# **Does Restricting Hand Gestures Impair Mathematical Reasoning?**

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#### Abstract

Gestures are associated with powerful forms of understanding; however, their causative role in mathematics reasoning is less clear. We inhibit college students' gestures by restraining their hands, and examine the impact on language, recall, intuition, and mathematical justifications of geometric conjectures. We test four mutually exclusive hypotheses: (1) gestures are facilitative, through cognitive off-loading, verbal support, or transduction, (2) gestures are not facilitative, but being inhibited from gesturing increases cognitive demands, (3) gestures are a byproduct of reasoning processes that would take place with or without the gestures' overt presence, and (4) gestures can cause learners to focus on concrete, salient representations, inhibiting abstraction. We find support for the third hypothesis, concluding that learners making or being inhibited from making gestures does not seem to impact their problem-solving, cognitive, or language processes. This suggests that being unable to overtly perform personally-generated gestures is not a hindrance to learners; however this would not necessarily hold for directed or structured gestures.

Keywords: gesture; proof; embodied cognition; gesture inhibition; geometry

#### **Does Restricting Hand Gestures Impair Mathematical Reasoning?**

## 1. Introduction

Embodied views on cognition posit that all mental processes are rooted in perceptual and motor systems (Wilson, 2002) and that mental representations of objects are experiential and multimodal in nature (Barsalou, 2008). Embodied approaches to teaching mathematics have become a particularly important area of study, challenging a tradition where mathematics is seen as disconnected from the body, action, and perception (Lakoff & Núñez, 2000). Geometry is an important area for embodiment investigations because of its spatial, dynamic relations and the complex interplay between language, symbols, and action (Nathan & Walkington, 2017).

One way in which mathematical reasoning is embodied is through *gesture*. We define gesture as personally-generated movements of the body that people use during reasoning about or communication of mathematical ideas. This follows McNeill (1992), who defines gestures as "all visible movements by the speaker" (p. 78) that do not involve object manipulation or actions like stroking one's hair. Under this definition, tracing a circle in the air while thinking about a geometric problem involving a circle would be a gesture, as would tilting the head to indicate the movement of an object translated on a Cartesian plane. Here we consider only gestures that are *mathematical* in nature – gestures that relate to mathematical reasoning, rather than gestures given for emphasis or to show other social cues (like nodding).

Learners' tendencies to produce mathematical gestures has been shown to predict learning and performance in mathematics (Cook & Goldin-Meadow, 2006), and students who gesture more and gesture in particular ways communicate more accurate geometry proofs (Nathan et al., 2014; Nathan & Walkington, 2017; Pier et al., 2019). *Dynamic gestures* (Garcia & Infante, 2012; Göksun, Goldin-Meadow, Newcombe, & Shipley, 2013) – gestures where the learner is depicting a motion-based transformation of a mathematical object through multiple states – are strongly associated with proof performance (Pier et al., 2019). An example of a dynamic gesture is formulating a triangle with thumbs and forefingers, and then having the triangle grow and shrink to show mathematical similarity. However, it is unclear whether such gestures are simply a byproduct of valid mathematical reasoning, or a causative factor. In other words, does formulating gestures provide conceptual support that allows students to be more successful, or do students who tend to have stronger mathematical knowledge also tend to gesture more?

One way to experimentally manipulate gesture is through gesture inhibition - physically inhibiting learners from being able to gesture and examining how this impacts reasoning. In the present study, we examine gesture inhibition for university students proving geometric conjectures. We examine how inhibition impacts mathematical reasoning and speech patterns, and how this effect is moderated by student-level characteristics.

#### 2. Theoretical framework

#### 2.1 Gesture as Simulated Action

Hostetter and Alibali (2008) proposed the *Gesture as Simulated Action* (GSA) framework, where gestures come about as a result of perceptual and motor simulations which arise from mental imagery and language processing. Gestures arise when pre-motor activation is activated beyond a speaker's current *gesture threshold* - the level of motor activation needed for a simulation to be expressed in overt action. This threshold can vary depending on factors such as the current task demands (e.g., strength of motor activation when processing spatial imagery, task difficulty), individual differences (e.g., level of spatial skills), and situational considerations (e.g., social contexts). Hostetter and Alibali (2007) hypothesized that people with low verbal skills but high spatial visualization skills would gesture most, as their mental images may not be well-connected to verbal forms they can orally communicate. Gestures are theorized to assist with "packaging" ideas for speech production (Alibali, Kita, & Young, 2000; Alibali, Yeo, Hostetter, & Kita, 2017); therefore, gesture production may be highest when speakers who have difficulty with verbal skills are presented with an organizationally demanding task (Alibali et al., 2000). A related idea is that gestures facilitate lexical retrieval – they allow learners to produce more fluent speech by facilitating better retrieval of words from memory (Krauss, 1998).

GSA suggests that inhibiting gesture may increase cognitive load, which may be particularly detrimental when learners are confronting a challenging task. *Cognitive load* is cognitive processing demands experienced by learners due to the relationship between a task's difficulty and a learner's cognitive system (van Merriënboer & Sweller, 2005). These demands draw upon *working memory* – the learner's cognitive capacity for in-the-moment processing, holding, and manipulation of information. Working memory demands can be reduced by utilizing external resources in the environment (e.g., writing down a phone number) through *cognitive offloading* (Risko & Gilbert, 2016). Gestures may relieve cognitive load by acting as an off-loading mechanism, allowing learners to bring new memory stores, such as spatial working memory, to bear. Thus, restricting the availability of gestures may prevent this beneficial off-loading from happening. Alternately, gesture inhibition itself may increase extraneous cognitive load, as stopping oneself from gesturing could be an effortful activity that utilizes working memory. This may be particularly detrimental to people with a low gesture threshold. GSA remains neutral on whether gesture inhibition itself utilizes cognitive resources because it is an

effortful task, or whether gestures function to relieve cognitive demand (Hostetter & Alibali, 2008).

#### 2.2 Cognition-action transduction

Nathan (2017) proposed to expand the GSA framework, citing recent research suggesting a *bidirectional* relation between action and cognition; this new theory is called *cognition-action transduction.* In addition to the hypothesis that mental simulations give rise to gestures, as proposed by the GSA framework of Hostetter and Alibali (2008), Nathan (2017) describes emerging evidence that the act of gesturing can itself activate mental simulations. In accordance with this view, superior problem-solving performance has been demonstrated when students follow directions to perform specific actions that correspond to cognitive operations that contribute to effective problem-solving strategies (e.g., Goldin-Meadow, Cook, & Mitchell, 2009; Ginns, Hu, Byrne, & Bobis, 2016; Hu, Ginns, & Bobis, 2015; Nathan et al., 2014; Novack et al., 2014). Cognition-action transduction allows that gesture inhibition could be detrimental, as people who are inhibited are not able to use gestures as a resource to understand new ideas. However, studies where learners are instructed to formulate particular highly-effective gestures are different than studies that allow learners to engage in their own personally-generated gesturing. Being instructed might be beneficial for low-knowledge learners who lack the resources to create their own effective gestures; these low-knowledge learners may actually generate misleading gestures illustrating incorrect relationships. However, Nathan et al. (2014) found that even purposefully-chosen directed gestures, when not properly understood, could lead learners down an incorrect solution path if they did not understand the relationships they were intended to be physically representing. Thus, it may only be when the person-environment

system offers appropriate feedback that cognition-action transduction would predict that the outward processes would be correct and lead to a desired change in cognitive state.

An alternate view is that gestures or directed actions may focus learners' attention on the specific concrete, spatial qualities of the objects they are physically representing or pointing to, therefore learners may not engage in generalization or abstraction – as described by Walkington, Nathan, Wolfgram, Alibali and Srisurichan (2014), they develop *modal-specific epistemological commitments*. These are situations where learners are so focused on immediately present, salient representations of concepts (like a concrete gesture) that they struggle to transfer this knowledge to other representations (Sloutsky, Kaminski, & Heckler, 2005), like a generalized mathematical proof. From a cognitive-action transduction standpoint, this could also lead them to give an incorrect or incomplete problem solution.

One way to study whether and how gestures affect cognition is to manipulate gestures through gesture inhibition.

### 2.3 Prior Gesture Inhibition Studies

Having learners tap with one hand in particular patterns that periodically change to hinder automaticity (spatial tapping) or that involve tapping repeatedly in one place (simple tapping) while solving problems has been studied as a method of gesture inhibition. Results from this line of research (Hegarty et al., 2005; Nathan & Martinez, 2015) with participants solving problems about mechanical and biological systems show that spatial tapping does indeed inhibit problemsolving performance ( $\eta^2 = 0.2$ ), while simple tapping does not. Hegarty et al. (2005) also found no effect for gesture inhibition through hand restriction. Together, these findings suggest that it is not the production of the gestures themselves that impact performance (i.e., not simple tapping or gesture inhibition). Instead, it is the demands of redirecting the processes involved in monitoring and executing particular motor sequences through the spatial tapping condition that selectively disrupts model-based reasoning, hampering performance on inference-making tasks. However, other researchers have examined the effects of hand restriction and found different results.

Several studies have looked at the impact of hand restriction on speech. Graham and Heywood (1975) found that gesture inhibition was associated with students using more spatial relation words, fewer demonstrative words, and more time spent pausing. Hostetter, Alibali, and Kita (2007) found that participants free to gesture used more semantically rich verbs (d=0.80) and were less likely to begin sentences with "and" (d=1.24). A similar study (Rauscher, Krauss, and Chen, 1996) found that gesture inhibition was associated with speaking more slowly and having more dysfluencies when discussing spatial content but speaking more quickly when discussing non-spatial content (ds=0.30-0.58). However, in a study of undergraduates giving others instructions on how to perform simple tasks, Hoetjes, Krahmer, and Swerts (2014) found no differences between hand-restricted and unrestricted participants on any speech category they measured – including speech duration or rate, number of words, pauses, or acoustic measures.

Other studies have examined the effect of hand restriction on recall. Frick-Horbury and Guttentag (1998) found gesture inhibition led to lower retrieval (ds=0.64-1.04) and recall (ds=1.32-1.98) of words and that this effect did not vary based on SAT scores. Beattie and Coughlan (1999) found that gesture-inhibited students were actually *more* likely to recall words, although this difference did not reach significance (d=0.29). Those who were inhibited were significantly less likely to report a "tip of the tongue" state (i.e., where they believed they knew the word but could not retrieve it; d=0.60) but were also less likely to be able to resolve this state when it happened (d=0.72).

Two recall studies have attempted to clarify the mechanisms through which gesturing impacts recall. Goldin-Meadow, Nusbaum, Kelly, and Wagner (2001) asked participants to solve math problems while keeping words or letters in memory, and found recall was higher when gesturing (d=0.35). They also compared instances where the participant was free to gesture but chose not to, versus being free to gesture and choosing to gesture, and found similar advantages of gesturing for recall. They concluded that gesture allows for cognitive offloading. In a similar study (Wagner, Nusbaum, & Goldin-Meadow, 2004) participants were asked to hold either a string of letters or a visuospatial configuration of dots in memory. No differences were found in speech patterns when participants did versus did not gesture, but not gesturing was associated with weaker recall. In addition, not gesturing when uninhibited was associated with negative outcomes that were similar to being inhibited from gesturing. The researchers conclude that gesturing reduces the load on both visuospatial and verbal working memory. However, they found that gesturing was only beneficial when it conveyed information that was also in speech, supporting the idea that gesture is beneficial because it helps learners organize information into the propositional form needed for speech. These studies are both of limited relevance because they do not contrast participants who were inhibited versus non-inhibited.

Alibali and Kita (2010) examined student explanations of Piagetian conservation tasks and found gesture inhibition caused children to express less perceptually present information (e.g., the glass is tall versus short) but more non-present information ( $\eta^2 = 0.16$ ). When inhibited, participants were more likely ( $\eta^2 = 0.28$ ) to call upon past events (e.g., "they were the same"), make hypotheses about things that might happen (e.g., "if the glass was fatter..."), and talk about transformations (e.g., "you moved it over"). When considering mathematical justifications, focusing on hypothetical states, past states, and transformations (rather than immediately-present, salient characteristics of mathematical objects) could be desirable (Harel & Sowder, 2005). This study points to the need to examine gesture inhibition for tasks like mathematical proof.

# 2.4 Research purpose

Prior research has not examined how gesture inhibition impacts mathematical reasoning generally, or geometric reasoning specifically, both of which have important visual, spatial, and motoric properties, in addition to powerful uses of language as a grounding mechanism (Lakoff & Núñez, 2000; Nathan, 2014). Mathematical reasoning is more complex than the simple recall or descriptive tasks examined in previous studies and has directly-actionable pedagogical implications. Geometric reasoning is an especially important area for the examination of gesture inhibition, given its spatial nature, use of transformational reasoning, and the prevalence of gestures (Nathan & Walkington, 2017; Walkington, Chelule, Woods, & Nathan, in press). Prior research has also not often examined whether effects of gesture inhibition vary based on learner characteristics, as this may influence students' ability to formulate their own effective gestures.

Prior gesture inhibition studies have also often utilized small sample sizes and betweensubjects comparisons. This makes it difficult to draw firm conclusions or conduct analyses of moderation effects, a primary focus here. Many prior studies have defined gestures as being done with the hands (e.g., Frick-Horbury & Guttentag, 1998; Goldin-Meadow et al., 2001; Rauscher et al., 1996; Wagner et al., 2004) and have not considered the various ways learners can still gesture with their hands restrained. Indeed, one study suggests learners with their limbs and hands restricted become more likely to gesture with other available body zones (e.g., eyebrows; Rimé, Schiaratur, Hupet, & Ghysselinckx, 1984). Finally, advances in computerized text analysis of speech patterns (McNamara, Louwerse, Cai, & Graesser, 2013) and the recent identification of dynamic gestures (e.g., Garcia & Infante, 2012) open up new possibilities for how gesture inhibition can be studied. The current study addresses each of these gaps.

## 2.5 Research questions and hypotheses

Our research questions (RQs) are:

- How do (a) speech patterns, and (b) gesture and dynamic gesture patterns, vary when participants are inhibited versus not inhibited from gesturing?
- 2) Does gesture inhibition impair recall, intuition, insight, or proof performance on geometric tasks, and does inhibition interact with participant characteristics?
- 3) How is the presence of gesture and dynamic gesture associated with recall, intuition, insight, and proof for only those trials when participants were free to gesture, and how do gesture effects interact with participant characteristics?

We pose four mutually exclusive hypotheses, with each hypothesis leading to different specific predictions for each research question. The first is the *facilitation hypothesis*, which posits that personally-generated gestures can causatively help learners. There are several conceptually distinct accounts in the literature as to why this might occur. First, gestures might reduce cognitive load through cognitive offloading. Second, gestures may allow learners to communicate their ideas better verbally, facilitating packaging of ideas into speech and/or allowing for lexical retrieval. Third, gestures might serve a transductive purpose by activating mental simulations, giving learners new, actionable ideas.

Second is the *interference hypothesis*, which posits that gestures do not have facilitative properties, but that preventing learners from gesturing in and of itself is an effortful activity that increases cognitive load, perhaps due to the novelty or discomfort of being inhibited from gesturing. Goldin-Meadow et al. (2001) describe this situation as "the observed effect is not due

to the beneficial effects of gesture, but to the deleterious effects of the constraining instructions. Asking speakers not to gesture is, in effect, asking them to do yet another task..." (p. 519).

Third is the *byproduct hypothesis*, which posits that gestures do not have facilitative properties, and that being inhibited from gesturing is not a cognitively effortful activity. This hypothesis would view gestures as merely an outgrowth of valid mathematical reasoning, rather than a causative factor. This hypothesis posits that gestures tend to co-occur with valid mathematical reasoning, without taking a role in causing that reasoning to happen. Fourth is the *concreteness hypothesis*, which posts that gestures may cause learners to focus on currently-present, spatial, salient forms of mathematical concepts, and disrupt possibilities for engaging in mathematical abstraction or hypothetical or deductive reasoning.

For **RQ1a** relating to speech patterns, the facilitation hypothesis would suggest that gesture inhibition would change speech patterns (H1a-facilitation), as facilitation in the form of offloading or improved retrieval or communication may allow for learners to give longer proofs that use more logical statements, describe more operations on objects, or that show more generalized or abstract thinking (Harel & Sowder, 2005; see Pier et al., 2019). In addition, a transduction effect may show proofs with more action and body-related words, as well as increased verb and cohesion measures related to situation models. Finally, when inhibited we may see speech changes consistent with prior studies reviewed above, such as fewer demonstrative words and semantically rich verbs.

The interference hypothesis would also posit that gesture inhibition changes speech patterns (H1a-interference). When cognitive load is increased, learners may use speech patterns that involve shorter proofs, less description of mathematical operations, less abstract or generalized language, and more dysfluent words or informal speech. The byproduct hypothesis would posit no relationship between gesture inhibition and speech patterns (H1a-byproduct). The concreteness hypothesis would posit that gesture inhibition causes participants to use language patterns that involve less concrete and spatial words, and more abstract terms and deductive language processes (H1a-concreteness).

For **RQ1b** regarding the impact of gesture inhibition on gesture, all four hypotheses would assume that gesture inhibition reduces gesture usage (H1b).

For **RQ2** relating to problem-solving performance, the facilitation hypothesis and the interference hypothesis would posit that gesture inhibition dampens problem-solving performance (H2-facilitation and H2-interference). The byproduct hypothesis would predict no relationship between gesture inhibition and performance (H2-byproduct), while the concreteness hypothesis would posit that gesture inhibition improves performance (H2-concretenes).

For **RQ3** relating to participant performance while free to gesture, the facilitation hypothesis and the byproduct hypothesis would predict that when free to gesture, gestures are associated with improved performance (H3-facilitation and H3-byproduct). The interference hypothesis would predict no association between gestures and performance when free to gesture (H3-interference), while the concreteness hypothesis would predict gesture use to be associated with *dampened* performance when uninhibited (H3-concreteness). The hypotheses and the research questions are summarized in Table 1.

#### Table 1

	Hypotheses							
	Facilitation	Facilitation Interference Byproduct Concreteness						
Inhibited versus not inhibited								
Speech (RQ1a) (H1a-facilitation) (H1a-interference) (H1a-byproduct) (H1a-con			(H1a-concreteness)					
	Inhibition may	Inhibition may	No differences	Inhibition may be				

Summary of research questions and hypotheses

	change language	change language		associated with
	patterns, as	patterns, as		fewer concrete/
	retrieval and/or	learners		spatial words, more
	packaging and/or	experience more		abstract words,
	communication is	cognitive load		more hypothetical
	facilitated, or	(e.g., more		statements
	transduction is	difficult word		
	instigated	retrieval)		
Gesture (RQ1b)	(H1b) Less gesture	occurs when learners	are inhibited from g	esturing
Performance (Intuition,	(H2-facilitation)	(H2-interference)	(H2-byproduct)	(H2-concreteness)
Insight, Proof; RQ2)	Inhibition is	Inhibition is	No differences	Inhibition is
	harmful	harmful		beneficial
Choose to gesture versu	s do not choose to	gesture (Uninhibit	ted trials only)	
Performance (Intuition,	(H3-facilitation)	(H3-interference)	(H3-byproduct)	(H3-concreteness)
Insight, Proof; RQ3)	Gesture use	No differences	Gesture use	Gesture use
	associated with		associated with	associated with
	higher		higher	lower performance
	performance		performance	

Research Questions 2-3 also allow that these hypotheses may not be uniform across participants. For example, offloading might only be beneficial when the learner has a less strong background in mathematics and needs to relieve working memory demands for in-the-moment problem solving, while the hypothesized verbal support from gestures may only be beneficial when the learner has low fluency skills and needs gestures to help retrieve words and package ideas into speech. Transduction might only occur when the learner has strong enough spatial skills to produce useful gestures to give them new ideas. Interference might only occur when the learner has a weak mathematical background and the cognitive system is already overloaded. Gestures may only be a byproduct of valid mathematical reasoning when learners have high enough spatial skills to formulate mathematical gestures to accompany speech. Participants with low spatial skills may be especially likely to fall prey to difficulty generalizing from concrete representations. By examining a variety of moderators, we can consider whether differential effects might be occurring. Finally, research question 3 also considers differences related to dynamic gestures as a special class of gesture that is particularly relevant to mathematical reasoning. We hypothesize that the presence of dynamic gestures will have a stronger association with insight and proof during uninhibited trials, compared to simply any gesturing being present. This is because dynamic gestures show transformations, which are central to the processes involved in understanding and generalizing mathematical relationships, which are key to having insights and formulating proofs of geometric conjectures.

# 3 Methods

# **3.1 Participants**

Undergraduate and graduate students (n=108; 48 male and 60 female) from a private university were recruited to participate in a laboratory study lasting 30-45 minutes. Math and statistics majors and graduate students were specifically targeted through department emails, signs, and class visits. Of the 108 participants, 34 were math or statistics majors, 7 were math or statistics graduate students, 5 were engineering majors, and 5 were science majors. The remaining 57 participants were undergraduate non-STEM majors or undeclared majors. The mean age was 20.41 years (*SD*=2.18). Fifty-five participants had taken a math class above calculus 1, 26 had taken up to calculus 1, and 27 had taken below calculus 1. Fifty-eight participants identified as Caucasian, 17 as Asian, 12 as African-American, 12 as Hispanic, and 9 as other races or biracial; 23 participants reported being non-native English speakers. One participant (a female math major) was omitted during the coding phase because she was not able to speak English well enough to respond to the prompts, for a final sample of 107.

#### **3.2 Power Analysis**

An a priori power analysis was conducted with G\*Power 3.1.9.2 (Faul, Erdfelder, Buchner, & Lang, 2009) using  $\beta$ =0.80 and  $\alpha$ =0.05. Based on previous data (Nathan & Walkington, 2017), correlations among a participant solving repeated geometry proofs were estimated at 0.6. We estimate an effect size of d=0.6 for gesture inhibition on proof performance from Walkington et al. (2014), a small pilot study where 15 participants proved a similar set of geometry conjectures while inhibited or not inhibited for all trials. This study was used because it had the closest outcome variable to the present study (mathematical proof performance); however, this effect size was generally consistent with effect sizes in other studies reviewed earlier. We additionally took into account being powered to detect mediation effects of gesture and speech (assuming partial mediation and small to medium-sized paths for alpha and beta, d=0.26-0.39; Fritz & MacKinnon, 2007), which led to a sample size of 86, taking into account the design effect. This was our minimum, but we accepted all participants who responded to the ads, with the restriction that we wanted to keep the number of non-STEM majors relatively balanced with the number of STEM majors. With 107 participants, a post-hoc sensitivity analysis showed that we should be able to detect effects for gesture inhibition that are as small in size as d=0.2.

# **3.3 Procedures**

Participants engaged in a one-on-one session with an interviewer. They were given four pre-measures (described later) and presented with 8 geometry conjectures (Table 2). The conjectures were ordered via a Latin Square and projected onto a screen one at a time. Participants were asked to read each conjecture out loud and state whether each conjecture was true or false and why it was true or false. For 4 of the 8 conjectures, participants were inhibited from gesturing by putting their hands in oven mitts that were attached to bottles attached to a music stand (Figure 1). Participants were either inhibited for the first four conjectures or the final four conjectures; inhibition order was counterbalanced. When they completed all 8 conjectures, participants were asked to, while uninhibited, recall as many of the conjectures as possible. All interviewer interaction with the participant was scripted, to ensure uniform treatment of inhibited versus uninhibited trials.

# Table 2

# Conjectures used in study, with average success rates for proof and insight

	Conjecture	Verity	Proof	Insight	Intuition	Recall
			Correct	Correct	Correct	Correct
1	An angle bisector of any angle of a	False	6.5%	23.4%	31.8%	61.68%
	triangle also bisects the opposite side.					
2	Any translation can be expressed as	True	5.6%	23.4%	43.0%	53.27%
	the composition of two reflections.					
3	If one angle of a triangle is larger than	True	29.9%	63.6%	88.8%	56.07%
	a second angle, then the side opposite					
	the first angle is longer than the side					
	opposite the second angle.					
4	The area of a parallelogram is the	True	29.0%	75.7%	81.3%	70.09%
	same as the area of a rectangle with					
	the same length and height.					
5	The segment that joins the midpoints	True	11.2%	46.7%	63.6%	50.47%
	of two sides of any triangle is parallel					
	to the third side.					
6	Any rotation can be expressed as the	True	4.7%	24.3%	51.4%	54.21%
	composition of two reflections.					
7	Given that you know the measure of	False	35.5%	39.3%	52.3%	43.93%
	all three angles of a triangle, there is					
	only one unique triangle that can be					
	formed with these three angle					
	measurements.					
8	If there are three points P, R, and Q in	True	25.2%	43.0%	56.1%	50.47%
	space, and the distance between P and					
	$\hat{\mathbf{Q}}$ equals the sum of the distance					
	between P and R and the distance					
	between R and Q, then points P, R,					
	and Q must all lie along the same line.					



Figure 1. Gesture inhibition rig

# 3.4 Measures

*Geometry Pretest*. Participants were given a geometry knowledge pretest, developed in a prior study (Nathan & Walkington, 2017; r=0.56 with performance on conjectures similar to those considered here), composed of twelve statements about triangles, parallelograms, and circles. Although the pretest had a moderate correlation with student performance on the conjectures in the present study (r = 0.41 with proof), it was ultimately not used in the models because of issues with internal consistency. Results for gesture inhibition were the same with or without pretest included, and pretest did not significantly interact with gesture inhibition in any model.

*Spatial Skills Test.* Participants were given the Paper Folding Test, from The Kit of Factor-Referenced Cognitive Tests (Ekstrom, French, Harman, & Derman, 1976), which measures participant's ability to visualize and manipulate images. Scores are calculated as the

number of items correct minus one-quarter of the number incorrect. Reliability for this measure is 0.75 for males and 0.77 for females.

*Phonemic Fluency Test.* The phonemic fluency measure tests speakers' ability to manage the organizational demands of speaking by rapidly generating words in a way that they do not typically organize them in their lexicon; here, by naming as many words as they can in 60 seconds that begin with the letter 's' and then the letter 't.' Score is the number of words generated in 60 seconds (omitting proper nouns and simple variants). Retest reliability is 0.88 (desRosiers & Kavanagh, 1987). For the present data we examined the correlation between the count of words each participant generated beginning with "t" and the count of words each participant generated beginning with "s." The correlation for these values (including word variants) was 0.73. Approximately 19% of the words participants generated for this test were simple variants of words they had already generated or proper nouns (19.7% for "s" and 18.6% for "t"). The mean (14.8) and standard deviation (4.8) for the phonemic fluency measure here was similar to other studies that have used this measure (Hostettar & Alibali, 2007; Yeudall, Fromm, Reddon, & Stefanyk, 1986).

*Demographic Questionnaire*. A paper questionnaire asked participants to identify their class/year, race/ethnicity, Math ACT/SAT scores, college major(s), age, gender, native language, and prior and current math courses taken. ACT/SAT scores were not used as 42 of the 108 responses were missing/ambiguous.

## 3.5 Coding

Participants were video-recorded and their speech was transcribed in the Transana video analysis software (Woods & Fassnacht, 2012). Individual clips were made of each participant

proving each conjecture for a total of 856 clips. One STEM major had his hands off-camera while uninhibited, thus his uninhibited data is omitted from gesture analyses.

*Coding Proof.* Participants' oral proofs for each conjecture were scored 0/1 in terms of correct or incorrect using a codebook (see Appendix A), which was developed from the criteria for valid mathematical proofs given by Harel and Sowder (2005). Cohen's Kappa reliability of 0.81 was achieved for 100 randomly-selected double-coded clips.

*Coding of Insight*. Given the relatively low rate of valid proofs, a complementary measure (insight) was included to assess whether participants demonstrated understanding of some of the key ideas, without necessarily getting all the way to a full deductive argument. Insight was defined according to Zhang, Lei, and Li (2016) as conscious retrieval of activated mathematical properties and examples that are both validly applied and relevant to the conjecture at hand. See Appendix A for how this was operationalized. Cohen's Kappa reliability of 0.80 was achieved for 100 randomly-selected double-coded clips.

*Coding of Intuition*. Participants' justifications were also coded for whether they correctly concluded the conjecture was true or false. If the participant changed their answer, only the final answer was considered for the coding. One hundred clips were randomly selected from the corpus for independent double-coding; a Cohen's Kappa reliability of 0.97 was achieved.

*Coding of Recall*. Participants were asked at the end of the session to repeat as many of the conjectures as they could remember. If the participant recalled a conjecture, they received a code of "1", otherwise they received a code of "0." Cohen's kappa of 0.96 was achieved for 100 randomly-selected double-coded clips.

*Coding of Gesture*. Each clip was coded for whether the participant made (1) any gesture at all, which represented, pointed to, or indicated movement or transformation of, mathematical

objects (e.g., sweeping the head left and upwards when indicating the upper left corner of a quadrilateral) or (2) any dynamic gesture, where participants showed a movement-based transformation of an object through multiple states (e.g., showing a translation of a mathematical figure by tilting the head or moving the hands). These categories were 0/1 variables, and gestures could fall into multiple categories. Reliability for inhibited versus uninhibited trials was calculated separately, due to the increased challenge of coding inhibited trials and differing gesture rates. Kappas of 0.90 (any gesture) and 0.87 (dynamic gesture) were achieved between two coders for the uninhibited trials on a random subset of 50 clips, while kappas of 0.81 (any gesture) and 0.81 (dynamic gesture) were achieved between two coders for the inhibited trials on a random subset of 50 clips.

Prior gesture inhibition studies have largely defined gestures in terms of hand movements, thus this coding represents a methodological expansion. Participants inhibited from gesturing would use their head to point to imagined figures in front of them or to show an object's movement. In addition, although not used in statistical analyses because of their rarity, we also looked at how often participants attempted hand gestures when gestures were inhibited. Occasionally the camera feed would capture slight but visible movements indicating participants were moving their fingers inside the oven mitts, that seemed to be related to their mathematical reasoning. We found that while hand gestures occurred in 62.74% of all trials while uninhibited, they only occurred in 4.45% of inhibited trials.

*Coding of Speech*. In order to examine the differences in speech patterns proposed in our hypotheses, the transcript of each participant's speech was entered into two text analysis software packages, Coh-metrix and LIWC. Coh-metrix (McNamara et al., 2013) codes texts based on 108 categories, which range from the number of words per sentence to the average

concreteness and age of acquisition of words. Prior research has found that Coh-metrix can distinguish important elements of mathematical arguments like using connective words, actions on mathematical objects, and deductive statements, as well as progressing through a logical structure through sentence overlap (Nathan et al., 2018; Pier et al., 2019). LIWC (Pennebaker, Chung, Ireland, Gonzales, & Booth, 2007) is a dictionary-based computerized text analysis tool that counts the number of words occurring in the text in 70 categories. Although not all LIWC categories are relevant, many categories (like cognitive process words) have been found to be important in prior investigation of oral proofs (Pier et al., 2019). All language variables tested are listed in Appendix B.

As indicated by our hypotheses (Table 1), we only investigated speech differences for inhibited versus uninhibited trials. How speech categories relating to mathematical proof practices change when learners choose to gesture versus not gesture has been examined extensively in other work (see Pier et al., 2019). By comparing the coded speech categories used during inhibited trials to uninhibited trials, we can see if there were significant differences in the kinds of words, phrases, and patterns of speech participants used that reflected the differences we proposed in our hypotheses.

#### **3.6 Analysis**

Our hypotheses (Table 1) relate to three comparisons – (1) participants' performance on inhibited versus uninhibited trials, (2) participants' speech patterns in inhibited versus uninhibited trials, and (3) participants' performance when they chose to gesture versus not gesture (when uninhibited). For the first comparison, we modelled performance as an outcome with inhibited/uninhibited as a predictor. For the second comparison, we modelled our quantitatively coded speech categories from Coh-Metrix and LIWC as an outcome, with

inhibited/uninhibited as a predictor. And for the third comparison, we modelled performance as an outcome (including only the uninhibited trials), with gesture/no gesture as a predictor.

For Research Question 1a, as an initial screening step, we first removed from consideration language categories in Coh-Metrix and LIWC that (1) were intended for text that and clear sentence delineations (rather than natural speech; e.g., number of sentences), (2) related to use of punctuation (e.g., incidence of semicolons), and (3) that were "0" (i.e., not present) for 75% or more of the data points. This left us with 53 different categories from LIWC and 95 different categories from Coh-Metrix (see Appendix B). All variables were continuous with the exception of word count. We then fit mixed effects linear models (with student and conjecture as random effects) predicting each language category with inhibition condition as a predictor. We used a cluster bootstrap to estimate the standard error of the regression coefficients. The cluster bootstrap was used because it can deal with issues of non-normality and heteroscedasticity, and works for data that have a lot of "0" values, as is typical for readability variables. Bootstrap samples were drawn by sampling individuals rather than observations, thus taking into account the nesting of observations within participant. We implemented the cluster bootstrap procedure by (i) generating 1000 bootstrap samples using the ClusterBootstrap library in R, (ii) applying the linear mixed effects models to each bootstrap sample, and (iii) computing the regression coefficients' standard errors from the bootstrap distribution. We applied the False Discovery Rate *p*-value correction to the significance tests for the regression coefficients (Benjamini & Hochberg, 1995).

For Research Question 1b, mixed effects logistic regression models were fit using the *glmer()* command (Bates, Maechler, Bolker, & Walker, 2014) in the R software package. Models predicted any gesture (coded 0/1) and dynamic gesture (coded 0/1), with participant, conjecture,

and which of the 8 Latin square orders they received as random effects. Fixed effects included whether the participant was inhibited for the conjecture, demographic variables (gender, language), and expertise variables (geometry pre-test score, spatial score, phonemic fluency score, STEM/non-STEM major, highest math course taken).

For Research Question 2, similar models were fit predicting correct proof (coded 0/1) and insight (coded 0/1). For the recall model only, an additional fixed effect was added to identify in what order during the session (1-8, a factor variable) participants had received the conjecture. We first fit main effects models examining the impact of gesture inhibition, and then examined two-way interactions between gesture inhibition and other fixed effects. Interactions were only retained if they significantly reduced deviance using the *anova()* command in R. The regression tables present raw coefficients that can be exponentiated to get odds ratios. Standardized mean difference-type effect sizes were calculated using the method in Chinn (2000).

For Research Question 3, the analysis process given above for Research Question 2 was repeated for the subset where participants were uninhibited (n = 428 trials). Additionally, dynamic gesture and any gesture were added as predictors.

#### 4 **Results**

Table 3 gives descriptive statistics for our measures. As can be seen from the table, our four performance measures (intuition, recall, insight, and proof) had different average accuracy levels – 58.5%, 55.0%, 42.4%, and 18.5%, respectively. As we coded the validity of participants' mathematical reasoning at a variety of different levels of task difficulty, we offset concerns of either having ceiling or floor effects. We also conducted supplementary analyses where we only examined the easier or more difficult conjectures, and results were the same.

# Table 3

## Average rates of correctness and gesture incidence

Measure	All Participants			
	( <i>N</i> =	= 107)		
Geometry Pre-Test Mean (SD)	80.61%	(12.26%)		
Spatial Skills Mean (SD)	12.20 (4.70)			
Phonemic Fluency Mean (SD)	14.87 (3.84)			
	Inhibited (428 trials)	Not (428 trials)		
% Trials Correct Proof	18.22%	18.69%		
% Trials Correct Insight	43.46%	41.36%		
% Trials Correct Intuition	59.11%	57.94%		
% Trials Correct Recall	55.61%	54.44%		
% Trials Any Gesture	29.67%	69.81%		
% Trials Dynamic Gesture	10.75%	32.78%		

### 4.1 RQ1: Association between gesture inhibition and speech and gesture

To examine how speech patterns varied when participants were inhibited versus not inhibited, we used a cluster bootstrap with mixed effects regression models to assess whether there were differences between uninhibited and inhibited trials according to the 148 different language measures. None were significant (consistent with H1a-byproduct). See Appendix C for information on the regression coefficients and significance tests. Appendix B also includes Cohen's *d* values that show the effect size of gesture inhibition for each speech category – *d* values were less than or equal to 0.3, with only three categories (past tense, positive emotion, and affect) having a *d* value greater than 0.2.

Participants inhibited from gesturing were less likely to make any gesture (Odds=0.09, d=-1.32, p<.001; consistent with H1b) and dynamic gestures (Odds=0.14, d=1.07, p<.001). When both including and removing the gesture inhibition variable, there were no instances where another fixed effect predicted gesture. Examining factors predicting gestures during only the

uninhibited trials yielded only the significant effect that students who had taken calculus 2 or a higher math course were significantly more likely to make dynamic gestures than those who had taken only calculus 1 (Odds = 3.36, d = 0.67, p = 0.034) or those who had not taken calculus (Odds = 3.55, d = 0.70, p = 0.036).

#### 4.2 RQ 2: Association between gesture inhibition and outcomes

For the recall model (Model 1 in Table 4), gesture inhibition had no effect (p=0.62, d=0.04). The only fixed effect predictive of recall was course taking, with participants whose highest math class was below calculus 1 less likely to recall a conjecture than participants above calculus 1 (Odds=0.46, d = -0.43, p=0.020). The order in which participants received conjectures was highly significant but is not shown in the table for brevity. For the intuition model (Model 2), gesture inhibition had no effect (p=0.77, d=0.02). No other fixed effects predicted intuition. Models 1 and 2 were re-fit examining whether gesture inhibition interacted with each of the other variables. No interaction terms were statistically significant.

### Table 4

	Model 1: Main Effects Recall	Model 2: Main Effects Intuition
Fixed Effects	B (SE) <sup>Sig</sup>	B (SE) <sup>Sig</sup>
(Intercept)	-0.39 (0.39)	0.54 (0.41)
Gestures Not Inhibited	(ref.)	(ref.)
Gestures Inhibited	0.08 (0.16)	0.05 (0.15)
Female	(ref.)	(ref.)
Male	0.03 (0.21)	0.18 (0.19)
Native English	(ref.)	(ref.)
Non-Native English	0.06 (0.28)	-0.06 (0.25)
Non-STEM major	(ref.)	(ref.)
STEM major	-0.31 (0.30)	-0.02 (0.26)
Phonemic Fluency	0.05 (0.03)	-0.01 (0.03)

Models predicting recall and intuition

Course Beyond Calc I	(ref.)	(ref.)			
Course Below Calc 1	-0.78 (0.34)*	-0.31 (0.31)			
Course Calc 1	-0.54 (0.31)	-0.39 (0.27)			
Spatial Score	0.02 (0.02)	0.02 (0.02)			
<i>Note</i> (ref.) denotes the reference category $*-n < 05$					

*Note*. (ref.) denotes the reference category. \*= p < .05

In the main effects model predicting insight (Model 3 in Table 5), spatial test score was significantly positively associated with correct insights (d=0.034 per 1 point on test, p=.014). Being male was also associated with a greater likelihood of correct insight (Odds=1.63, d=0.27, p=0.024), as was taking a math course beyond calculus 1, rather than no calculus (Odds = 0.49, d=-0.40, p = 0.044) or calculus 1 only (Odds = 0.51, d = -0.37, p = 0.034). There was no main effect for gesture inhibition (p=0.44, d=0.07).

In the main effects model predicting proof (Model 4), spatial test score was significantly positively associated with correct proofs (d=0.07 per 1 point on test, p=.001). Being male was also associated with a greater likelihood of correct proof (Odds=1.89, d=0.35, p=0.023). Having a highest math course above calculus 1 was associated with a higher likelihood of correct proof, compared to only calculus 1, (Odds=2.96, d=0.60, p=0.011), and below calculus 1 (Odds = 2.81, d = 0.57, p = 0.030). There was no main effect for gesture inhibition (p=0.88, d=0.02). Models 3 and 4 were re-fit examining whether gesture inhibition interacted with each of the other variables. No interaction terms were statistically significant (ps>.05).

In sum, gesture inhibition did not predict any of the performance measures, consistent with H2-byproduct.

Table 5

# Models predicting insight and proof

	Model 3: Main Effects Insight	Model 4: Main Effects Proof
	B (SE) <sup>Sig</sup>	B (SE) <sup>Sig</sup>
(Intercept)	-0.24 (0.45)	-2.02 (0.56)***
Gestures Not Inhibited	(ref.)	(ref.)
Gestures Inhibited	0.12 (0.16)	0.03 (0.21)
Female	(ref.)	(ref.)
Male	0.49 (0.22)*	0.64 (0.28)*
Native English	(ref.)	(ref.)
Non-Native English	-0.57 (0.29)	-0.38 (0.37)
Non-STEM major	(ref.)	(ref.)
STEM major	0.06 (0.30)	0.23 (0.39)
Phonemic Fluency Score	0.01 (0.03)	-0.02 (0.04)
Course Beyond Calc I	(ref.)	(ref.)
Course Below Calc 1	-0.72 (0.36)*	-1.04 (0.48)*
Course Calc 1	-0.67 (0.32)*	-1.08 (0.42)*
Spatial Score	0.06 (0.02)*	0.12 (0.04)**

*Note.* (ref.) denotes the reference category. \* = p < .05, \*\* = p < .01, \*\*\* = p < .001

#### 4.3 RQ3: Association between gesture and outcomes when uninhibited

We next considered only trials where participants were free to gesture (Table 6). For the models predicting recall and intuition, neither gesture type (any gesture, dynamic gesture) was associated with outcomes. For the models predicting insight, dynamic gestures were associated with valid insights (Odds=2.27, d=0.45, p=0.014), but any gesture was not (p=0.16, d=0.21). None of the other predictors had a significant interaction with dynamic gestures. For the models predicting proof, dynamic gestures were strongly associated with valid proofs (Odds=3.81, d=0.74, p<.001). Any gesture was not associated with valid proofs (p=0.45, d=0.14). None of the other predictors had a significant interaction with dynamic gestures. Being male was associated with a higher likelihood of insight and proof across models, while being a non-native English speaker was associated with a lower likelihood of insight. For all four models, spatial test score

significantly positively predicted valid proofs and insights. For the dynamic gesture proof model, being a STEM major significantly positively predicted valid proofs.

As there were positive results for gestures predicting performance during uninhibited trials, these results are consistent with H3-byproduct. We would also expect this effect under H3-facilitation, but the results from RQ2 rule out facilitation as being the appropriate hypothesis.

# Table 6

	Model 5: Any Gesture	Model 6: Dynamic	Model 5: Any Gesture Proof	Model 6: Dynamic
	Insight	Gesture Insight		Gesture Proof
Fixed Effects	B (SE) <sup>Sig</sup>	B (SE) <sup>Sig</sup>	B (SE) <sup>Sig</sup>	B (SE) <sup>Sig</sup>
(Intercept)	-0.74 (0.57)	-0.84 (0.58)	-2.79 (0.75)	-3.40 (0.79)
Female	(ref.)	(ref.)	(ref.)	(ref.)
Male	0.66 (0.26)*	0.70 (0.27)**	0.91 (0.34)**	1.02 (0.35)**
Native English	(ref.)	(ref.)	(ref.)	(ref.)
Non-Native	-0.87 (0.36)*	-0.81 (0.36)*	-0.30 (0.44)	-0.18 (0.44)
English				
Non-STEM major	(ref.)	(ref.)	(ref.)	(ref.)
STEM major	0.27 (0.36)	0.36 (0.36)	0.80 (0.49)	1.01 (0.51)*
Phonemic Fluency	0.03 (0.03)	0.03 (0.03)	0 (0.04)	-0.02 (0.04)
Course Beyond	(ref.)	(ref.)	(ref.)	(ref.)
Calc I				
Course Below	-0.54 (0.41)	-0.48 (0.41)	-0.62 (0.58)	-0.13 (0.54)
Calc 1				
Course Calc 1	-0.41 (0.38)	-0.33 (0.38)	-1.10 (0.53)*	-0.75 (0.52)
Spatial Score	0.06 (0.03)*	0.06 (0.03)*	0.12 (0.05)*	0.13 (0.05)**
Any Gesture	0.38 (0.27)		0.26 (0.34)	
Dynamic Gesture		0.82 (0.33)*		1.34 (0.40)***

Models predicting insight and proof, with gesture as predictor

*Note.* (ref.) denotes the reference category. \* = p < .05, \*\* = p < .01, \*\*\* = p < .001

# 5 Discussion

Our results support our third hypothesis, the *byproduct hypothesis* (Table 1; H1abyproduct, H1b, H2-byproduct, H3-byproduct). Gesture inhibition had no significant effect on a variety of outcome measures – including speech patterns, recall, and giving valid intuitions, insights, and proofs for geometry conjectures. Analyses of interaction effects suggested that inhibition had no significant effect regardless of gender, language status, spatial skills, phonemic fluency, college major, or math course-taking history. However, gesturing, particularly making dynamic gestures, was associated with improved insight and proof, and inhibiting gestures via our gesture inhibition rig dramatically reduced tendency to gesture. How can these results be reconciled?

An explanation for these findings is that gesture is merely a byproduct of – rather than a causative factor in – valid geometric proof construction. In other words, college students in the study who tended to do better at these geometry tasks also tended to gesture more and to gesture in certain ways. But their gestures may not actually be *influencing* or *causing* their valid reasoning. If this was the case, when inhibited from gesturing, we would expect them to see no ill effect, since their gestures may have been simply an outgrowth of valid reasoning that was already established and that would have taken place with or without gesture.

This interpretation runs counter to other accounts in the literature – including the GSA framework (Hostetter & Alibali. 2008), which posits that gestures can relieve cognitive load, and/or that inhibiting gestures may increase cognitive load. There are a large number of other studies suggesting that gesture inhibition impacts a variety of outcomes, from language to recall to problem-solving performance (Alibali & Kita, 2006; Beattie & Coughlan, 1999; Frick-Horbury & Guttentag, 1998; Goldin-Meadow et al., 2001; Hostetter et al., 2007; Nathan & Martinez, 2015; Rauscher et al., 1996; Wagner et al., 2004). However, these studies had varied

populations, inhibition methods, sample sizes, and content areas, and these methodological details may be important in explaining the differing results. The difference between child versus young adult cognitive processing may be particularly important. In addition, this study directly addresses a number of correlational studies that link more gesturing or gesturing in certain ways to better outcomes for mathematical activities (Gerofsky, 2010; Pier et al., 2019; Walkington et al., 2014; Nathan & Walkington, 2017). This effect, while reliably detected across studies and relatively large in size, may not be a causative relationship, and thus may not be a useful malleable factor to consider intervening upon.

Theories of cognition-action transduction posit that gestures can give learners new ideas (Nathan, 2017), and this hypothesis is supported by studies suggesting a positive effect for directing gestures on mathematical outcomes (Goldin-Meadow et al., 2009; Novack et al., 2014). While directing participants to gesture in specific ways that are known to be effective may have a transductive impact on cognitive states, this study suggests that for young adults in mathematics, it may not be the case that personally-generated gestures have this impact. Rather than our learners' gestures giving them new actionable ideas about geometric proofs, the present study suggests that these gestures may simply illustrate reasoning that would be happening one way or another. In order for transduction to reliably take place in a study like the present one, gestures may need to be explicitly directed by an outside agent or through structuring of the environment. Studies that come to conclusions that gesturing improves learning should be careful to qualify how those gestures were directed or structured to come about, to build a clear evidence base.

In addition, our results support the hypothesis that dynamic gestures tend to be significantly associated with insight and proof whereas a general category of "any gesture" is not, indicating dynamic gestures' important association with valid geometric reasoning. Dynamic gestures show transformations of mathematical objects through multiple states, and thus may signal learners' understanding of geometric relations. This is consistent with predictions about dynamic gestures given in Nathan and Walkington (2017). However, this again may not be a causative relationship. We also found that gestures and dynamic gestures did not show a significant association with recall or intuition. This is consistent with Nathan and Martinez (2015), who found spatial tapping selectively impaired making inferences from reading science text, but showed no difference on textbase recall or performance.

#### Limitations and Future Directions

Although it is difficult to extend implications for age groups beyond the one examined in this study (college students at a selective university), among a population similar to ours, this type of gesture inhibition may not be detrimental to students' reasoning on geometric proof tasks. Despite the fact that we used a college student population, note that the tasks we gave participants were challenging enough for them, as demonstrated by the low success rates on our most stringent measure of mathematical reasoning (proof).

In addition, although studies reviewed here did involve coding of gestures, most looked only at hand gestures. Here we took a broader view of what constitutes a gesture, as participants seemed able to point to and represent the movement of mathematical objects with their heads rather than their hands. Whether head gestures would serve the same purpose in other content domains is less clear -- perhaps they are more useful in geometric reasoning. While the studies that involve spatial tapping do have some clear methodological limitations, one of the major reasons this method of gesture inhibition is used is because it may be more likely to inhibit *all* gestures – not just hand gestures. However, it is important to note that even with our liberal definition of gestures, we did see gesture rates fall dramatically with our inhibition method, with no accompanying significant change in any performance or language measure. It is also worth mentioning that participants could have been making "micro movements" inside the gloves or with other body parts that were too subtle to detect using visual means. The issue of micro movements is a limitation of all gesture inhibition studies that use a physical form of hand restriction. Despite this issue, most prior gesture inhibition studies using hand restriction have found significant differences.

A number of interventions for mathematics learning have been developed that direct learners to gesture in particular ways (e.g., Agostinho et al., 2015; Ginns et al., 2016; Goldin-Meadow et al., 2009; Hu et al., 2015; Nathan & Walkington, 2017; Ottmar & Landy, 2017; Petrick & Martin, 2012; Smith, King, & Hoyte, 2014). These interventions may be effective because they give learners well-thought-out gestural schemas to use that are more effective than the gestures that learners would use if left to their own devices. In other words, having learners simply gesture more may not be a particularly beneficial path – in order for gesture to give learners new ideas about geometry, learners may need to be taught to adopt specific types of gestures that are specially designed to demonstrate and embody powerful ideas and relationships. This may hold regardless of the level of mathematical expertise of the learner.

An important question is, how can these "effective" gestures be selected, and then how can they be passed on to learners in personally meaningful ways? In addition, to what degree do learners need to actually be directed to produce specific gestures? Research by Abrahamson and Trninic (2015) on the development of proportional reasoning using the body does not direct learners to do particular gestures, but rather creates an environment with a "field of promoted action" that loosely encourages particular kinds of body movement through feedback and interaction. These gestures are developed spontaneously and are personal, while at the same time are structured by the environment. An alternative approach is illustrated in a video game for promoting geometry reasoning developed by Nathan and Walkington (2017) that elicits directed actions by having players mimic the actions performed by in-game avatars. Other interventions that give the learner highly specific instructions about tracing relational parts of geometric figures have also been found to be effective (Ginns et al, 2015; Hu et al., 2015). If gesture is going to be leveraged to play a causative role mathematical reasoning, these varied forms of intervention are important considerations to be addressed by future work.

#### 6 Conclusions

Prior research has suggested somewhat uniform, detrimental effects for gesture inhibition; however, we discovered that personally-generated gestures may not play a causative role in geometric reasoning, supporting the *gestures as a byproduct hypothesis*. These results call into question a long line of studies suggesting detrimental effects for gesture inhibition. They also problematize theories that suggest that gesture can play a causative role in supporting learners' reasoning. However, this is one of the only studies looking at the effects of inhibition on mathematical reasoning, in the area of high school level geometry. This suggests that the causative role of gesture in promoting changes in language, recall, and reasoning might be different in other domains and developmental levels. While mathematical ideas are inherently embodied and perceptual (Lakoff & Núñez, 2000), it may be challenging for learners to spontaneously and meaningfully connect the embodied roots of mathematical ideas to the abstractions, definitions, and theorems they encounter in the typical classroom. What we tested here were highly academic tasks, firmly situated in the system of "school mathematics." In the mathematics classroom, learners are accustomed to only expressing their mathematical reasoning via written notation, rather than oral language accompanied by action. The ways in which

learners use gestures and their bodies is certainly influenced by this overarching system of norms and beliefs in mathematics, and learners might need to be instructed upon particular gestural schemas to bridge this divide and realize the power of gestures.

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