

Teaching Counting

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Teaching Counting: Considerations for Instruction

Purpose and Overview of Guide

The purpose of this guide is to provide strategies and materials for developing and implementing lessons for students who need intensive instruction in the area of place value, numeracy, and counting. Resource room teachers, math interventionists, and others working with struggling students may find this guide helpful.

Within college- and career-ready standards, place value, numeracy, and counting are taught in Grades 1-2. This guide may be used as these concepts are introduced, or with students in higher grade levels who continue to struggle with the concepts.

The guide is divided into four sections:

1. Sequence of skills as defined by college- and career-ready standards
2. A list of important vocabulary and symbols
3. A brief explanation of the difficulties students may have with counting
4. Suggested activities and strategies for teaching counting concepts

Sequence of Skills—College- and Career-Ready Standards

(The grade level of a standard is represented by the number or letter in parentheses.)

Know number names and the count sequence.

- Count to 100 by ones and by tens. (K)
- Count forward beginning from a given number. (K)
- Write numbers from 0 to 20. (K)
- Represent a number of objects with a written numeral 0–20. (K)

Count to tell the number of objects.

- Understand the relationship between numbers and quantities. (K)

- Connect counting to cardinality. (K)
- When counting objects, do the following:
 - Say the number names in the standard order. (K)
 - Pair each object with one and only one number name, and each number name with one and only one object. (K)
 - Understand that the last number name said tells the number of objects counted. (K)
 - Understand that the number of objects is the same regardless of their arrangement or the order in which they were counted. (K)
 - Understand that each successive number name refers to a quantity that is one larger. (K)
- Count to answer “How many?” questions about as many as 20 things arranged in a line, a rectangular array, or a circle, or as many as 10 things in a scattered configuration. (K)
- Given a number from 1–20, count out that many objects. (K)

Compare numbers.

- Identify whether the number of objects in one group is greater than, less than, or equal to the number of objects in another group. (K)
- Compare two numbers between 1 and 10 presented as written numerals. (K)

Extend the counting sequence.

- Count to 120, starting at any number. (1)
- Read and write numerals (to 12), and represent a number of objects with a written numeral. (1)
- Count within 1,000. (2)
- Skip count by 5s, 10s, and 100s. (2)

Add and subtract within 20.

- Relate counting to addition and subtraction. (1)

Vocabulary and Symbols

The following terms are important for students to understand when working with counting.

<p>Number: An object used to count.</p> <p>0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10</p>	<p>Numeral: A symbol used to describe a number.</p> <p>3 57</p>	<p>Counting: Finding the amount of a set.</p>
<p>Cardinal number: The amount of a set.</p> <p>1, 2, 3 objects: 3 is the cardinal number.</p>	<p>Ordinal number: A word that shows the order in a set.</p> <p>third fifty-seventh</p>	<p>Even: A number divided evenly by 2.</p> <p>0, 2, 4, 6, 8, 10</p>
<p>Odd: A number not divided evenly by 2.</p> <p>1, 3, 5, 7, 9</p>	<p>Quantity: The amount of a set.</p>	<p>More: A word describing a set that is larger.</p>
<p>Less: A word describing a set that is smaller.</p>	<p>Equal: Two sets have the same amount.</p>	

Common Areas of Difficulty

- Counting principles
- Understanding of numbers and what numbers represent

Five Counting Principles

- **Stable order.** The order in which students count is stable. In English, we start with 1 and count forward: 1, 2, 3, 4, 5, 6, 7, 8, 9, 10. The counting order never changes.
- **One-to-one correspondence.** When counting, students assign one (and only one) count to each object of a set. Partitioning and tagging helps with this skill.
 - **Partition.** Touch or move one object.
 - **Tag.** Assign a number to that one object.
- **Cardinality.** When counting objects in a set, the last count represents the number of objects in the set. For example, if 5 objects are on the table, the student counts, “1, 2, 3, 4, 5.” When asked how many objects, the student answers, “5.”

- **Abstraction.** Counting can be used to count any collection of objects. It does not matter whether all the objects in the set are the same. “Objects” can also be claps, sounds, or imaginary objects.
- **Order-irrelevance.** The way objects are counted (e.g., left to right, top to bottom) does not matter when counting. The counting order does not change the cardinality of the set.

Conceptual Understanding

Manipulatives can be used to help practice counting skills. Some examples of counting manipulatives include cubes, clips, toy animals, chips, and toy cars.



Activities and Strategies Related to Specific Standards

Know number names and the count sequence.

- Teach and sing counting songs. A variety of songs are available on YouTube at <http://www.youtube.com/>.
 - Don't always stop counting at 10. Continue counting to 20.
 - When counting, show the written numbers that accompany the number word.
- Teach skip counting through chants or songs.
 - Practice counting with number lines or hundreds charts.

Hundreds Chart

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

- Give a number (e.g., 6) and count on.
 - *Start with 6 and count up to 15. Ready? 6, 7, 8, 9, 10, 11, 12, 13, 14, 15.*
- Present story problems that require counting on.
 - *Devin had 5 apples in his basket and then he picked some more. Let's start at 5 and count more apples.*
- Write numbers.
 - Practice motions of writing numbers in rice, pudding, glitter, sand, or dirt.
 - Teach appropriate pencil hold.
 - Practice writing numbers on paper.
 - Learn rhymes for writing numbers.

Number Writing Rhymes

Number 1 is like a stick, a straight line down that's very quick.

For number 2 go right around, then make a line across the ground.

Go right around, what will it be? Go round again to make a 3.

Down and over and down some more, that's the way to make a 4.

Go down and around, then you stop, finish the 5 with a line on top.

Make a curve, then a loop, there are no tricks to making a 6.

Across the sky and down from heaven, that's the way to make a 7.

Make an "S" and then don't wait, go up again to make an 8.

Make a loop and then a line, that's the way to make a 9.

- Show a set of objects and write the number.

Count to tell the number of objects.

- Show a set of objects and count. Partition and tag items as they are counted. At the end of counting, say the total number of objects in the set.
- For example:



- *There are one* (touch the blue dino), *two* (touch the yellow dino), *three* (touch the lime green dino), *four* (touch the dark green dino), *five* (touch the orange dino). *There are five dinosaurs.*
- *I can count these in a different way. There are one* (touch the dark green dino), *two* (touch the yellow dino), *three* (touch the orange dino), *four* (touch the lime green dino), *five* (touch the blue dino). *There are still five dinosaurs.*
- Show a set of objects and answer the question, “How many?” For example:
 - Place nine chips in a line and ask, “How many?”
 
 - Place nine chips in a rectangle shape and ask, “How many?”
 
 - Place nine scattered chips and ask, “How many?”
 
- Say a number and show that many objects. For example:
 - *Show me 13 cubes.*

Compare numbers.

- Show two sets of objects and ask: “Which set has more?” “Which set has less?” “Are the sets the same or equal?”
- Show two written numerals and ask: “Which is more?” “Which is less?” “Are the numbers the same or equal?”
 - At first, choose numbers with a greater difference in magnitude (e.g., 2 and 9, 3 and 8).
 - Then, choose numbers closer in magnitude (e.g., 3 and 5, 7 and 8).
 - Once place value is introduced, choose numbers that are often confusing (e.g., 17 and 71, 23 and 32).
- Teach signs.



Extend the counting sequence.

- Teach counting to 120, starting at any number. Use number lines or hundreds charts.
- Teach counting to 1,000, starting at any number.
- Reinforce skip counting skills.
 - Flash one hand (i.e., five fingers) when counting by fives.
 - Flash two hands when counting by tens.

Add and subtract within 20.

- Start with a number and count on.
 - Start with 4 and count up 2 more. Ready? 4, 5, 6. 4 plus 2 is 6.
 - It may be helpful to teach showing the number counted on with fingers:
 - Put the 4 in your head. Now, we count on 2. Ready? 5 (hold up 1 finger), 6 (hold up 2 fingers). 4 plus 2 is 6.

2. Count to Tell the Number of Objects

Sample Activities

- a) Sample Activity 1: Count to Tell the Number of Objects

Worksheet

- a) Count to Tell the Number of Objects

Sample Counting Concepts Activity 1: Count to Tell the Number of Objects

College- and Career-Ready Standards Addressed:

K.CC.4. Understand the relationship between numbers and quantities; connect counting to cardinality.

- a. When counting objects, say the number names (i.e., standard order), pairing each number with one and only one number name, each number name with one and only one object.
- b. Understand that the last number name said tells the number of objects counted. The number of objects is the same regardless of their arrangement or the order in which they were counted.
- c. Understand that each successive number name refers to a quantity that is one larger.

K.CC.5. Count to answer “how many?” questions about as many as 20 things arranged in a line, a rectangular array, or a circle, or as many as 10 things in a scattered configuration; given a number from 1 to 20, count out that many objects.

Activity One: Using Manipulatives to Demonstrate Rational Counting

Purpose: Count up to 20 objects in a group; connect counting to cardinality.

Materials: Small, concrete manipulatives such as cubes, clips, toy animals, chips, or base-10 blocks (available for download from NCII)

Student Worksheet: Counting Activity 1 (available for download from NCII)



Modeling:

1. Review **rote counting** (i.e., stating the number words in order) to 20 with the student. (Use nursery rhymes, chants, songs, or YouTube videos such as [Counting Numbers 1–10](#) or [1–20 Chant!](#) by [ELF Learning](#) to practice rote counting.)
2. Tell the student counting is used to tell *how many* of something.
3. Place a handful of objects (fewer than 10) in a straight line.
4. Demonstrate touching each object one at a time, slowly, stating the number word for each object as you touch it. Tell the student the last number word said tells *how many* there are. “One, two, three, four, five, six, seven. The last number I said was seven, so there are seven animals.”
5. Tell the student, “Let’s do this together. I’ll point and you count with me.” Repeat touching and counting each object; have the student count with you while you point.
6. Tell the student, “Now I’m going to move the animals around so they’re all mixed up.” Take the same set of objects and rearrange them in a scattered assortment.
7. Ask the student how many animals there are now. Allow the student to answer, then demonstrate touching each object one at a time, slowly, stating the number word for each object as you touch it. Tell the student the last number word said tells *how many* there are. “One, two, three, four, five, six, seven. The last number I said was seven, so there are seven animals.”
8. Confirm with the student that the amount of objects (i.e., the set’s cardinality) does not change simply because the objects have been moved around; whether they are in a straight line or all mixed up, the total amount remains the same.
9. Repeat with at least two more sets of objects (e.g., four cubes and 19 chips). Have the student count with you as you touch each object.

Guided Practice:

1. Place a handful of objects (e.g., 10 cubes) on the table in a random assortment. Point to and touch each object, while the student counts out loud. Have the student state *how many* objects there are on the table.

2. Now, using the same set of objects, rearrange them to line up in a straight line. Have the student predict how many there are in the set now; then, touch each object while the student counts. Have the student state *how many* there are and confirm the lined-up set of objects is the same amount as the original, randomly assorted pile.
3. Repeat with at least two more sets of objects (e.g., six cubes, 17 clips).
4. Have the student place a handful of objects (e.g., 12) on the table, in a random pile. Have the student point to and touch each object, assigning cardinality to the set. Have the student arrange objects in a line, predicting how many there are. The student touches and counts each object again, confirming the amounts are the same.
5. Repeat with at least two more sets of objects (e.g., 18 animals, 20 cubes).

Corrective Feedback:

Example 1: Coordination Errors

Student response: The student has difficulty coordinating rote counting (number words) with touching the objects.

Teacher feedback: Provide an audible signal (e.g., a finger snap, a clap, a small bell) to signal each transfer between objects.

Example 2: Omission Errors

Student response: The student misses items when counting (i.e., skips over an object and does not assign it a number word).

Teacher feedback: Have the student physically move each object as it is counted. For example, the student moves each item from the tabletop to a paper plate or counting mat as it is counted.

Example 3: Double-Count Errors

Student response: The student touches an item more than once when counting (i.e., touches an object and says “three,” then touches it again and says “four”).

Teacher feedback: As with Example 2, have the student physically move each object as it is counted. For example, the student moves each item from the tabletop to a paper plate or counting mat as it is counted.

Example 4: Idiosyncratic Counting Sequence Errors

Student response: The student touches items appropriately but does not state numbers in the correct order (e.g., while counting, states, “one, two, three, five, four, six, seven”).

Teacher feedback: Practice rote counting using chants, songs, nursery rhymes, or videos, following along by pointing to numbers printed on a number line while counting out loud.

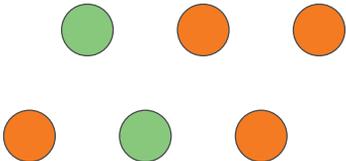
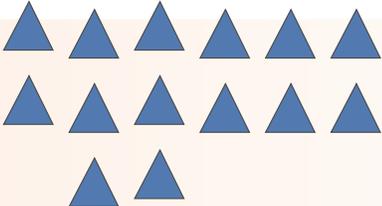
Note: Regardless of the type of counting error, the teacher should always model the correct response and have the student demonstrate the correct procedure before moving on.

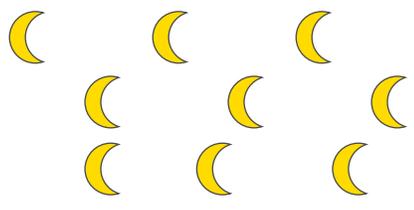
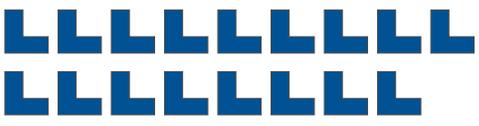
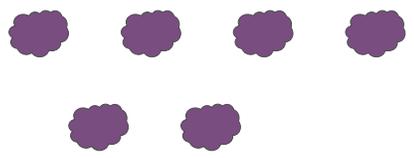
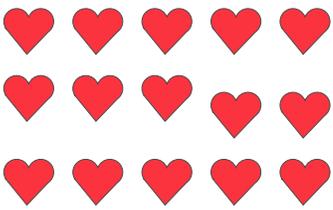
Worksheet

Count to Tell the Number of Objects

Objective: Count up to 20 objects in a group to tell “how many.”

Directions: Count, and then write how many objects are in each group.

 <p>How many? _____</p>	 <p>How many? _____</p>
 <p>How many? _____</p>	 <p>How many? _____</p>

 <p>How many? _____</p>	 <p>How many? _____</p>
 <p>How many? _____</p>	 <p>How many? _____</p>
 <p>How many? _____</p>	 <p>How many? _____</p>



3. Compare Numbers

Sample Activities

- a) Sample Activity 1: Compare Numbers

Worksheet

- a) Compare Numbers

Sample Activity 2: Greater Than, Less Than, Equal To Comparison Poster

College and Career and Readiness Standards Addressed:

K.CC.6. Identify whether the number of objects in one group is greater than, less than, or equal to the number of objects in another group (e.g., by using matching and counting strategies).

Purpose: To compare discrete sets of objects and state whether one group is greater, lesser, or equal to a second set.

Materials: Small, concrete manipulatives such as cubes, chips, or base-10 blocks/squares (available for download from NCII)

Three cards depicting the symbols $<$, $>$, and $=$ with the words “less than,” “greater than,” and “equal to” printed below the symbol (available for download from NCII)

Poster for classroom depicting symbols and meanings (available for download from NCII)

Dry-erase board and markers or paper and pencil

Student Worksheet: Compare Numbers (available for download from NCII)



Modeling:

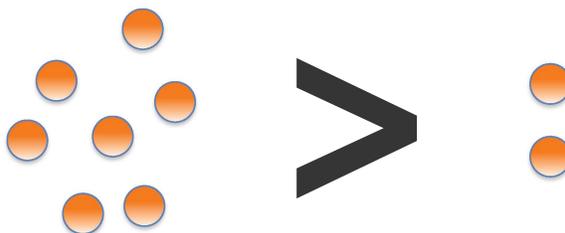
1. Introduce the student to the symbols for “**greater than**, **less than**, and **equal to**.” Explain that **greater** is another word for **bigger** and that when we say one set is **greater** than, that means it has more.



2. Put a pile of objects (e.g., 7) on the table. Then, put a much smaller amount (e.g., 2) on the table, separate from the first pile.

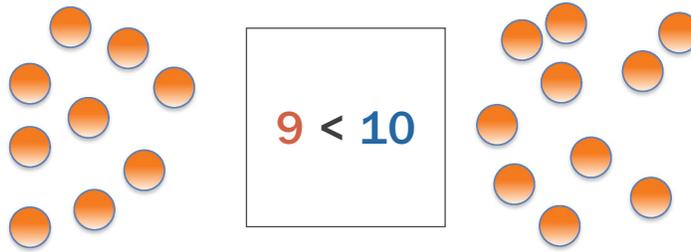
NOTE: It is important to exaggerate the difference in amount initially; one set should be markedly larger/smaller than the other.

3. Ask the student which pile is **greater**. When the student indicates the first pile, show all three cards of **greater than**, **less than**, and **equal to**.



4. Tell the student that the symbol is open to the side that is **greater** and closed to the side that is **less than**.
5. Repeat with sets of, for example, 1 and 9, 2 and 2, and 8 and 3. For each comparison, state whether one set is **greater than**, **less than** (i.e., *smaller than*), or **equal to** (i.e., *the same as*) its counterpart.
6. Clear the table of objects. Agree with the student that, so far, it was easy to tell which pile of objects was **greater** (or if they were **equal**). Tell the student that sometimes you can't tell just by looking which pile is **greater**.

7. Put 10 objects on the table in a pile; in a separate pile, put 9 objects.



8. Ask the student if he or she can tell just by looking which pile is **greater**. When the student indicates that he or she can't, suggest that the student count each pile to find out which one has more.
9. Line up the objects from the first pile. Touch each object while counting out loud. State that there are 9 objects, and write "9" on the dry-erase board. Tell the student we write "9" to help us remember there are 9 objects in this pile.
10. Line up the objects from the second pile. Touch each object while counting out loud. State there are 10 objects in the second pile, and write "10" on the dry-erase board. Tell the student we write "10" to help us remember there are 10 objects in that pile.
11. Tell the student you know that 10 is greater than 9. Place the appropriate card between 9 and 10.
12. Tell the student that to show which number is greater, you draw the symbol with the opening facing the greater number. This is the sign we use in mathematics to tell which number greater. Move the card aside and write "<" on the board. Point to the sign and then trace the sign. Tell the student that this sign means "less than." Read to the student while pointing to each symbol: "9 is less than 10."
13. Repeat with sets of, for example, 5 and 5, and 8 and 7.

- Guided Practice:**
1. Place a set of objects (e.g., 8 objects) on the table, in a random assortment. Place a second set of objects (e.g., 5 objects) on the table in a separate pile.
 2. Ask the student to decide which pile is greater. Have the student touch and count each pile, and write the amounts on the board.
 3. Have the student write “<,” “>,” or “=” between the numbers.
 4. Have the student read the equation out loud, using the correct vocabulary: greater than, less than, or equal to.
 5. Repeat with at least six examples so that the student has practice with each symbol (e.g., 2 and 2, 5 and 7, 8 and 3, 10 and 10, 4 and 6, 9 and 5).

Corrective Feedback:

Example 1: Counting Errors

Student response: The student makes **coordination, omission, double-count, or idiosyncratic sequencing** counting errors.

Coordination Errors

Student response: The student has difficulty coordinating rote counting (number words) with touching the objects.

Teacher feedback: Provide an audible signal (e.g., a finger snap, clap, or small bell) to signal each transfer between objects.

Omission Errors

Student response: The student misses items when counting (i.e., skips over an object and does not assign it a number word).

Teacher feedback: Have the student physically move each object as it is counted. For example, the student moves each item from the tabletop to a paper plate or counting mat as it is counted.

Double-Count Errors

Student response: The student touches an item more than once when counting (i.e., touches an object and says “three,” then touches it again and says “four”).

Teacher feedback: As with Example 2, have the student physically move each object as it is counted. For example, the student moves each item from the tabletop to a paper plate or counting mat as it is counted.

Idiosyncratic Sequencing Counting Errors

Student response: The student touches items appropriately but does not state numbers in the correct order (e.g., while counting, states, “one, two, three, five, four, six, seven”).

Teacher feedback: Practice rote counting using chants, songs, nursery rhymes, or YouTube videos, following along by pointing to numbers printed on a number line while counting out loud.

Example 2: Writing Errors

Student response: The student selects the appropriate greater than, less than, or equal to card when comparing sets but struggles to write the symbol.

Teacher feedback: Using a utility knife or sharp scissors, cut out the shape on the card so that the student can use the cut-out portion to trace the symbol correctly.

Example 3: Naming Errors

Student response: The student writes the number sentence correctly but has difficulty remembering the terminology “greater than,” “less than,” and “equal to.”

Corrective feedback: Create cards (or posters) with the symbol printed directly above the word. Leave the cards on the desk (or the poster on the wall) for the student to refer to when working on this skill.

For all errors, the teacher should always model the correct response and have the student demonstrate the correct procedure before moving on.

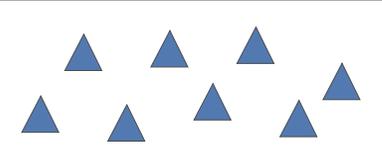
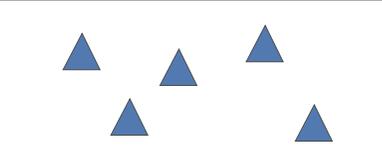
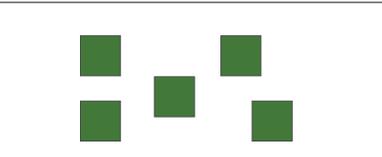
Worksheet

Compare Numbers

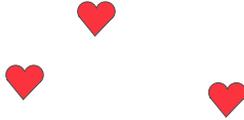
Objective: Compare discrete sets of objects using correct vocabulary (greater than, less than, or equal to).

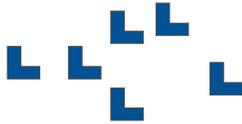
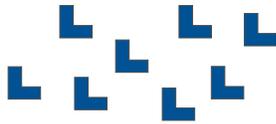
Directions: Students count the number of objects in a set and write the number below each set. They then compare the two numbers to determine whether the first is greater than, less than, or equal to the second. Write the correct symbol (<, >, =) in the middle box of the “compare” row.

Example:

			
Count	8		5
Compare	8	>	5
		=	
Count			
Compare			
			
Count			
Compare			

			
Count			
Compare			

			
Count			
Compare			

			
Count			
Compare			

			
Count			
Compare			

			
Count			
Compare			

4. “Count On” to Add and Subtract

Sample Activities

- a) Sample Activity 1: “Count On” to Add and Subtract

Worksheets

- a) Counting On to Add
- b) Counting On to Subtract

Sample Activity 3: “Count On” to Add and Subtract

College- and Career-Ready Standards Addressed:

K.CC.2. Count forward beginning from a given number within the known sequence (instead of having to begin at 1).

K.CC.7. Compare numbers between 1 and 10 presented as written numerals.

1.OA.5. Relate counting to addition and subtraction (e.g., by counting on 2 to add 2).

Part One: “Counting On” to Add

Purpose: Use the “minute” strategy to count on when adding two numbers within 20.

Materials: Addition flashcards (available for download from NCII)

Timer

The Best Time Scorecards (available for download from NCII)

Small prizes (e.g., stickers, smiley-face stamps, free time on computer, goldfish crackers, and so on)

Student Worksheet: “Counting On” to Add (available for download from NCII)

Modeling:

1. Show the student the flashcards and scorecard. Explain to the student that you are going to play a game in which the goal is for the student to beat his or her own score. Tell the student that his or her score is the number of flashcards he or she can answer correctly in one minute.
2. Tell the student that the fastest way to answer cards correctly is to know the answer right away. But, if the student gets a card he or she doesn't already know, he or she should “count up” on his or her fingers to find the answer.
3. Show the student the first flashcard in the pile (e.g., $2 + 2$). Say, “ $2 + 2$. I know this one! $2 + 2$ equals 4.”

4. Show the student the next flashcard (e.g., $7 + 4$). Pretend to not know the answer. Say, *“Hmmm. $7 + 4$. I don’t remember this one. I need to count up to find the answer. To do that, I put the greater number in my head. I count up the lesser number on my fingers. 7 is the greater number. 4 is the lesser number. I put 7 in my head. I put 4 on my fingers.”* Hold up 4 fingers.
5. *“I start counting with the greater number. I keep counting up until I’ve counted on all the fingers I’m holding up. Then, my answer will be the last number I say! Watch me. 7...8, 9, 10, 11.”* (Wiggle each finger as you count.) *“The last number I say is the answer. So, 11 is the answer. $7 + 4$ equals 11!”*
6. Show the student the next flashcard. This time, the first addend should be greater than the second addend (e.g., $3 + 6$). Remind the student of the commutative property of addition. That is, addends can be added in any order without changing the total amount: $3 + 6 = 6 + 3$. Ask the student which is the greater number, 3 or 6. Repeat step 5 with this flashcard.
7. Repeat with three more flashcards from the pile, modeling by thinking aloud to count up for each card.

Guided Practice:

1. Shuffle the cards and put the pile face down on the table.
2. Tell the student that he or she will have a short amount of time (one minute) to answer as many cards as possible and that you will put the score on the scorecard. Then, he or she will have another minute to try to beat the score. If he or she does, he or she wins the game and gets to have a prize. (See the list of materials for suggested prizes.)
3. Remind the student that the best way to score points is to know the answer to the math problem as quickly as possible. But, if he or she doesn’t know the answer, he or she should count up to find it.
4. Set timer for one minute, and turn cards over one at a time for the student to answer. If the student answers correctly, put the card in a “correct” pile. If the student answers incorrectly, have him or her repeat that card immediately, counting up to get the correct answer. Assist the student, as needed. Then, put that card in the “correct” pile.

5. After the timer beeps, count the number of correctly answered cards, and mark that score on the scorecard. Then, shuffle the cards and allow the student to repeat for a chance to beat the score. If he or she does, mark that score on the scorecard and reward the student with a prize. If he or she does not, set the timer and provide one more opportunity. Mark on the scorecard the highest score for the day and attempt to beat that score the next time you play.

Part Two: “Counting On” to Subtract

Purpose: Use a counting-on strategy to determine the difference between two numbers.

Materials: Subtraction flashcards (available for download from NCII)
Timer
Graph to record performance data (available for download from NCII)
Small prizes (e.g., stickers, smiley-face stamps, free time on computer, goldfish crackers, and so on)
Student Worksheet: “Counting On” to Subtract

Modeling:

1. Show the student the flashcards and scorecard (available for download from NCII). Explain to the student that you are going to play a game in which the goal is for the student to beat his or her own score. Tell the student that his or her score is the number of flashcards answered correctly in one minute.
2. Tell the student that the fastest way to answer cards correctly is to know the answer right away. But, if the student gets a card he or she doesn't already know, he or she should “count up” on his or her fingers to find the answer.
3. Show the student the first flashcard in the pile (e.g., $2 - 1$). Say, “ $2 - 1$. I know this one! $2 - 1$ equals 1.”
4. Show the student the next flashcard (e.g., $8 - 5$). Pretend to not know the answer. Say, “Hmmm. $8 - 5$. I don't remember this one. I need to count on to find the answer. To do that, I put the subtrahend (the number we subtract) in my head. I count up to the greater number. The number of fingers I have up is my answer. 5 is the lesser number. 8 is the greater number. I put 5 in my head. I count up on my fingers until I get to the greater number.”

5. *"I hold the lesser number in my head. I keep counting up until I get to the greater number. I put up another finger for each number word I say. Then, my answer will be the number of fingers I have up! Watch me. 5! (Close your fist as if you are grabbing something and holding it tight.) 6 (hold up 1 finger)...7 (hold up 2 fingers)...8 (hold up 3 fingers). I have 3 fingers up, so the answer is 3. $8 - 5$ equals 3!"*
6. Show the student the next flashcard (e.g., $14 - 6$). Remind the student that, with subtraction, it's important to always hold the lesser number in his or her head and count up to the greater number. The answer will be the number of fingers up. Ask the student which is the greater number, 14 or 6. Repeat step 5 with this flashcard.
7. Repeat with three more flashcards from the pile, modeling by thinking aloud to count up for each card.

Guided Practice:

1. Shuffle the cards and put the pile face down on the table.
2. Tell the student he or she will have a short amount of time (one minute) to answer as many cards as possible, and that you will put the score on the scorecard. Then, he or she will have another minute to try to beat the score. If he or she does, he or she wins the game and will get to have a prize. (See the list of materials for suggested prizes.)
3. Remind the student that the best way to score points is to know the answer to the math problem as quickly as possible. But, if he or she doesn't know the answer, he or she should count up to find it.
4. Set the timer for one minute, and turn the cards over one at a time for the student to answer. If the student answers correctly, put the card in a "correct" pile. If the student answers incorrectly, have him or her repeat that card immediately, counting up to get the correct answer. Assist the student, as needed. Then, put that card in the "correct" pile.
5. After the timer beeps, count the number of correctly answered cards and mark that score on the scorecard. Then, shuffle the cards and allow the student to repeat for a chance to beat the score. If he or she does, mark that score on the scorecard and reward the student with a prize. If he or she does not, set the timer and provide one more opportunity. Mark on the scorecard the highest score for the day, and attempt to beat that score the next time you play.

Corrective Feedback:

Student response 1: The student has difficulty coordinating rote counting (number words) with each finger count.

Teacher feedback: Provide an audible signal (e.g., a finger snap, clap, or small bell) or touch the fingers for the student to signal each transfer between objects.

Student response 2: The student has difficulty identifying the minuend and subtrahend and understanding difference.

Teacher feedback: Provide a number line for the student to find the minuend and subtrahend and determine the difference between the two using the number line. Have the student demonstrate the correct response before moving on.

For all errors, model the process and have the student demonstrate the correct response before moving on.



Worksheet

“Counting On” to Add

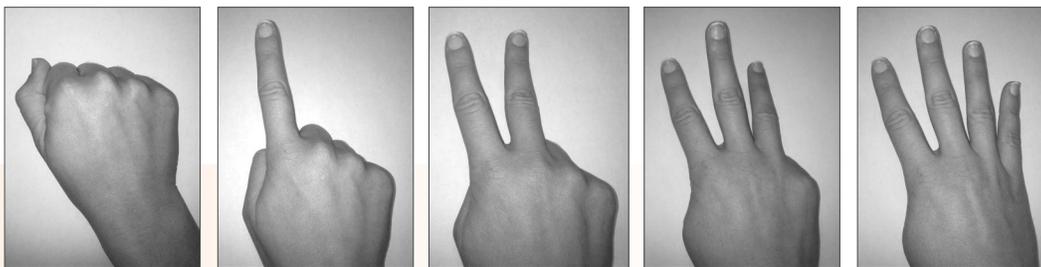
Objective: Add using the “counting on” strategy to find the sum of two numbers.

Directions:

1. Start with the greater number in your head.
2. Count up the lesser number on your fingers.
3. The answer is the last number you say.

Example: $7 + 4 =$

1. 7 is the greater number. We start counting with 7.
2. Count up the lesser number with your fingers.



7

8

9

10

11

3. The answer is the last number: 11.

Practice	
$3 + 1 =$	$4 + 2 =$
$2 + 2 =$	$5 + 3 =$
$9 + 3 =$	$8 + 5 =$
$7 + 6 =$	$5 + 5 =$
$2 + 8 =$	$8 + 8 =$
$3 + 6 =$	$5 + 9 =$

Worksheet

“Counting On” to Subtract

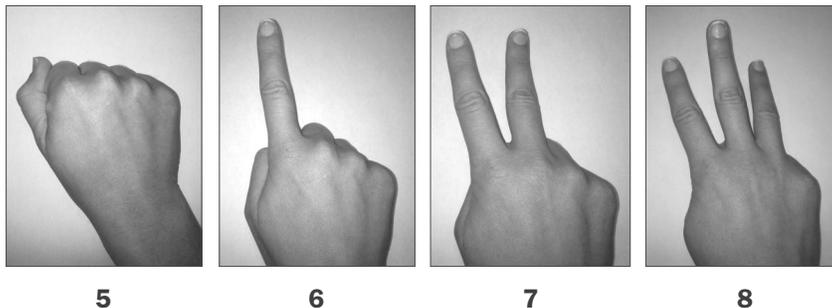
Objective: Subtract using the “counting on” strategy to find the difference between two numbers.

Directions:

1. Start with the lesser number in your head.
2. Count up to the greater number with your fingers.
3. The answer is the number of fingers you have up.

Example: $8 - 5 =$

1. 5 is the lesser number. We start counting with 5.
2. Count up to the greater number (8) with your fingers.

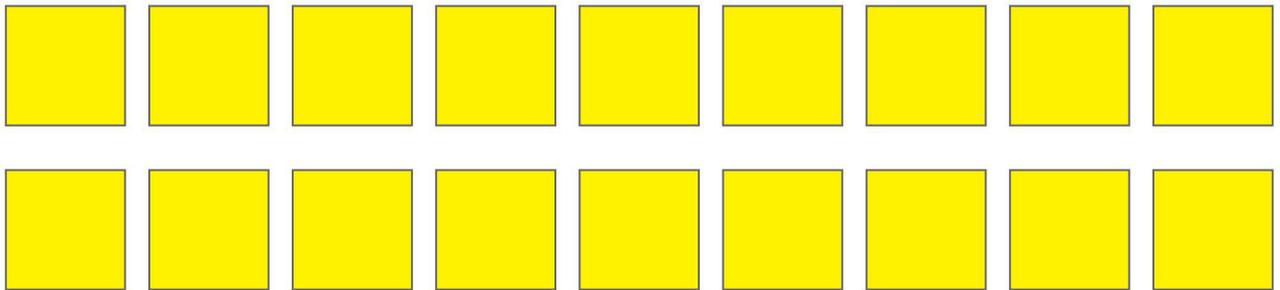
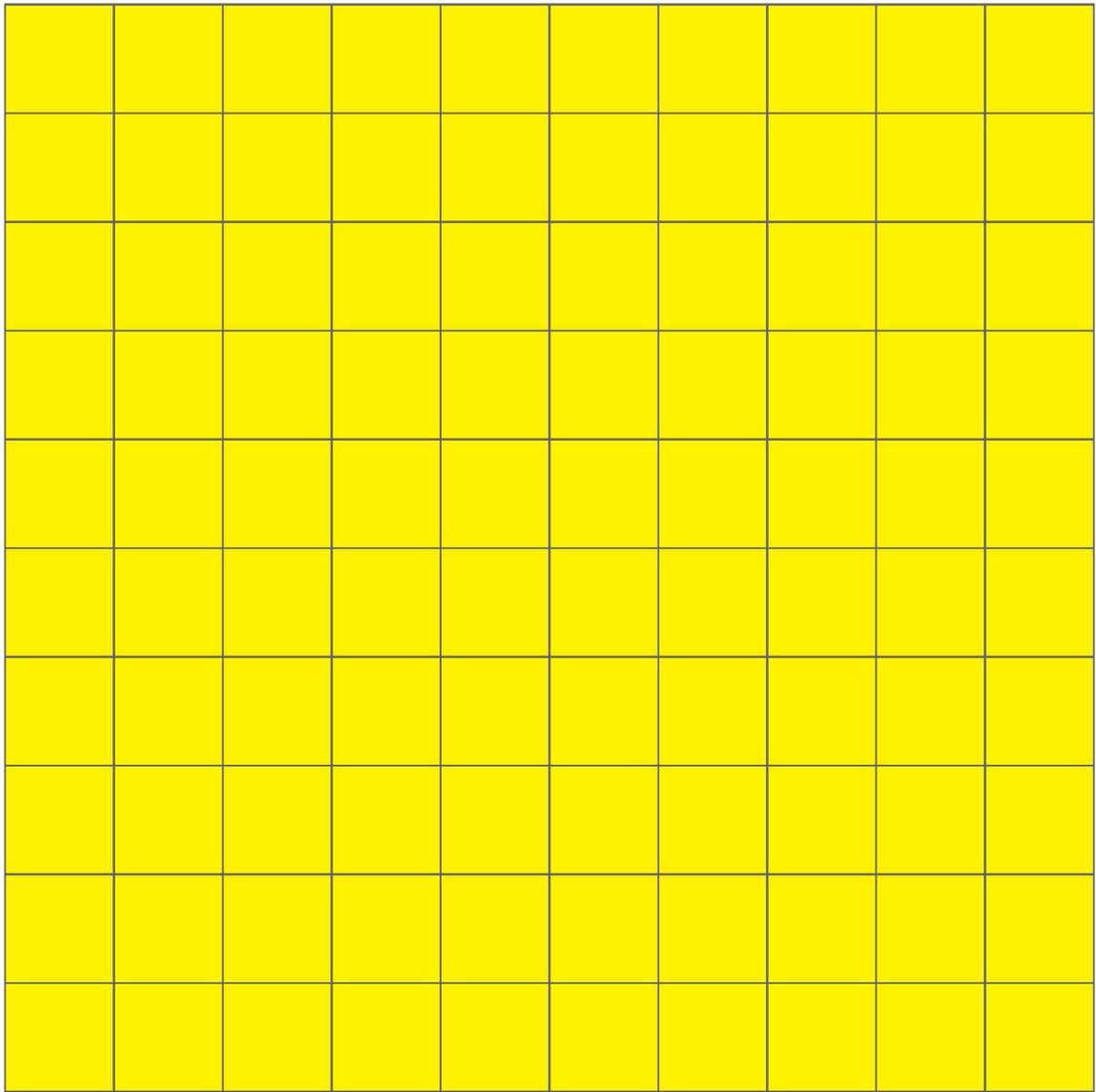


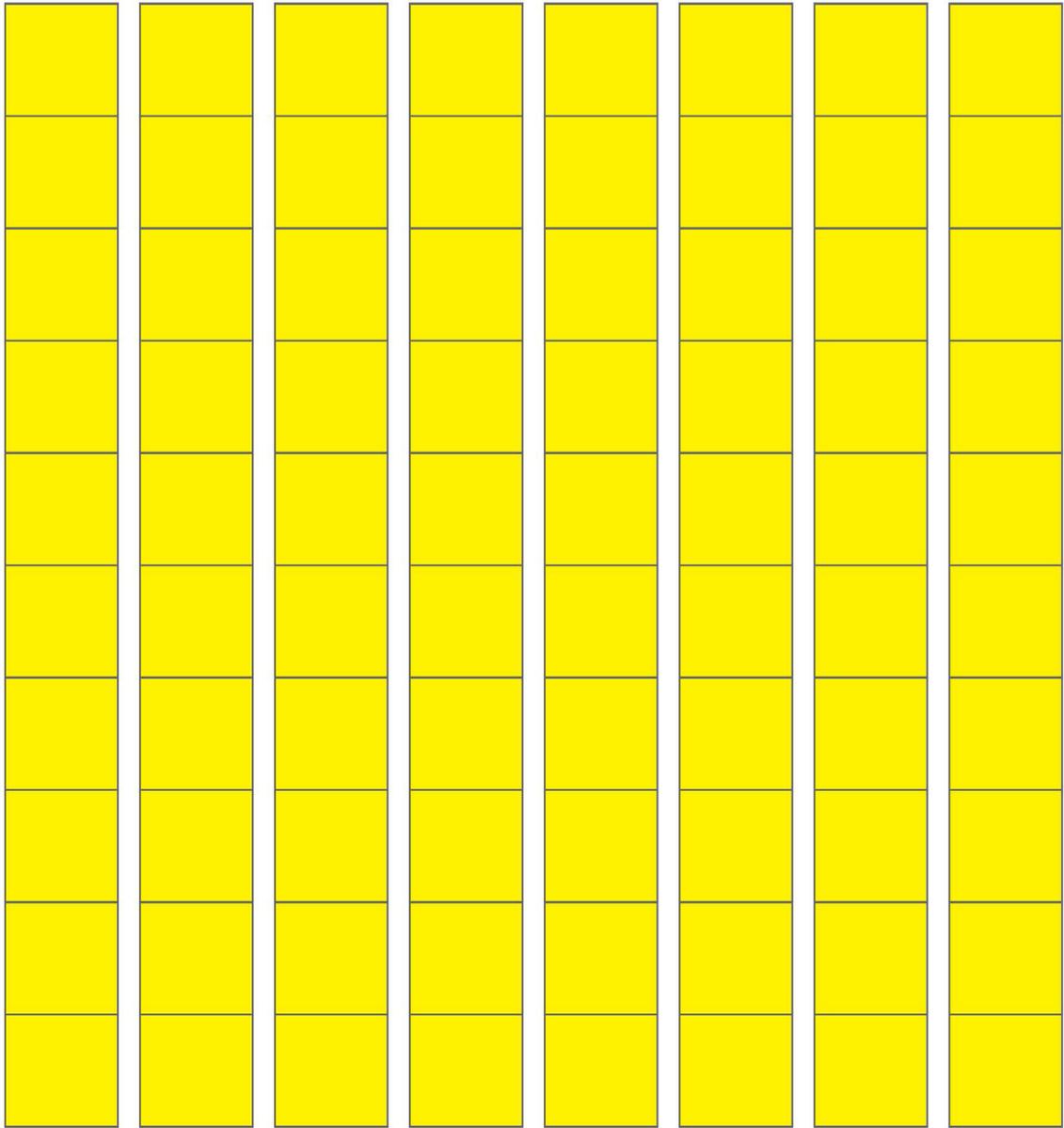
3. We're holding up three fingers, so the answer is 3.

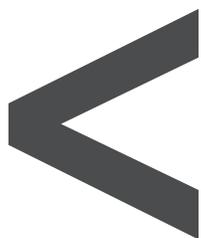
Practice	
$5 - 1 =$	$4 - 3 =$
$6 - 2 =$	$8 - 4 =$
$9 - 3 =$	$10 - 6 =$
$13 - 5 =$	$9 - 4 =$
$17 - 8 =$	$14 - 5 =$
$15 - 12 =$	$18 - 7 =$

5. Supplemental Materials (used across activities)

- a. Base 10 Squares
- b. Greater Than, Less Than, Equal To Comparison Cards
- c. Greater Than, Less Than, Equal To Comparison Cards
- d. Addition Flashcards
- e. Subtraction Flashcards
- f. Best Time Scorecard



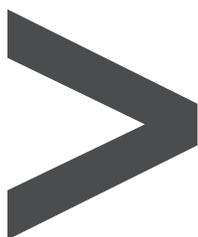




Less Than



Equal To



Greater Than

$$1 + 1 =$$

$$1 + 2 =$$

$$1 + 3 =$$

$$1 + 4 =$$

$$1 + 5 =$$

$$1 + 6 =$$

$$1 + 7 =$$

$$1 + 8 =$$

3

2

5

4

7

6

9

8

$1 + 9 =$

$1 + 10 =$

$1 + 0 =$

$2 + 0 =$

$2 + 1 =$

$2 + 2 =$

$2 + 3 =$

$2 + 4 =$

1 1

1 0

2

1

4

3

6

5

$$2 + 5 =$$

$$2 + 6 =$$

$$2 + 7 =$$

$$2 + 8 =$$

$$2 + 9 =$$

$$2 + 12 =$$

$$3 + 0 =$$

$$3 + 1 =$$

8

7

10

9

14

11

4

3

$$3 + 2 =$$

$$3 + 3 =$$

$$3 + 4 =$$

$$3 + 5 =$$

$$3 + 6 =$$

$$3 + 7 =$$

$$3 + 8 =$$

$$3 + 9 =$$

6

5

8

7

10

9

12

11

$3 + 10 =$

$4 + 0 =$

$4 + 1 =$

$4 + 2 =$

$4 + 3 =$

$4 + 4 =$

$4 + 5 =$

$4 + 6 =$

4

1 3

6

5

8

7

1 0

9

$4 + 7 =$

$4 + 8 =$

$4 + 9 =$

$4 + 10 =$

$5 + 0 =$

$5 + 1 =$

$5 + 2 =$

$5 + 3 =$

1 2

1 1

1 4

1 3

6

5

8

7

$$5 + 4 =$$

$$5 + 5 =$$

$$5 + 6 =$$

$$5 + 7 =$$

$$5 + 8 =$$

$$5 + 9 =$$

$$5 + 10 =$$

$$6 + 0 =$$

10

9

12

11

14

13

6

15

$$6 + 1 =$$

$$6 + 2 =$$

$$6 + 3 =$$

$$6 + 4 =$$

$$6 + 5 =$$

$$6 + 6 =$$

$$6 + 7 =$$

$$6 + 8 =$$

8

7

10

9

12

11

14

13

$$6 + 9 =$$

$$6 + 10 =$$

$$7 + 0 =$$

$$7 + 1 =$$

$$7 + 2 =$$

$$7 + 3 =$$

$$7 + 4 =$$

$$7 + 5 =$$

16

15

8

7

10

9

12

11

$7 + 6 =$

$7 + 7 =$

$7 + 8 =$

$7 + 9 =$

$7 + 10 =$

$8 + 0 =$

$8 + 1 =$

$8 + 2 =$

14

13

16

15

8

17

10

9

$$8 + 3 =$$

$$8 + 4 =$$

$$8 + 5 =$$

$$8 + 6 =$$

$$8 + 7 =$$

$$8 + 8 =$$

$$8 + 9 =$$

$$8 + 10 =$$

1 2

1 1

1 4

1 3

1 6

1 5

1 8

1 7

$9 + 0 =$

$9 + 1 =$

$9 + 2 =$

$9 + 3 =$

$9 + 4 =$

$9 + 5 =$

$9 + 6 =$

$9 + 7 =$

10

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14

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$$9 + 8 =$$

$$9 + 9 =$$

$$10 + 0 =$$

$$10 + 1 =$$

$$10 + 2 =$$

$$10 + 3 =$$

$$10 + 4 =$$

$$10 + 5 =$$

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$$10 + 6 =$$

$$10 + 7 =$$

$$10 + 8 =$$

$$0 + 0 =$$

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16

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18

$$0 - 0 =$$

$$1 - 0 =$$

$$1 - 1 =$$

$$2 - 0 =$$

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$13 - 2 =$

$13 - 5 =$

$14 - 5 =$

$14 - 7 =$

$14 - 6 =$

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$14 - 8 =$

$15 - 4 =$

$15 - 7 =$

$15 - 9 =$

$15 - 6 =$

$16 - 7 =$

$16 - 8 =$

$16 - 9 =$

11

6

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$17 - 9 =$

$18 - 9 =$

9

8

Best Time Scorecard

Student Name:

	Time 1	Time 2	Time 3	Best Time
Date:				

Student Name:

	Time 1	Time 2	Time 3	Best Time
Date:				

Student Name:

	Time 1	Time 2	Time 3	Best Time
Date:				
Date:				