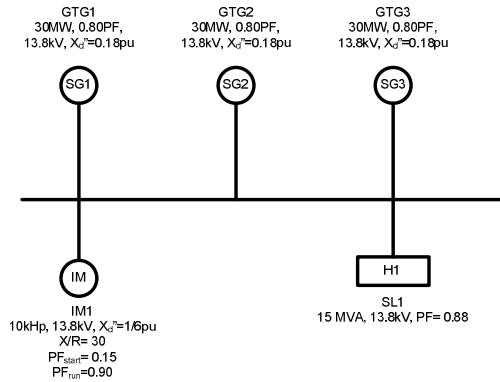
## Motor Starting

- Captive Transformer – Comparison



## Motor Starting

### Islanded Systems



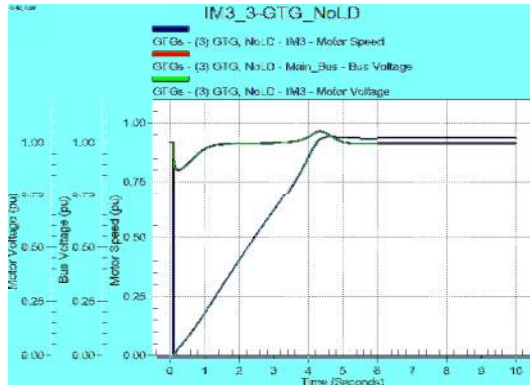
## Motor Starting

### Typical Application – Cont.

- Condition 1 (TMS)
  - Large IM start only, no other loads
  - (3) GTGs On-Line
- Condition 2 (TMS)
  - Large IM start only, no other loads
  - (2) GTGs On-Line
- Condition 3 (TMS)
  - Large IM start only with other loads
  - (2) GTGs On-Line
- Condition 4 (TMS/ISIM)
  - Motor inrush 6x FLA
  - Motor inrush 3x FLA

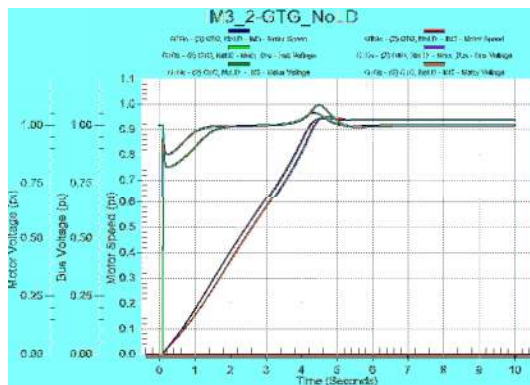
## Motor Starting

- Condition 1
  - Large IM start only, no other loads
  - (3) GTGs On-Line



## Motor Starting

- Condition 2
  - Large IM start only, no other loads
  - (2) GTGs On-Line

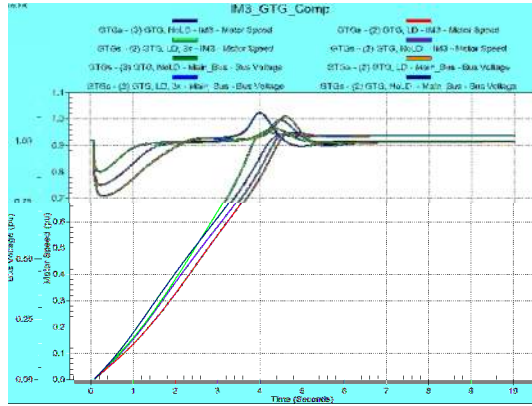






## Motor Starting

- Condition 4
  - Motor inrush 6x FLA
  - Motor inrush 3x FLA

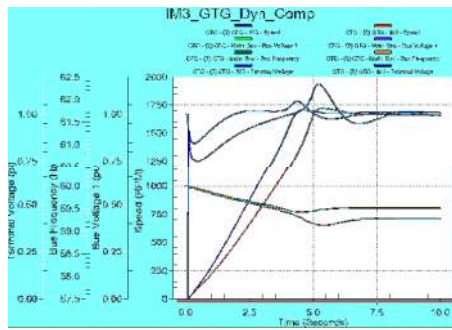
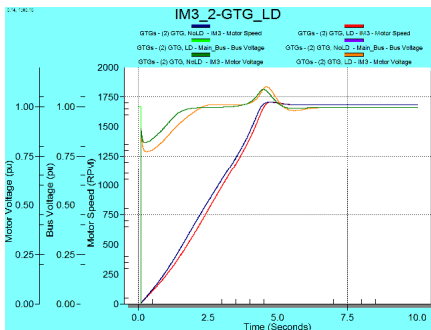


## Motor Starting

- Comparison – TMS vs. ISIM

### Transient Motor Starting

### Dynamic Motor Starting



## Motor Starting

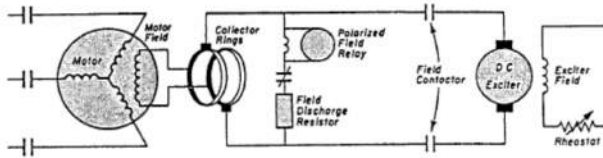
- Comparison -  
System Element Models vs. Calculation Method

Power System Elements	TS - Transient Stability	Dynamic Motor Acceleration	Static Motor Acceleration	Notes
	ISIM - Industrial Simulation	TMS - Transient Motor Starting		
Generator	Dynamic Model	Constant Voltage Behind $X_d'$	Constant Voltage Behind $X_d'$	
Exciter/ Governor	Dynamic Model	Not Modeled	Not Modeled	
Utility Grid/ Interties	Constant Voltage Behind $X''$ , or $X'$	Constant Voltage Behind $X''$ , or $X'$	Constant Voltage Behind $X''$ , or $X'$	
Running Motors ( $>0.90 \times \text{RPMn}$ )	Dynamic Model or Constant kVA	Constant kVA	Constant kVA	
	Single Brach, Double Branch, or Block Diagram	Single Brach, Double Branch, or Block Diagram	Single Brach, Double Branch, or Block Diagram	
Starting Motors	Single1, Single2, DBL1, & DBL@ Models	Single1, Single2, DBL1, & DBL@ Models	Locked-Rotor Z and Power Factor	
	Single Brach, Double Branch, or Block Diagram	Single Brach, Double Branch, or Block Diagram	Single Brach, Double Branch, or Block Diagram	
Starters & Control Models	Not Modeled	Modeled	Modeled	
	Modeled			

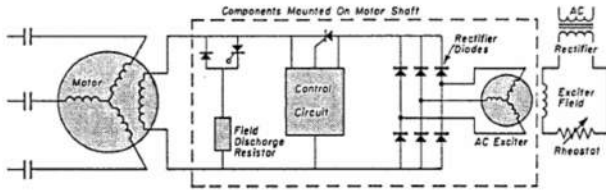
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## Synchronous Motor Starting Methods

## Synchronous Motor Starting

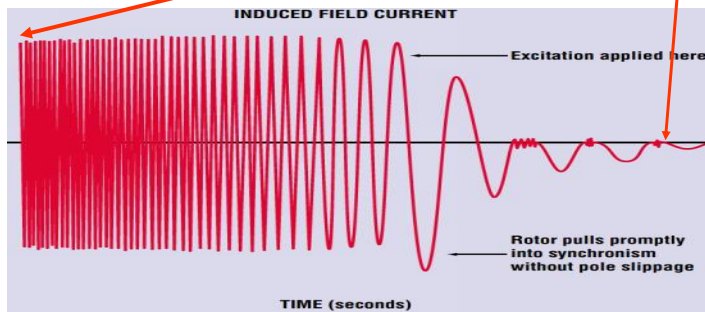
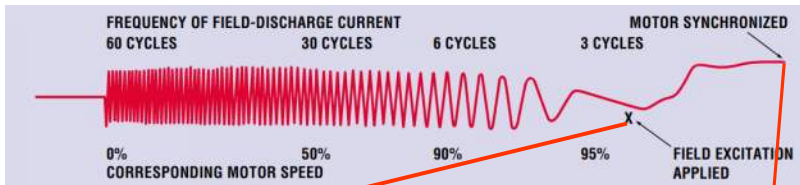


BRUSH-TYPE SYNCHRONOUS MOTOR

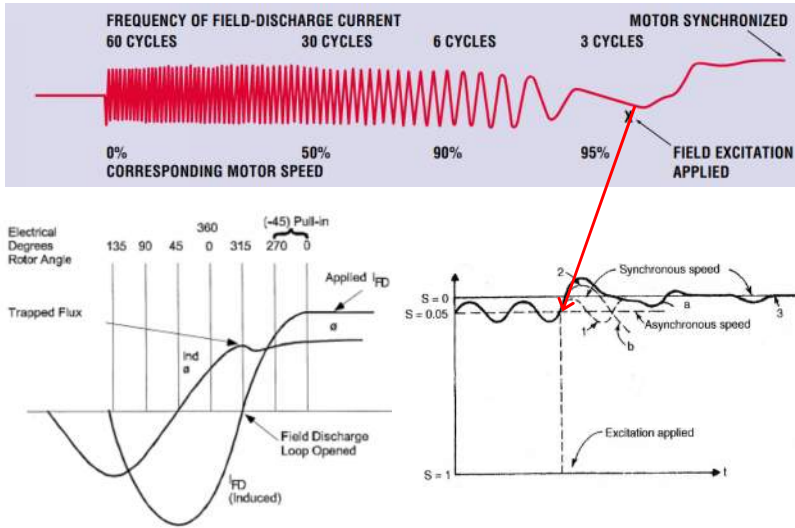


BRUSHLESS-TYPE SYNCHRONOUS MOTOR

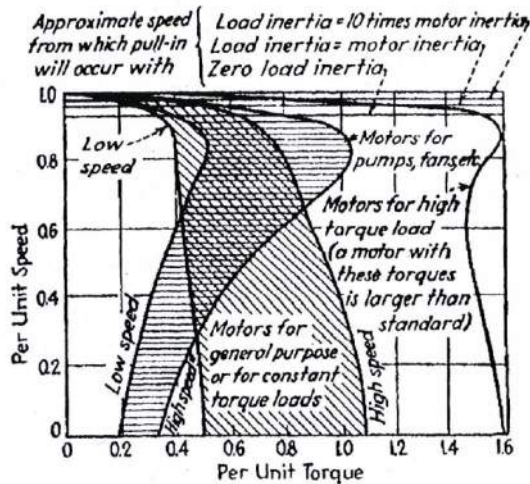
## Synchronous Motor Starting



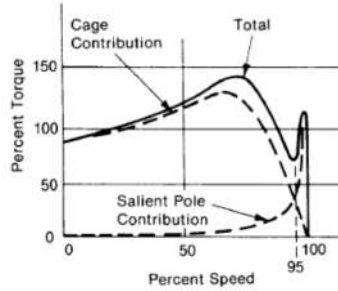
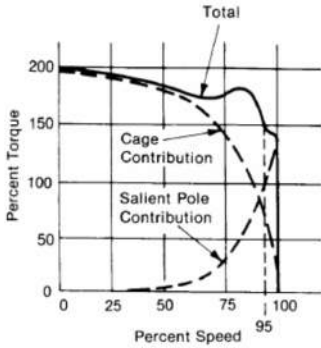
# Synchronous Motor Starting



# Synchronous Motor Starting

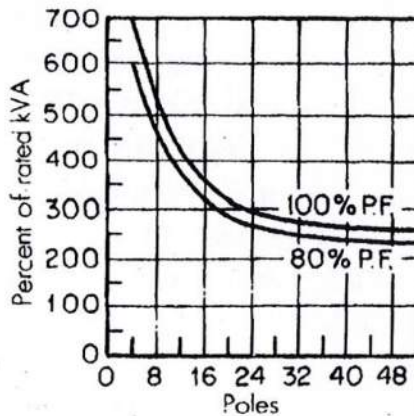


## Synchronous Motor Starting

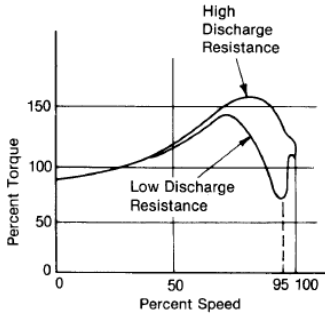


## Synchronous Motor Starting

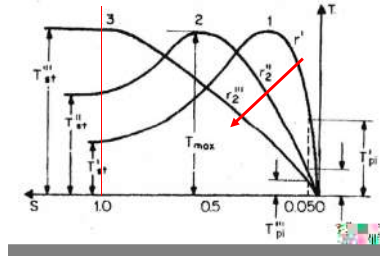
- Approximate starting torque in kVA of SM



## Synchronous Motor Starting



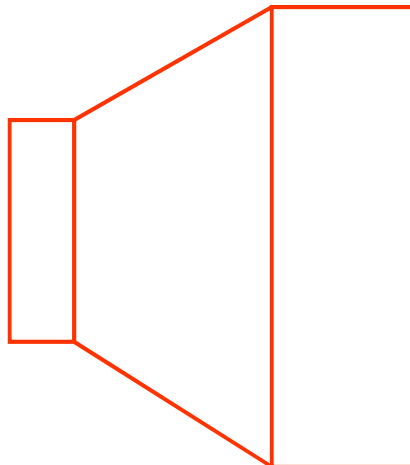
Starting Torque Control via Discharge Resistor

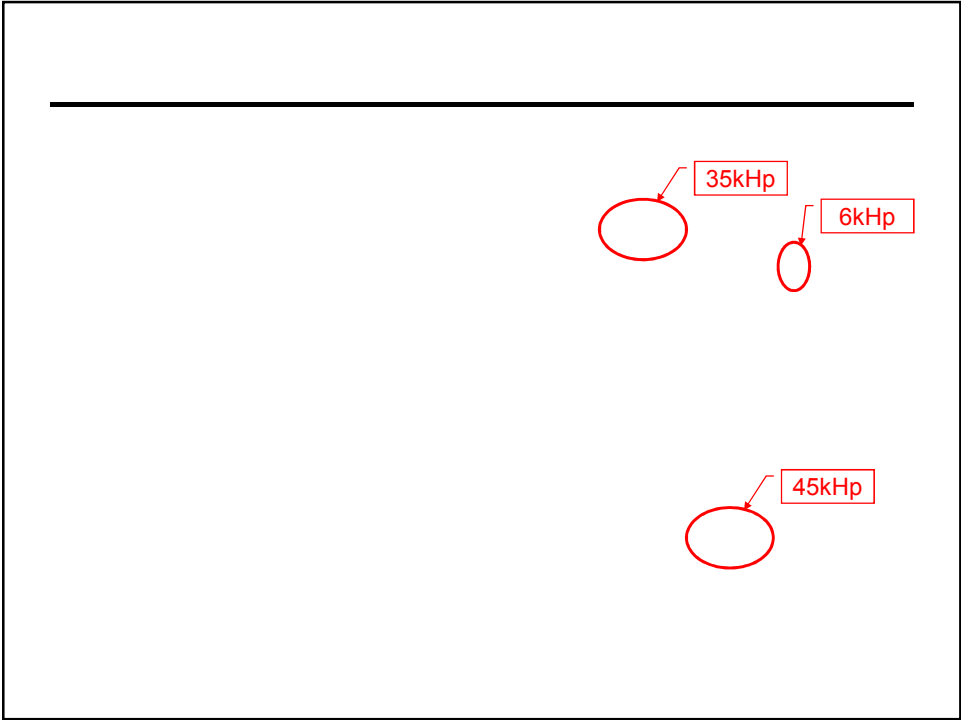


Starting and Pull-In Torque control by resistivity of damper winding material

## Synchronous Motor Starting

- Example of damper and field winding interaction





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**Special Consideration**

## **Special Consideration**

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- Harmonic Flux

## **Special Consideration**

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- Harmonic Torques



## **Special Consideration**

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- Typical Slot Design

## **Special Consideration**

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- Typical Slot Design

## **Special Consideration**

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- Others:
  - Number of starts (or restarts)
  - Process special requirements vs. thermal lockout
  - System stability
  - System harmonic resonances
  - System sub-synchronous resonance

---

**Calculations, Data, Simulation, Applications**

## Calculations, Simulation, Applications

---

### Software

- ETAP, SKM/PTW
  - Sufficient for DOL starting and reduce voltage discrete calculations; not applicable for RVSS starters analysis
- SPICE, MATLAB, EMTP-ATP
  - Applicable for motor starting analysis with control loops considerations, can predict waveforms and effect on power system
- Custom Software
  - Write own software utilizing Compilers or high level language (i.e. Matlab)
- Hand Calculations
  - Utilize MathCad or other mathematical analysis package; must understand electrometrical theory

## Calculations, Simulation, Applications

---

### Equivalent Schematic Parameters – Calculations

#### Motor Data

$$P_n := 1200 \cdot \text{Hp}$$

$$f_n := 60 \cdot \text{Hz}$$

$$f_s := f_n$$

$$p := 2$$

$$P_n = 895.2 \text{ kW}$$

$$U_n := 4 \text{ kV}$$

$$m_{gr} := 1.8$$

$$PF_n := 0.87$$

$$n_n := 1789 \cdot \text{RPM}$$

$$\eta_n := 0.9595$$

$$i_r := 5.0$$

$$m_r := 0.7$$

## Calculations, Simulation, Applications

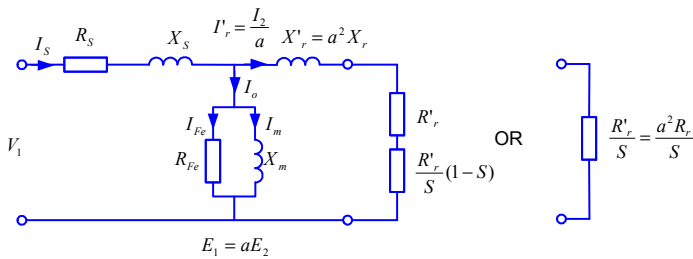
### Equivalent Schematic Parameters – Calculations

#### Nominal Parameters

$I_n := \frac{P_n}{\eta_n \cdot \sqrt{3} \cdot U_n \cdot PF_n}$	$I_n = 154.79A$	
$T_n := \frac{P_n}{\frac{\pi \cdot n_n}{30}}$	$T_n = 4778.38N \cdot m$	$T_n = 3524.36ft \cdot lbf$
$\omega_s := \frac{2 \cdot \pi \cdot f_s}{p}$	$n_s := \frac{60 \cdot f_s}{p}$	$\omega_s = 188.5s^{-1}$ $n_s = 1800RPM$
$s_n := \frac{n_s - n_n}{n_n}$	$s_n = 0.0061$	
$Z_z := \frac{U_n}{\sqrt{3} \cdot i_r \cdot I_n}$	$Z_z = 2.98\Omega$	

## Calculations, Simulation, Applications

### Equivalent Schematic Parameters – Calculations



## Calculations, Simulation, Applications

### Equivalent Schematic Parameters – Calculations

**Iteration starting parameters:**

$$R_z := 0.001 \cdot \Omega \quad X_z := 0.2 \cdot \Omega$$

Given { From motor equivalent diagram }

$$Z_z = \sqrt{R_z^2 + X_z^2}$$

$$m_p \cdot T_n = \frac{3}{\omega_s} \cdot \left( \frac{U_n}{\sqrt{3}} \right)^2 \cdot \frac{R_z}{R_z^2 + X_z^2}$$

$$\begin{pmatrix} R_z \\ X_z \end{pmatrix} := \text{Find}(R_z, X_z) \quad R_z = 0.7 \Omega \quad X_z = 2.9 \Omega$$

	Design Class				Wound Rotor
	A	B	C	D	
$X_r/X_L$	0.5	0.4	0.3	0.5	0.5
$X_z/X_L$	0.5	0.6	0.7	0.5	0.5

## Calculations, Simulation, Applications

### Equivalent Schematic Parameters – Calculations

$$R_s := R_z \cdot \frac{5}{10} \quad R_s = 0.35 \Omega$$

$$X_s := X_z \cdot \frac{5}{10} \quad X_s = 1.45 \Omega$$

$$R'_r := R_s \quad X'_r := X_s$$

$$\Delta P_n := P_n \cdot \frac{1 - \eta_n}{\eta_n} \quad \Delta P_n = 37.79 \text{ kW}$$

$$\Delta P_{u_n} := \frac{3}{2} \cdot I_n^2 \cdot R_z \quad \Delta P_{u_n} = 25.22 \text{ kW}$$

$$\Delta P_m := 0.01 P_n \quad \Delta P_m = 8.952 \text{ kW}$$

$$\Delta P_{\text{fen}} := \Delta P_n - \Delta P_{u_n} - \Delta P_m \quad \Delta P_{\text{fen}} = 3.61 \text{ kW}$$

$$R_{fc} := \frac{U_n^2}{\Delta P_{\text{fen}}} \quad R_{fc} = 4426.97 \Omega$$

$$I_{fc} := \frac{U_n}{\sqrt{3} \cdot R_{fc}} \quad I_{fc} = 0.52 \text{ A}$$

$$I_0 := 20\% \cdot I_n \quad I_0 = 30.96 \text{ A}$$

$$I_m := \sqrt{I_0^2 - I_{fc}^2} \quad I_m = 30.95 \text{ A}$$

$$X_m := \frac{U_n}{\sqrt{3} \cdot I_m} \quad X_m = 74.61 \Omega$$

## Calculations, Simulation, Applications

### Equivalent Schematic Parameters – Calculations

$$Z_s(f) := R_s + \frac{f}{f_n} \cdot j \cdot X_s \quad \text{Change "f" only when analysis with VSD}$$

$$Z_t(s, f) := \frac{R'_t}{s} + \frac{f}{f_n} \cdot j \cdot X'_t$$

$$Z_m := \frac{R_{fe} \cdot X_m \cdot j}{R_{fe} + X_m \cdot j}$$

$$Z_m(f) := \frac{\left(\frac{f}{f_n}\right)^{0.7} \cdot R_{fe} \cdot \frac{f}{f_n} \cdot X_m \cdot j}{\left(\frac{f}{f_n}\right)^{0.7} \cdot R_{fe} + \frac{f}{f_n} \cdot X_m \cdot j}$$

$$\underline{\underline{Z}}(s, f) := Z_s(f) + \frac{Z_t(s, f) \cdot Z_m(f)}{Z_t(s, f) + Z_m(f)}$$

$$U(f) := U_n \cdot \frac{f}{f_n}$$

$$n(s, f) := \frac{60 \cdot f}{p} \cdot (1 - s)$$

$$I_s(s, f) := \frac{U(f)}{\sqrt{3} \cdot Z(s, f)}$$

$$I'_t(s, f) := I_s(s, f) \cdot \frac{Z_m(f)}{Z_t(s, f) + Z_m(f)}$$

$$T_d(s, f) := \frac{3 \cdot p}{2 \cdot \pi \cdot f} \cdot (|I'_t(s, f)|)^2 \cdot \text{Re}(Z_t(s, f))$$

## Calculations, Simulation, Applications

### Equivalent Schematic Parameters – Calculations

#### Nominal Slip Calcs

$$\underline{\underline{s}} := 0.0100$$

Given

$$T_e(s, f_n) \cdot \frac{\pi \cdot n(s, f_n)}{30} = P_n + \Delta P_m$$

$$\underline{\underline{s}}_{\text{opt}} := \text{Find}(s)$$

$$s_n = 0.0228$$

$$\underline{\underline{I}}_n := |I_s(s_n, f_n)|$$

$$I_n = 147.59 \text{ A}$$

$$\underline{\underline{T}}_n := T_e(s_n, f_n)$$

$$T_n = 4908.38 \text{ N} \cdot \text{m}$$

# Calculations, Simulation, Applications

## Equivalent Schematic Parameters – IEEE 112

Form F-3  
Method F: Solution of Equivalent Circuit

Motor Serial No. \_\_\_\_\_ Model No. \_\_\_\_\_  
Type \_\_\_\_\_ Horsepower \_\_\_\_\_ Voltage \_\_\_\_\_ Synchronous Speed \_\_\_\_\_ Frequency \_\_\_\_\_ m-Phase \_\_\_\_\_  
Before starting calculations, fill in following items, obtained from previous tests.  
 $V_s$  \_\_\_\_\_ V = phase volts  $I_s$  \_\_\_\_\_ and  $W_{TLL}$  \_\_\_\_\_ from Form F-2  
also all the items below which are marked with an asterisk.  
Assume a value of  $s$  corresponding to expected full-load speed for full-load point and proportional values for other loads. For motor operation  $s$  is positive, as are all other numeric values below. Numbers in () represent item numbers.

Item	Description	1	2	3	4	5	6	7	8
1	$\mu = \omega / \omega_s$ , per unit								
2	$s$ , %								
* 3	$Z_s$								
4	$Z^2 = (2)^2 + (3)^2$								
5	$R_s = (2)/(4)$								
* 6	$Z_{sc}$								
7	$Z^2 = (6)^2 + (8)^2$								
8	$X_s = (2)/(4)$								
* 9	$-bR =$								
10	$-b = (8) + (9)$								
11	$Y^2 = (7)^2 + (10)^2$								
12	$R_c = (7)/(11)$								
*13	$r =$ resistance per phase								
14	$r = (12) + (13)$								
15	$R_{sc} = (10)/(11)$								
*16	$Z_{sc}$								
17	$Z^2 = (15)^2 + (16)^2$								
18	$Z = \sqrt{(17)^2 + (17)^2}$								
19	$R = W_s/(18)$								
20	$W_s = I_s^2 \sqrt{(4)^2 + (11)^2}$								
21	Watts Input = $m \cdot (19)^2 \cdot (14)$								
22	Sec. Input = $m \cdot (20)^2 \cdot (2)$								
23	Stator I <sup>2</sup> R = $m \cdot (19)^2 \cdot (13)$								
24	Core Loss = $m \cdot (19)^2 \cdot (6)/(11)$								
25	Sec. I <sup>2</sup> R = $(13) \cdot (22)$								
26	Friction and Windage Loss								
27	$W_{FL} = W_{TLL} \cdot [(20)/(I_s)]^2$								
28	Losses = Items (23) Through (27)								
29	Watts Output = (21) - (28)								
30	Eff. (%) = $100 \cdot [(1) \cdot (29)/(21)]$								
31	PF (%) = $100 \cdot (14)/(18)$								
32	HP Output = (29)/746								
33	Speed = $(1 - (1)) \cdot \text{Sync. speed}$								
34	Torque = $K_T \cdot (29)/(33)$								

# Calculations, Simulation, Applications

## Equivalent Schematic Parameters – Sensitivity Calculations

IEEE TRANSACTIONS ON INDUSTRY APPLICATIONS, VOL. 25, NO. 6, NOVEMBER/DECEMBER 1989

1035

## Parameter Estimation for Induction Machines Based on Sensitivity Analysis

SOMCHAI ANSUI, MEMBER, IEEE, FARROKH SHOKOEH, SENIOR MEMBER, IEEE, AND  
ROLAND SCHINZINGER, SENIOR MEMBER, IEEE

Basis for ETAP Motor Estimating Calcs

## Calculations, Simulation, Applications

### Equivalent Schematic Parameters – Sensitivity Calculations

```
C:\DOCUME~1\ROBERT-1\LOCALS~1\Temp\TEMPOR-3.ZIP\WINDSYNW.EXE
```

Output data file	6 ch. name + ext		
Rotor type	enter w/s/d/b	single cage	w = wound
System frequency	Hz	60	s = single cage
Rated voltage L-L rms	kV	10.0	d = double cage
Rated horsepower	hp	1000	b = deep bar
Synchronous speed rpm	rpm	1800	
Power factor	p.u.	0.9	
Full load slip	%	1.0	
Full load eff'y < 1-slip /0.75	p.u.	0.98	
Starting current	p.u.	6.0	
Starting torque	p.u.	0.95	
Maximum torque	no entry required	p.u.	
Inertia constant H OR W		1	H = H const. kWs/kVA
Inertia constant	kWs/kVA or ft-lb^2	0.97	W = WR^2 lb-ft^2
Load torque at rated slip	p.u.	1.0	
Saturation starts at current	p.u.	2.0	

```
1 - use Up/Down keys to select, type new entry if desired
2 - use Up/Down or ENTER to accept new or old entry
3 - use hcl to erase entry
4 - after completing table press F10 to continue
5 - press Ctl-Brk at any time to quit
```

EMTP-ATP Group Software

## Calculations, Simulation, Applications

### Equivalent Schematic Parameters – Sensitivity Calculations

```
C:\DOCUME~1\ROBERT-1\LOCALS~1\Temp\TEMPOR-3.ZIP\WINDSYNW.EXE
```

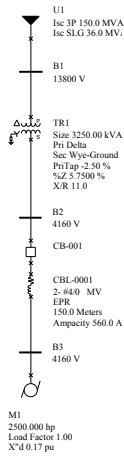
Stator resistance	p.u.	0.008182
Stator leakage reactance x1	unsaturated * p.u.	0.057759
Stator leakage reactance x1sat	saturated * p.u.	0.024052
Rotor x1's same as stator		
Magnetizing reactance xm	no saturation p.u.	3.523040
Rotor outer cage resistance r1	p.u.	0.025503
Rotor inner cage resistance r2	p.u.	0.000000
Rotor inner cage reactance x2.	p.u.	0.000000
Rotor type	single cage	

```
* these are the components of the leakage reactance
  the total unsaturated value for both the stator and rotor is 2 * x1
  while the total saturated value is x1 + x1s, where x1s is based on
  saturation at the value of the starting current
  no saturation is taken for the rotor inner cage reactance
press any key to continue
```

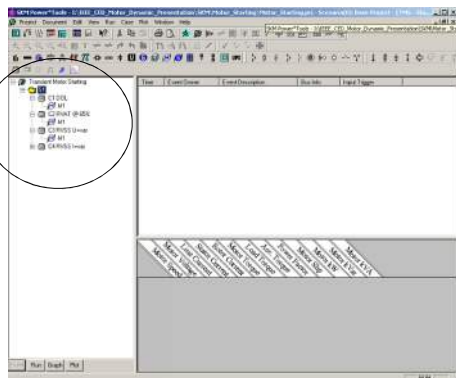
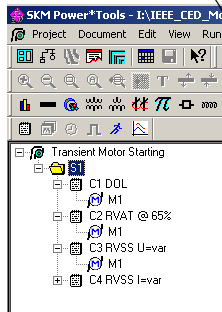
EMTP-ATP Group Software



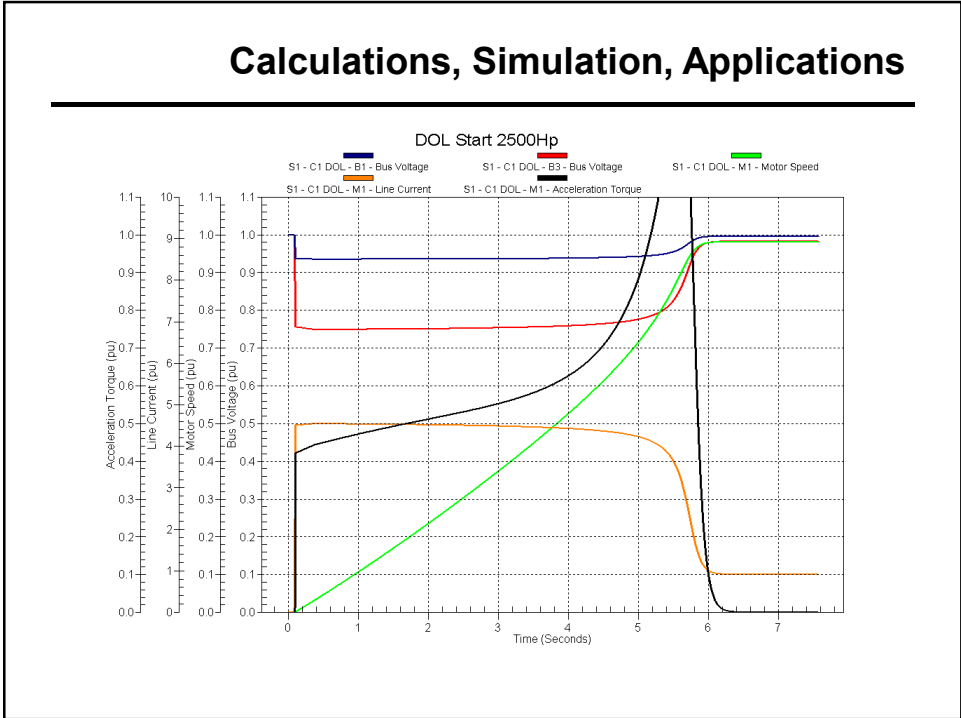
# Calculations, Simulation, Applications



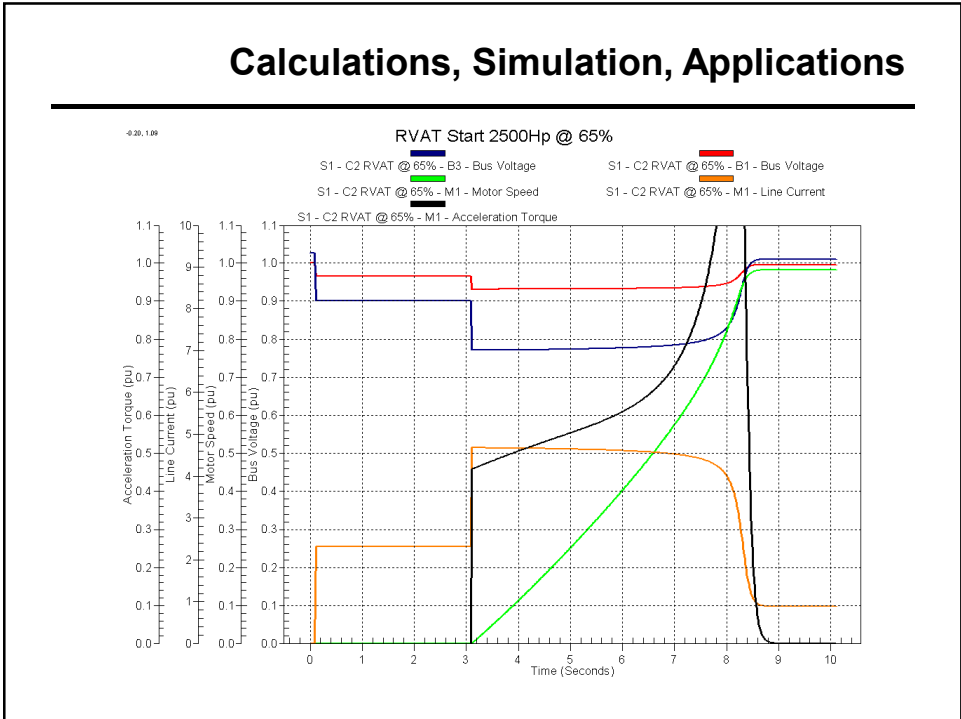
# Calculations, Simulation, Applications



# Calculations, Simulation, Applications



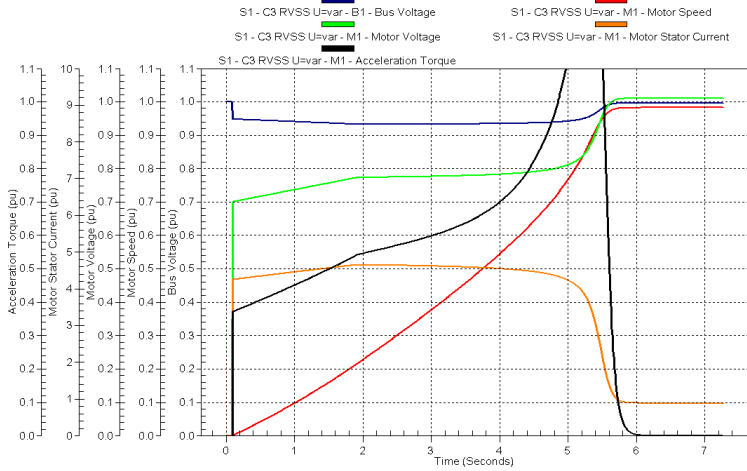
# Calculations, Simulation, Applications



# Calculations, Simulation, Applications

541.107

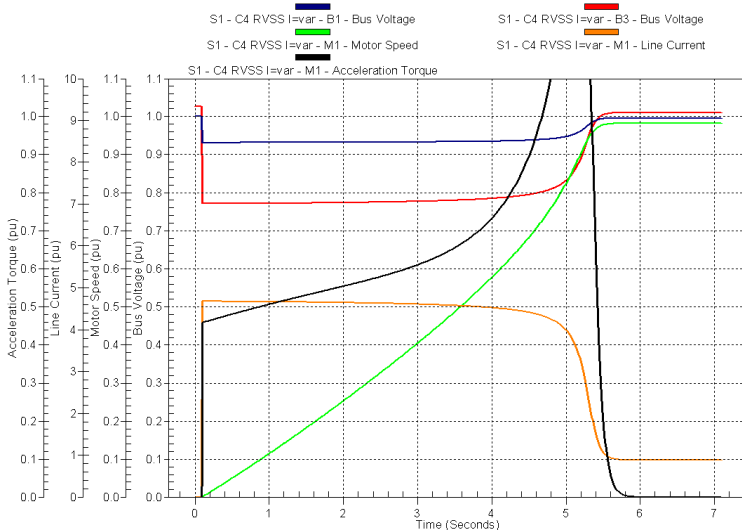
## RVSS Start 2500Hp @ U=var



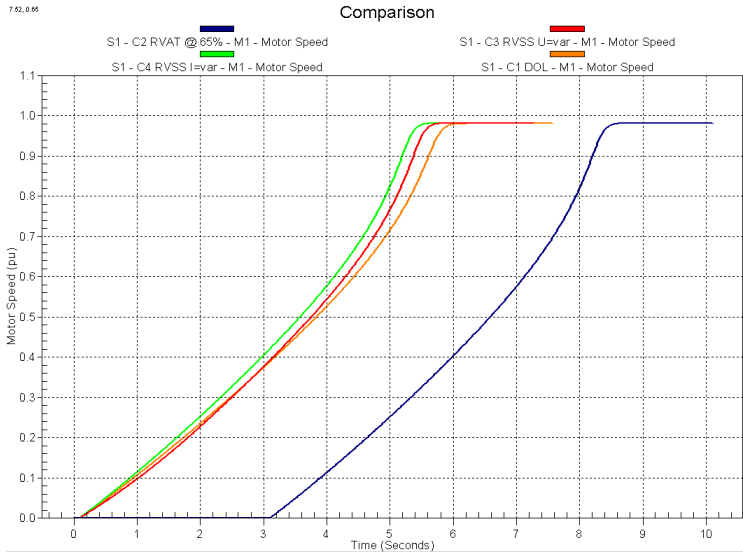
# Calculations, Simulation, Applications

3.12.0.29

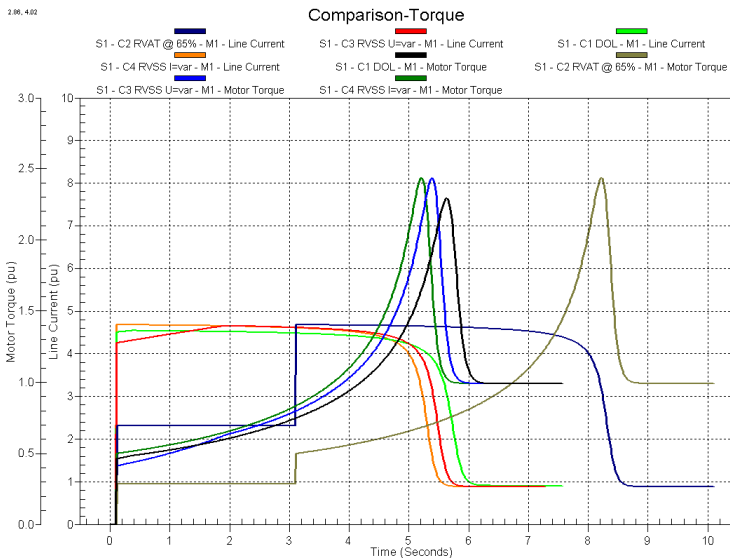
## RVSS Start 2500Hp @ I=var



# Calculations, Simulation, Applications



# Calculations, Simulation, Applications



# Calculations, Simulation, Applications

234.002

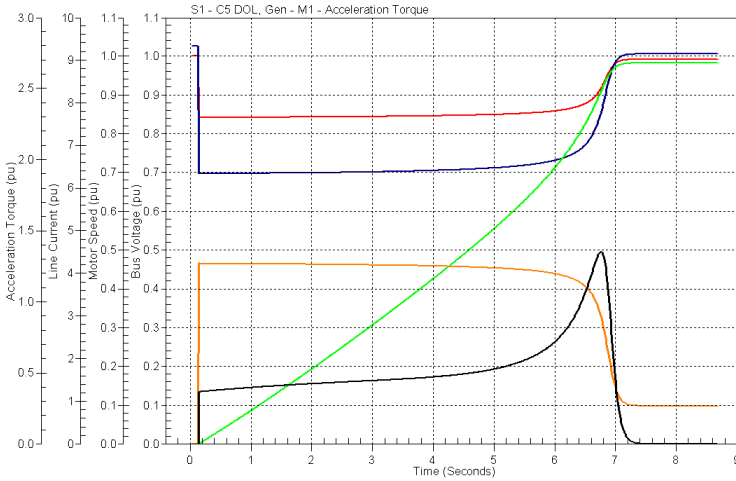
## DOL Start 2500Hp (Gen)

S1 - C5 DOL, Gen - B3 - Bus Voltage

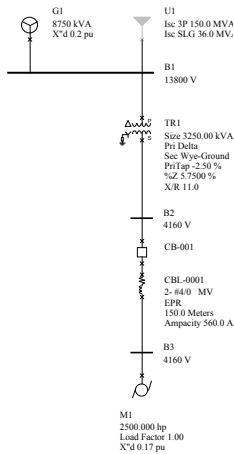
S1 - C5 DOL, Gen - B1 - Bus Voltage

S1 - C5 DOL, Gen - M1 - Motor Speed

S1 - C5 DOL, Gen - M1 - Line Current

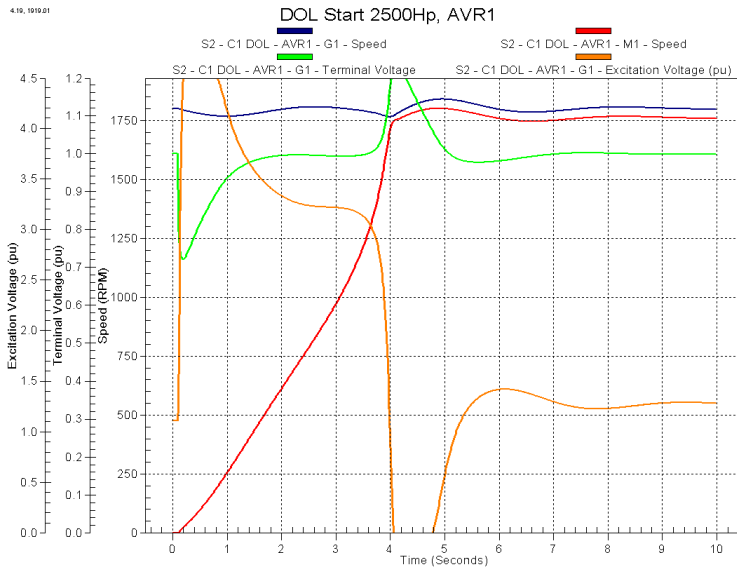


# Calculations, Simulation, Applications



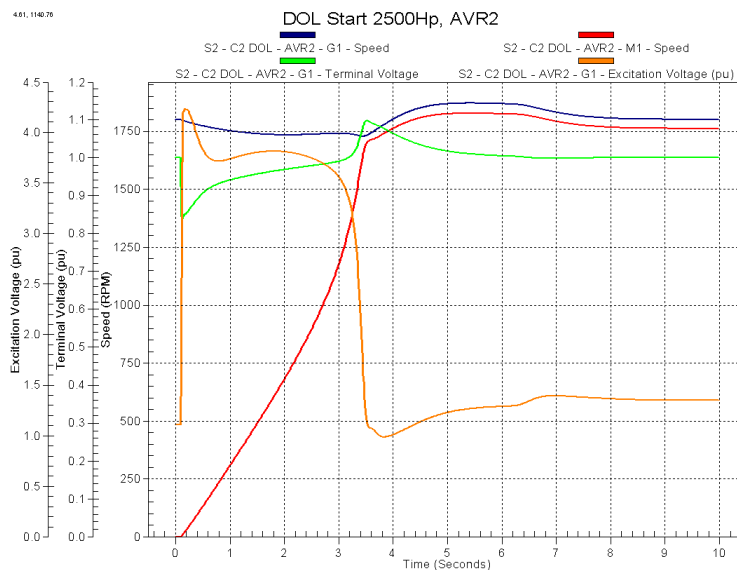
# Calculations, Simulation, Applications

419, 101921

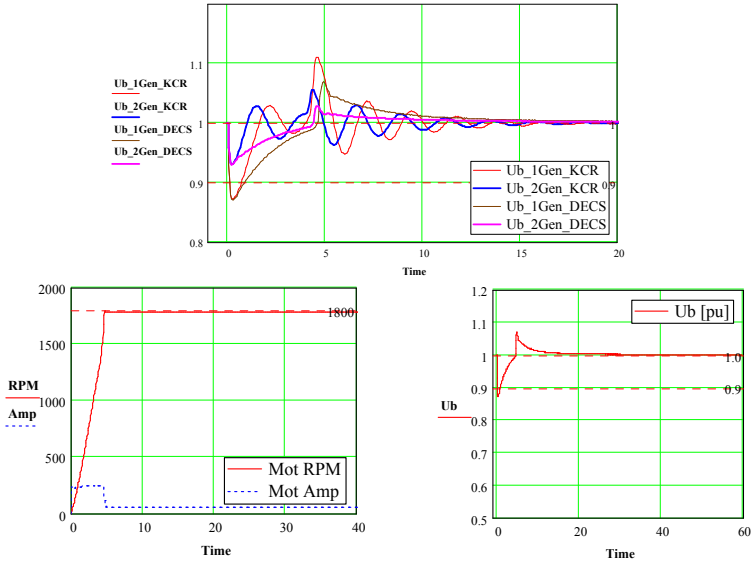


# Calculations, Simulation, Applications

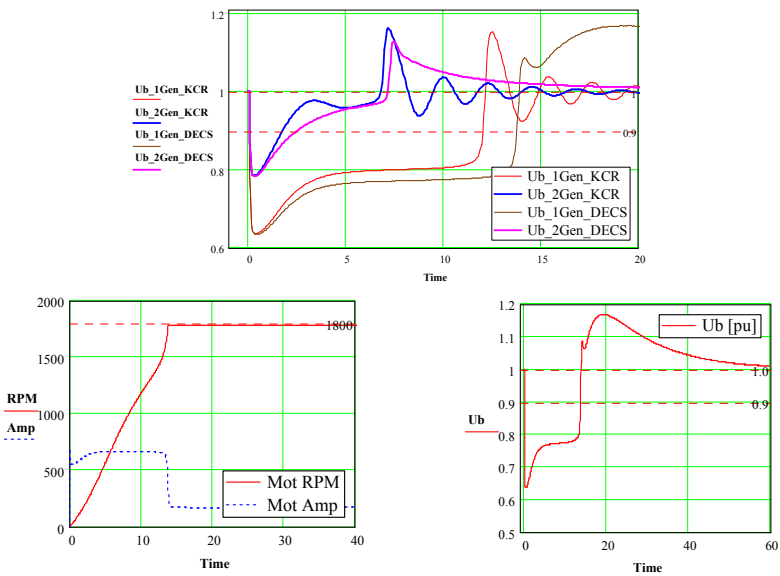
481, 114076



# Calculations, Simulation, Applications

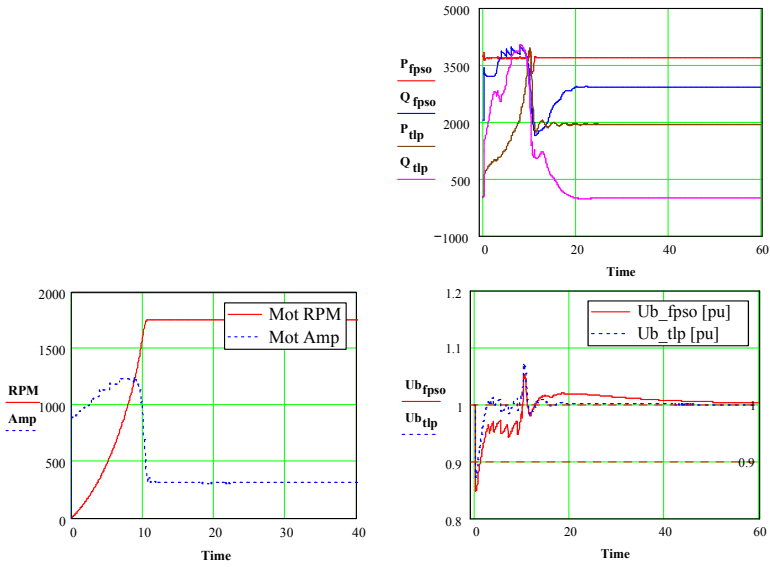


# Calculations, Simulation, Applications



# Calculations, Simulation, Applications

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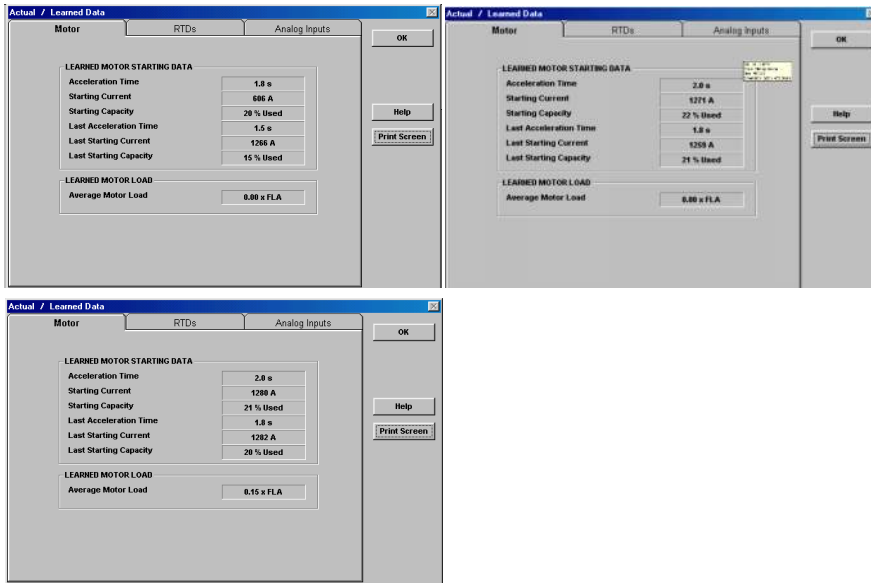


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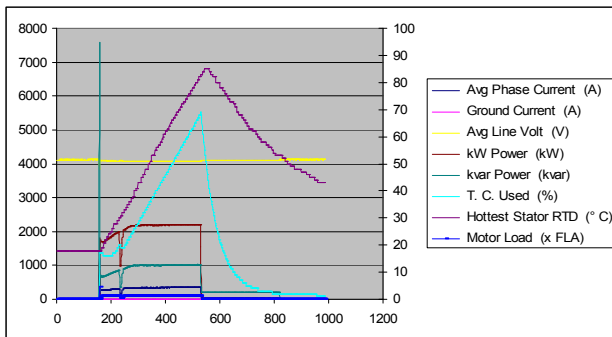
## Testing/Protection



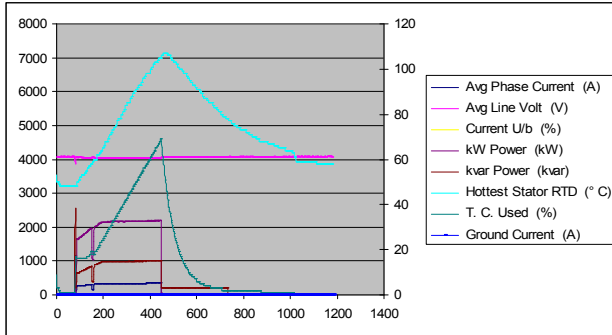
# Testing/Protection



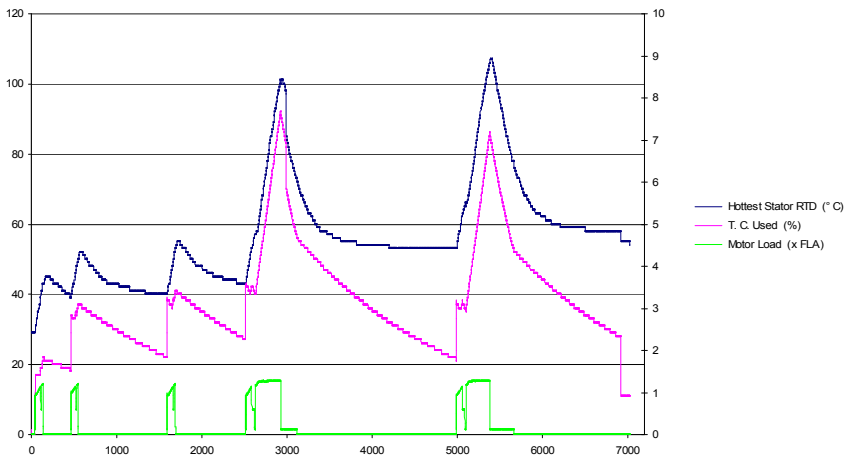
# Testing/Protection



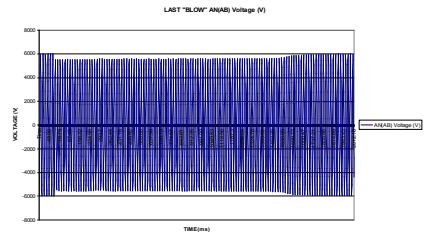
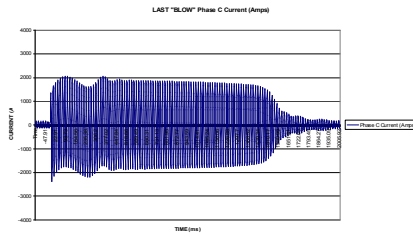
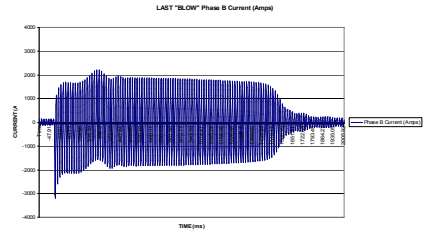
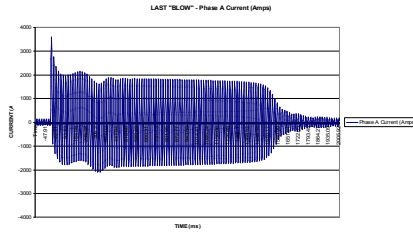
## Testing/Protection



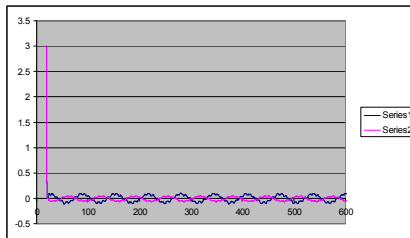
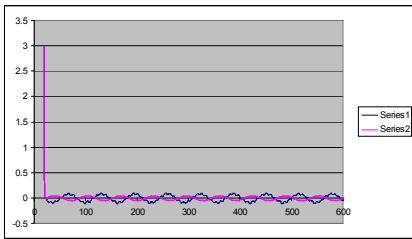
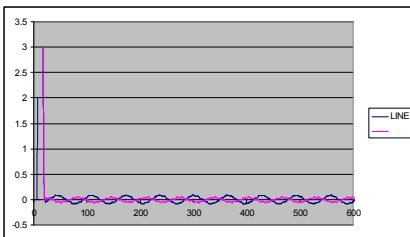
## Testing/Protection



# Testing/Protection



# Testing/Protection



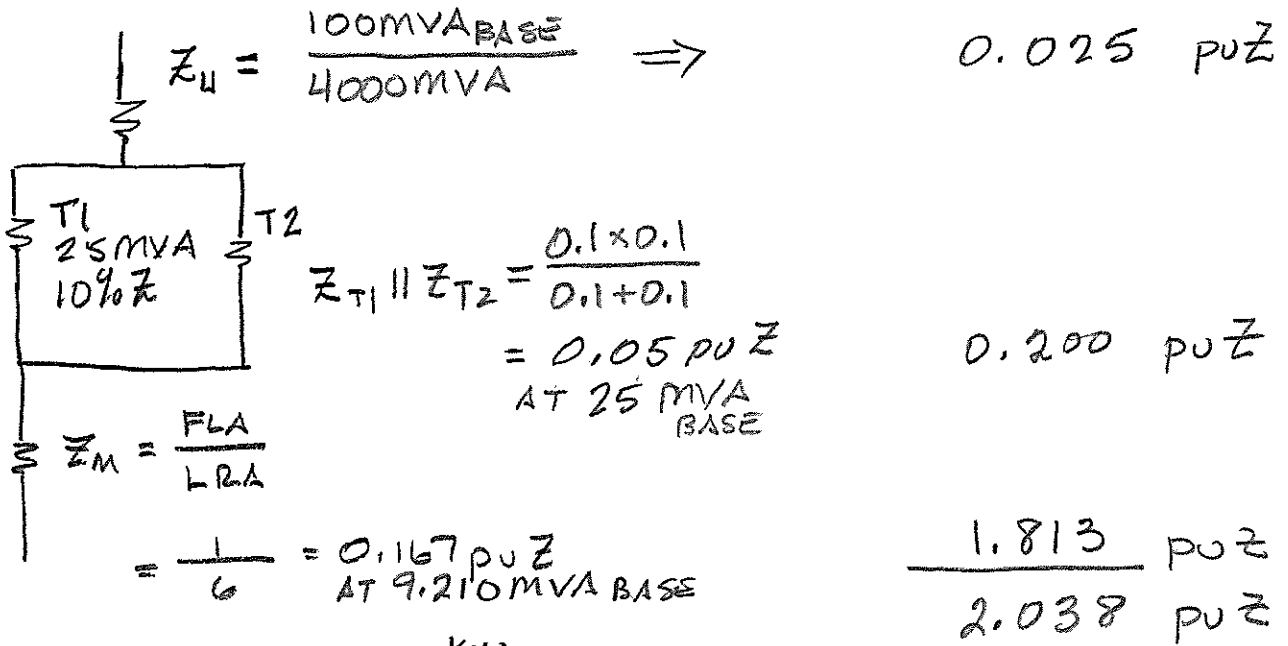
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## Questions?

## References

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100MVA BASE

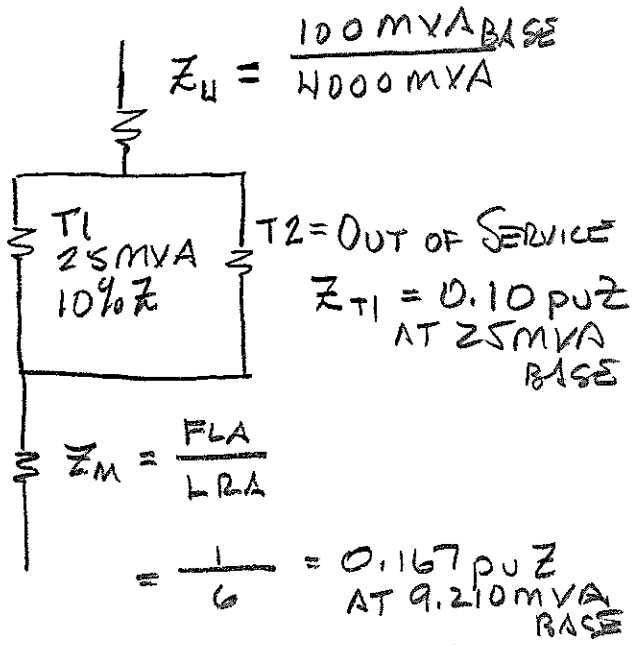


$$\text{MVA} = \frac{10\text{KHP} \times 0.746 \frac{\text{KW}}{\text{HP}}}{0.9\text{PF} \times 0.9\text{EFF}}$$
$$= 9.210\text{MVA}$$

VOLTAGE AT MOTOR TERMINALS  
(VOLTAGE DIVIDER)

$$\frac{1.813}{2.038} \times 100 = 88.96\% \text{ V}$$

MOTOR STARTING - DOL  
UTILITY 4000 MVA<sub>sc</sub>  
T1 ONLINE, T2 ONLINE



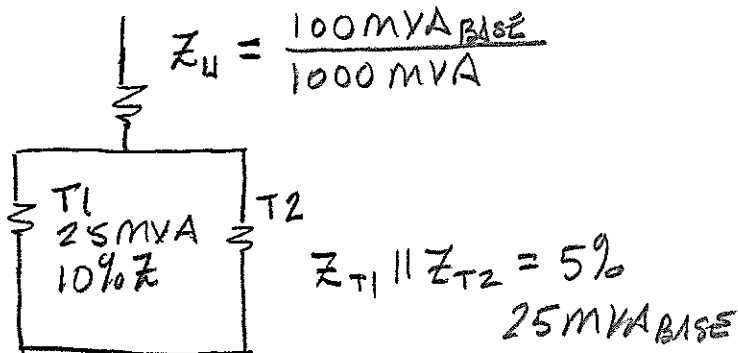
100 MVA BASE	
	0.025 pu Z
	0.400 pu Z
	<u>1.813 pu Z</u>
	2.238 pu Z

$$\begin{aligned}
 \text{MVA} &= \frac{10 \text{ KHP} \times 0.746 \frac{\text{KW}}{\text{HP}}}{0.9 \text{ PF} \times 0.9 \text{ EFF}} \\
 &= 9.210 \text{ MVA}
 \end{aligned}$$

VOLTAGE AT MOTOR TERMINALS  
(VOLTAGE DIVIDER)

$$\frac{1.813}{2.238} \times 100 = 81.019\% \text{ V}$$

MOTOR STARTING - DOL  
 UTILITY 4000 MVASC  
T1 ONLINE, T2 OUT OF SERVICE



$$0.100 \text{ puZ}$$

$$0.200 \text{ puZ}$$

$$Z_M = \frac{FLA}{LRA}$$

$$= \frac{1}{6} = 0.167 \text{ puZ}$$

9.210 MVA BASE

<u>1.813</u>	puZ
2.113	puZ

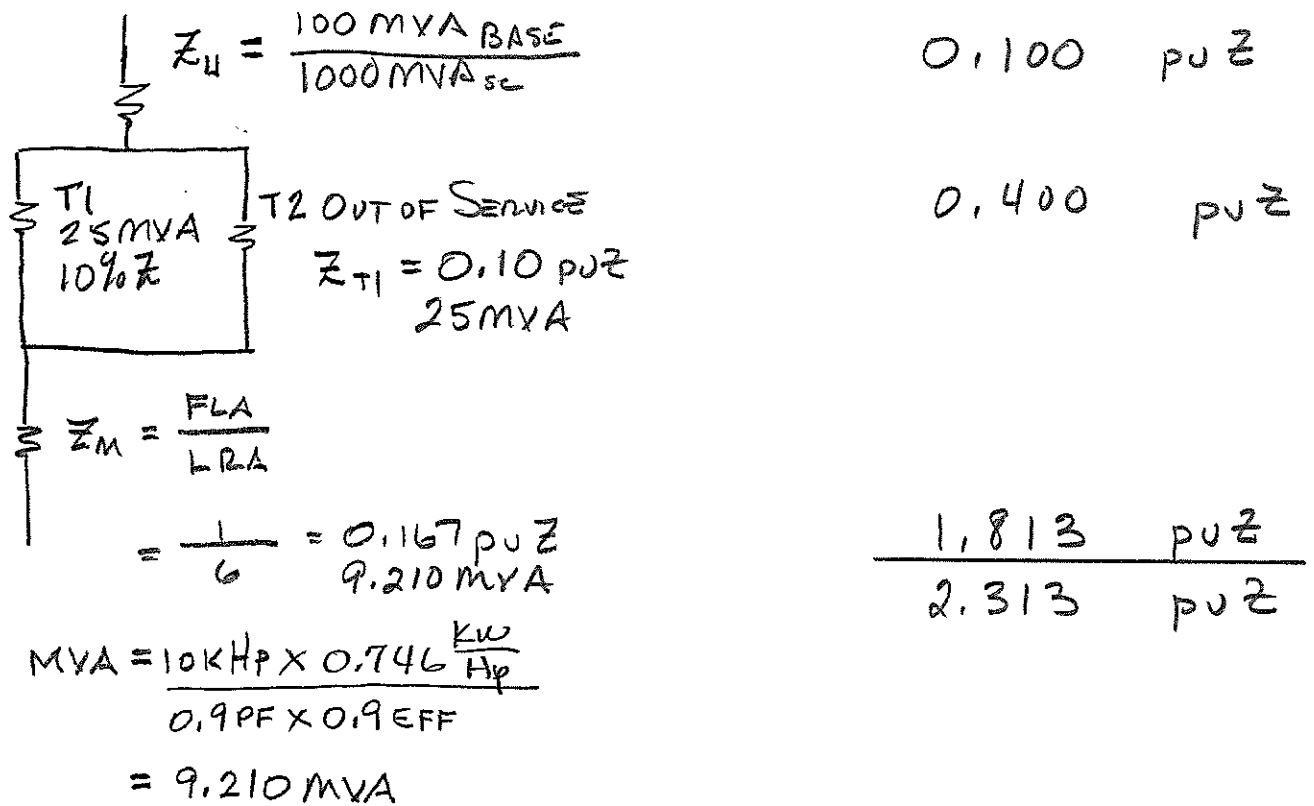
$$MVA = \frac{10 \text{ KHP} \times 0.746 \frac{\text{KW}}{\text{HP}}}{0.9 \text{ PF} \times 0.9 \text{ EFF}}$$

$$= 9.210 \text{ MVA}$$

VOLTAGE AT MOTOR TERMINALS  
(VOLTAGE DIVIDER)

$$\frac{1.813}{2.113} \times 100 = 85.80\% V$$

MOTOR STARTING - DOL  
UTILITY 1000 MVA SC  
T1 ONLINE, T2 ONLINE

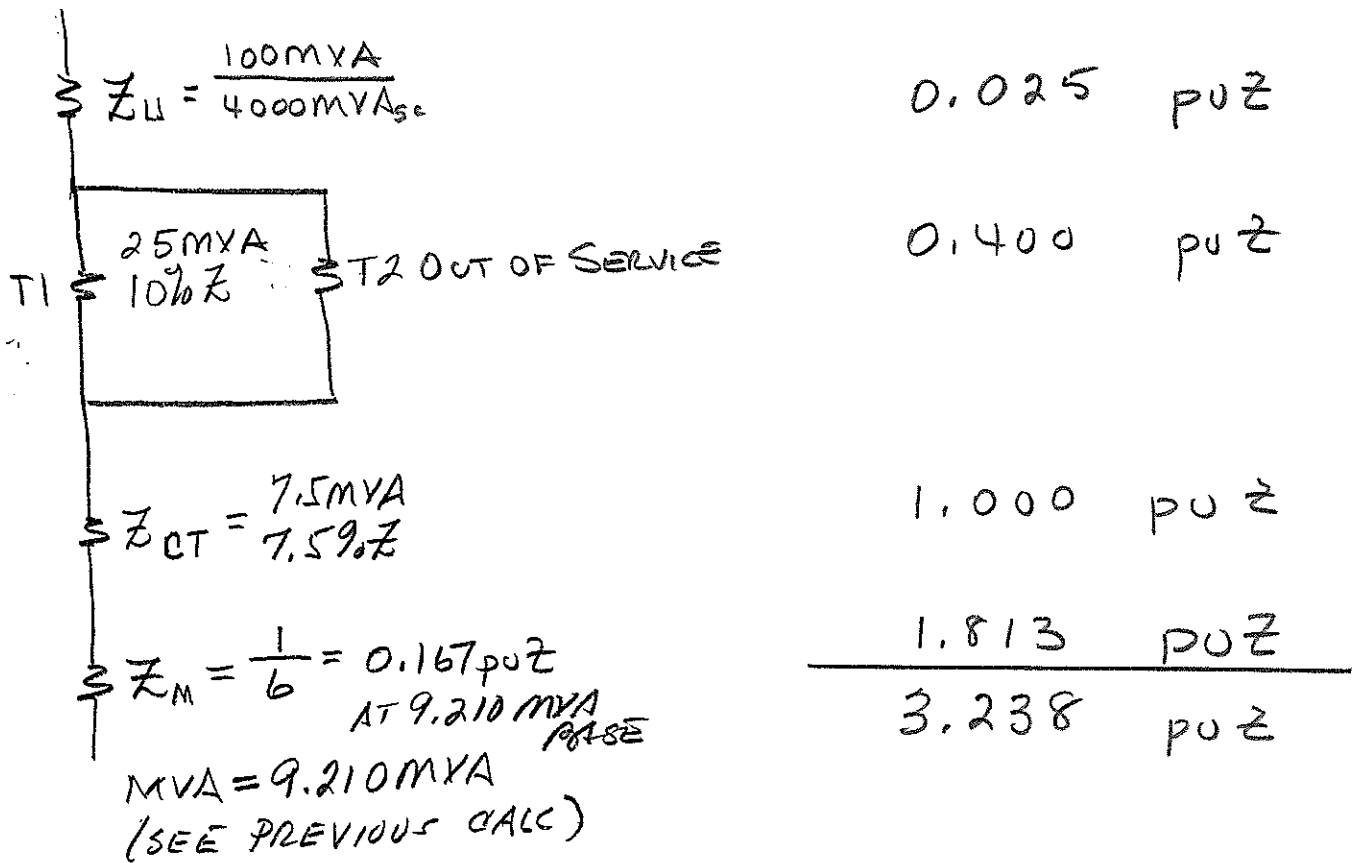


VOLTAGE AT MOTOR TERMINALS  
(VOLTAGE DIVIDER)

$$\frac{1.813}{2.313} \times 100 = 78.38\% V$$

MOTOR STARTING - DOL  
UTILITY 1000 MVA<sub>sc</sub>  
T1 ONLINE, T2 OUT OF SERVICE





VOLTAGE AT MOTOR TERMINALS  
(VOLTAGE DIVIDER)

$$\frac{1.813}{3.238} \times 100 = 55.99\% V$$

MOTOR STARTING - CAPTIVE XFMR  
UTILITY 4000 MVA<sub>sc</sub>  
T1 ONLINE, T2 OUT OF SERVICE

100 MVA BASE

$Z_U = \frac{100 \text{ MVA BASE}}{1000 \text{ MVA}}$	0.100 pu Z
	0.400 pu Z
$Z_{CT} = \frac{7.5 \text{ MVA}}{7.5\% Z} \times \frac{100 \text{ MVA}}{7.5 \text{ MVA}} \times 0.075$	1.000 pu Z
$Z_M = \frac{1}{6} = 0.167 \text{ pu Z}$ AT 9.210 MVA BASE	1.813 pu Z
MVA = 9.210 MVA (SEE PREVIOUS CALC)	<hr/> 3.313 pu Z

VOLTAGE AT MOTOR TERMINALS  
(VOLTAGE DIVIDER)

$$\frac{1.813}{3.313} \times 100 = 54.72\% V$$

MOTOR STARTING - CAPTIVE XFMR  
UTILITY 1000 MVA<sub>sc</sub>  
T1 ONLINE, T2 OUT OF SERVICE

37.5 MVA BASE

---

$$\frac{30 \text{ MW}}{0.8 \text{ PF}} = 37.5 \text{ MVA}$$

$$X' = 25\% \text{ FOR 1 GEN} \\ \text{FOR 3 GEN'S } 25\% / 3$$

$$0.0833 \text{ puZ}$$

$$Z_{10000 \text{ HP}} = 0.167 \text{ puZ} \\ 9.210 \text{ MVA}$$

$$0.6780 \text{ puZ}$$

---

FROM PREVIOUS CALC'S

$$0.7613 \text{ puZ}$$

VOLTAGE AT 13.8 KV BUS

$$\frac{0.678}{0.7613} \times 100 = 89.06\% \text{ V}$$

WITH 2 GEN'S  
10,000 HP MOTOR

$$0.125 \text{ puZ}$$

$$0.678 \text{ puZ}$$

$$0.803 \text{ puZ}$$

$$V_{13.8 \text{ KV BUS}} = \frac{0.678}{0.803} \times 100 = 84.49\% \text{ V}$$

WITH 1 GEN  
10,000 HP MOTOR

$$0.250 \text{ puZ}$$

$$0.678 \text{ puZ}$$

$$0.928 \text{ puZ}$$

$$V_{13.8 \text{ KV BUS}} = \frac{0.678}{0.928} \times 100 = 73.06\% \text{ V}$$

MOTOR STARTING  
ISLANDED SYSTEM  
3 - 30 MW GENERATORS  
MOTOR LRA = 6 X FLA

---

---

37.5 MVA BASE

GENERATOR  
37.5 MVA  
 $X' = 25\%$   
FOR 3 GEN'S  $25\%/3$  0.0833 pu $\bar{z}$

$Z_{10,000HP} = \frac{FLA}{LRA} = \frac{1}{3} = 0.333$  1.3558 pu $\bar{z}$   
FROM PREVIOUS CALC 9.210 MVA 1.4391

---

$$V_{13.8KV BUS} = \frac{1.3558}{1.4391} \times 100 = 94.21\% V$$

---

WITH 2 GEN'S  
10,000 HP 0.1250 pu $\bar{z}$   
1.3558 pu $\bar{z}$

$$V_{13.8KV BUS} = \frac{1.3558}{1.4808} \times 100 = 91.56\% V$$
1.4808 pu $\bar{z}$

---

WITH 1 GEN'S  
10,000 HP 0.2500 pu $\bar{z}$   
1.3558 pu $\bar{z}$

$$V_{13.8KV BUS} = \frac{1.3558}{1.6058} \times 100 = 84.43\% V$$
1.6058 pu $\bar{z}$

MOTOR STARTING  
ISLANDED SYSTEM  
3.30 MW GENERATORS  
MOTOR LRA = 3 X FLA

250 KVA BASE

ONE GEN.  
250KVA, 480V  
 $X'_d = 33\%$

0.33 pu Z

INDUCTION MOTOR  
75HP, 460V  
90% EFF.  
85% P.F.  
P.F. START = 20%  
LRA = 6XFLA

0.571 pu Z

0.901 pu Z

$$KVA = \frac{75HP \times 0.746 \frac{KW}{HP}}{0.90EFF \times 0.85PF}$$

$$= 73.1 KVA \text{ WITH } Z = 0.167$$

$$V_{480V \text{ BUS}} = \frac{0.571}{0.901} \times 100 = 63.4\%V$$

WITH  $X'_d = 17\%$   
75HP

0.17 pu Z

0.571 pu Z

0.741 pu Z

$$V_{480V \text{ BUS}} = \frac{0.571}{0.741} \times 100 = 77\%V$$

MOTOR STARTING  
DIESEL GENERATOR  
250KVA  
STANDARD  $X''_d$ , "LOW"  $X''_d$