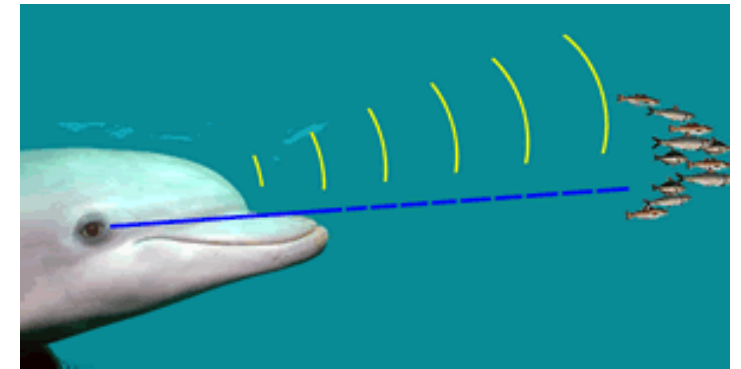
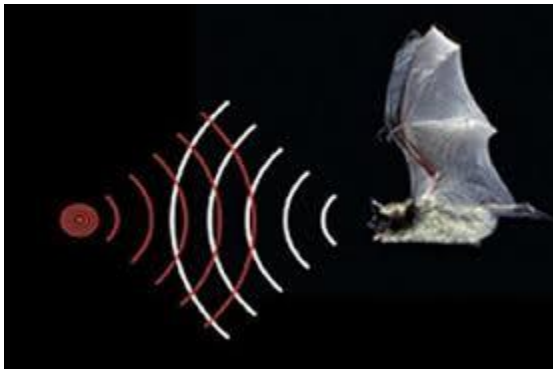


UWB Passive SAW Sensors Based on Hyperbolic Frequency Modulation (HFM)

Victor Plessky

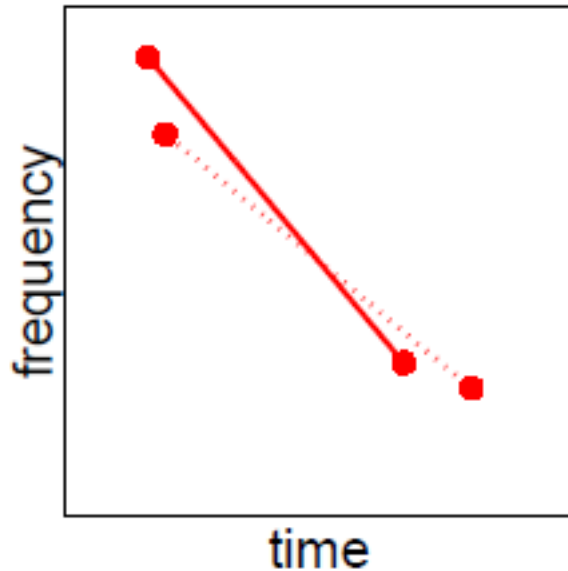
Thanks to Marc Lamothe

PWST Workshop, 10-12 Oct. 2017
Montreal, Canada



But do the bats and dolphins use LFM chirps?

linear chirp

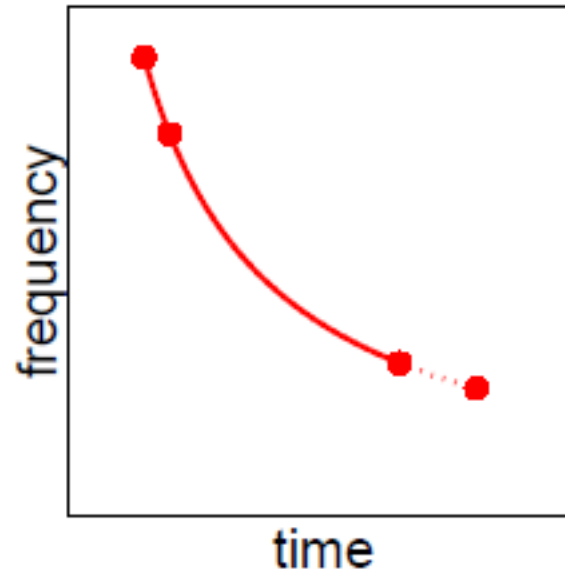


$$B * T * (K - 1) > 1$$

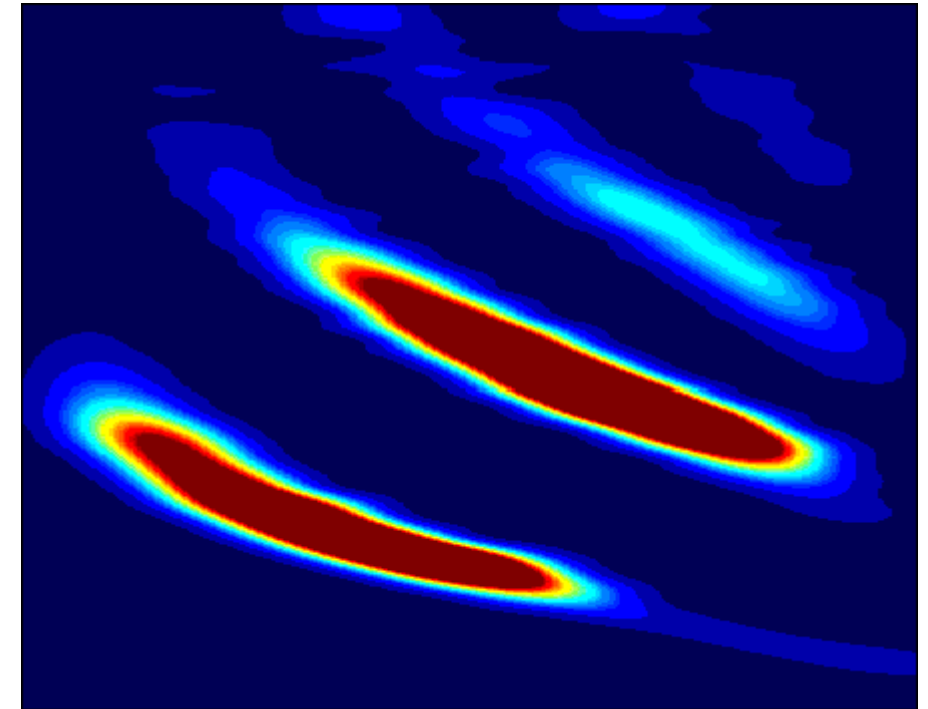
(K- scaling factor)

LFM signal compression
deteriorates significantly

hyperbolic chirp

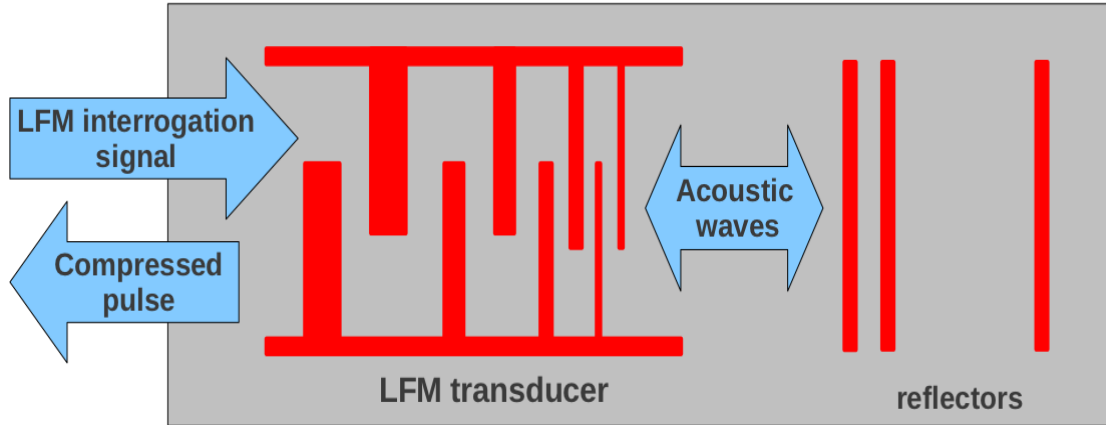


No visible deterioration of
compressed pulse



horizontal axis: time (0-2.5ms),
vertical axis: frequency (0-70kHz)

Purely geometric problem



$$x_{n+1} - x_n = p_0 + \varepsilon \cdot x_n$$

This formula can be treated as an equation in integer numbers, which has unique solution:

$$x_n = \frac{(1+\varepsilon)^n - 1}{\varepsilon} \cdot p_0$$

If the period of an array increases linearly with coordinate, how can the coordinate x_n of n -th element of this array be calculated?

For the geometric structure of electrodes (strips, grooves, etc.) with period linearly changing with coordinate x one can write the following relation:

For algebra amateurs (1)

Or, calculating the n -th period:

$$p_n = x_{n+1} - x_n = (1 + \varepsilon)^n \cdot p_0$$

Two parameters p_0 and ε completely determine the array.

If we fix the first period p_0 and the last period $x_{N+1} - x_N = p_{end}$ we can find that

$$\varepsilon = \left(\frac{p_{end}}{p_0}\right)^{\frac{1}{N}} - 1$$

and re-write the formulas (2) and (3) in the following form:

$$x_n = \frac{\left(\frac{p_{end}}{p_0}\right)^{\frac{n}{N}-1}}{\left(\frac{p_{end}}{p_0}\right)^{\frac{1}{N}-1}} \cdot p_0 \quad , \quad p_n = \left(\frac{p_{end}}{p_0}\right)^{\frac{n}{N}} \cdot p_0$$

For algebra amateurs (2)

If the total length $L=x_N$ of the structure is known the number of periods N :

$$\left(\frac{p_{end}}{p_0}\right)^{\frac{1}{N}} = 1 + \frac{p_{end}-p_0}{L}; \quad x_n = L \cdot \frac{p_0}{p_{end}-p_0} \cdot \left\{ \left(\frac{p_{end}}{p_0}\right)^{\frac{n}{N}} - 1 \right\}$$

If our structure corresponds to a SAW propagating with velocity V , and the periods of the structure are related to frequency as

$$p_0 = \frac{V}{(F_0 - \frac{B}{2})}, \quad p_{end} = \frac{V}{(F_0 + \frac{B}{2})}$$

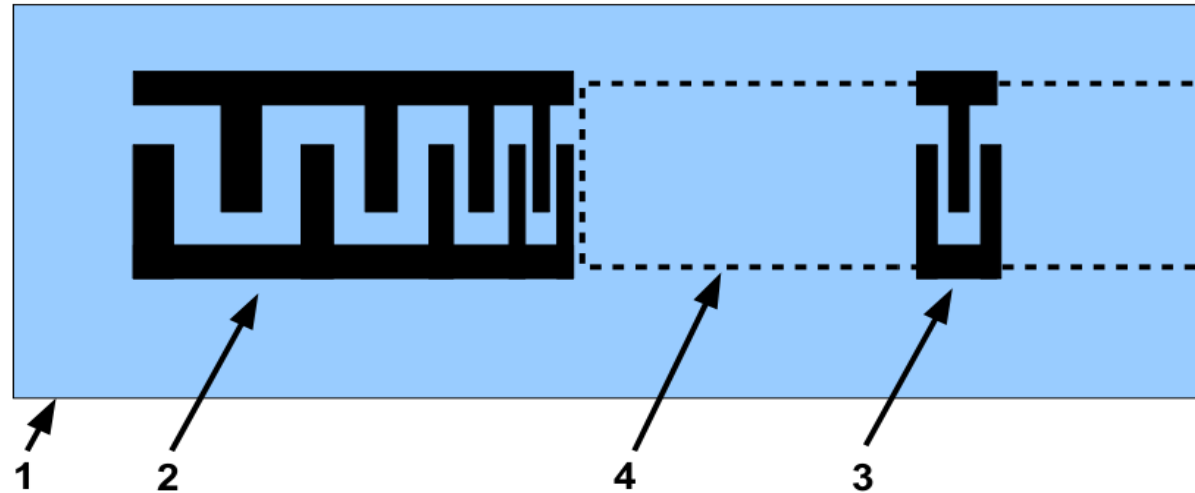
(here F_0 is the centre frequency, $|B|$ - the frequency band),

introducing $L=x_N$ - total length, for the case when there is 1 element per period (RACs):

$$x_n = -L \cdot \frac{F_0 + B/2}{B} \cdot \left\{ \left(1 - \frac{B \cdot V}{L \cdot (F_0^2 - (\frac{B}{2})^2)} \right)^n - 1 \right\}$$



Numeric simulations



128°-LiNbO₃

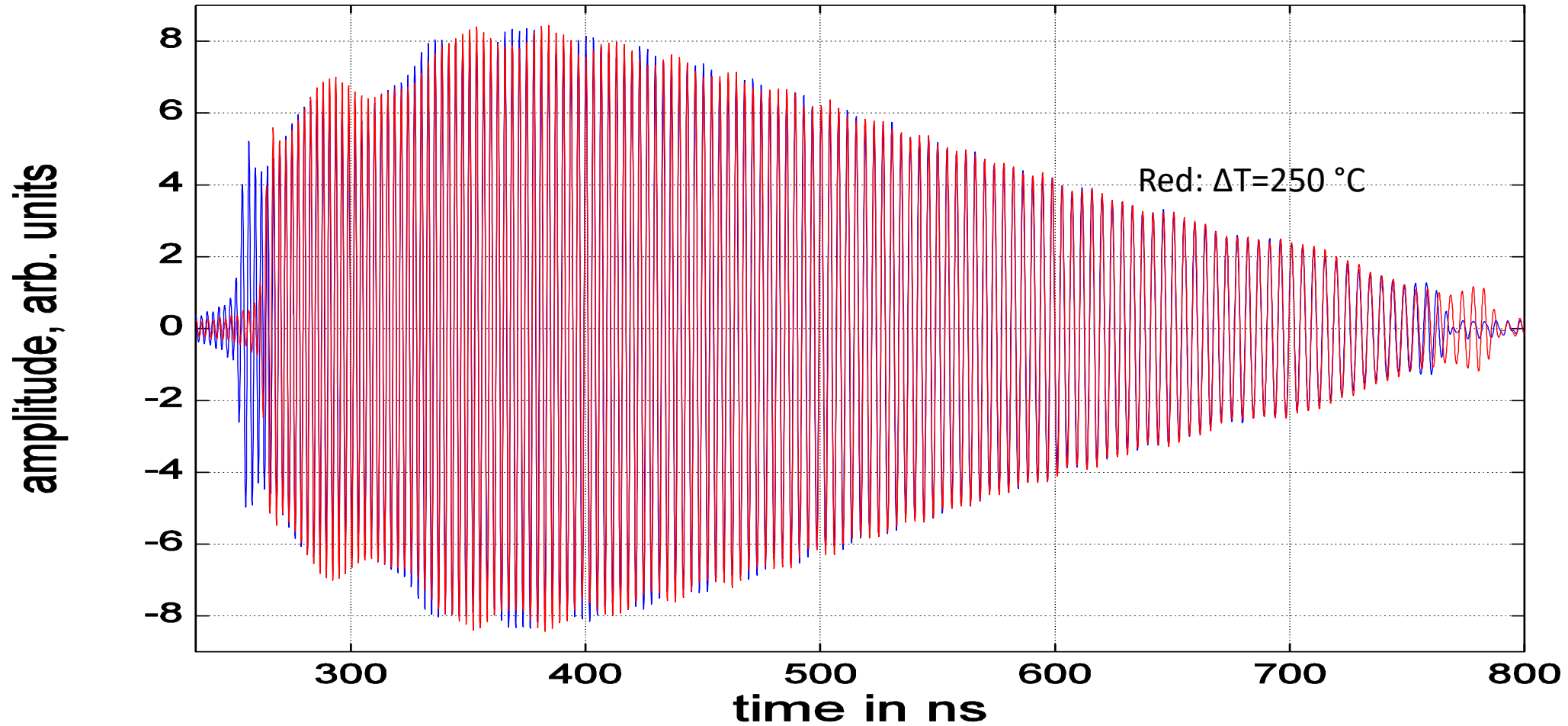
frequency range 200MHz-400MHz

The dispersive delay time T is equal to 0.5 μ s, $B \cdot T$ product thus being $B \cdot T = 100$

$P_0 = 19.2 \mu\text{m}$, $p_N = 9.6 \mu\text{m}$

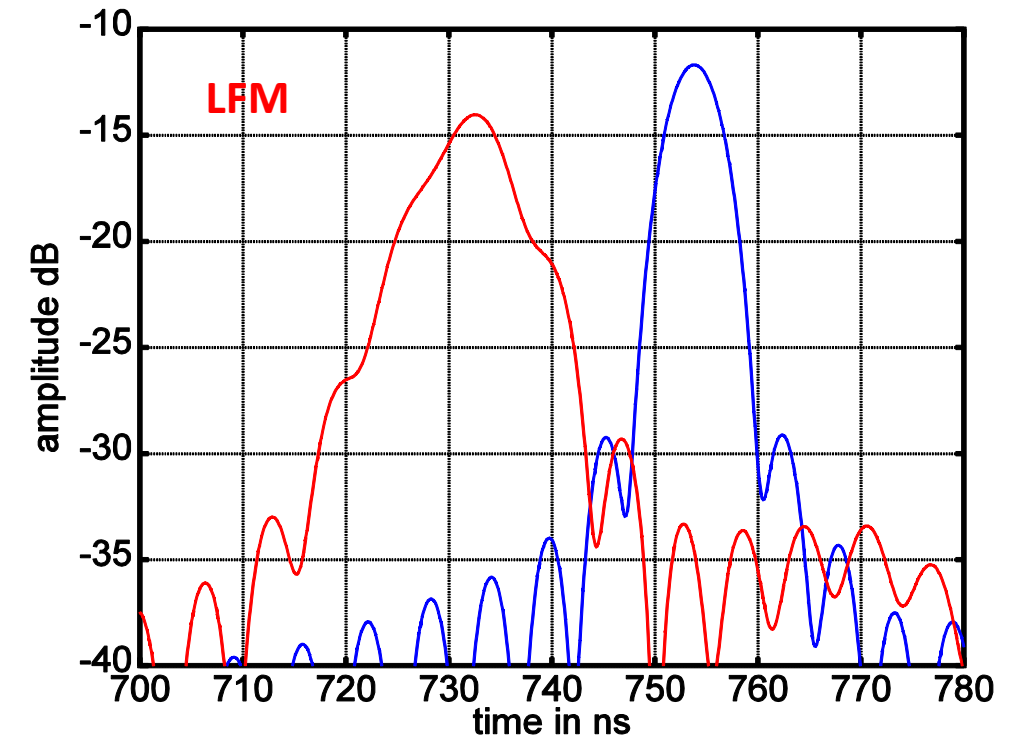
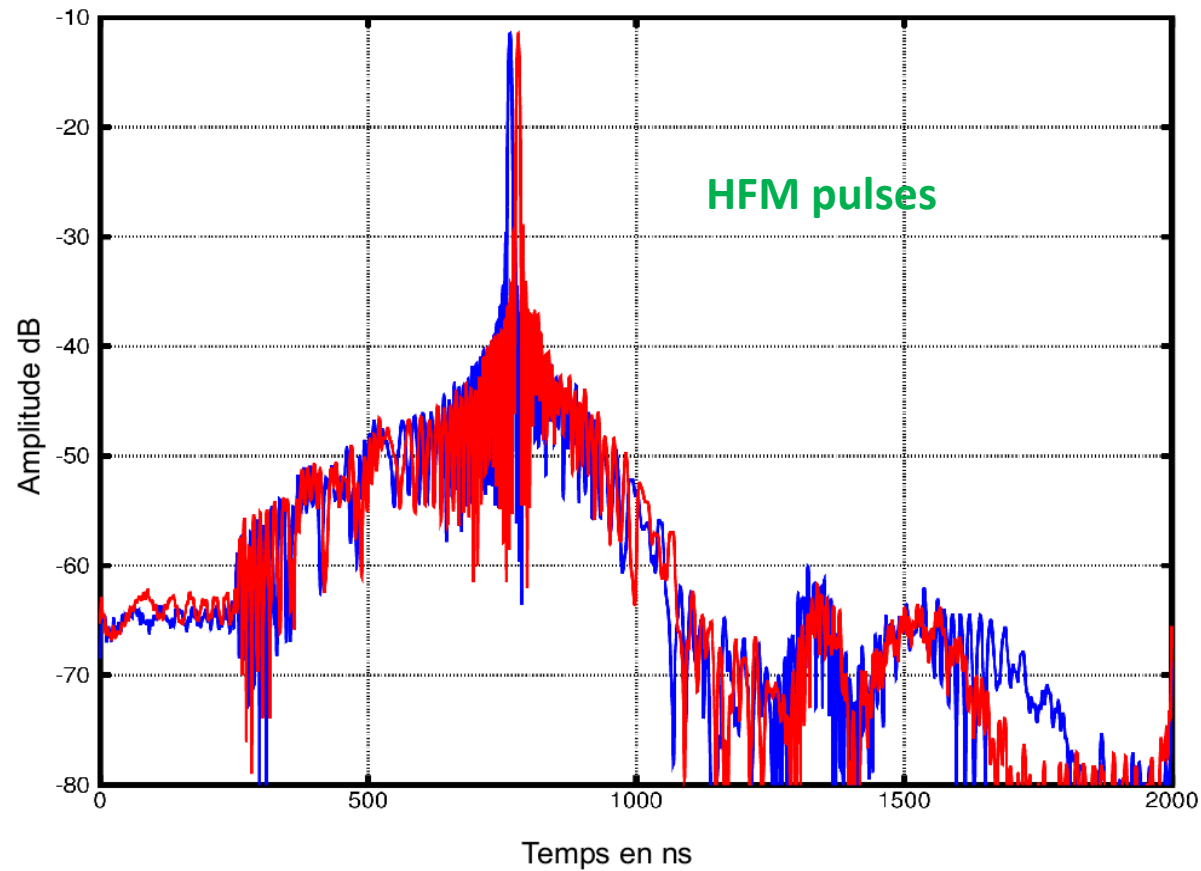
$N = 279$

Simulation results



The main part of this response geometrically is not only similar, but *identical* to the initial response

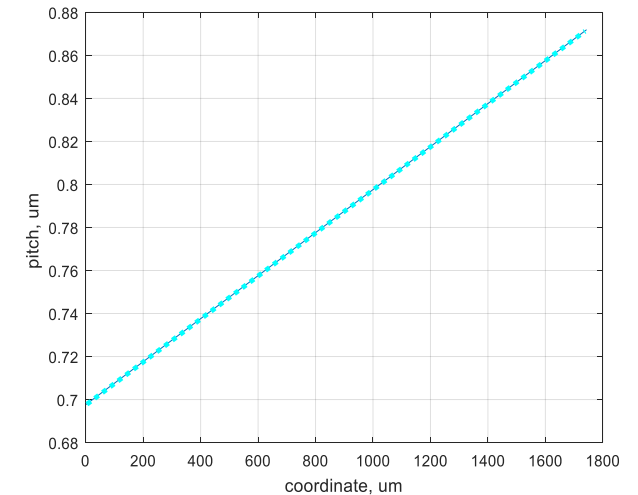
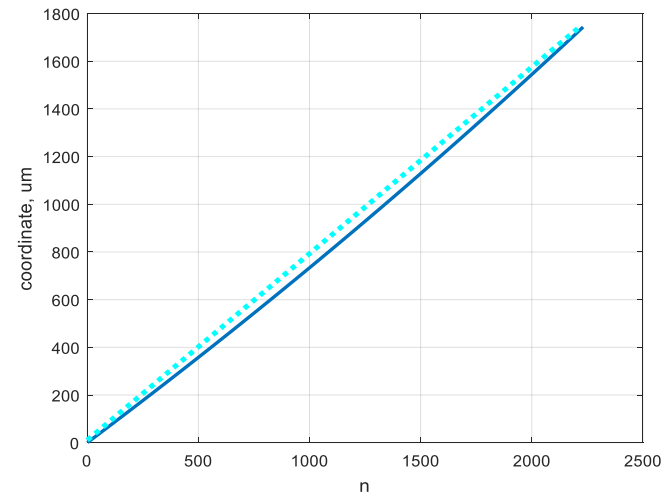
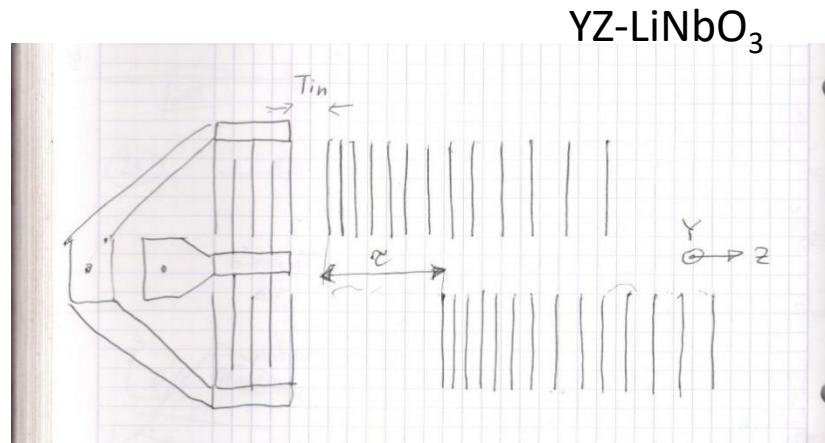
Compressed peaks



LFM case. Right curve compressed pulse at initial temperature, left curve – 2% expanded chirp.

Swiss-Lithuanian Project

Eurostars No E!10640 UWB_SENS



$F = 2000 \text{ MHz to } 2500 \text{ MHz},$
 $p_0 = 697.6 \text{ nm}, \quad pN = 872.0 \text{ nm}$
 $N = 2231 \text{ grooves, for } T = 1000 \text{ ns}$

$$L = V * \frac{T}{2} = 1744 \text{ } \mu\text{m}$$

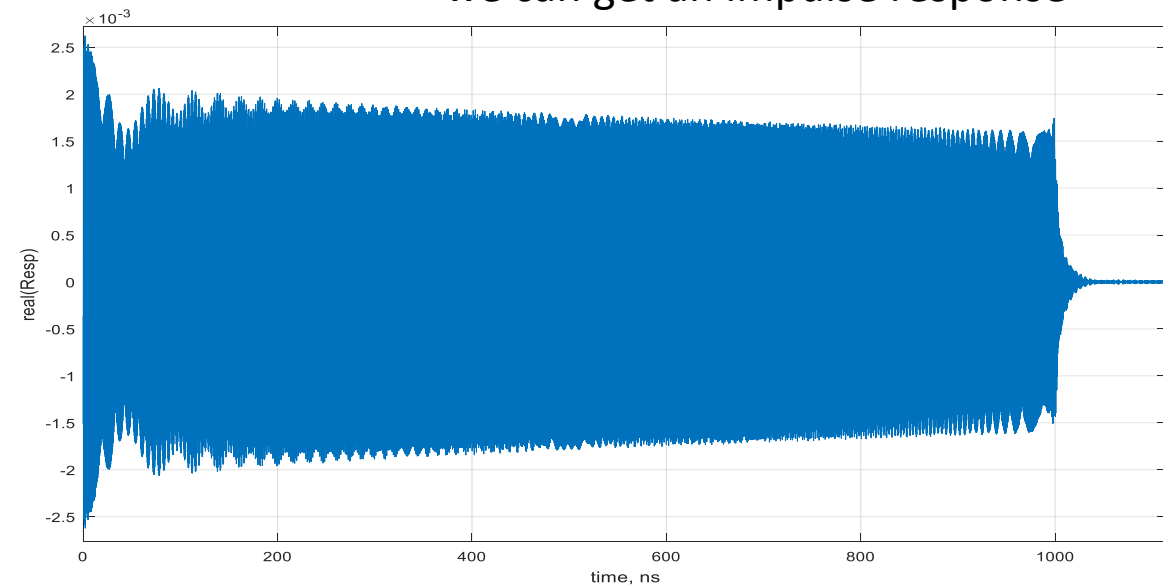
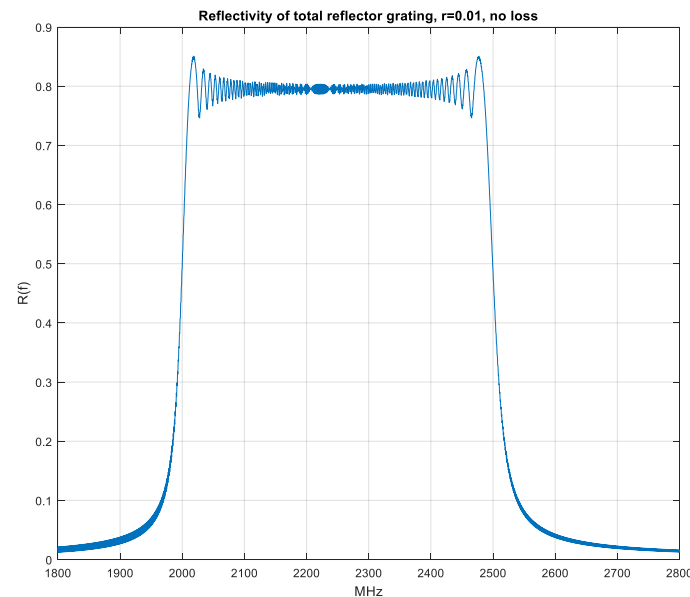
The coordinate of the grove reflector center
 is non-linear function of its number,
 while the pitch of the grating **is** linear function
 of the coordinate of reflecting element.

Reflectivity of the chirp grating (no loss included)

For $|r| = 0.01$ – reflection coefficient by a single groove

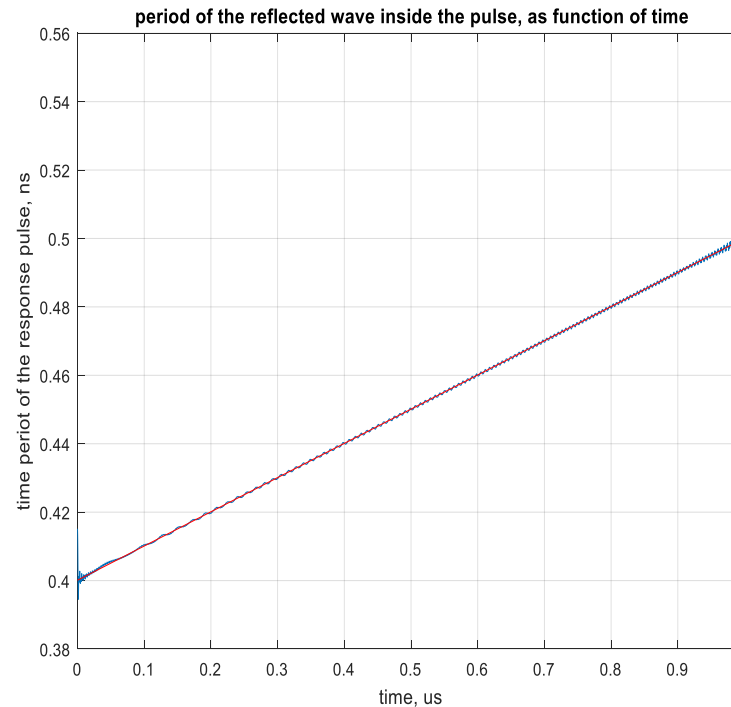
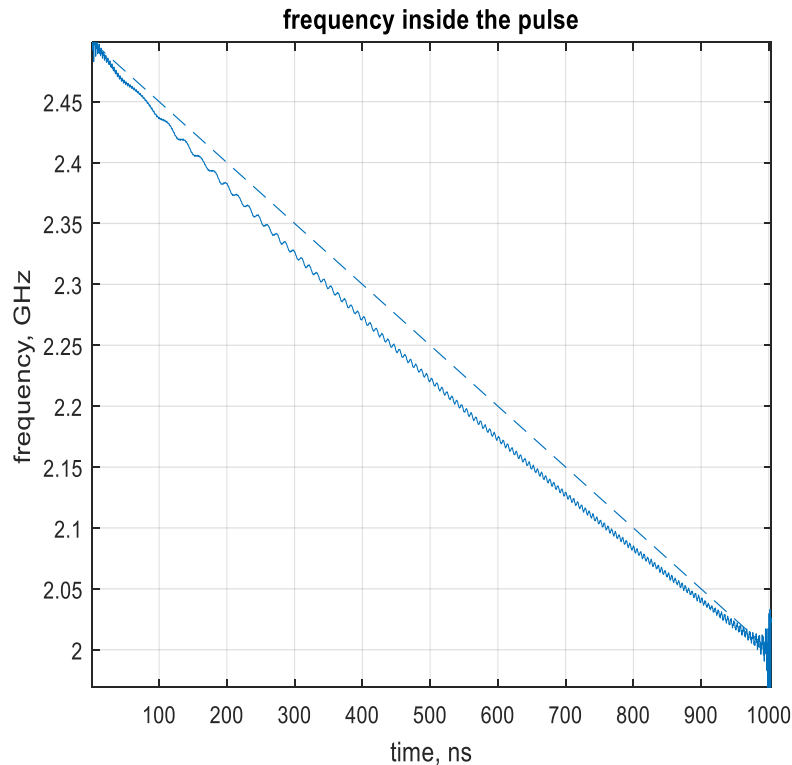
For YZ-LN $r = 0.6 * (h/\lambda)$; $\lambda \approx 1.55 \mu m$, $h \approx 250 \text{Å}$

Using Inverse Fast Fourier Transform (IFFT)
we can get an impulse response



We have used $N_{fr}=2001$ frequency points, $fr=[1800:0.5: 2800]$;

Hyperbolic Frequency Modulation



Linear increase of time period ($1/f$); red line – ideal fitted straight line.

Polynomial fit is

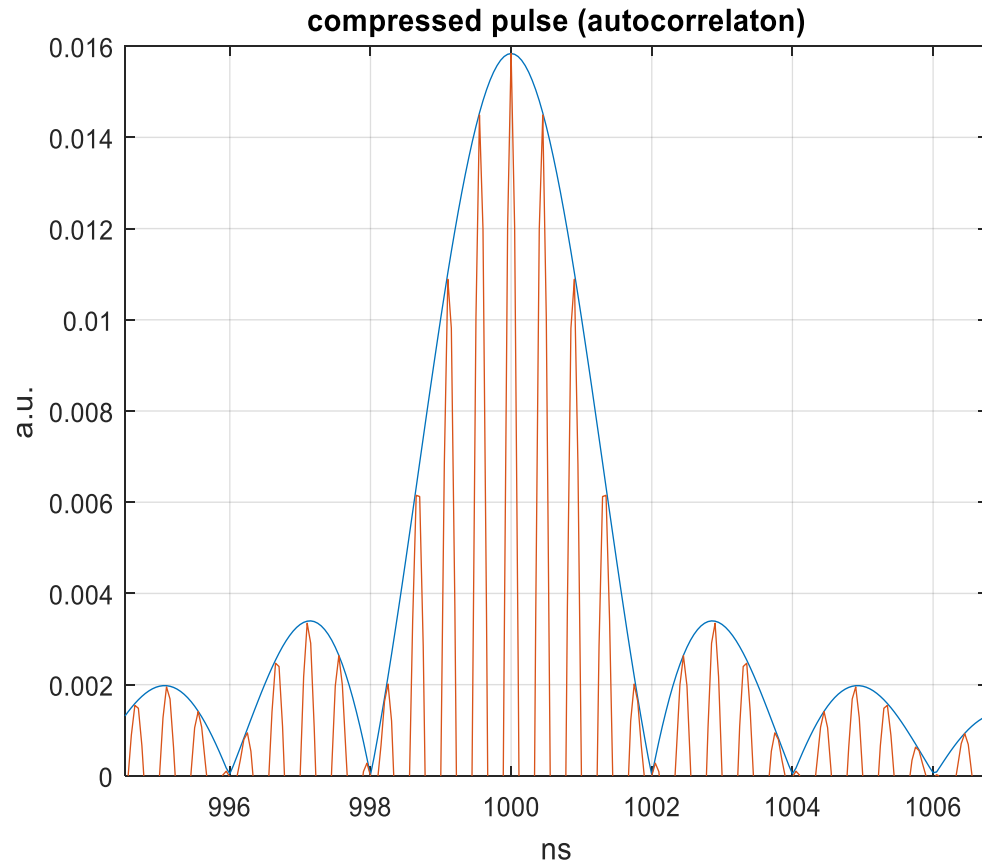
$$y = 0.4001 + 0.1 * t$$

with the correct beginning period **0.4 ns** = $1 / 2.5$ GHz, end period

0.5 ns = $1 / 2.0$ GHz, and expected rate coefficient $(2.5 - 2.0) / 1.0 = 0.1$.

***For comparison:
– dotted straight line***

Simulated compressed pulse



The compressed pulse has form close to sinc/x with the width around $1/500\text{MHz} = 2 \text{ ns}$. Its form (red line shows *real* part of the signal) is unique, and its position can be determined without uncertainty of phase (2π). If in a sensor response we will have 2 such pulses, by correlation method we will find the distance between this peaks.

Theoretical (ideal) HFM signal used for compression of sensor response

$$T(t) = T_0 + \frac{T_N - T_0}{T} * t$$

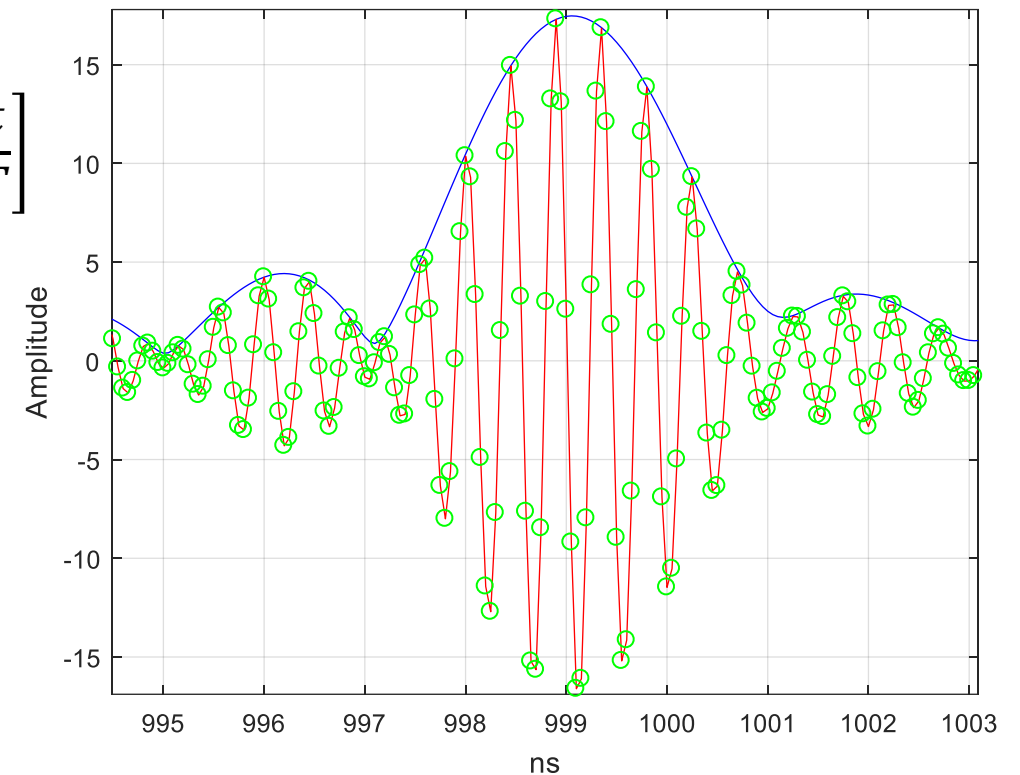
Introducing phase

$$\Phi = 2\pi \cdot \int_0^t \frac{dt}{T(t)} = 2\pi \cdot \int_0^t \frac{dt}{T_0 + \frac{\Delta T}{T} \cdot t} = 2\pi \cdot \frac{T}{\Delta T} \cdot \ln \left[1 + \frac{\Delta T}{T_0} \cdot \frac{t}{T} \right]$$

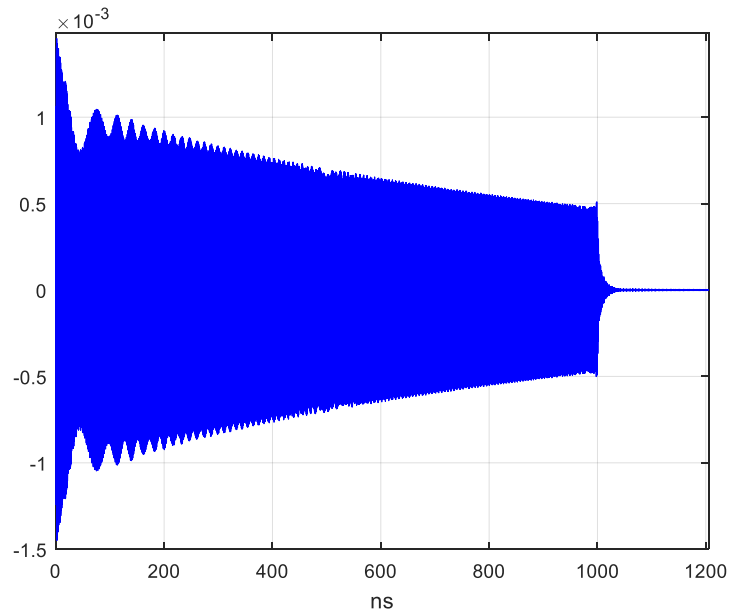
$$\Phi = -2\pi \cdot \frac{T}{B} \cdot (F_0^2 - \left(\frac{B}{2}\right)^2) \cdot \log \left(1 - \frac{B}{F_0 + B/2} \cdot \frac{t}{T} \right)$$

$$U = 1 \cdot \exp(1i \cdot \Phi)$$

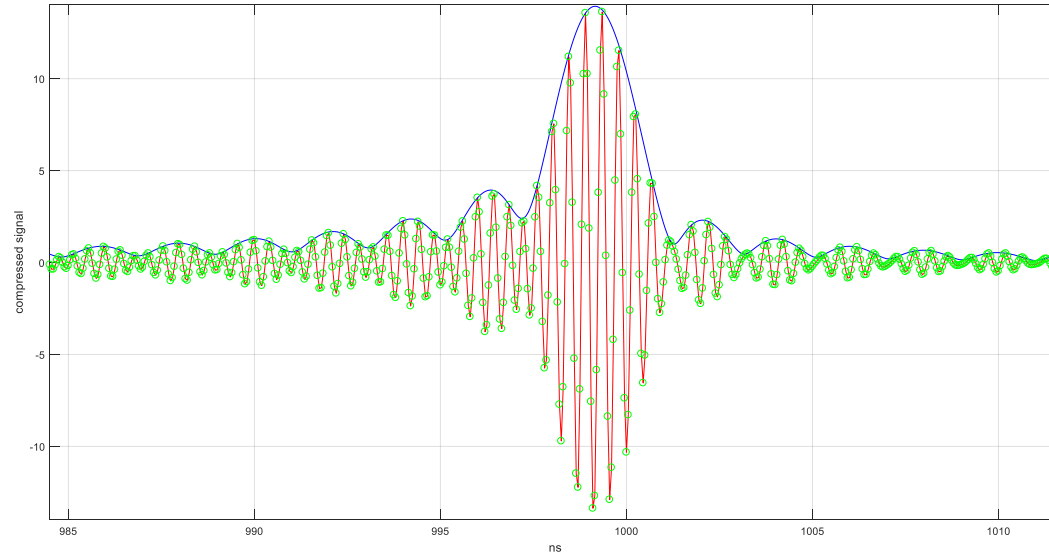
The “compression gain” = 17.5 times, or about 25 dB, which close to ideal value about $10 \cdot \log_{10}(B \cdot T) = 27$ dB



SAW attenuation included

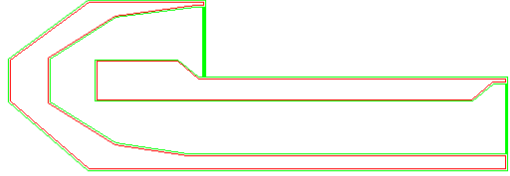


6dB/ μ s at 2GHz in LiNbO3



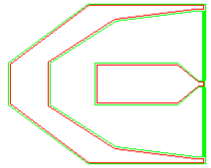
The “compression gain” using ideal HFM signal as reference is about 14 times, or 23 dB

YZ16500



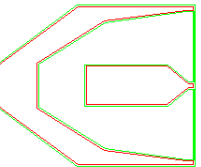
Profile groove etching

YZ1A600



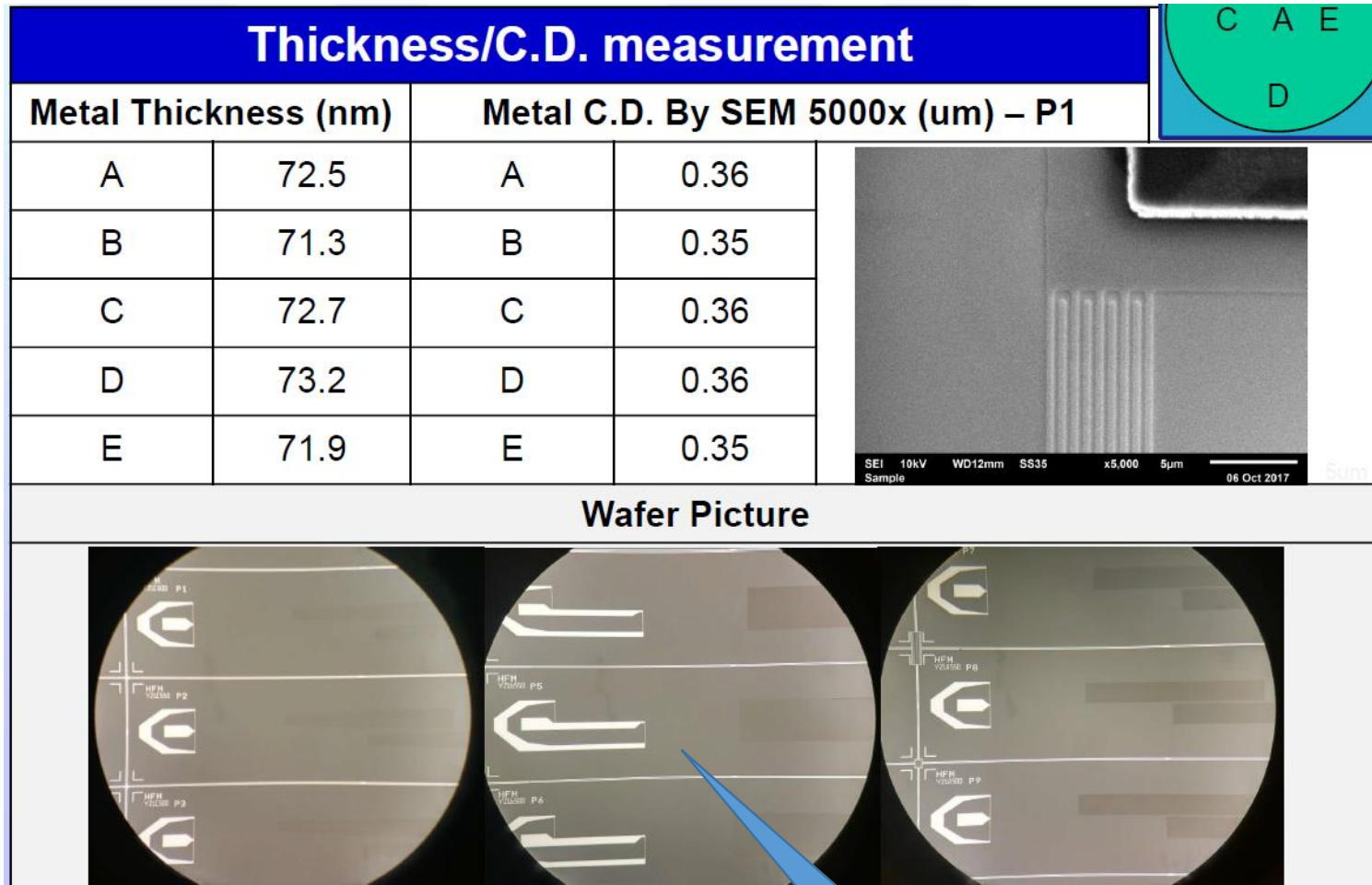
Uniform groove etching

YZ1C550



Uniform etching, aperture weighted

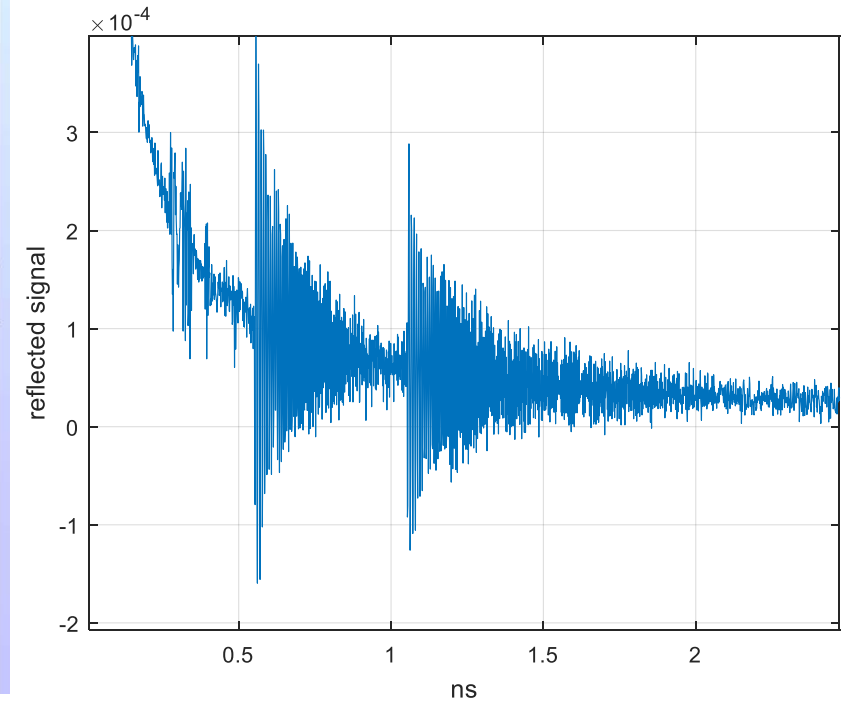
Etching grooves



P5

First samples manufactured

Reflected chirps (sample P5)



Conclusions

$$B * T * (K - 1) > 1$$

(K- scaling factor)

LFM signal compression deteriorates significantly

The **Hyperbolically Frequency Modulated (HFM)** signals and transducers/reflectors
are ideally suitable for SAW-sensors and SAW-tags,
since compression of such signals, being temperature-invariant,
can be achieved with always the same matched-to-signal filter,
simplifying significantly the interrogation algorithm.

Acknowledgements

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Thanks!

Thank you!