



# Introduction to Quantum Computing

**Trung T. Pham**

**Cyberworx & Department of Computer Science**

**United States Air Force Academy**

**Colorado, USA**

# Agenda

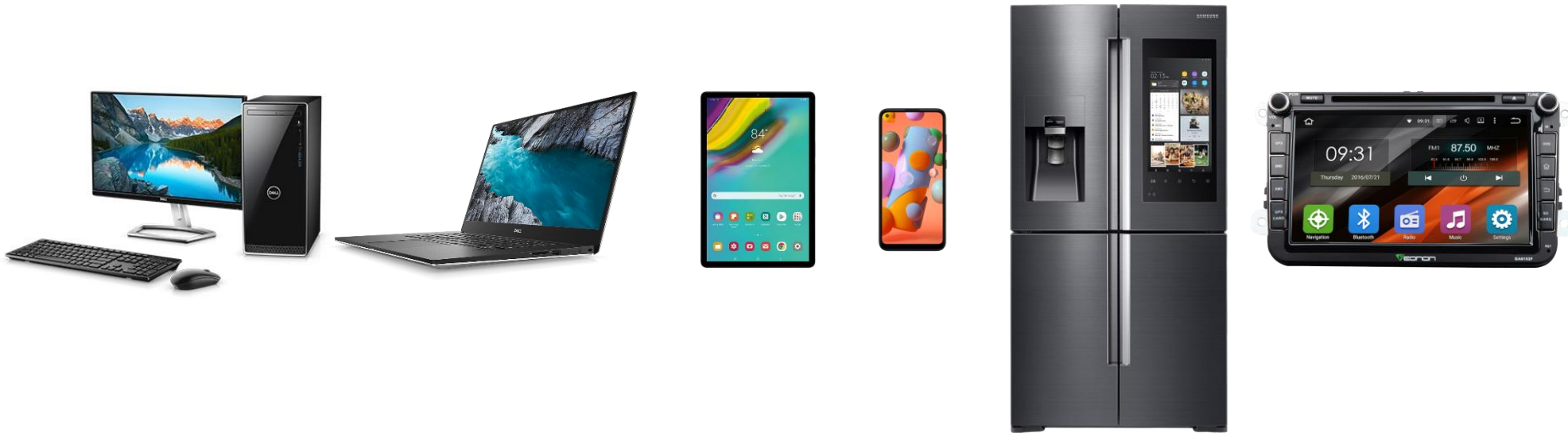
- Introduction
- Traditional Digital Computers
- Concept of Quantum Computers
- Quantum Computing
- Research Topics & Applications
- Conclusion

# Introduction

- Digital computers have been popularized through their implementation in various devices that we use in our everyday routines

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# Introduction

- **As digital computers gain more computational power, more software applications were developed to help every aspect of our lives**
  - **the ubiquity of computers in our daily lives makes digital computers even more popular**
  - **the thirst for more computing power is a good motivation to push the state of the arts further**

# Introduction

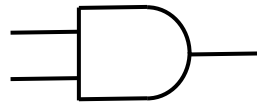
- **One direction of pushing the state of the art in computational power is the concept of developing a quantum computer**
  - **the continuous state inside a quantum computer can simplify computation scheme and improve efficiency**
  - **faster computation will allow more sophisticated software application beyond imagination**

# Traditional Digital Computers

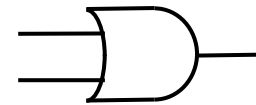
- **Traditional digital computers were built based on hardware that can represent and process binary data**
  - **electronic components rely on using measurable electrical voltage to represent data**
  - **high voltage of 5V was used to represent a 1 and low voltage of 0V was used to represent a 0**
  - **electronic hardware was designed to have output of either 5V or 0V**

# Traditional Digital Computers

- Traditional digital computers were built around the basic digital circuits representing logical AND and logical OR operators



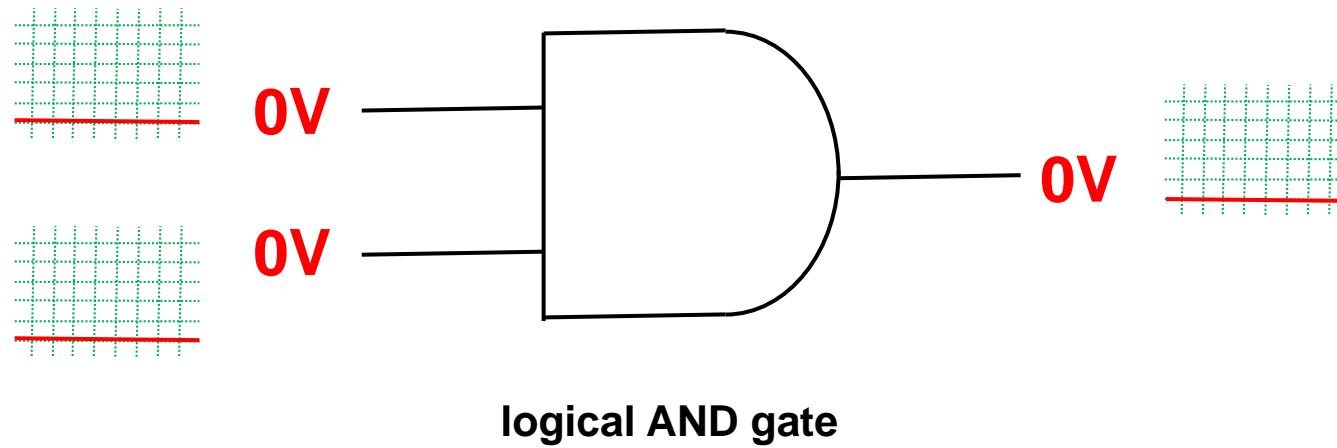
logical AND gate



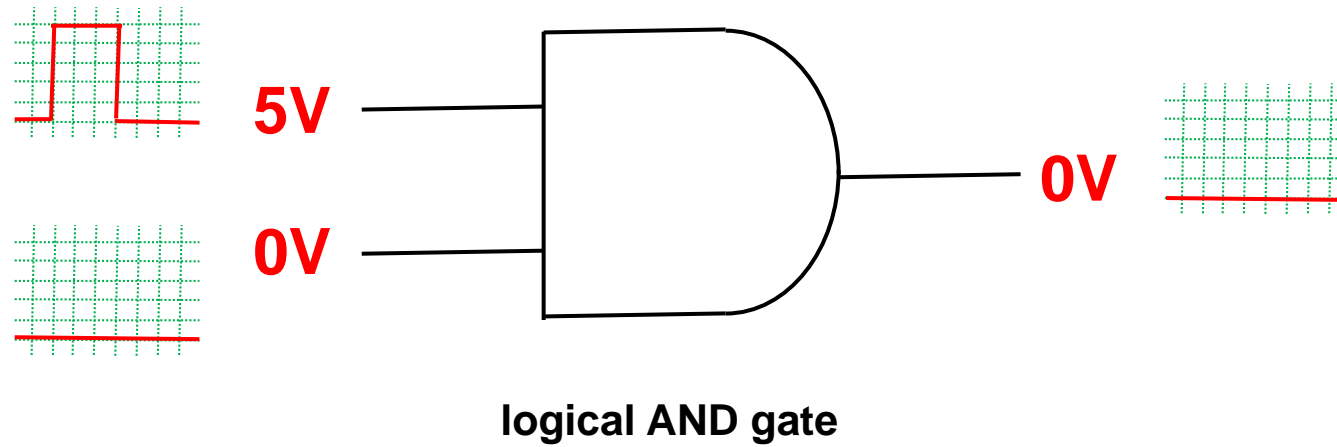
logical OR gate



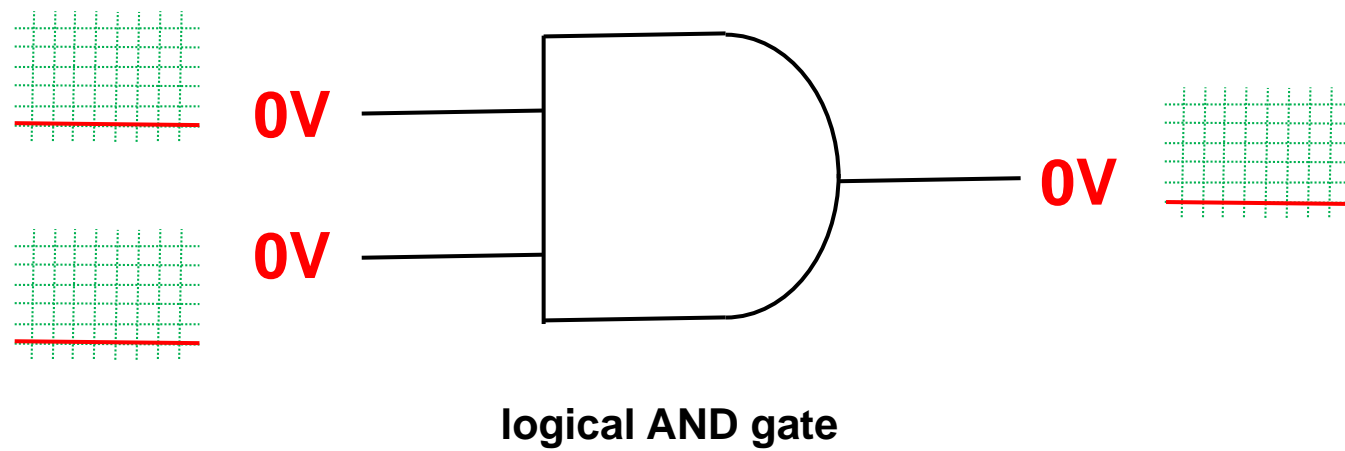
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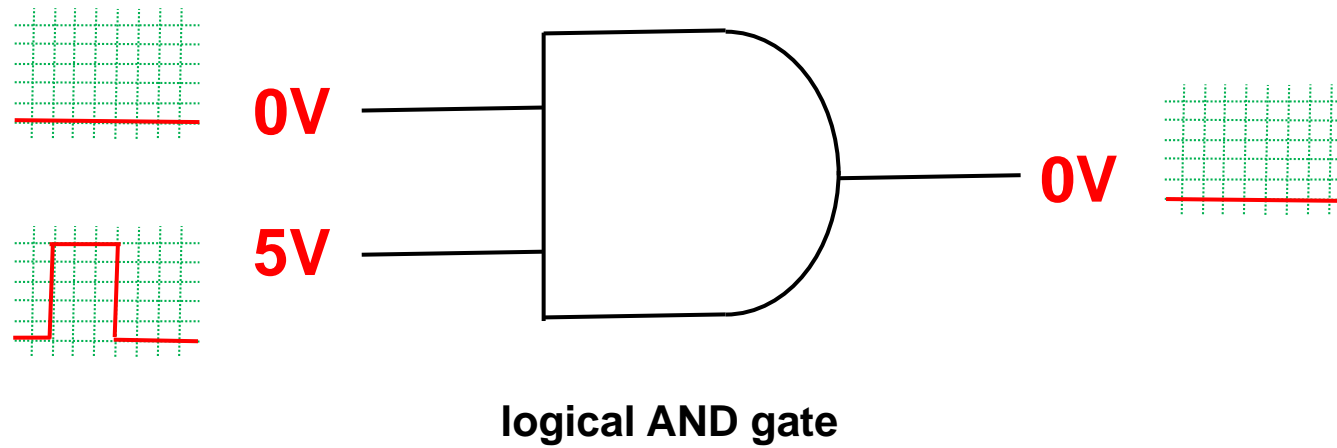
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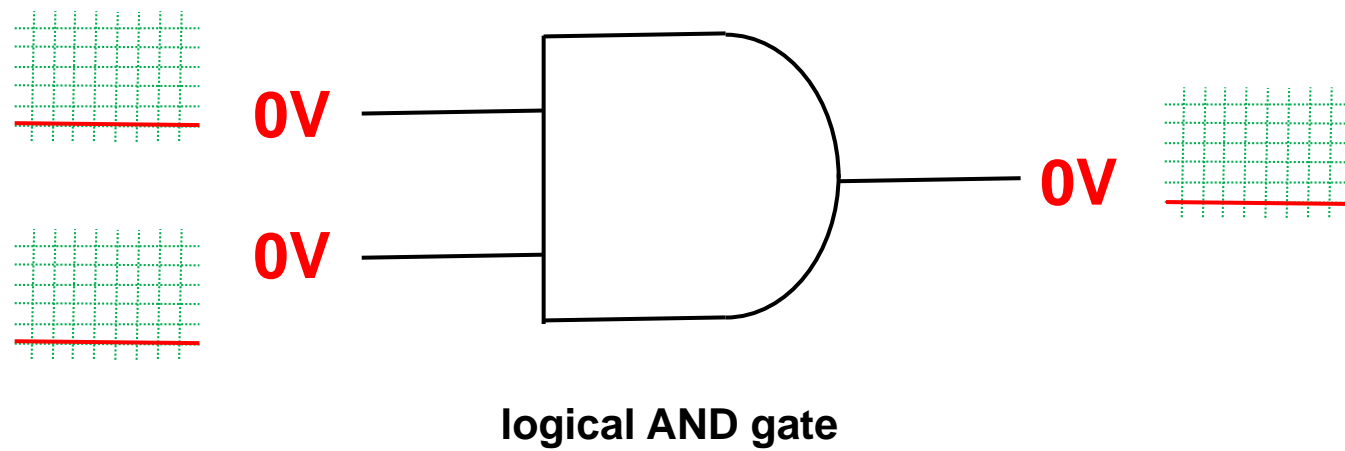
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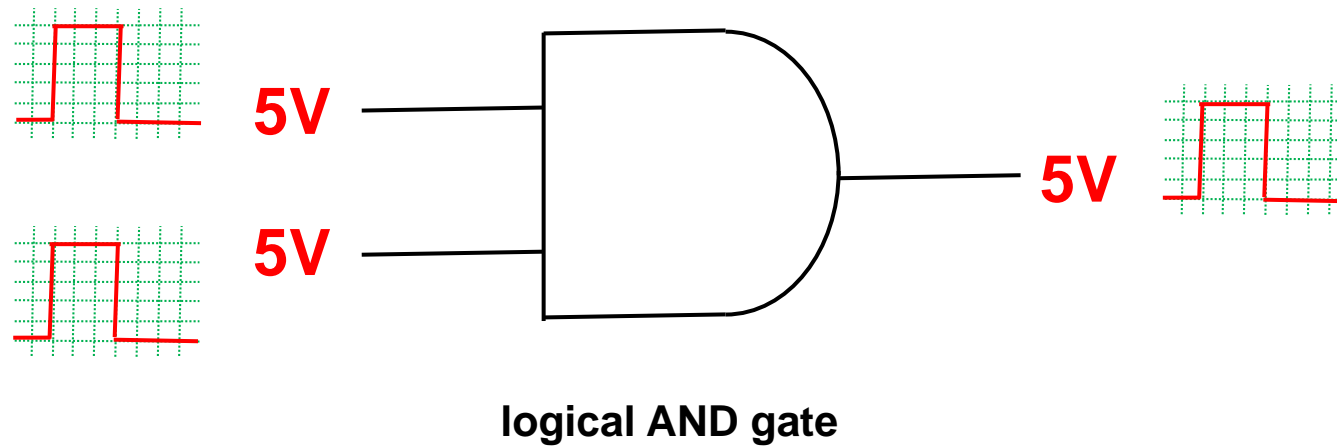
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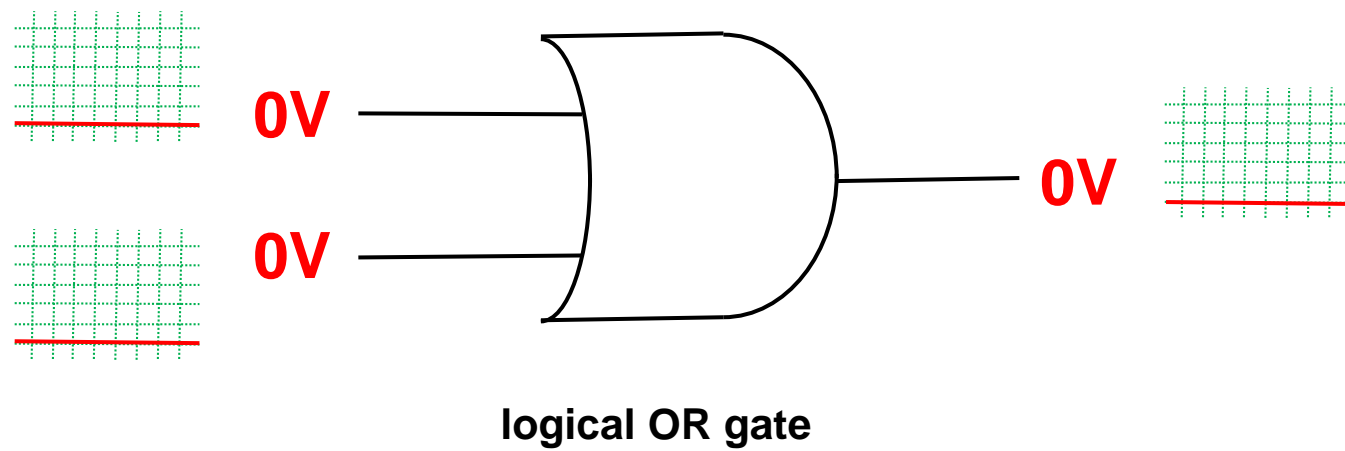
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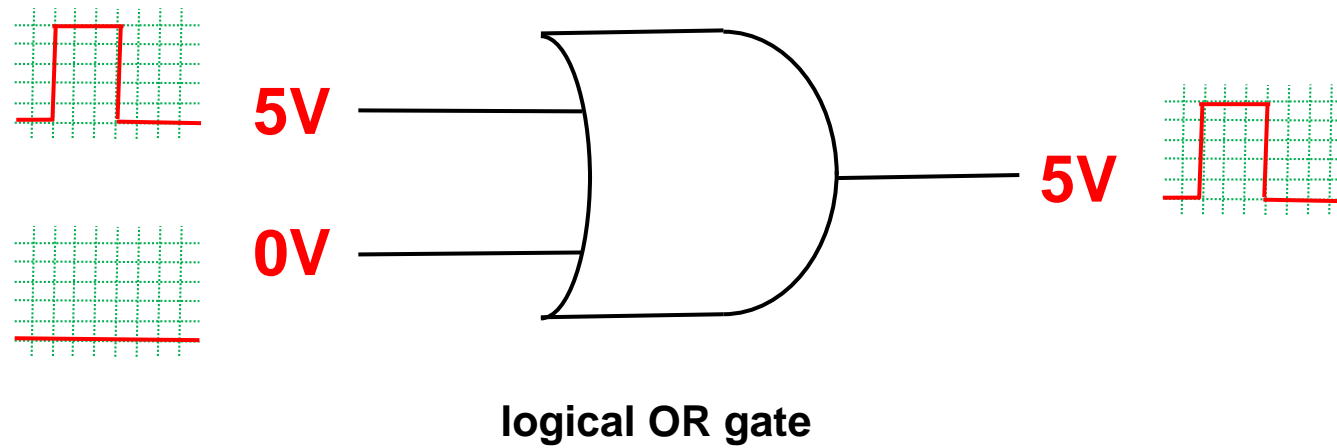


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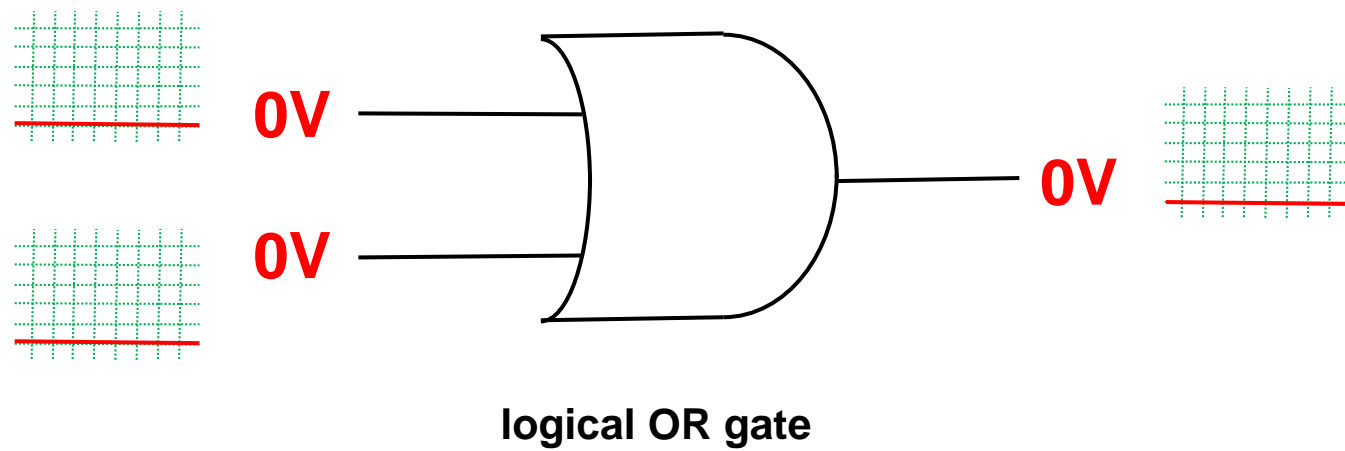




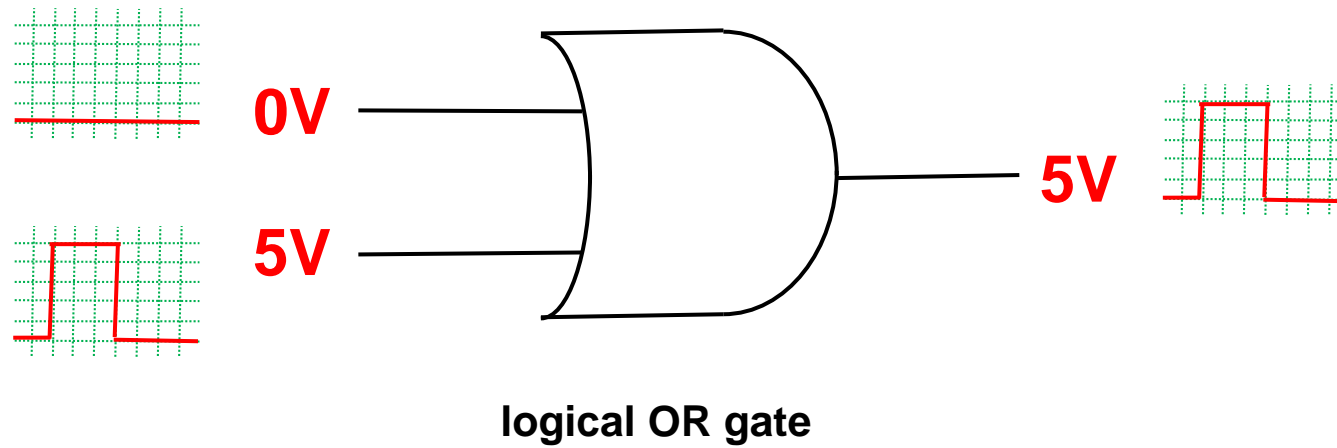
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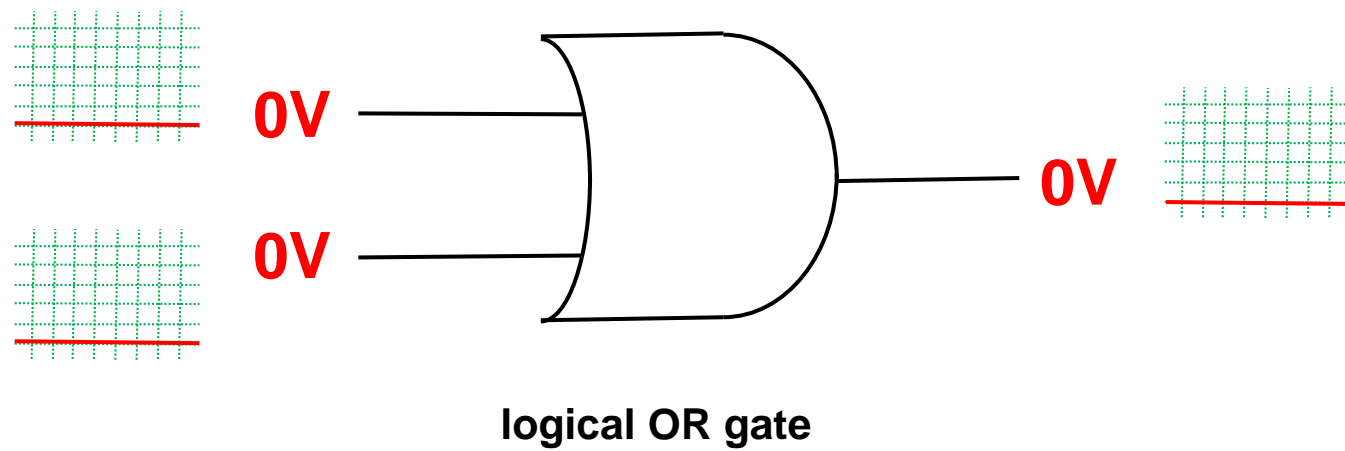
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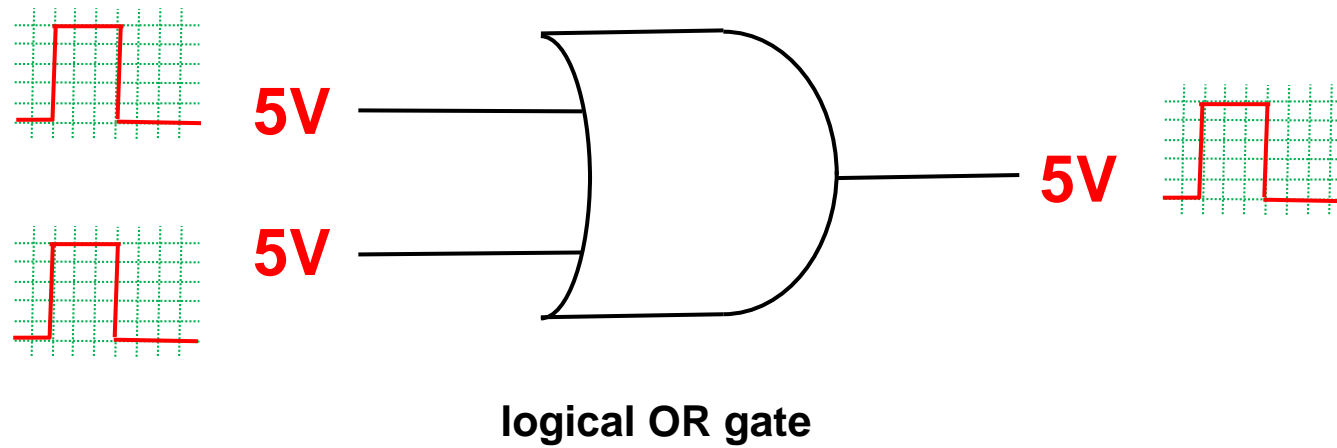
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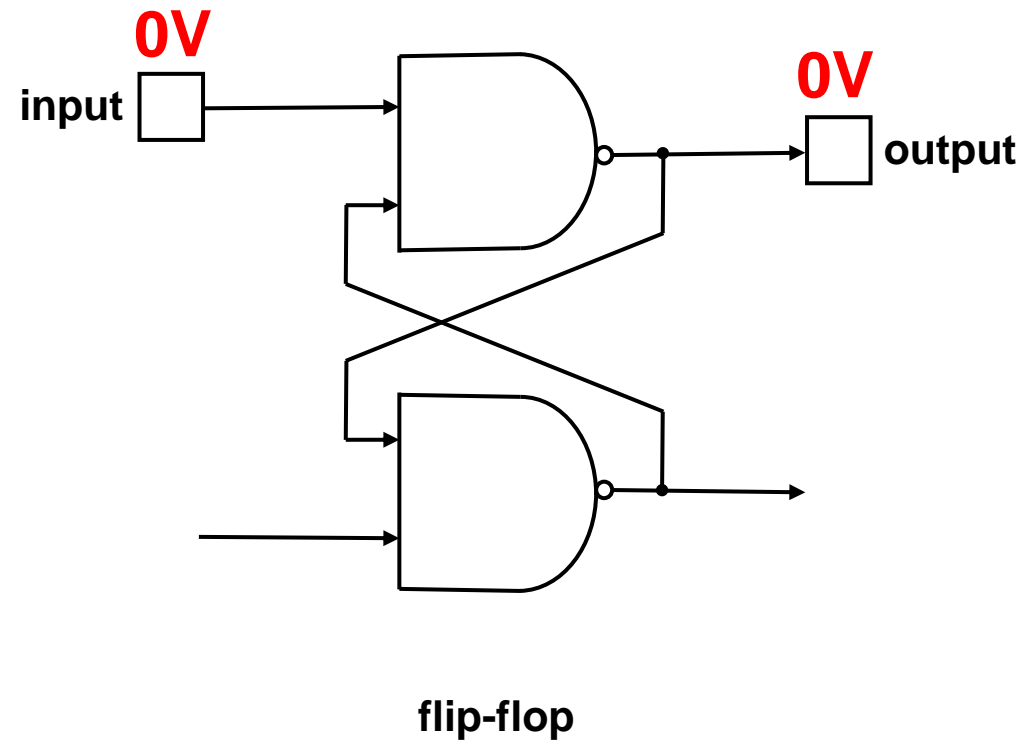
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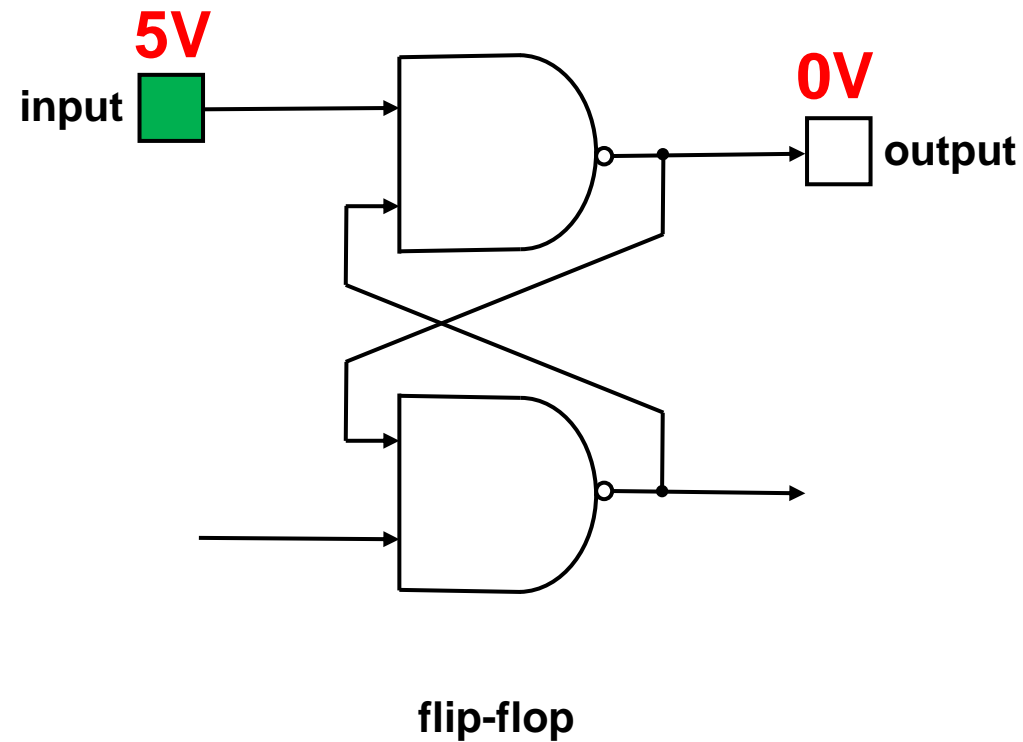
- Logical AND gate and logical OR gates are combined to build:
  - flip-flop: a basic unit of memory
  - adder: basic unit of computation

# Traditional Digital Computers

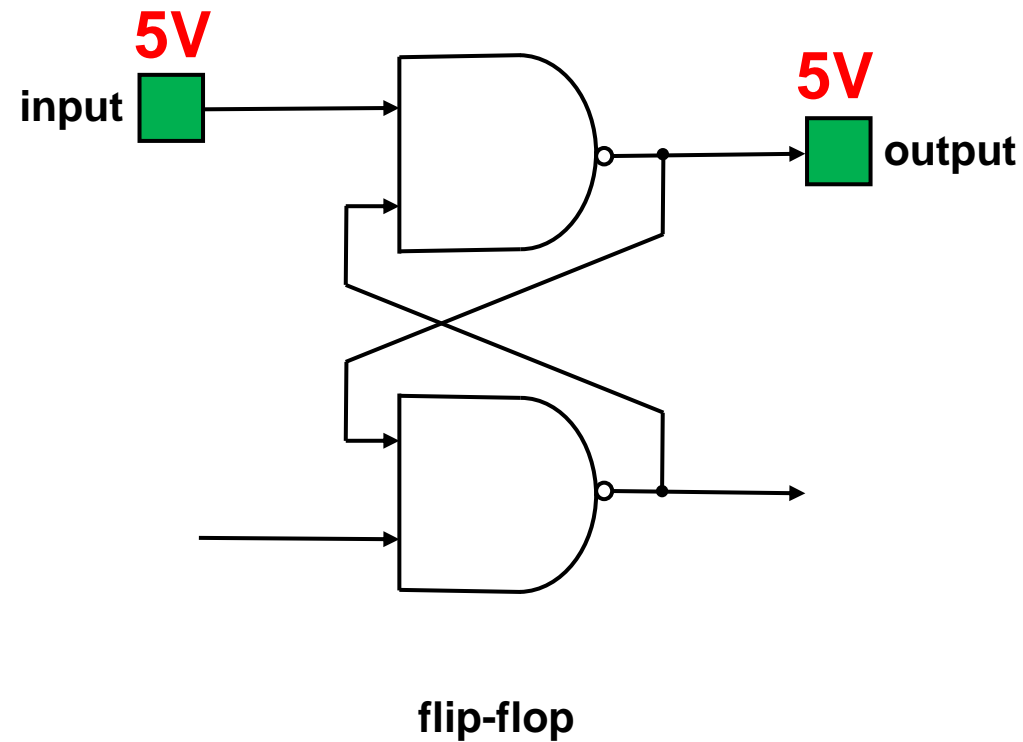




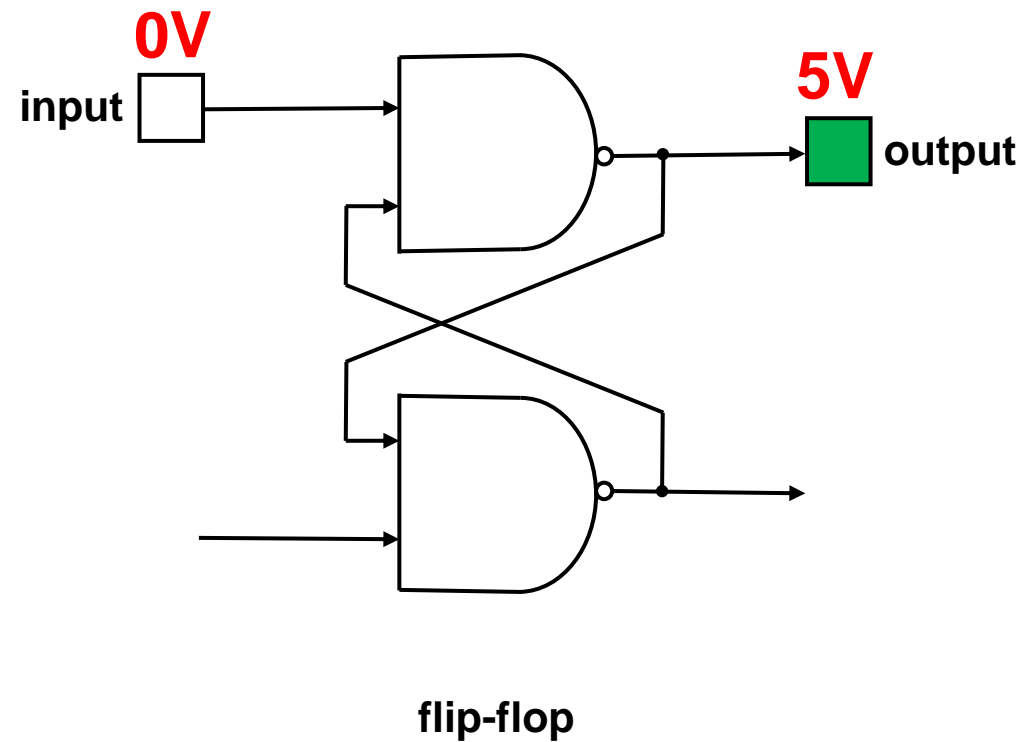
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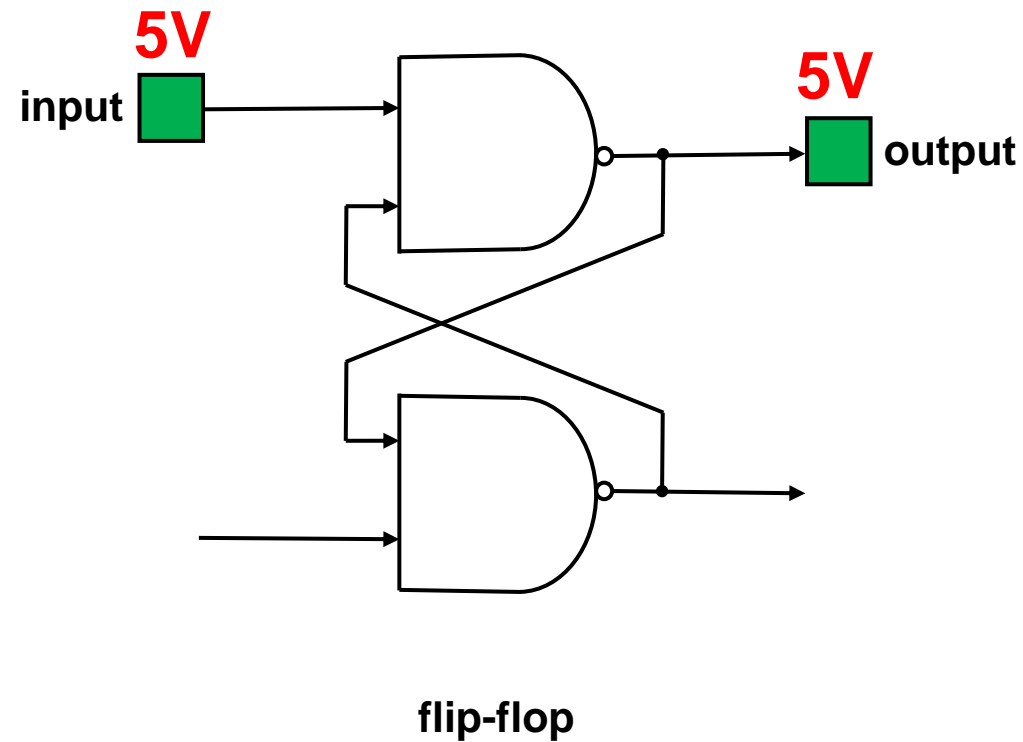
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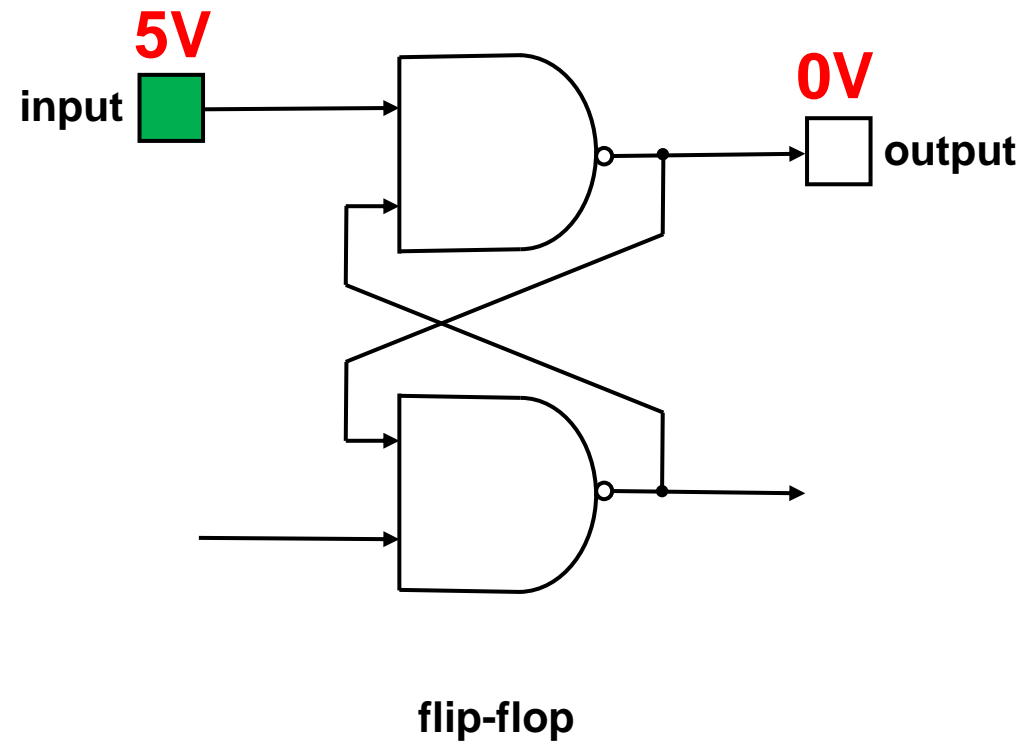
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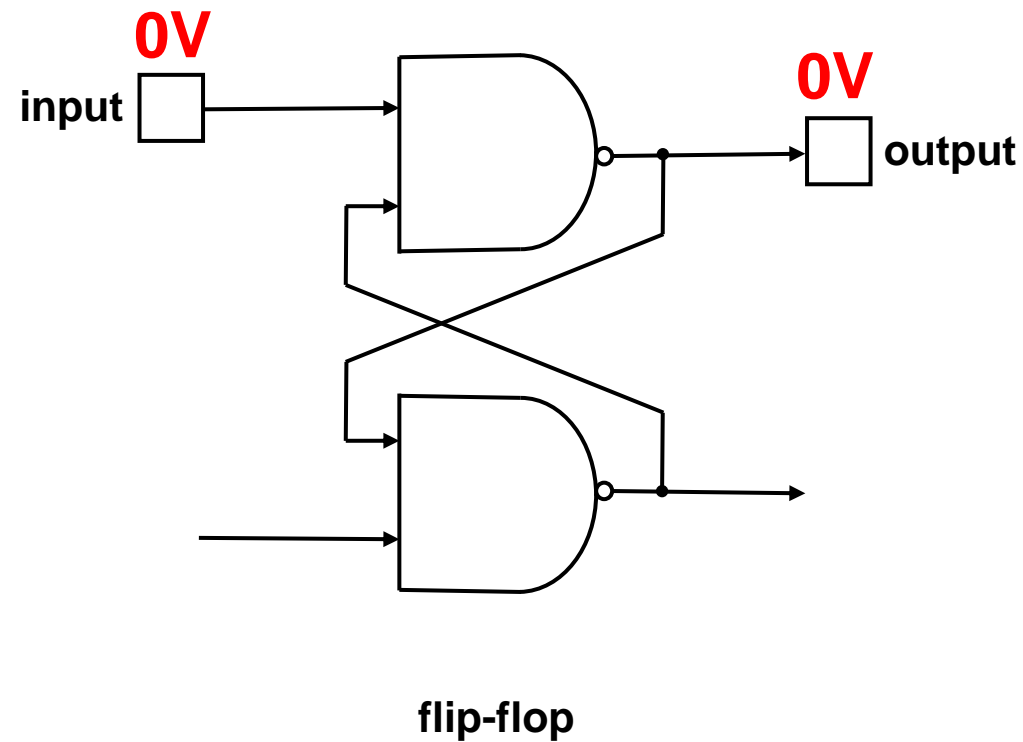
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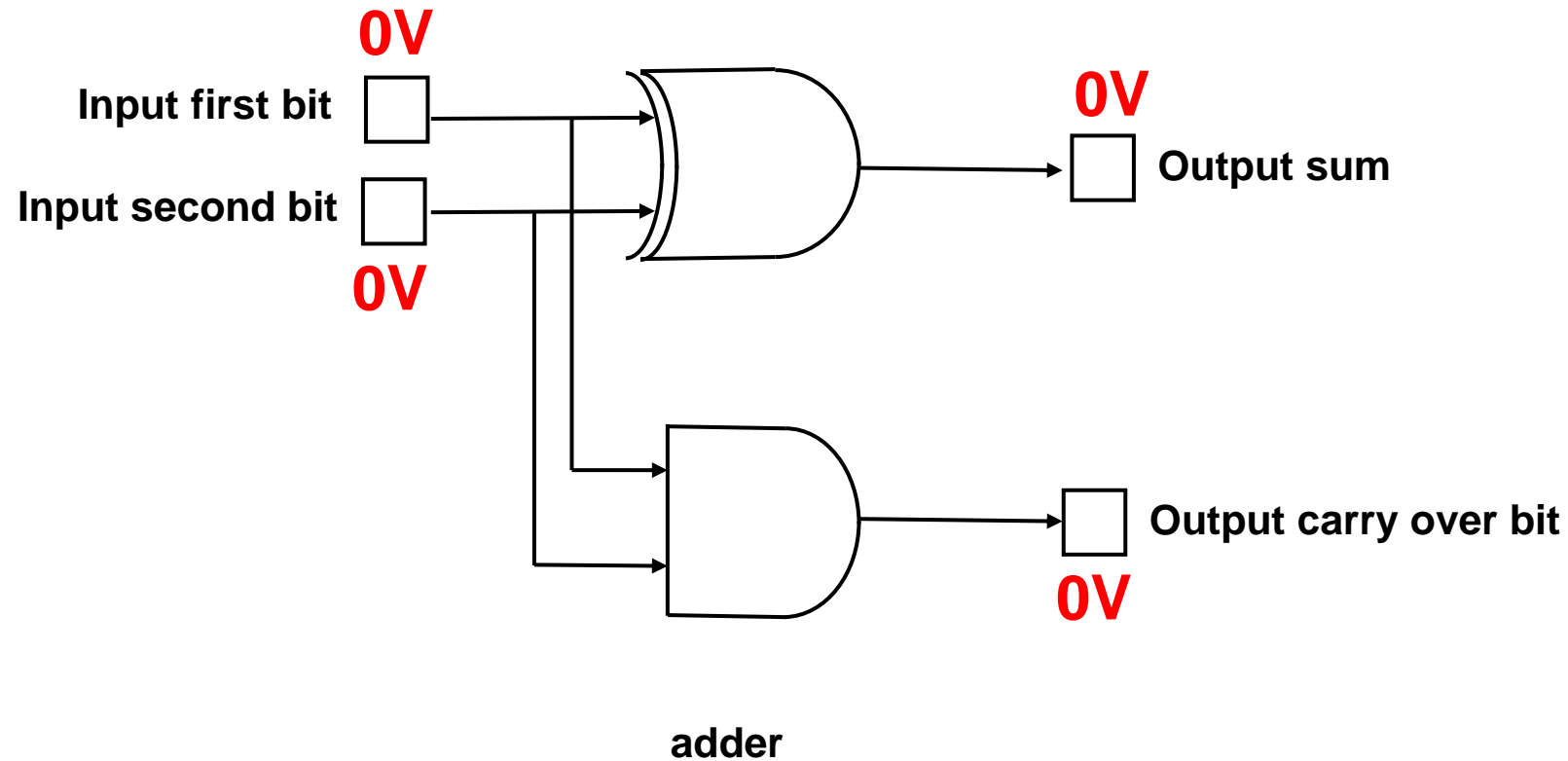
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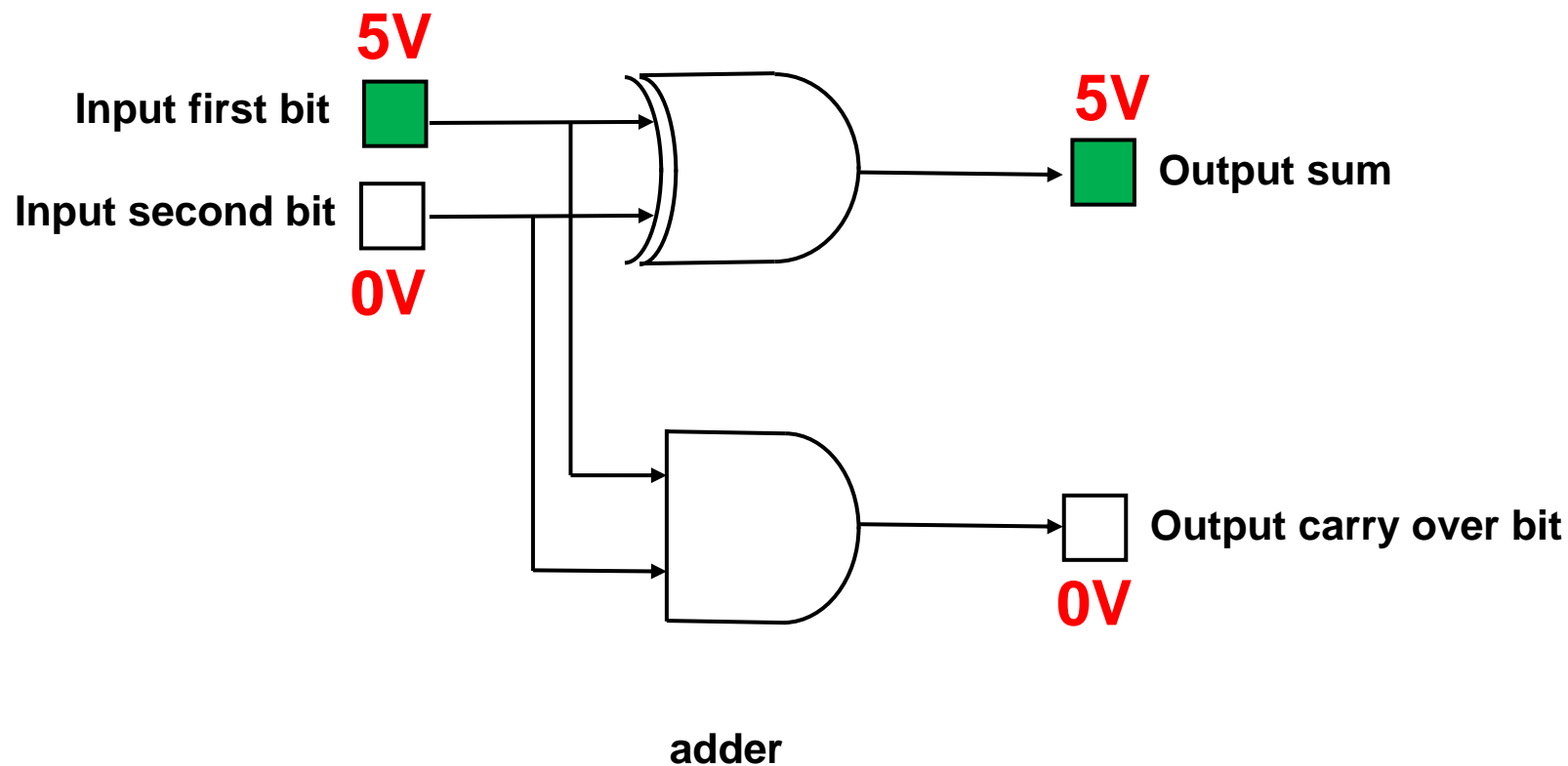


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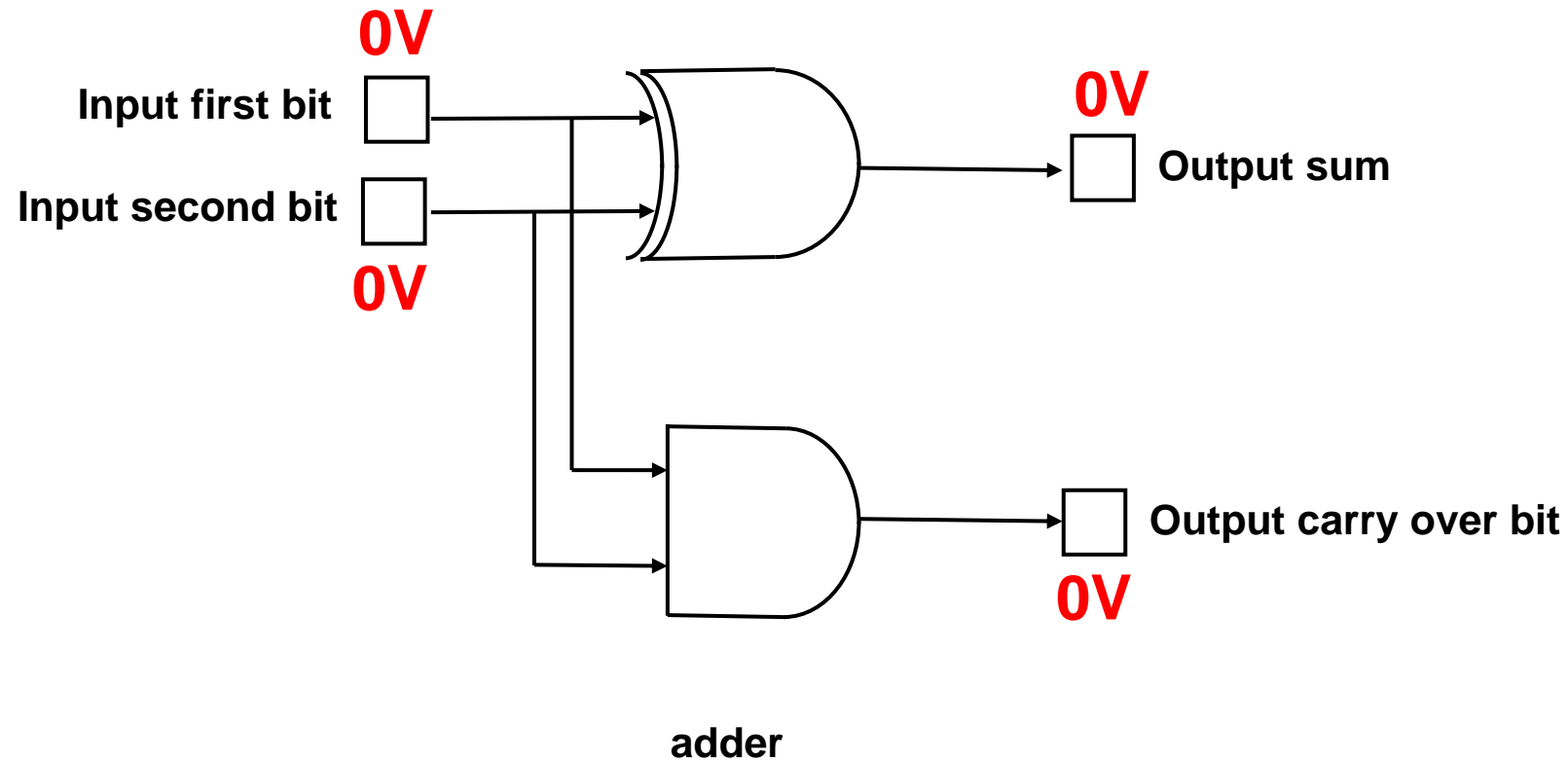




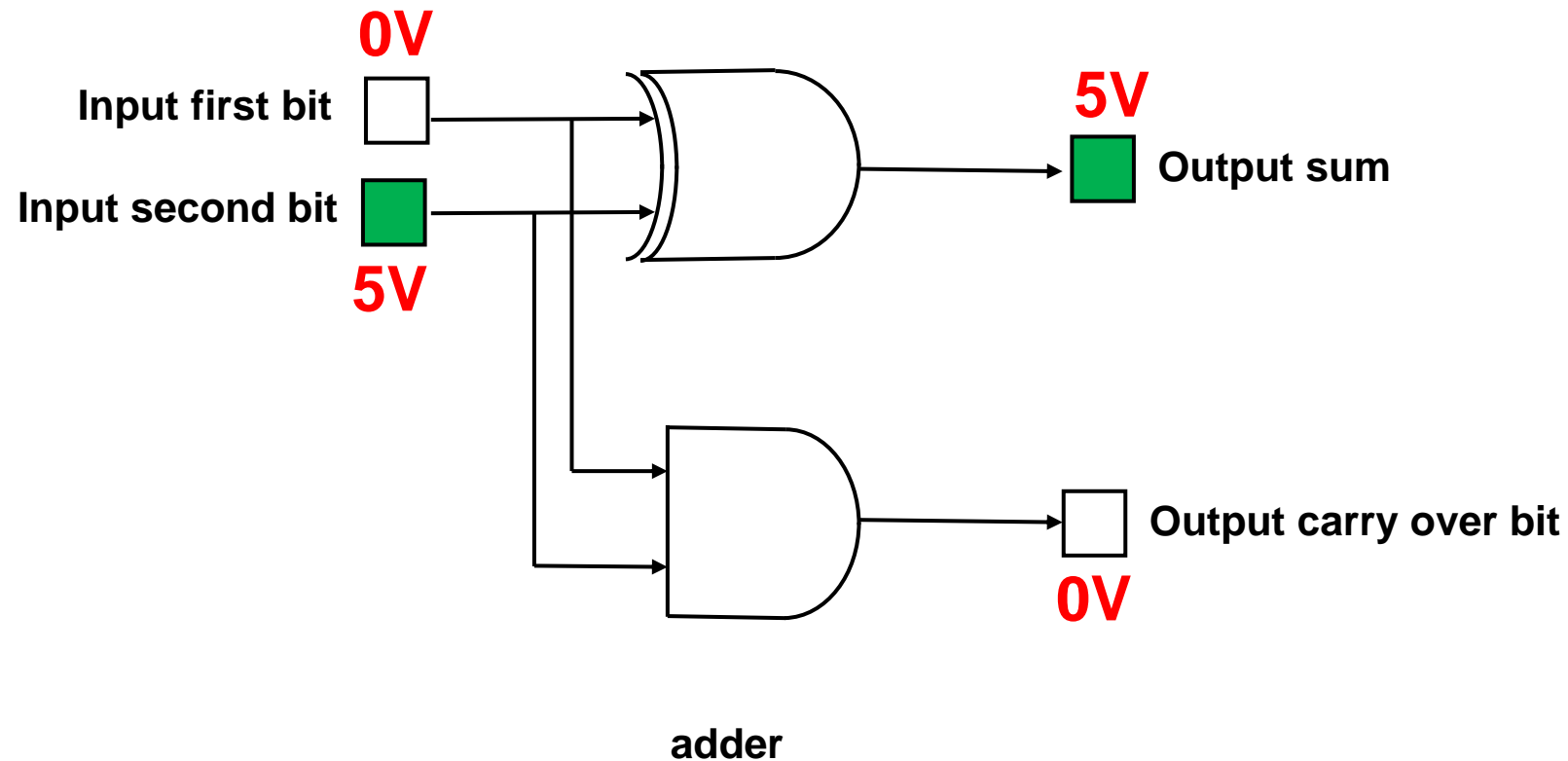
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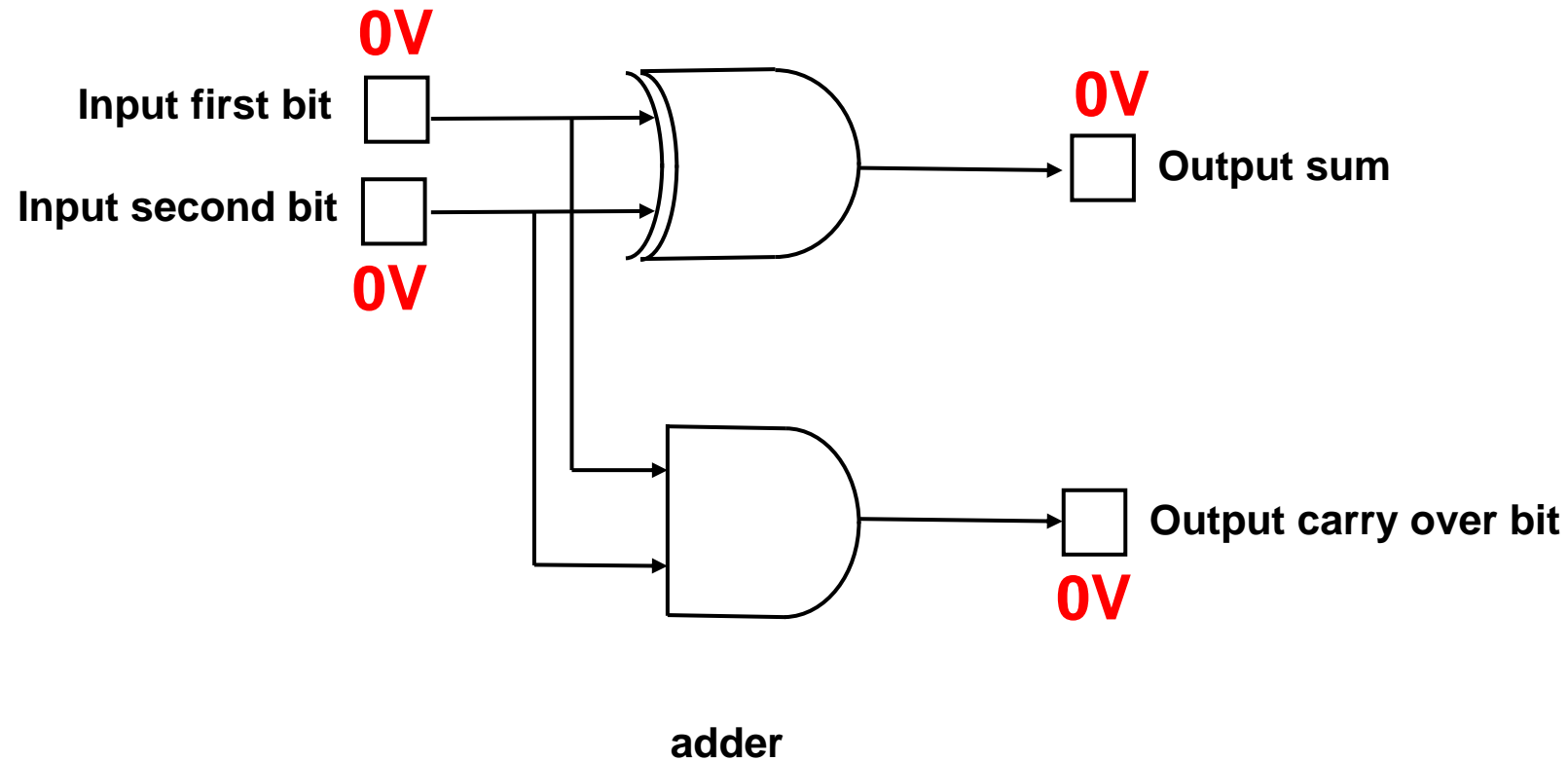
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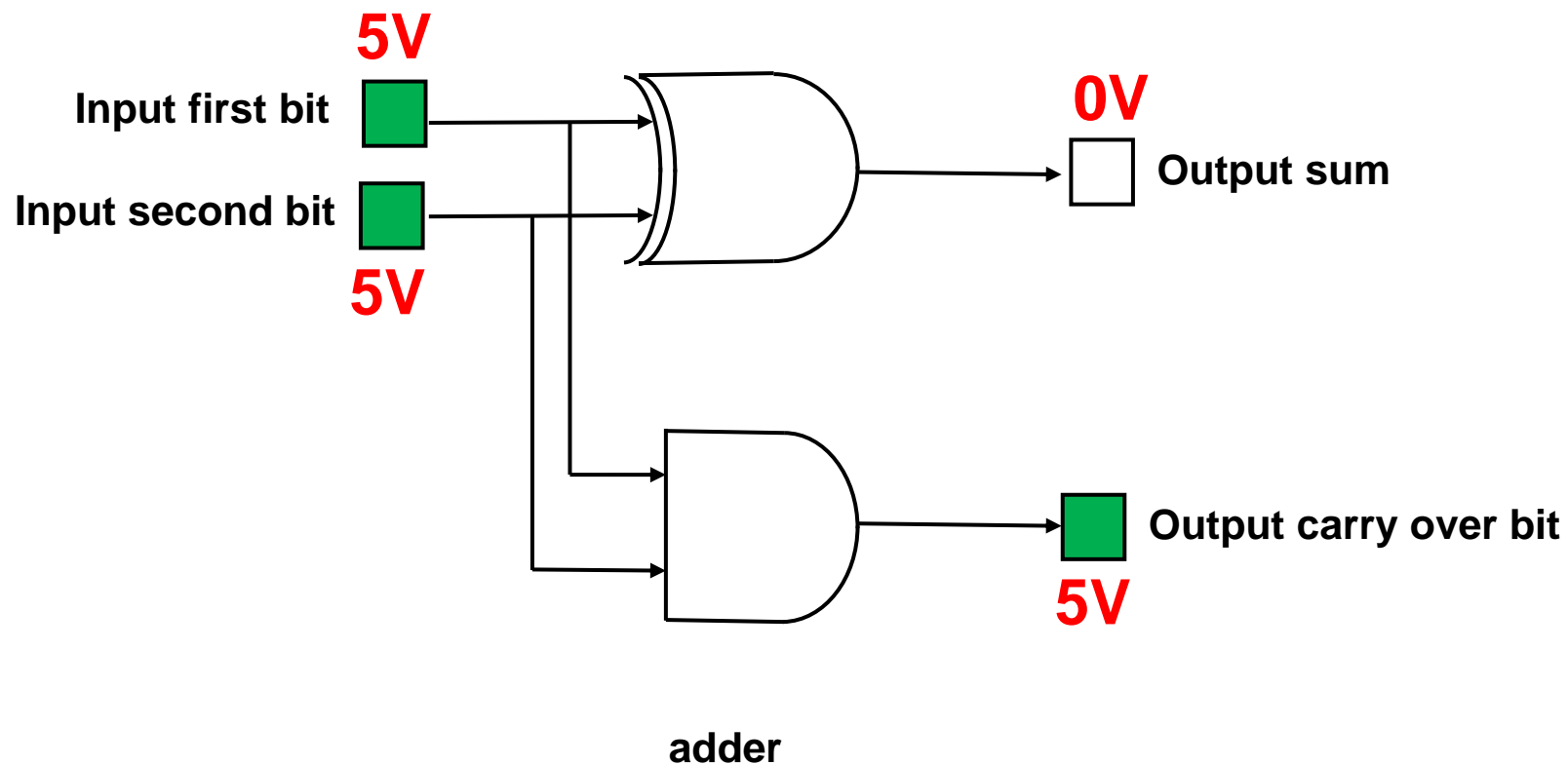
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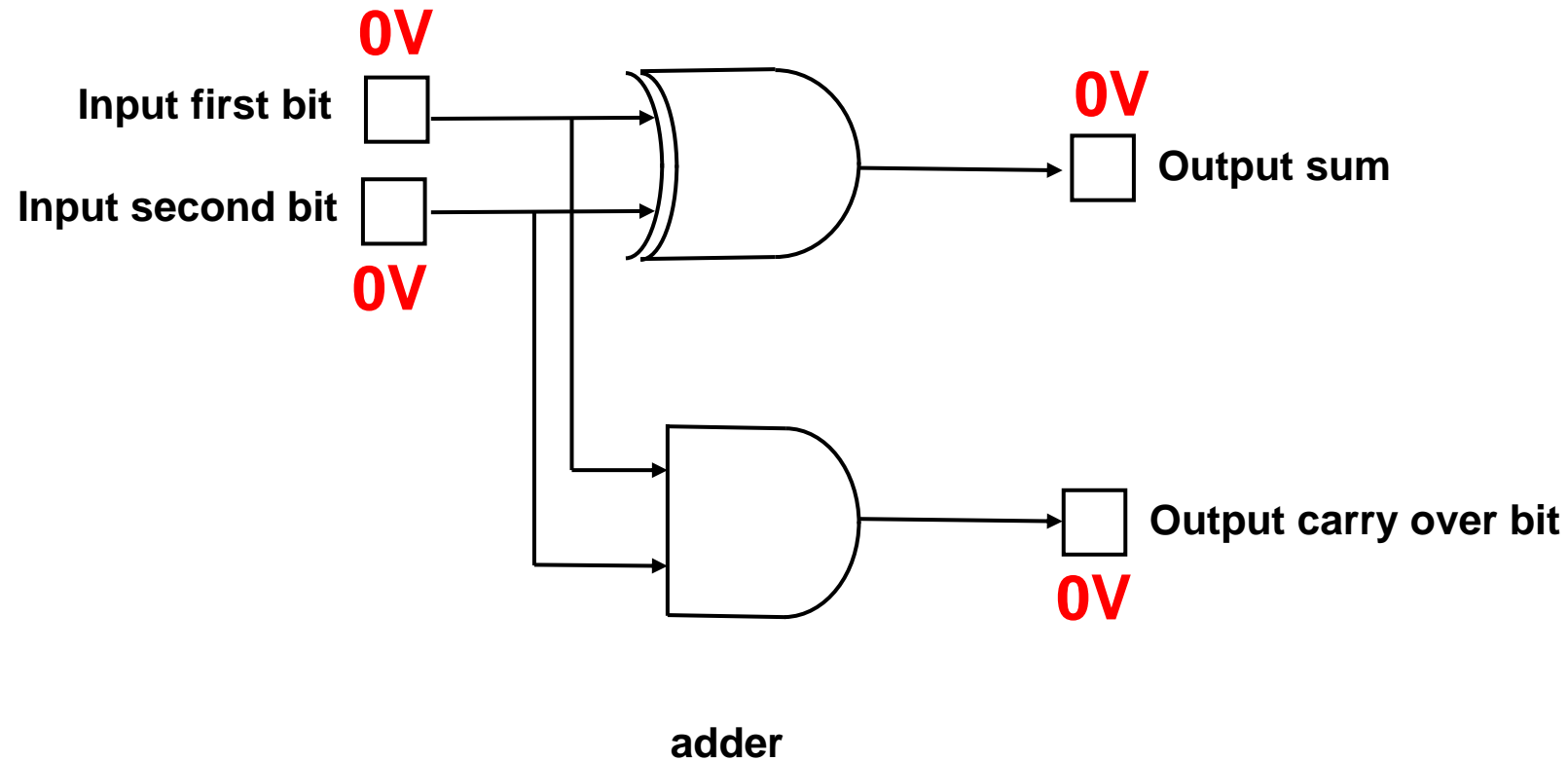
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# Traditional Digital Computers

- **Software was developed around a context-free language to instruct a digital computer of what to do**
  - **variable: an allocated memory area to hold data**
  - **operator: an instruction of what to do with the data stored in the variables**



# Traditional Digital Computers

```
main ()  
{  
}
```









# Traditional Digital Computers

```
main ()  
{  
  int myVariable = 50;  
  int myResult = myVariable + 1;  
}
```

myVariagle

myResult

calculate and assign data content



# Traditional Digital Computers

- **Traditional digital computers combine both hardware and software together so that**
  - **users see only an integrated product that can be configured according to the needs**
  - **the software platform can be updated automatically to improve the performance**



# Concept of Quantum Computers



# Concept of Quantum Computers

- **Quantum computers are computers that designed and built based on the hardware that can represent and process data in the quantum state**
  - **electronic components rely on using measurable electrical voltage to represent data**
  - **voltage can be varied between an acceptable range to represent data in the quantum state**
  - **electronic hardware was designed to accept, process, and produce data in the quantum state**

# Concept of Quantum Computers

- **Quantum bit is the smallest unit of data in a quantum computer**
  - **a quantum bit consists of two parts representing the quantum states of the two binary outcomes**
  - **voltage can be varied between an acceptable range to represent data in the quantum state**
  - **electronic hardware was designed to accept, process, and produce data in the quantum state**

# Concept of Quantum Computers

- A quantum bit is represented by a linear combination of two orthogonal vectors  $|0\rangle = [1 \ 0]^T$  and  $|1\rangle = [0 \ 1]^T$

$$\mathbf{b}_{\text{quantum}} = \alpha |0\rangle + \beta |1\rangle$$

Where  $\alpha$  is the probability of  $|0\rangle$  and  $\beta$  is the probability of  $|1\rangle$ , and

$$\alpha^2 + \beta^2 = 1$$

# Concept of Quantum Computers

- **Similar to logic gates in traditional digital computer, there are various gates designed for quantum computers**
  - **Pauli X gate: an equivalent of the NOT gate reversing the binary data**
  - **SWAP gate: swapping the two input quantum bits**

# Concept of Quantum Computers

- Similar to logic gates in traditional digital computer, there are various gates designed for quantum computers
  - definitions of more gates can be found at

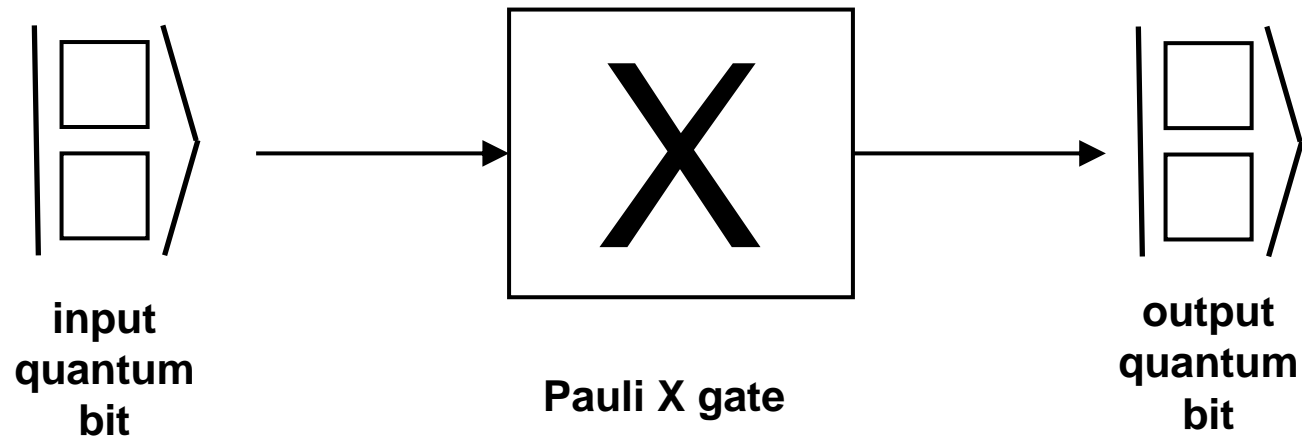
[https://en.wikipedia.org/wiki/Quantum\\_logic\\_gate](https://en.wikipedia.org/wiki/Quantum_logic_gate)

# Concept of Quantum Computers



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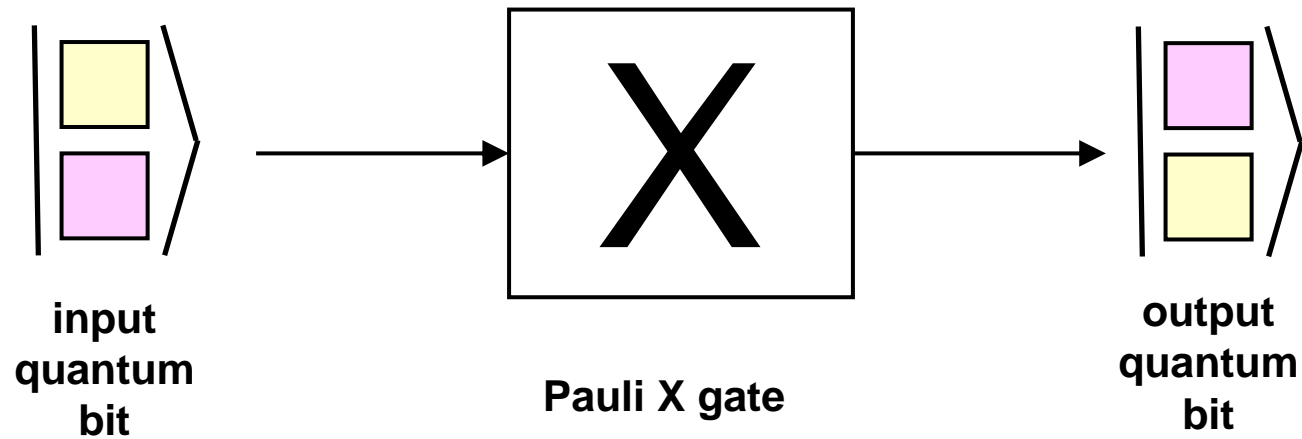
$$\begin{bmatrix} \alpha_{\text{output}} \\ \beta_{\text{output}} \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} \alpha_{\text{input}} \\ \beta_{\text{input}} \end{bmatrix}$$





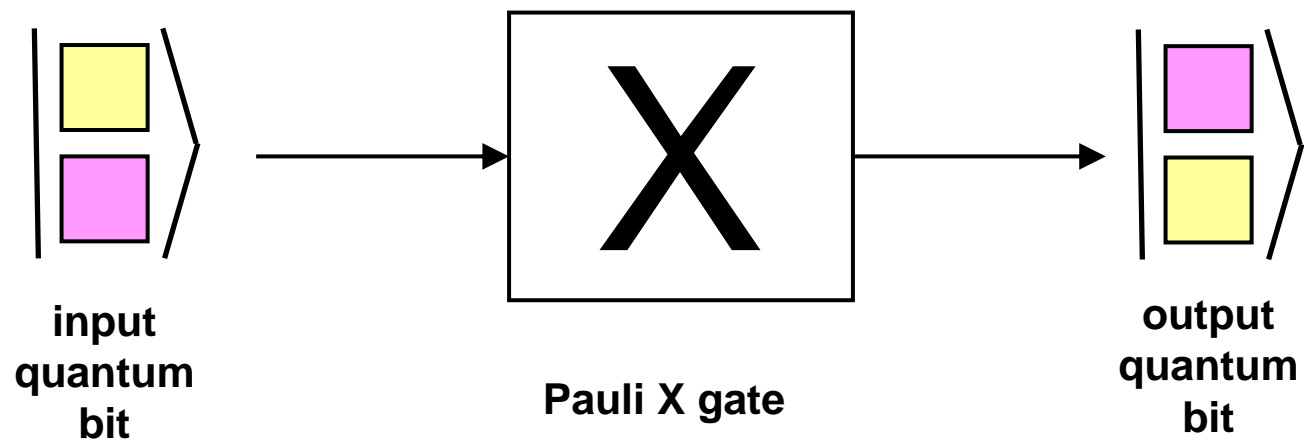
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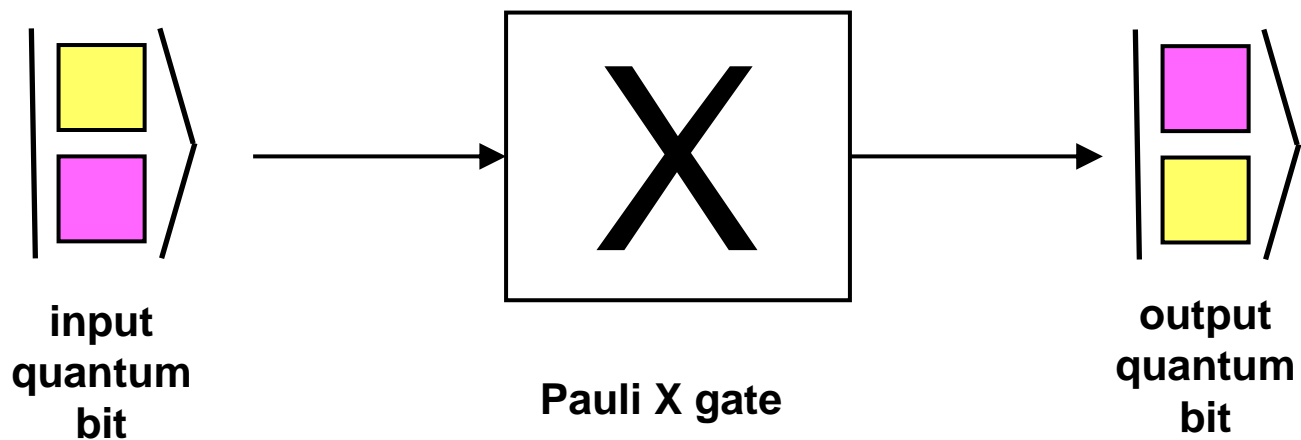
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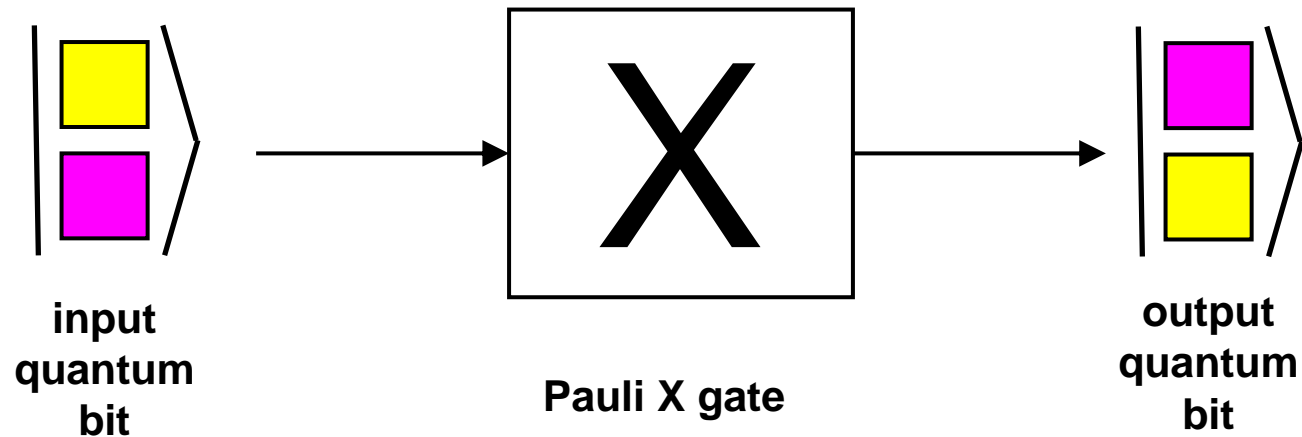
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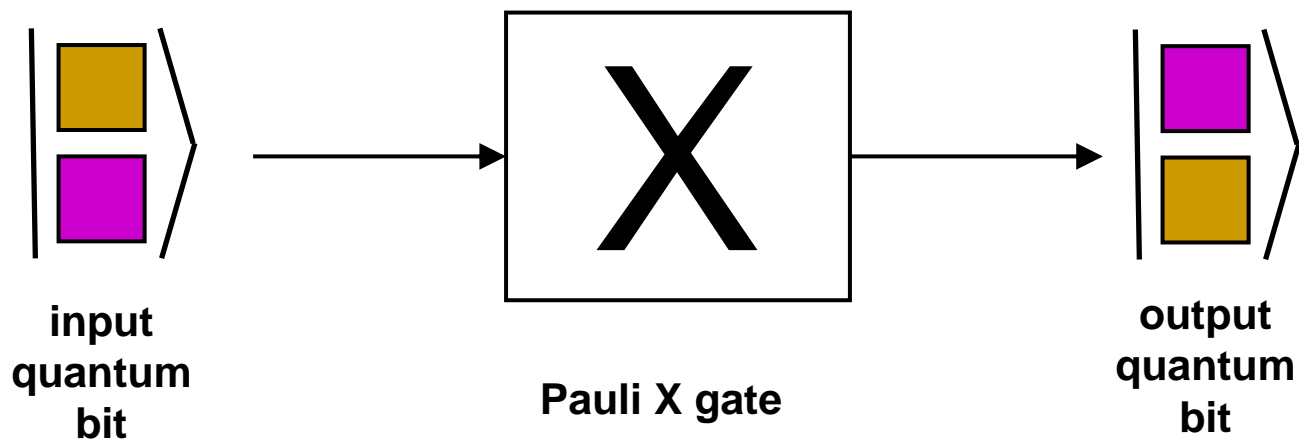
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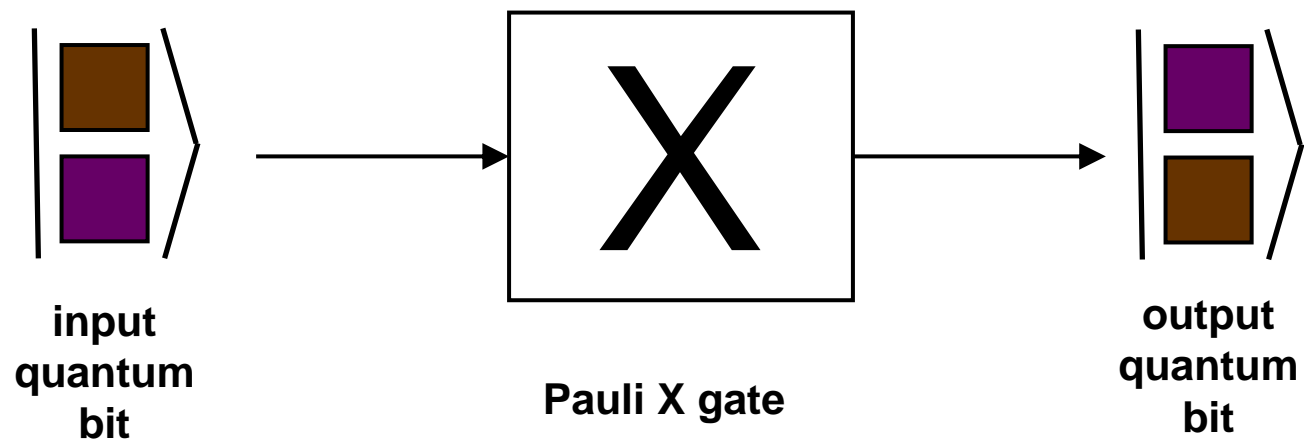
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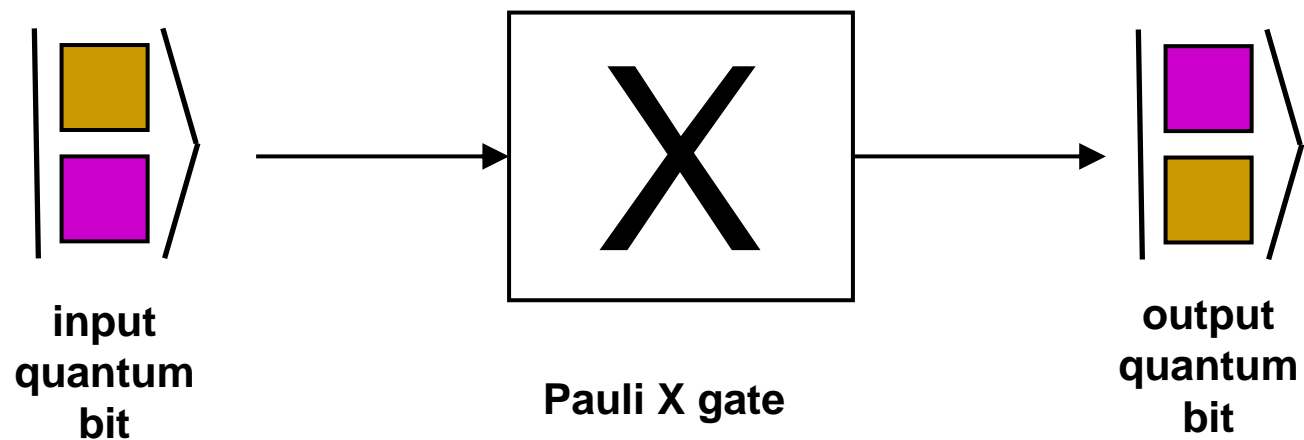
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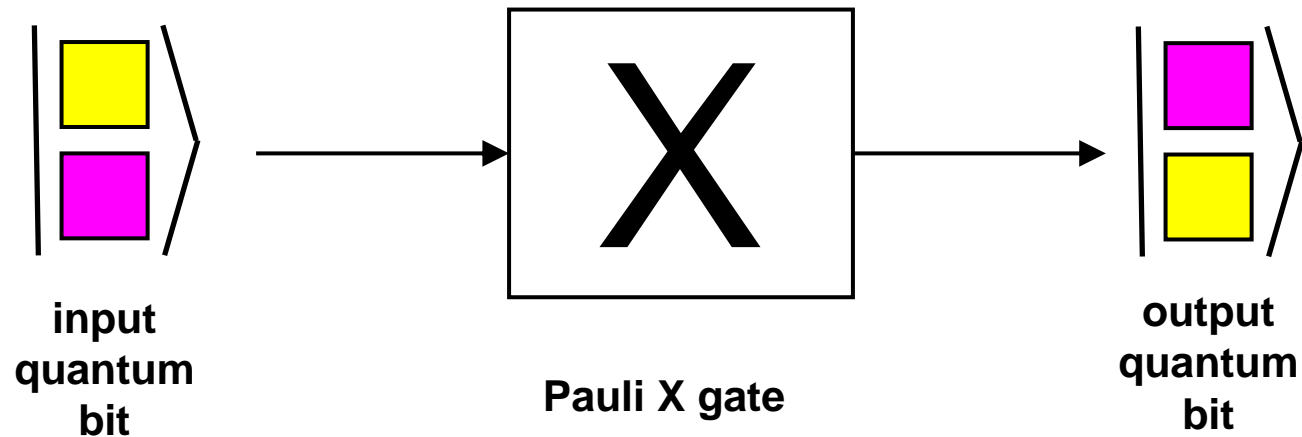
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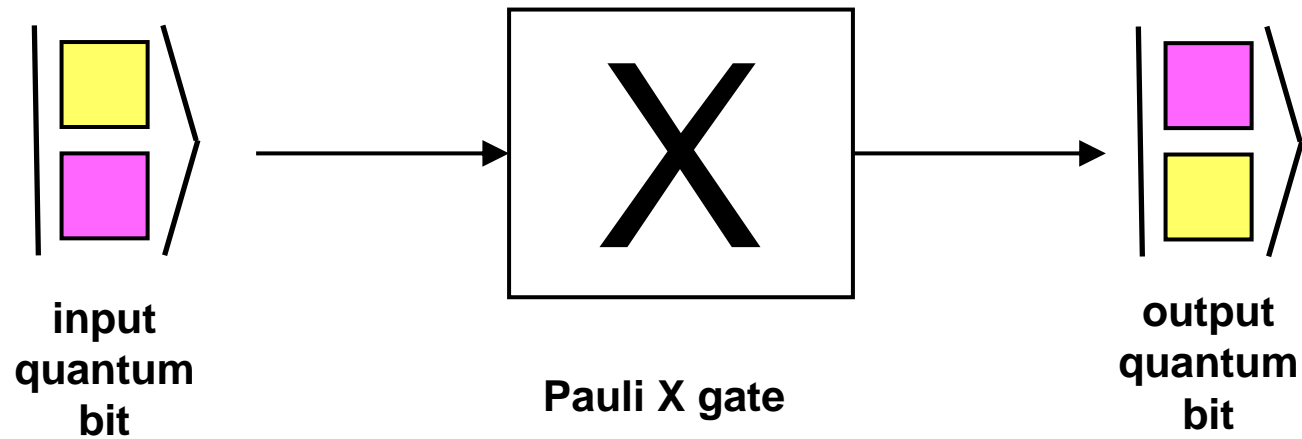
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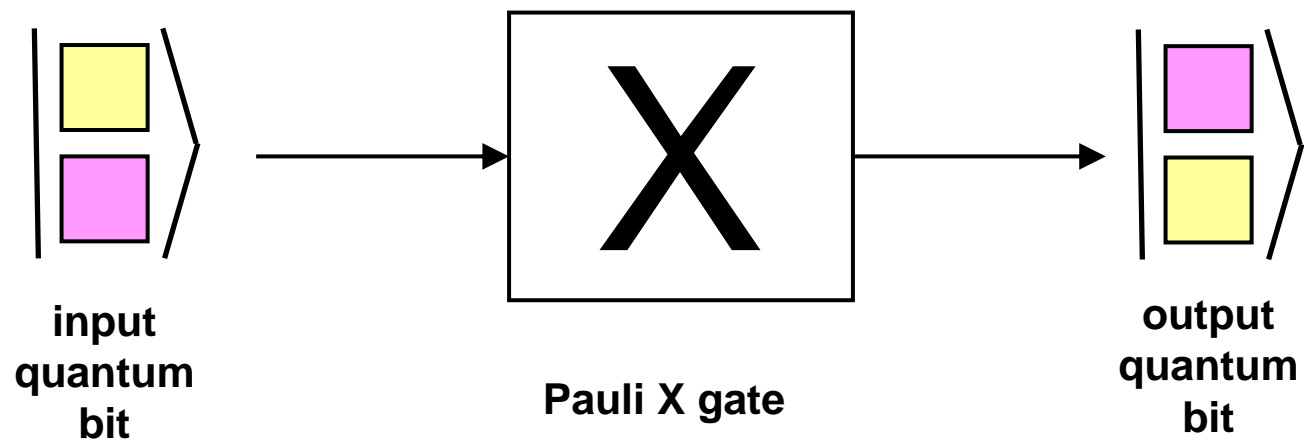
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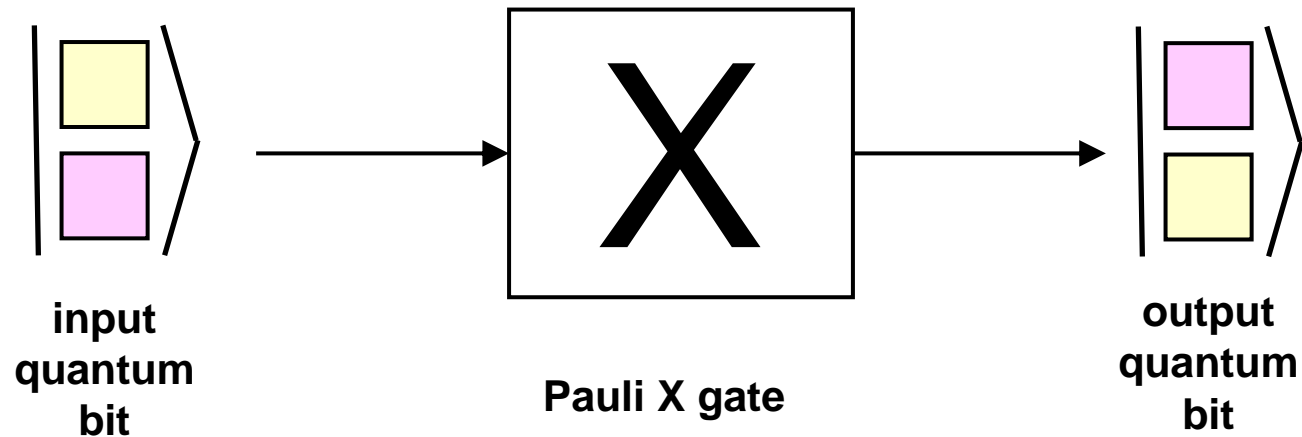
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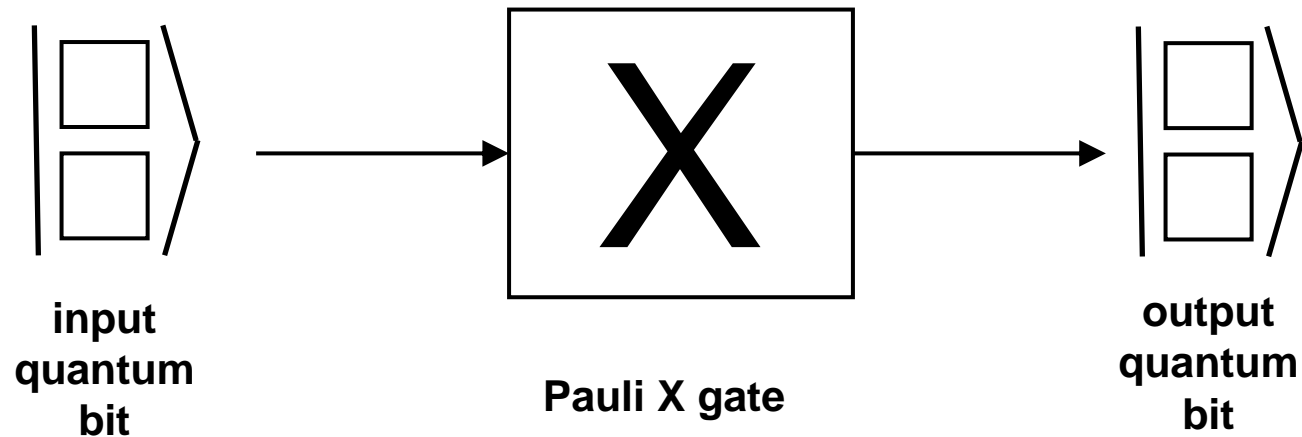
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# Concept of Quantum Computers



# Concept of Quantum Computers

$$\begin{bmatrix} \alpha_{\text{input},1} \\ \beta_{\text{input},1} \end{bmatrix}$$

$$\begin{bmatrix} \alpha_{\text{input},2} \\ \beta_{\text{input},2} \end{bmatrix}$$

combining two quantum bits into a vector  
for mathematical calculation

# Concept of Quantum Computers

$$\begin{bmatrix} \alpha_{\text{input},1} \\ \beta_{\text{input},1} \end{bmatrix} \rightarrow \begin{bmatrix} \alpha_{\text{input},1} & \begin{bmatrix} \alpha_{\text{input},2} \\ \beta_{\text{input},2} \end{bmatrix} \\ \beta_{\text{input},1} & \begin{bmatrix} \alpha_{\text{input},2} \\ \beta_{\text{input},2} \end{bmatrix} \end{bmatrix}$$

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combining two quantum bits into a vector  
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# Concept of Quantum Computers

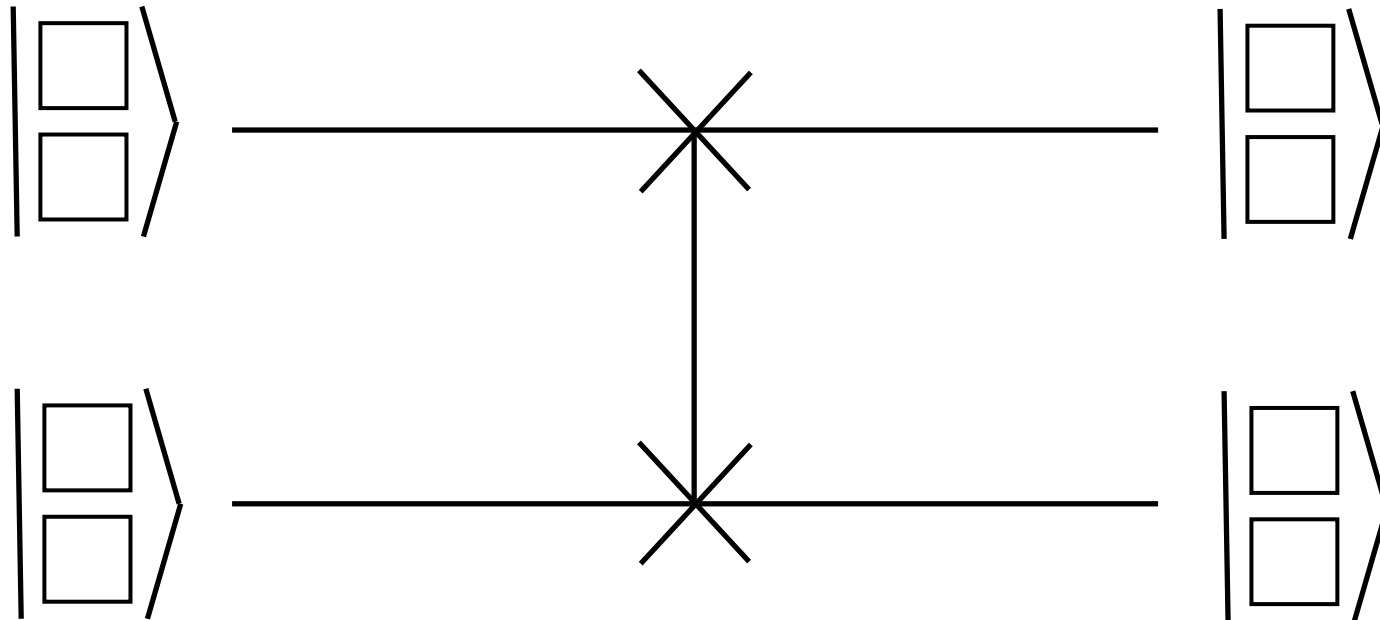
$$\begin{bmatrix} V_{\text{output},00} \\ V_{\text{output},01} \\ V_{\text{output},10} \\ V_{\text{output},11} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} V_{\text{input},00} \\ V_{\text{input},01} \\ V_{\text{input},10} \\ V_{\text{input},11} \end{bmatrix}$$

mathematical representation of  
SWAP gate

# Concept of Quantum Computers

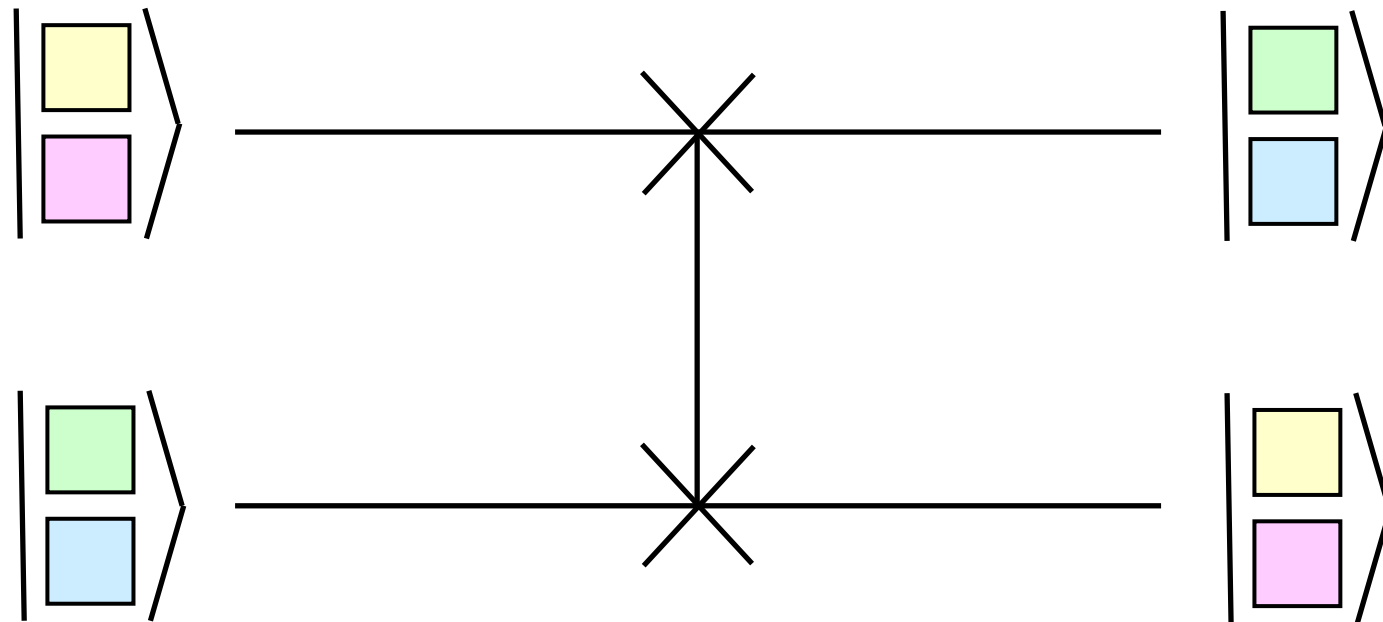


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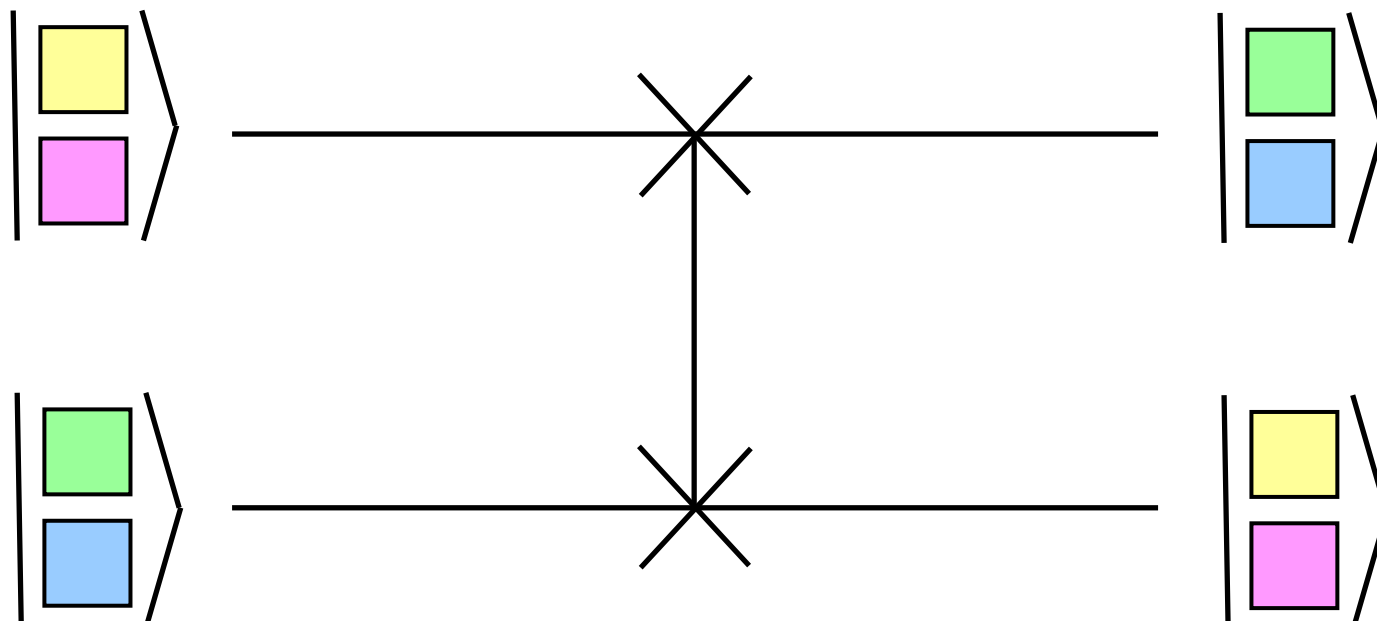
graphical representation of  
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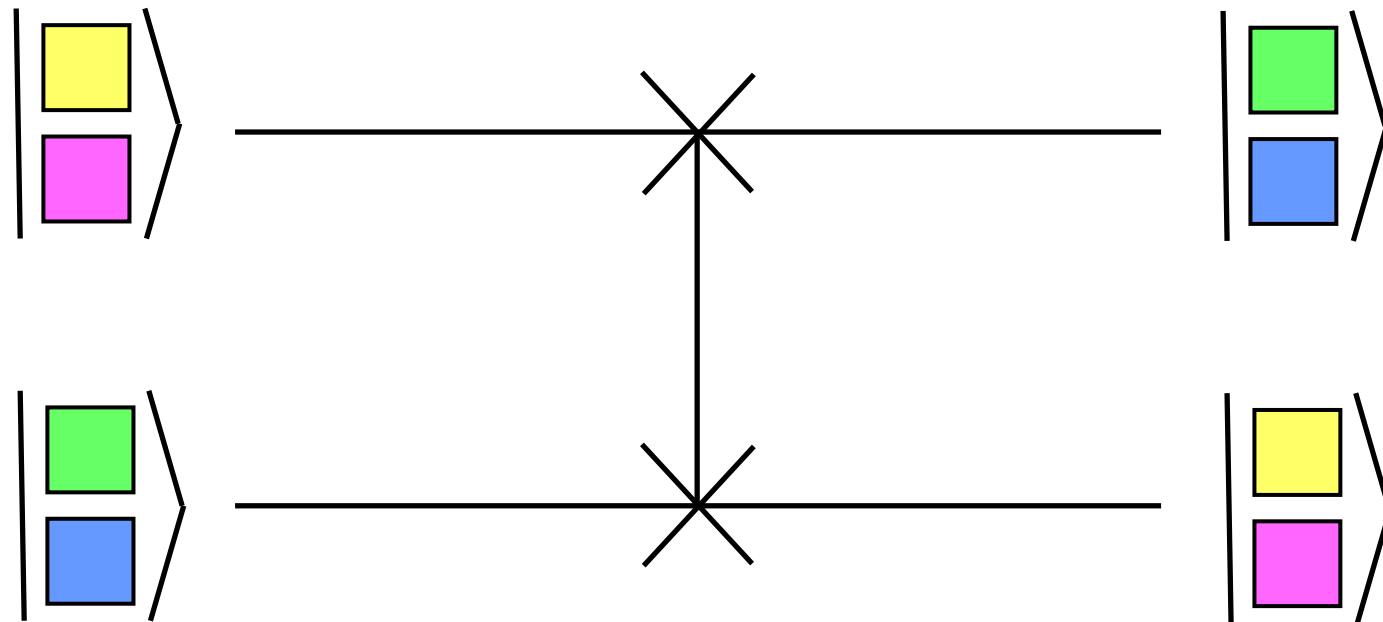
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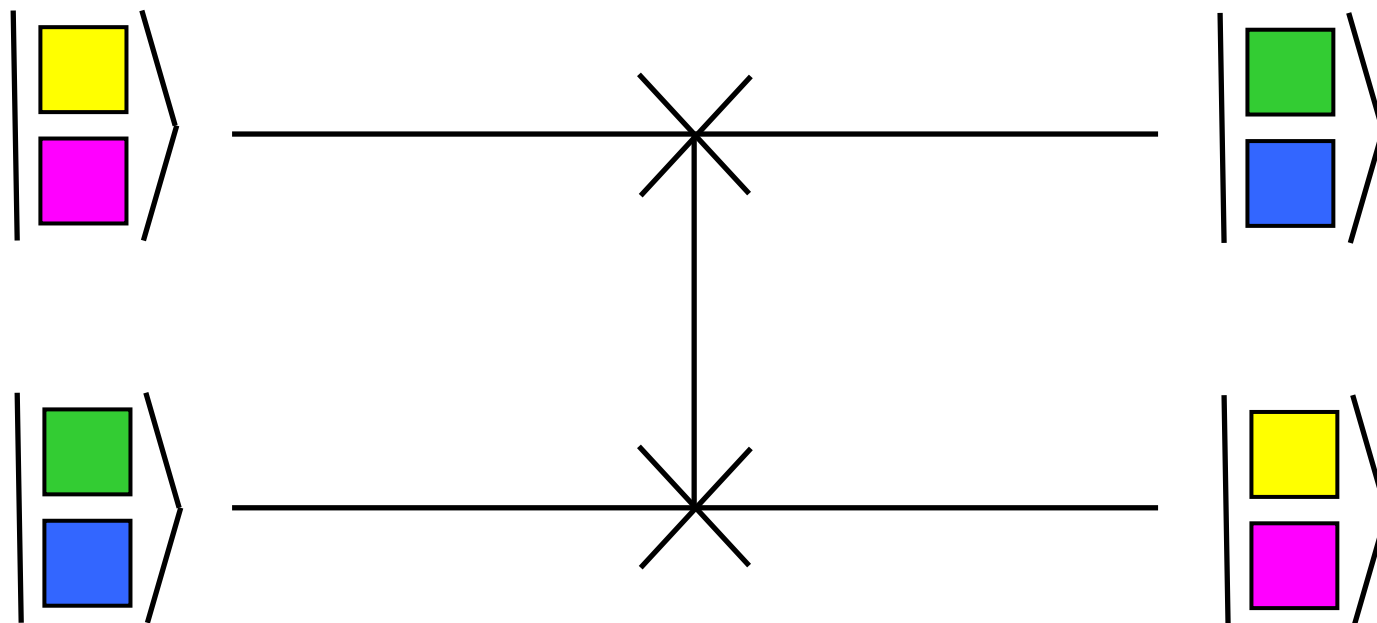
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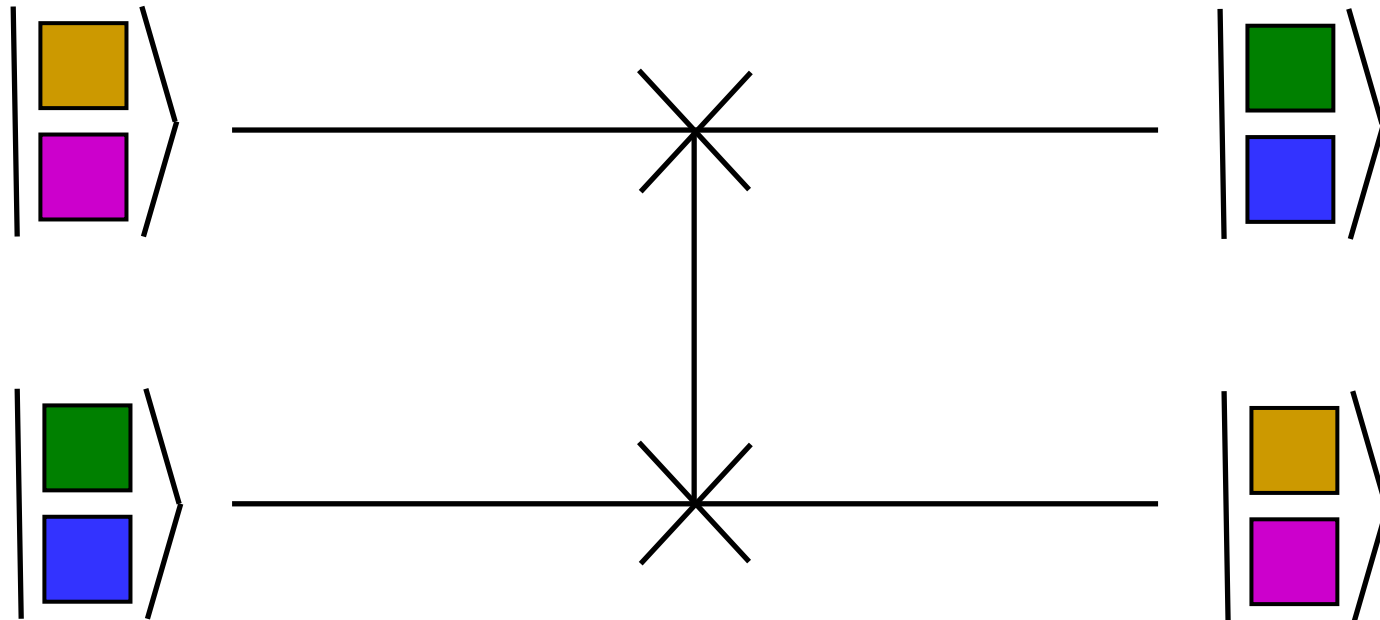
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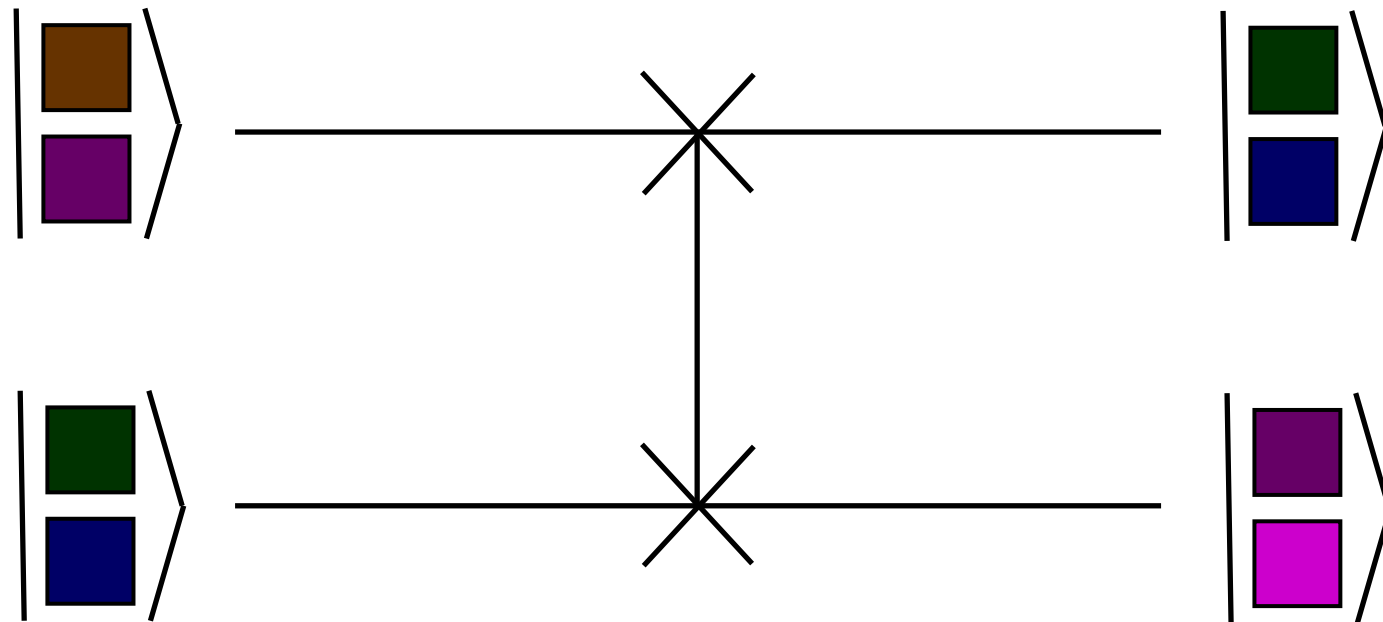
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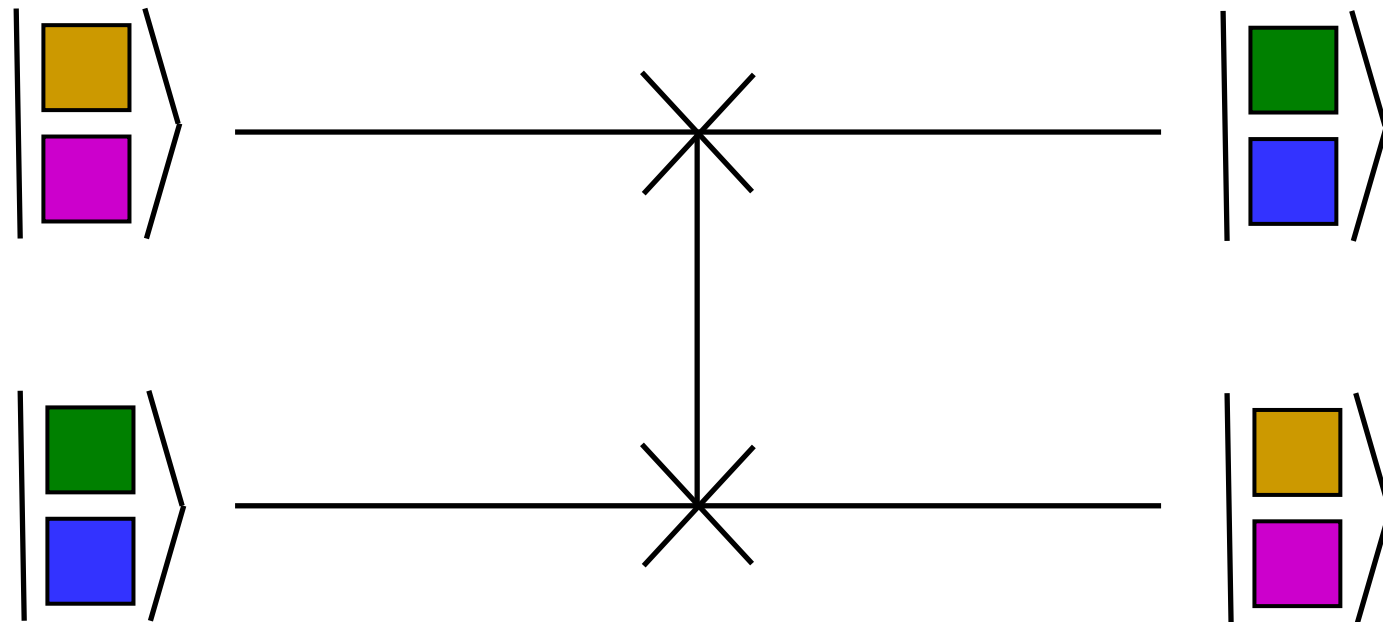


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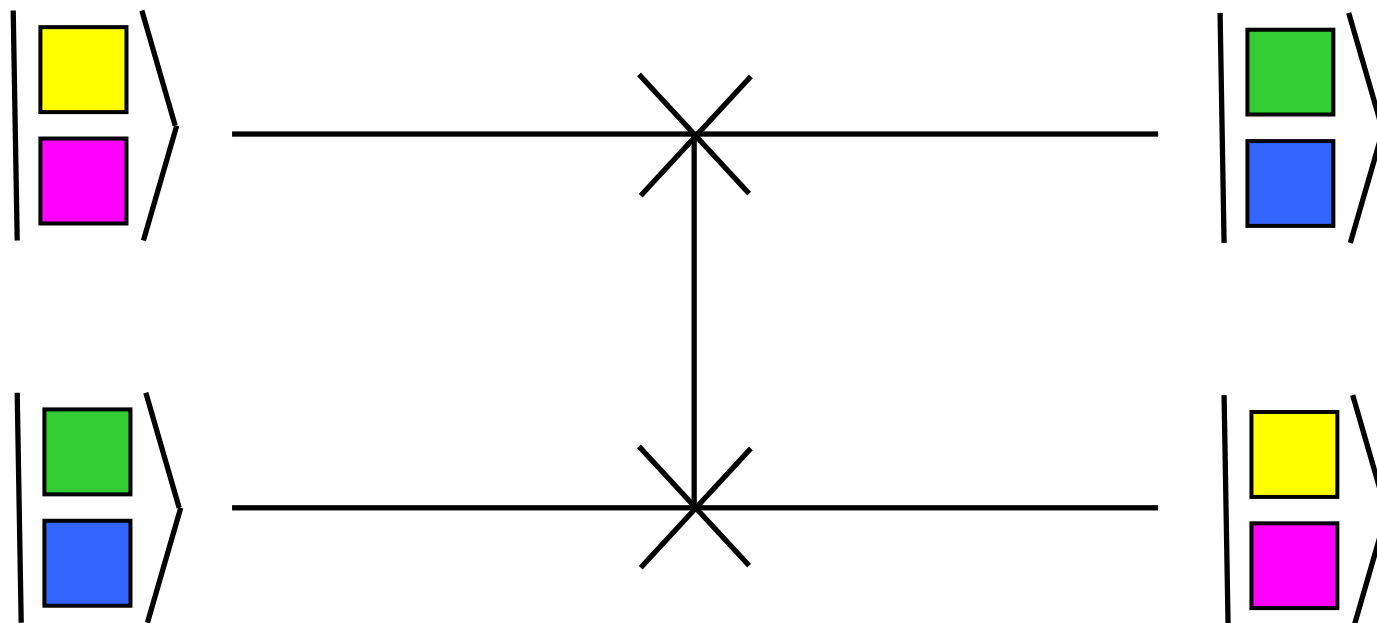
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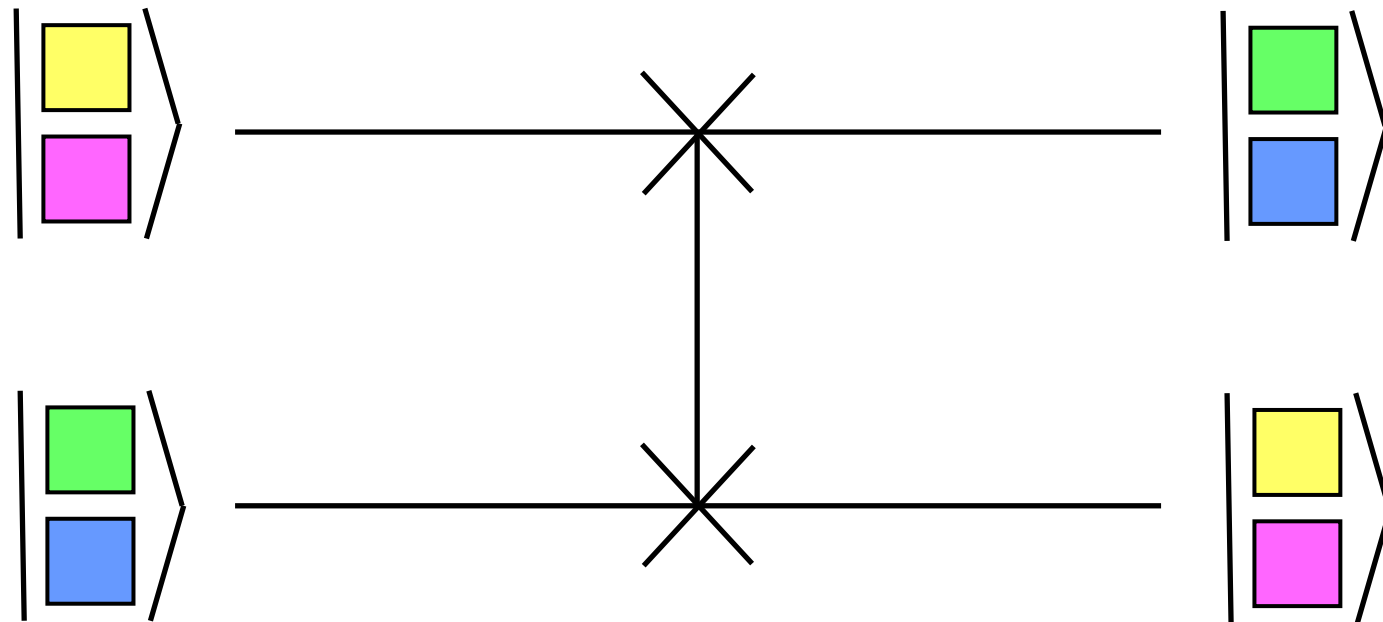
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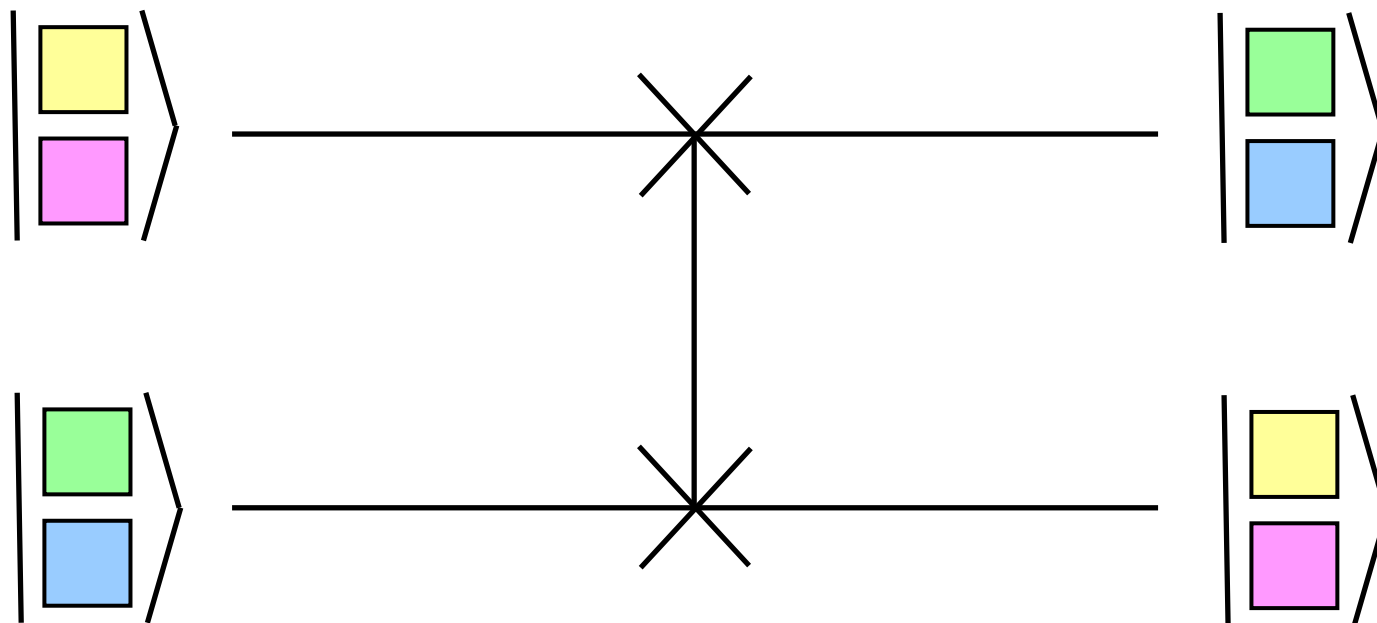
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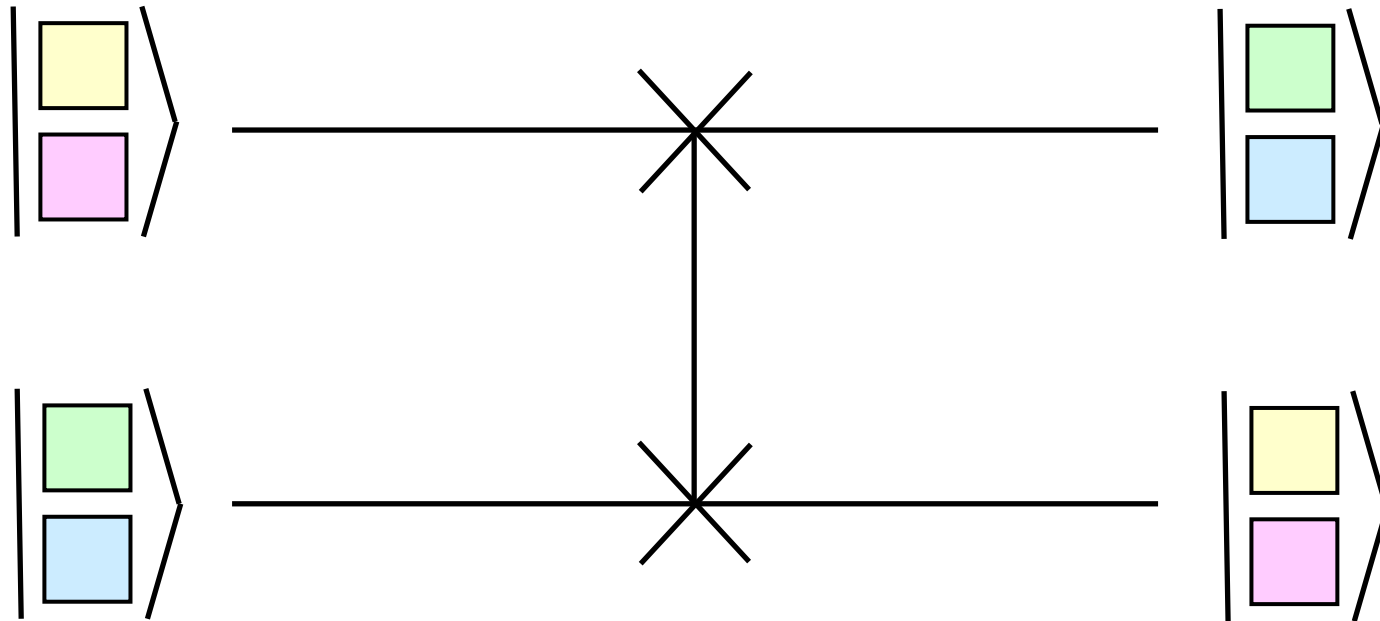
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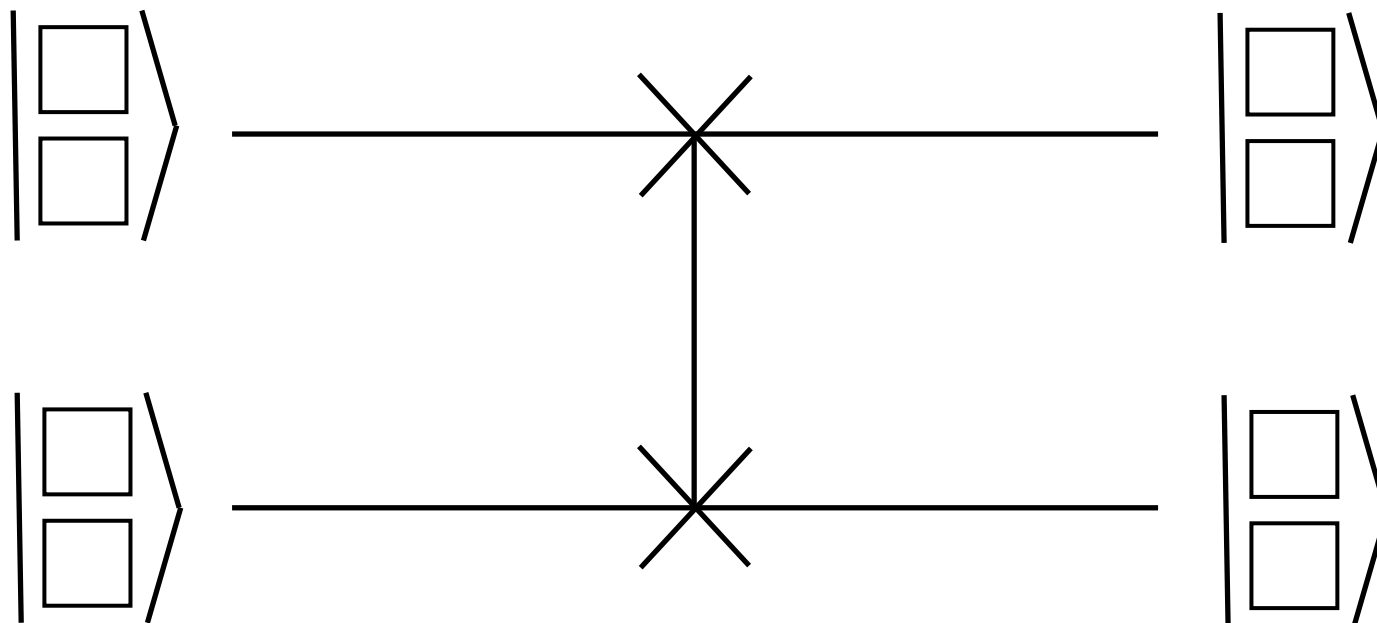
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# Concept of Quantum Computers



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graphical representation of  
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# Concept of Quantum Computers





# Concept of Quantum Computers

- Quantum gates are combined to build more complex quantum calculation units and quantum memory
  - hardware still under development: some working models
  - no standardized design for a general quantum computer

# Concept of Quantum Computers

- Recent news about Google Quantum Computer

<https://www.livescience.com/google-hits-quantum-supremacy.html>

# Concept of Quantum Computers



- **Google Quantum Computer**
  - a basic computing chip using various quantum gates
  - 1.5 trillion times faster than traditional digital computer
  - requires 200 seconds to do equivalent work of 10,000 years by a current super computer

# Concept of Quantum Computers

- **Since the quantum computing chip is just introduced, quantum software is probably at the very infancy stage similar to that of the Assembly Language when the Z80 chip was introduced in the 80s**
  - **low level codes to move data in various memory registers and perform basic arithmetic operation**
  - **proof of concept is shown for comparison with existing computing power**

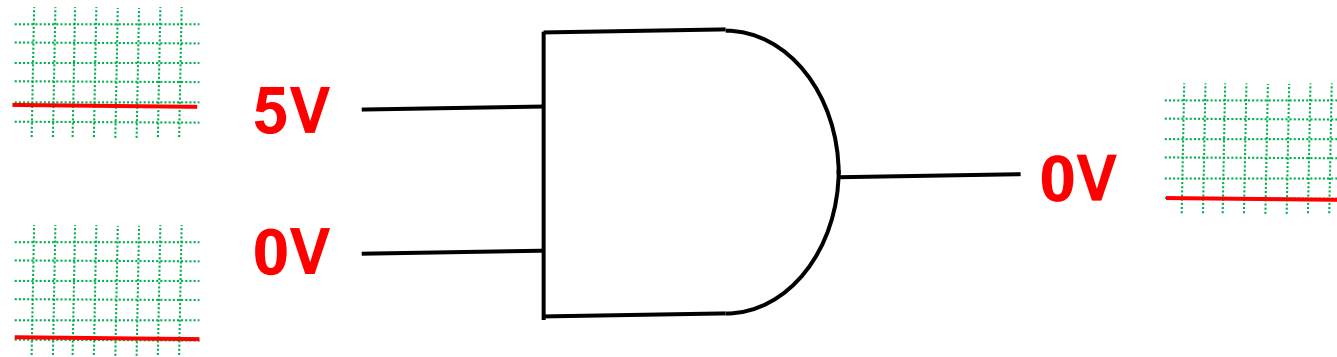
# Concept of Quantum Computers

- **General observation about a quantum computer**
  - a quantum computer is probably fast because it (the hardware) is more spontaneous in its continuous quantum state
  - a quantum computer is probably powerful because more data can be squeezed into a single unit of memory

# Concept of Quantum Computers

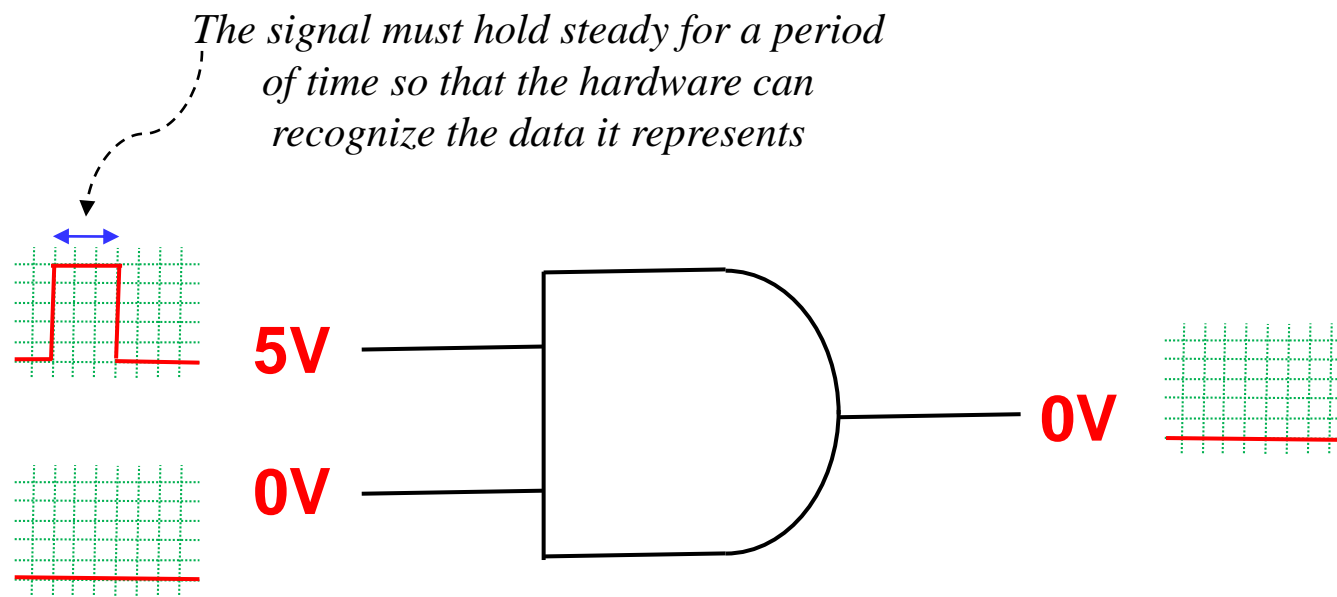


# Concept of Quantum Computers



Traditional Hardware  
In a Digital Computer

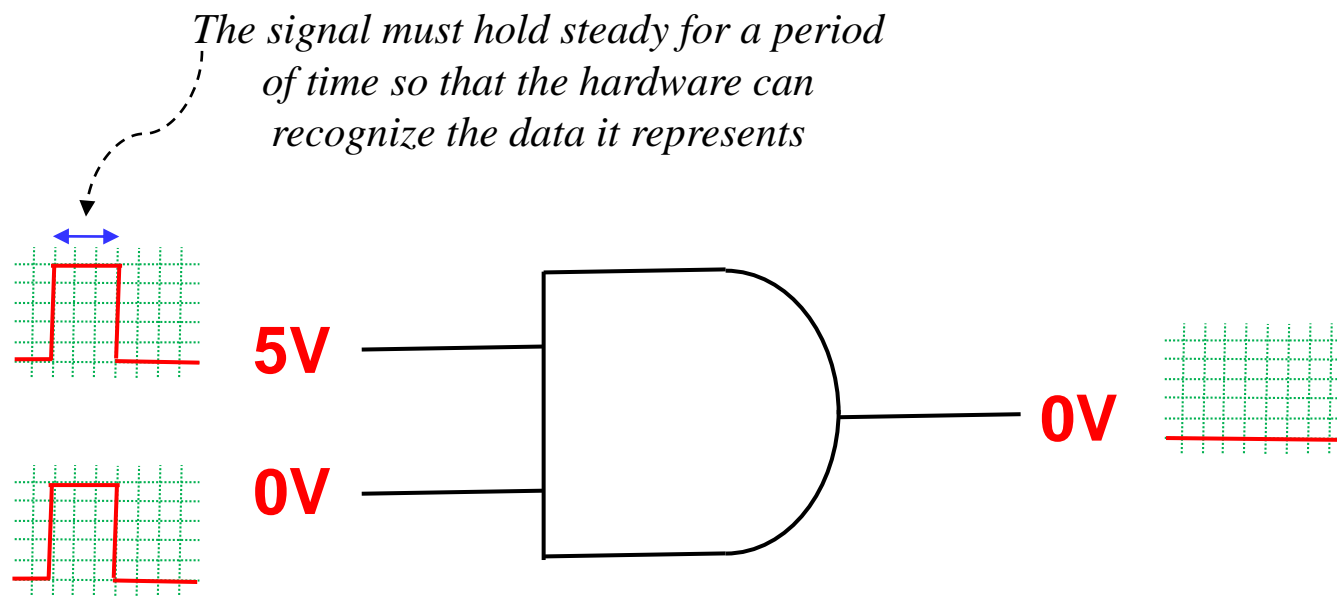
# Concept of Quantum Computers



**Traditional Hardware  
In a Digital Computer**



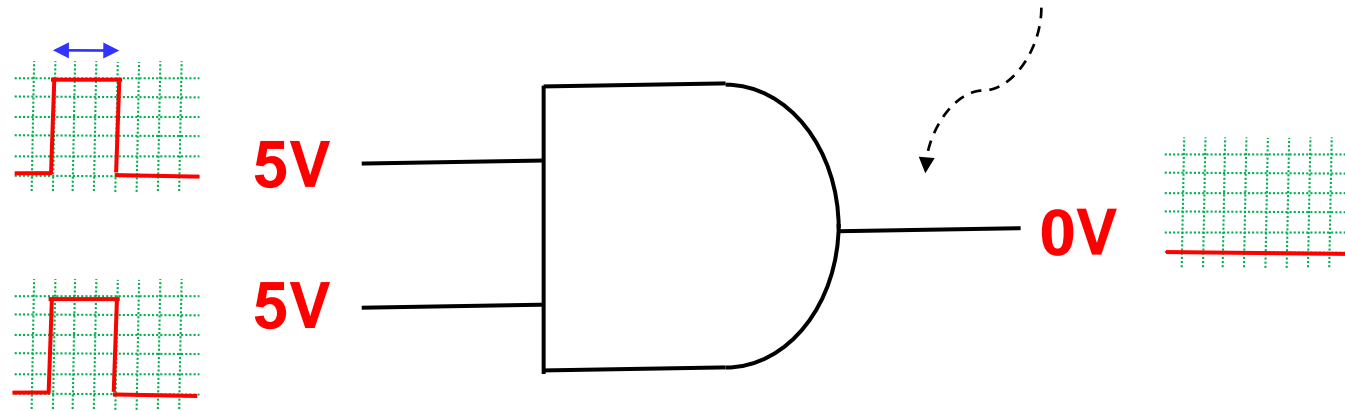
# Concept of Quantum Computers



**Traditional Hardware  
In a Digital Computer**

# Concept of Quantum Computers

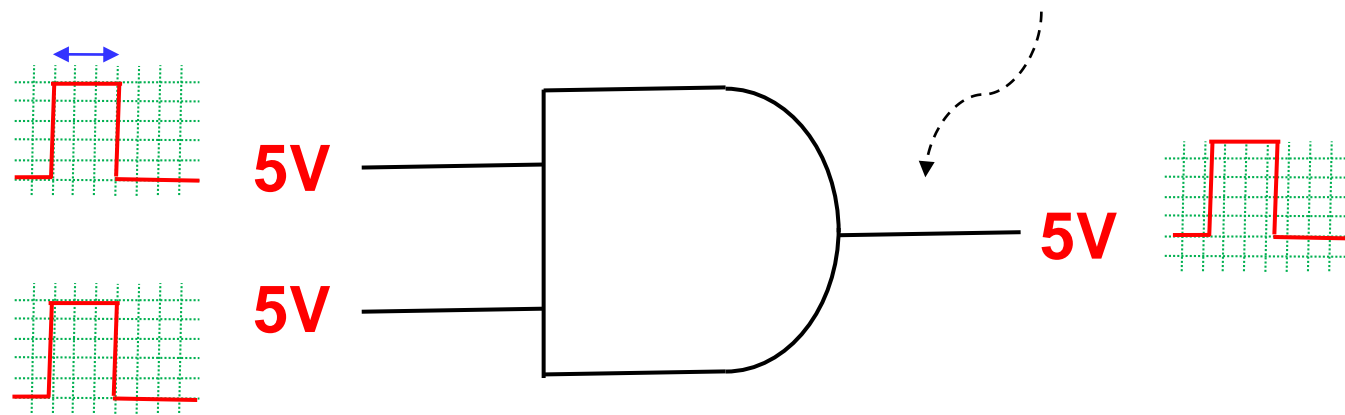
*There will be a brief delay before the hardware can produce the output*



**Traditional Hardware  
In a Digital Computer**

# Concept of Quantum Computers

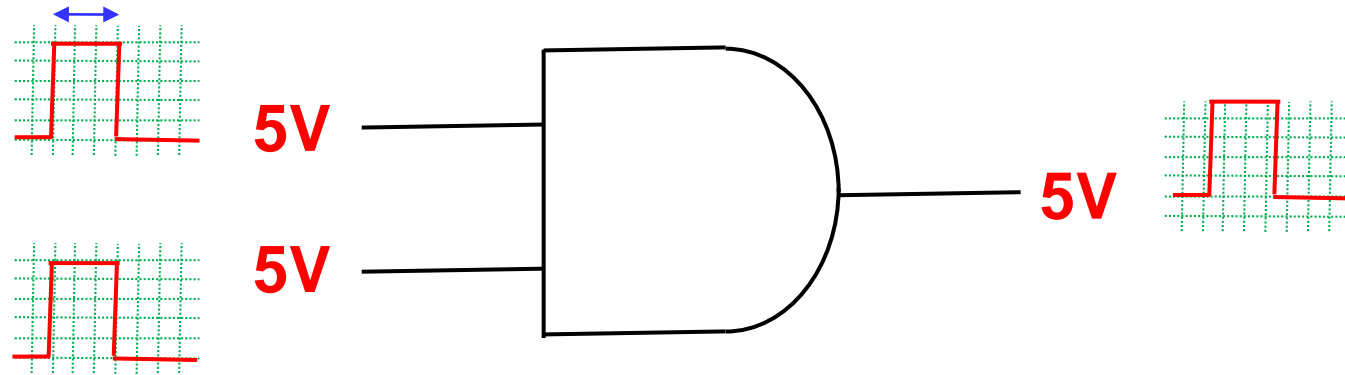
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**Traditional Hardware  
In a Digital Computer**

# Concept of Quantum Computers

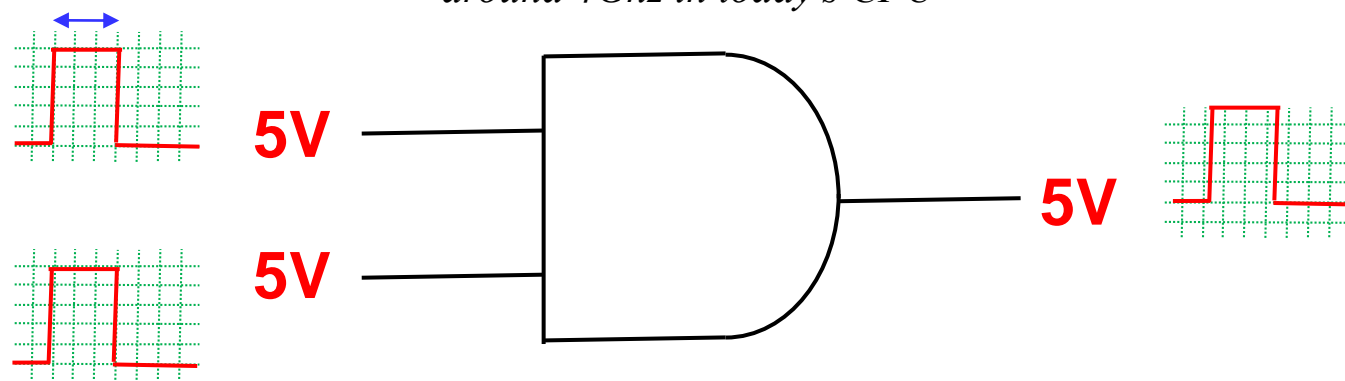
*The duration that a signal must hold steady and the delay of its output defines a computational cycle*



**Traditional Hardware  
In a Digital Computer**

# Concept of Quantum Computers

*The computational cycle has been improved with time, from the 5Mhz to 10 Mhz in the 8088 chip in 1979 to around 4Ghz in today's CPU*

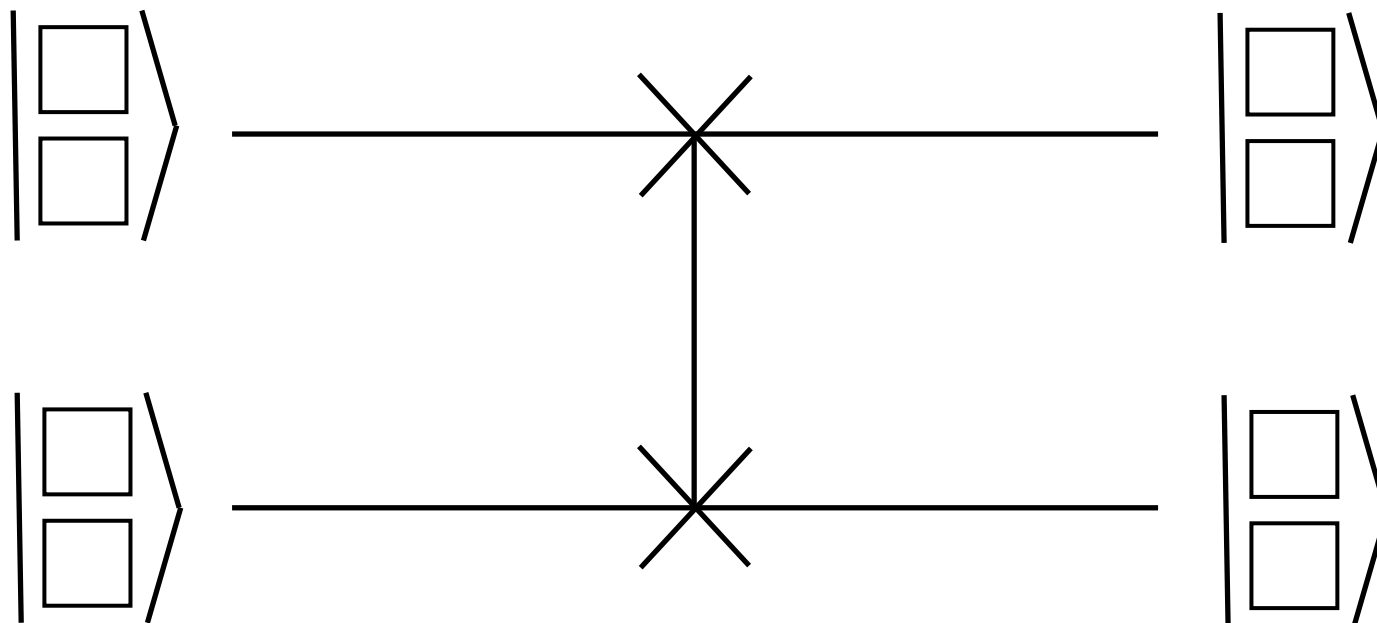


**Traditional Hardware  
In a Digital Computer**

# Concept of Quantum Computers



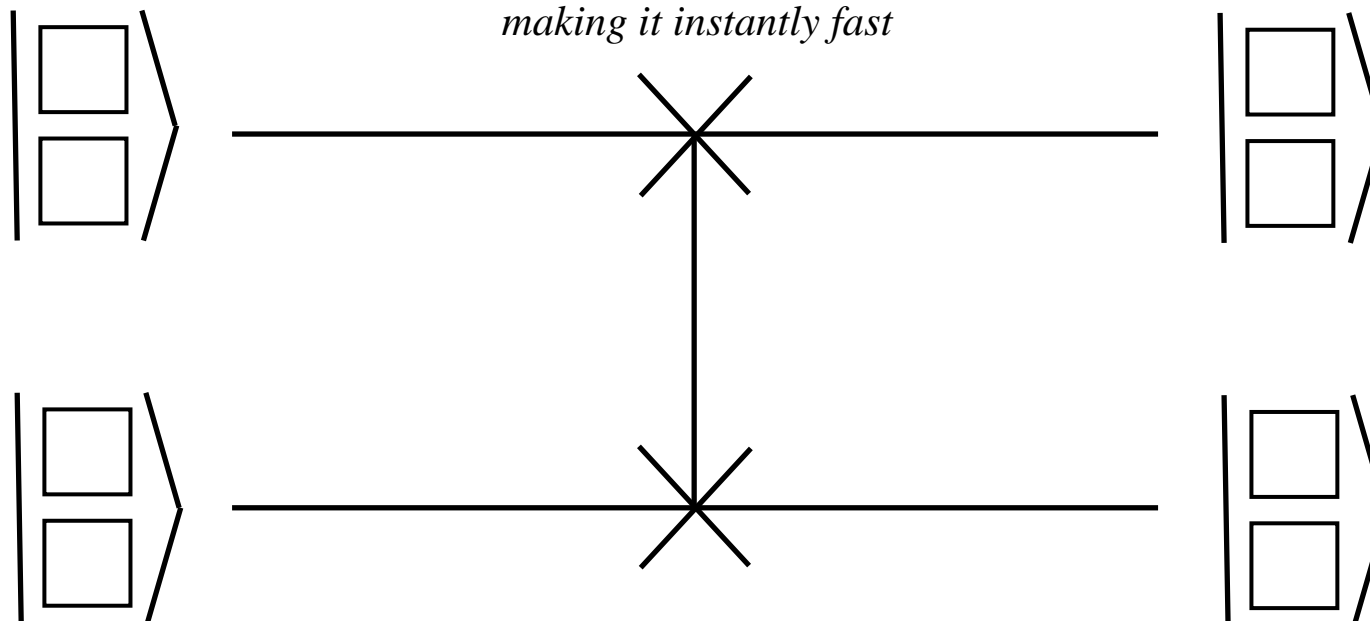
# Concept of Quantum Computers



graphical representation of  
SWAP gate

# Concept of Quantum Computers

*It is speculated that the quantum hardware  
will be spontaneous in managing data,  
making it instantly fast*

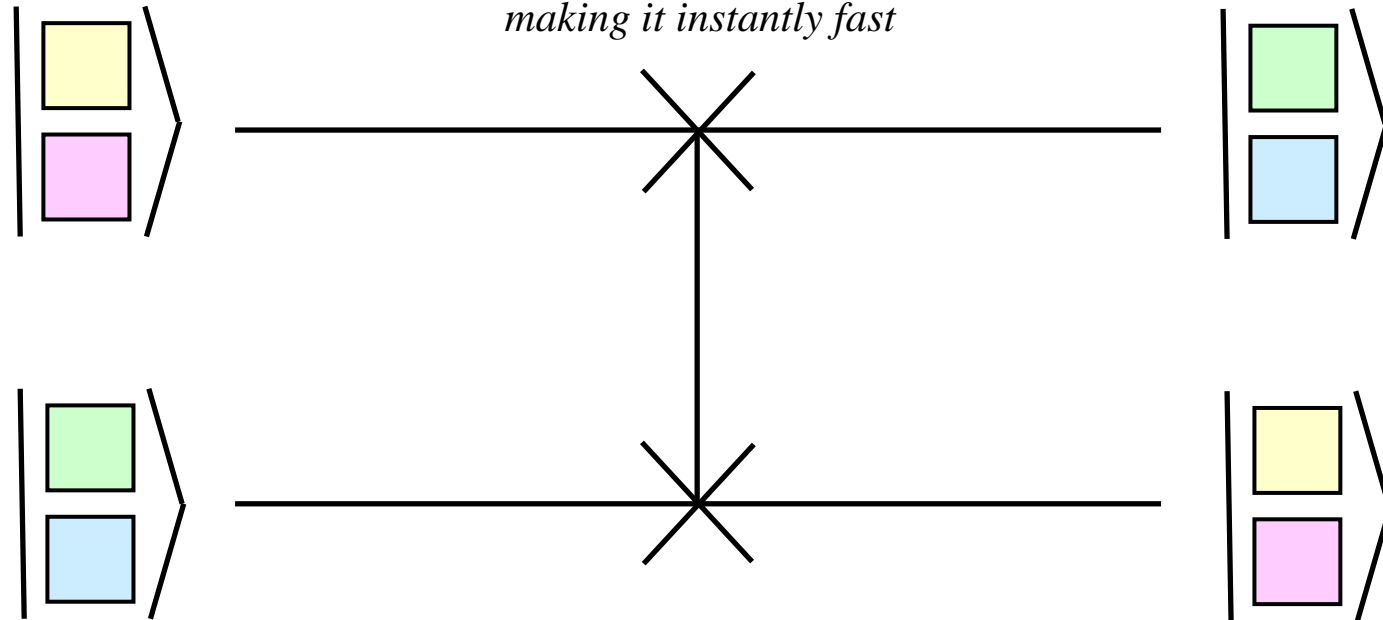


graphical representation of  
SWAP gate



# Concept of Quantum Computers

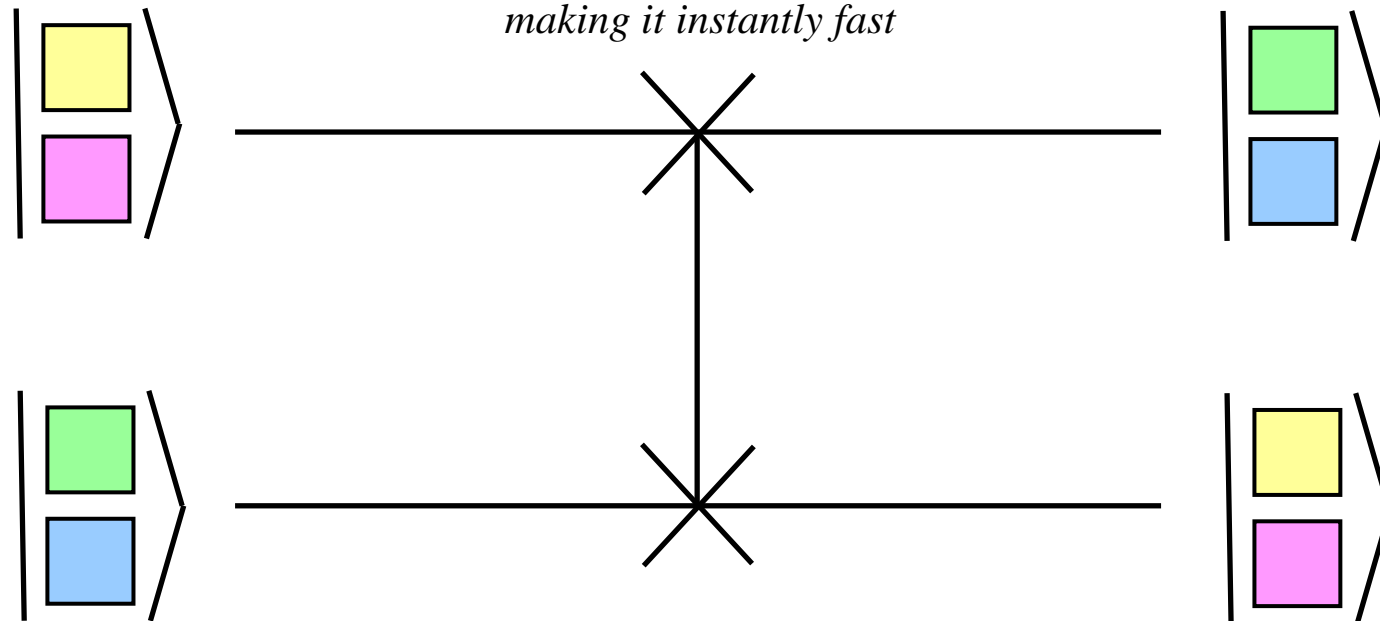
*It is speculated that the quantum hardware  
will be spontaneous in managing data,  
making it instantly fast*



graphical representation of  
SWAP gate

# Concept of Quantum Computers

*It is speculated that the quantum hardware  
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graphical representation of  
SWAP gate

# Concept of Quantum Computers



# Traditional Digital Computers

```
main()  
{  
    int myVariable = 50;  
}
```

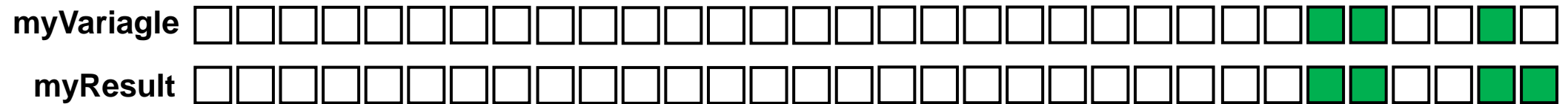
*a number of memory bits must be allocated  
to represent a single number  
in a traditional digital computer*



# Traditional Digital Computers

```
main()  
{  
  int myVariable = 50;  
}
```

*calculation must be repeated in every  
memory bit, making it extremely inefficient*



# Concept of Quantum Computers



# Concept of Quantum Computers

```
main()  
{  
    int myVariable = 50;  
}
```

*theoretically, a single quantum bit should be sufficient to represent a number*

myVariagle

# Concept of Quantum Computers

```
main()  
{  
    int myVariable = 50;  
}
```

*theoretically, a single quantum bit should be sufficient to represent a number*

myVariagle



# Concept of Quantum Computers

```
main()  
{  
    int myVariable = 50;  
}
```

*calculation in just one bit of data must be  
more efficient than calculation in many bits  
of data*

**myVariagle** 

**myResult** 

# Concept of Quantum Computers

```
main()  
{  
    int myVariable = 50;  
}
```

*theoretically, a single quantum bit should be sufficient to represent a number*

myVariagle 

# Concept of Quantum Computers



# Quantum Computing

- **Quantum computing is the process of using quantum computers to perform computationally intensive tasks that a traditional digital computer cannot do within some “reasonable time”**
  - **as proof concept, quantum computers are designed to do calculation similar to traditional digital computer for comparison**
  - **in reality, a quantum computer can be designed radically different to do things beyond our imagination**

# Quantum Computing

- **Software designed for quantum computing is probably very basic and application dependent so that**
  - **brute computational power can be measured and benchmarked**
  - **the programming language supporting quantum software will evolve with the advance of the quantum hardware**

# Quantum Computing



# Research Topics & Applications

- **Since quantum computers demonstrated a tremendous computational power, the push to advancement is justified**
  - hardware development
  - software development
  - application development

# Research Topics & Applications

- **Hardware Development**
  - **chip designs: CPU, memory, storage, etc.**
  - **integration designs: data bus**
  - **supporting designs: cooling systems, chip interface**



# Research Topics & Applications

- **Software Development**

- **programming language: simplification of the coding process**
- **compiler: efficient translation of programming language to basic instructions in a quantum chip**
- **simulation: testbed environment for both hardware development and software development**

# Research Topics & Applications

- **Application Development**
  - **since quantum computing is still in its infancy, application development often focus on problems that require intense computational power**
    - encryption & decryption
    - big data

# Research Topics & Applications



# Research Topics & Applications

- Application Development

- **encryption** is the process of scrambling data into something that unauthorized users cannot understand
  - encryption algorithms depend on mathematical formula that is known to everybody
  - the secret of encryption is kept in a key that only an authorized user has to decrypt the data

# Research Topics & Applications

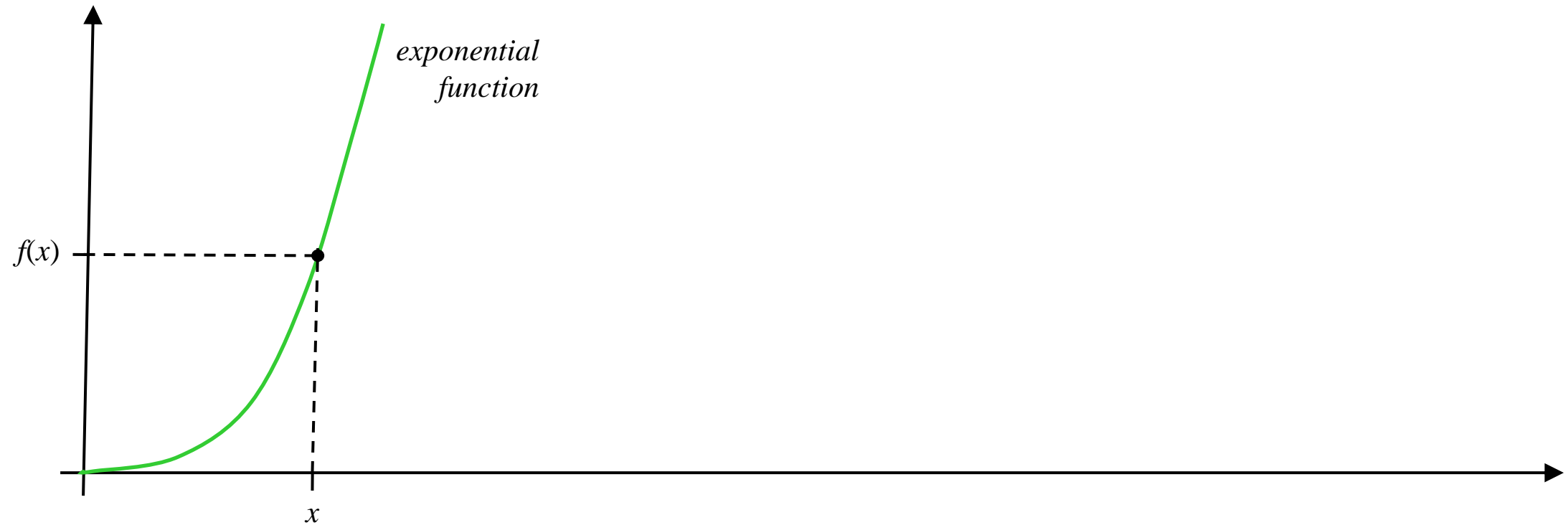
- Application Development

- *encryption algorithms* often develop around the exponential function and the mod function
  - the exponential function permits the development of reverse algorithms
  - the mod function prevents derivation of an inverse function the original data

# Research Topics & Applications

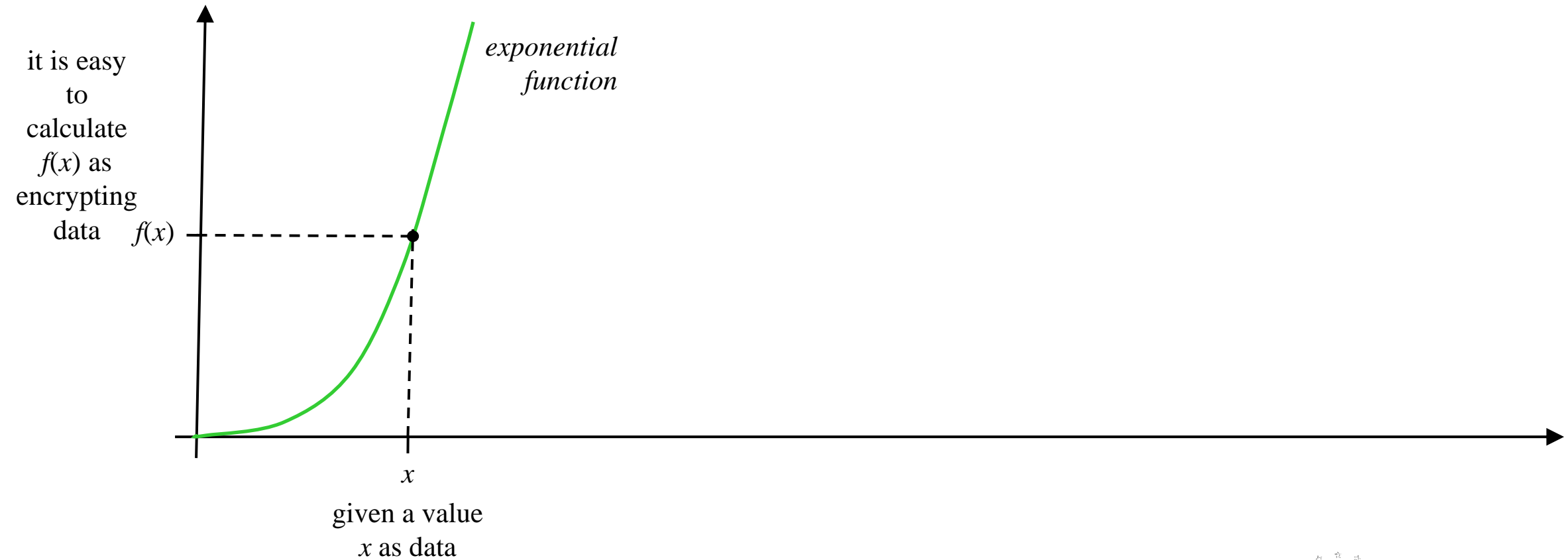


# Research Topics & Applications



given a value  
 $x$  as data

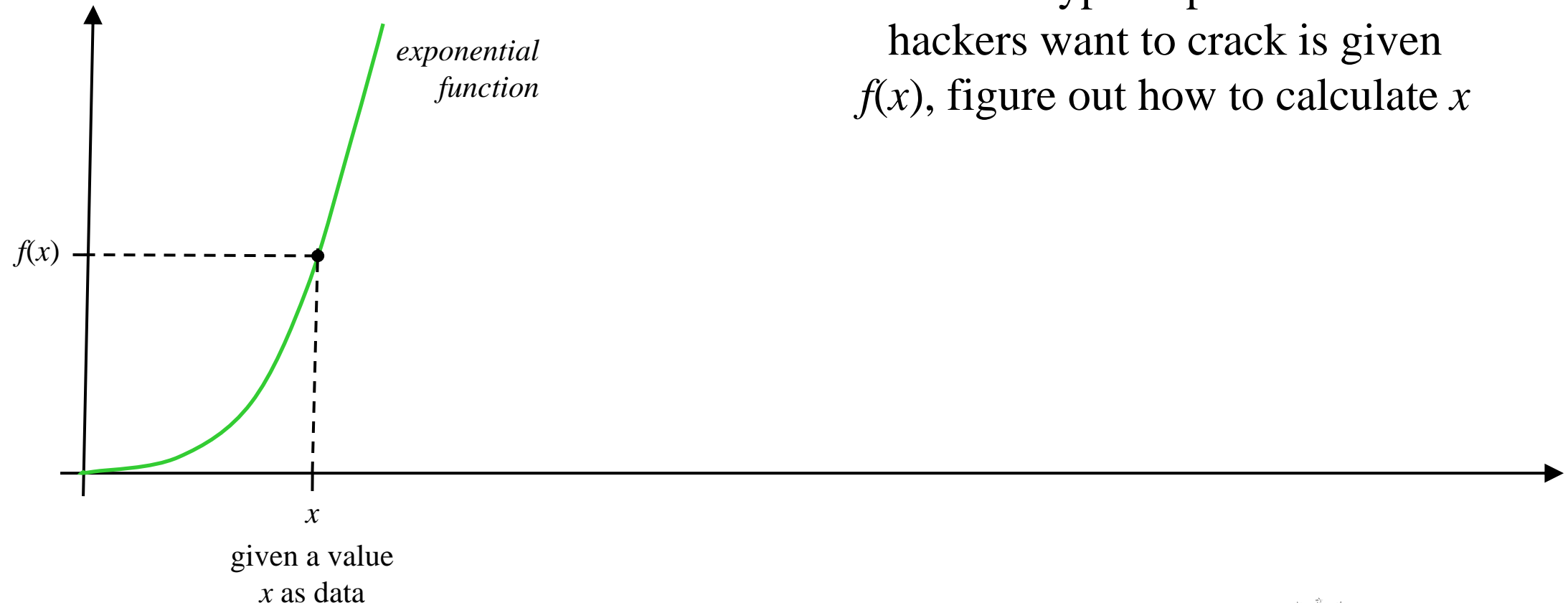
# Research Topics & Applications



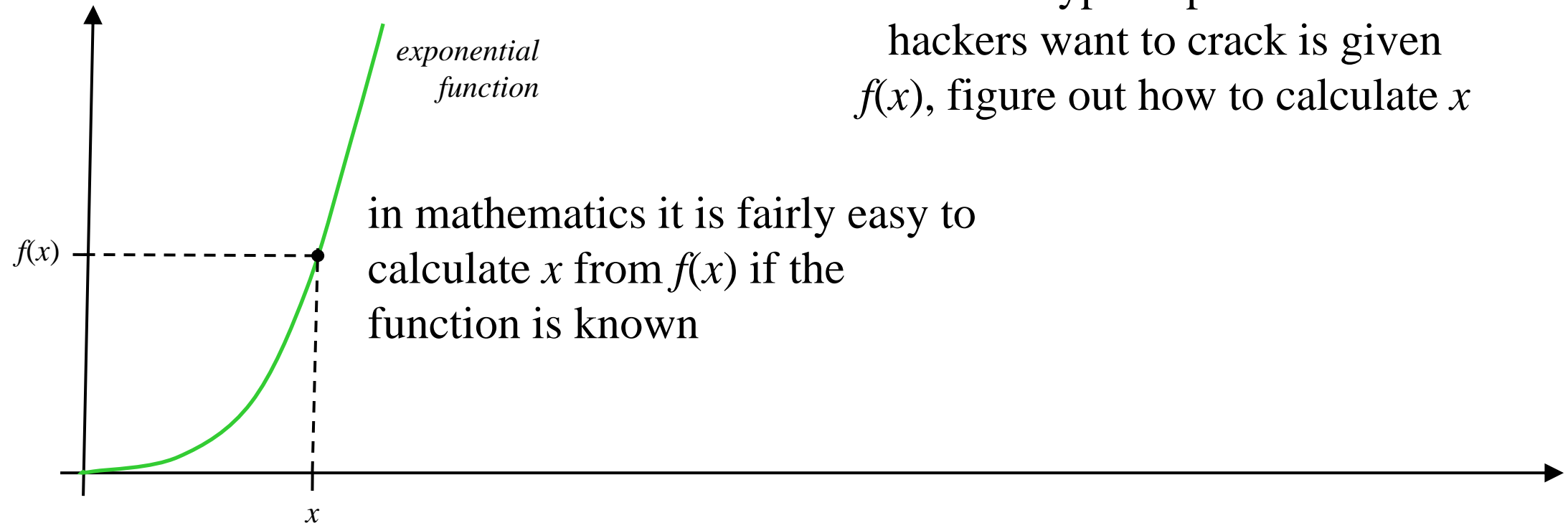


# Research Topics & Applications

the decryption problem that hackers want to crack is given  $f(x)$ , figure out how to calculate  $x$



# Research Topics & Applications



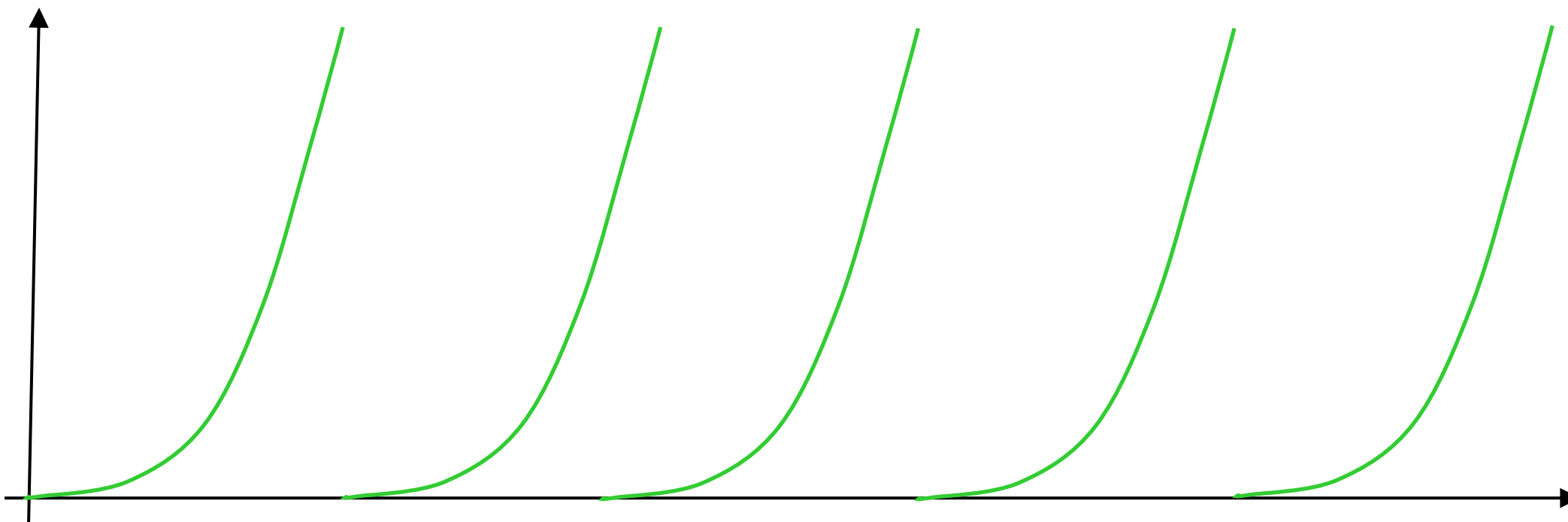
the decryption problem that hackers want to crack is given  $f(x)$ , figure out how to calculate  $x$

in mathematics it is fairly easy to calculate  $x$  from  $f(x)$  if the function is known

given a value  $x$  as data

# Research Topics & Applications

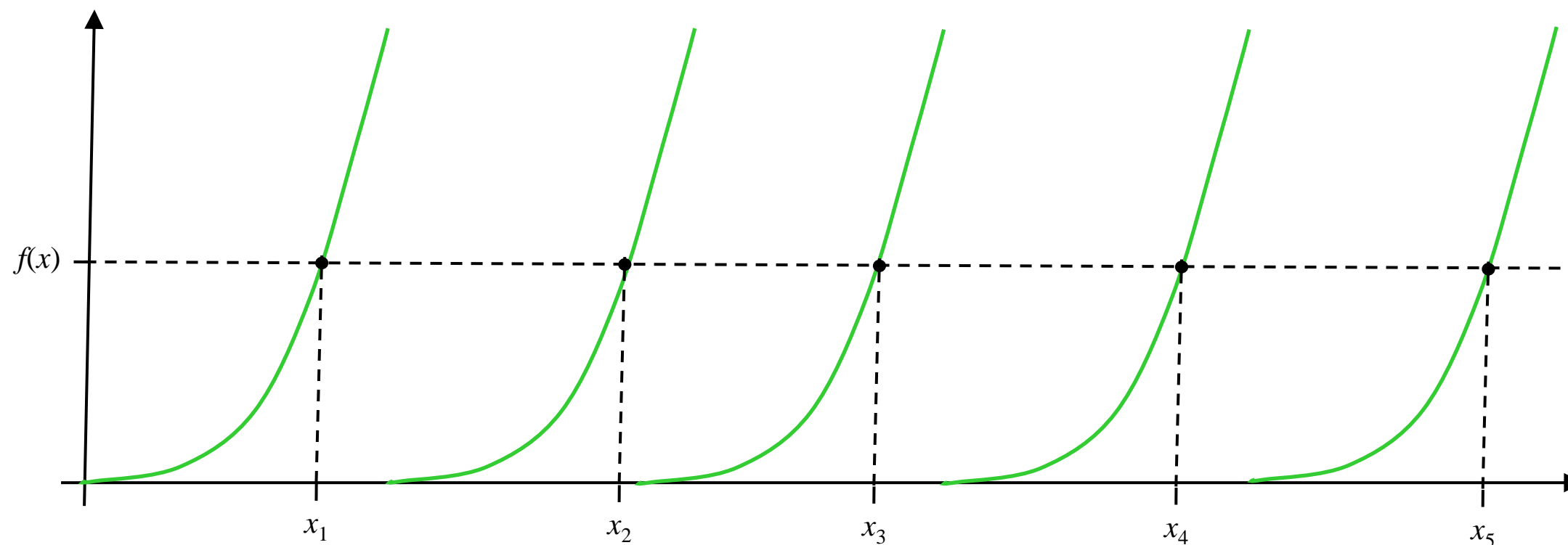
*mod of an exponential function*



the mod function is used to  
prevent reverse engineering

# Research Topics & Applications

*mod of an exponential function*



for a given value  $f(x)$ , there are infinitely many possible values  $x$  that satisfy the equation, making it impossible to solve for  $x$

# Research Topics & Applications

- **Application Development**

- **breaking an encryption algorithm requires additional clue**
  - the context of the data, e.g., the English language and its vocabulary
  - the construction of the data structure, e.g., how a cypherblock is built based on a sequence of many data points

# Research Topics & Applications

- Application Development

- breaking an encryption algorithm is mathematically possible but requires a lot of computational power to evaluate the correct combination to determine a key
  - a strong encryption is how much time it requires to crack the key (in the order of  $10^x$  years, with  $x$  being very large)
  - a quantum computer that can perform a calculation task that requires a traditional digital computer  $10^x$  years to complete, but only in a few hundred seconds will *radically* change the practice of cybersecurity

# Research Topics & Applications



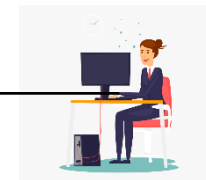
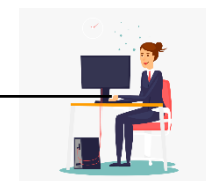
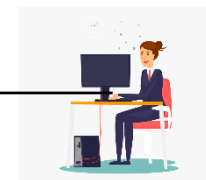
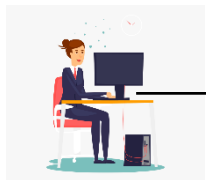
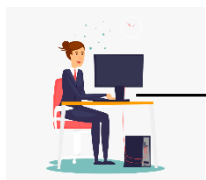
# Research Topics & Applications

- **Application Development**

- **big data is the analytic process of working with a massive amount of data that traditional method of handling them cannot perform**
  - big data normally refers to data of all activities on the Internet
  - processing big data often involves data mining algorithm to discover pattern of behavior (both individual behavior and collective behavior)
  - current data mining algorithms are computationally intensive and cannot deliver the results on big data within some “reasonable time”



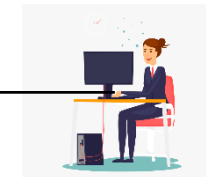
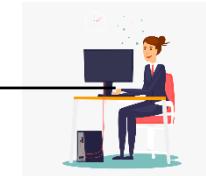
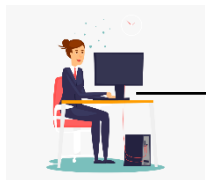
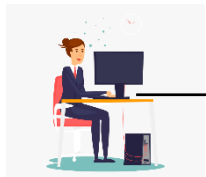
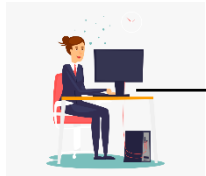
# Research Topics & Applications



# Research Topics & Applications



*Internet and its Activities*

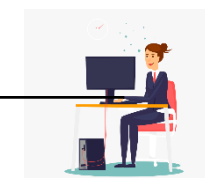
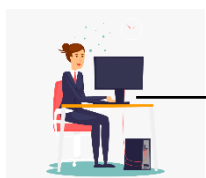
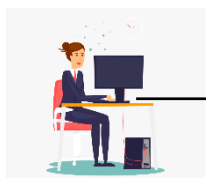
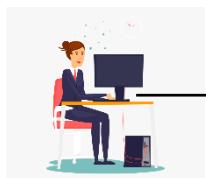
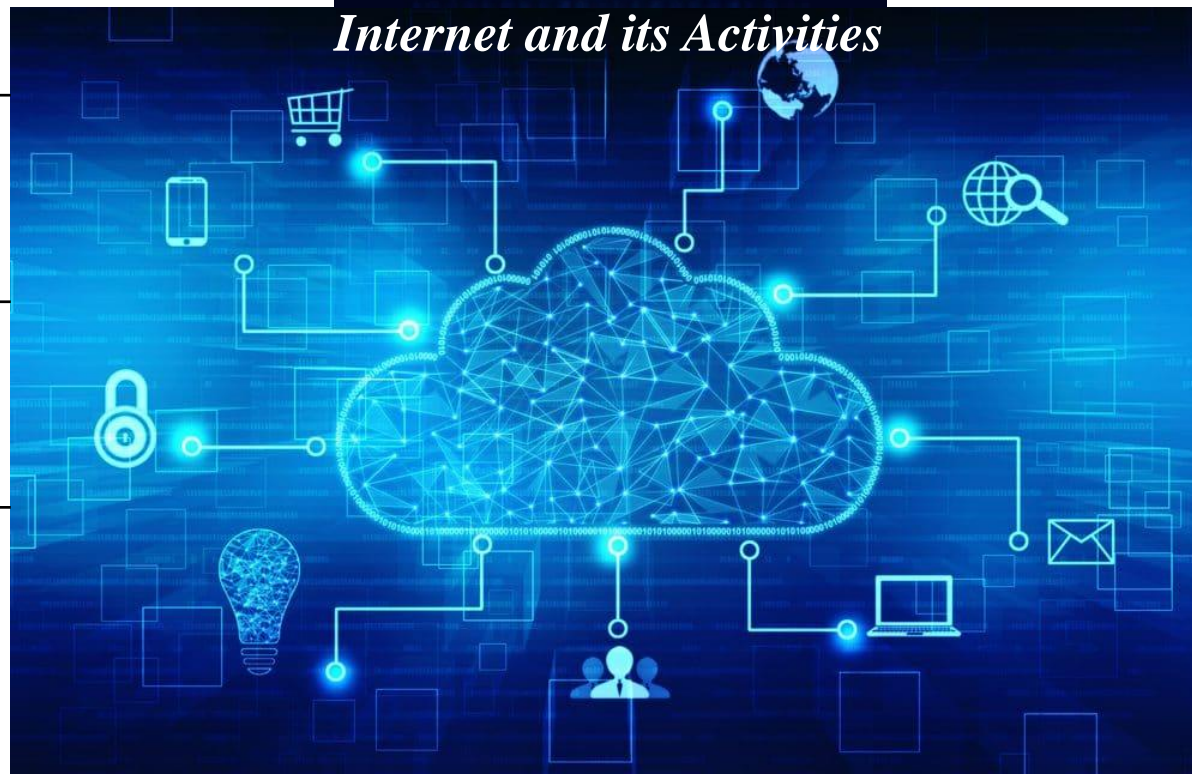


# Research Topics & Applications

Google



*Internet and its Activities*



# Research Topics & Applications





# Conclusion



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- Quantum computing is a reality that is happening right now

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- **While quantum computing is still evolving, it is always possible to do R&D work through simulations without waiting for access of an actual working quantum computer**

# Conclusion

- Quantum computing is a reality that is happening right now
- While quantum computing is still evolving, it is always possible to do R&D work through simulations without waiting for access of an actual working quantum computer
- **The future world with quantum computers is both exciting and scary, thus it is important for us to collaborate together to prepare ourselves for it**



# THANK YOU

