













## Handout 1A.3 (Continued)

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How-to Steps	Notes
<p><b>How-to Step 3:</b> Show students how to convert the visually represented information into mathematical notation.</p>	















































## Handout 3A.3

### Guiding Questions for Designing Worked Example Comparisons

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**1. When selecting the mathematical skill or topic**

- a. Am I introducing something new or reviewing?
- b. What mathematical concept(s) or skills do I want to highlight?
- c. What background knowledge do my students already have (i.e., what do my students already understand; what do they not understand)?

**2. When selecting the solutions for the topic**

- a. Could I include at least one solution that includes a visual representation? Why or why not?
- b. What features of each solution might I focus on to highlight the mathematical concepts included in each solution?
- c. In what ways is the comparison of these two solutions important for students' progress in problem solving and mathematical development?











# Handout 3A.5 (Continued)

When selecting the mathematical skill or topic	Participant Answer
Am I introducing something new or reviewing?	<i>Reviewing fraction division dividing a whole number by a fraction</i>
What mathematical concept(s) do I want to highlight?	<i>Concept of division with fractions</i>
What background knowledge do my students already have (i.e. what do my students already understand; what do they not understand)?	
Should I compare:  Two algorithms?  A visual and an Algorithm?  Why?	

## Handout 3A.5 (Continued)

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When selecting the mathematical skill or topic	Participant Answer
What features of each solution should I focus on when comparing the two solutions?	
How does comparing these two solutions support students' progress in problem solving and mathematical development?	

## Handout 3B.1a

### Designing A Worked Example Comparison (Concept A)

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**Math concept:** fraction division

**Solve:**  $1\frac{1}{2} \div \frac{1}{8}$

Solution 1	Solution 2
When selecting the mathematical skill or topic	Participant Answer
Am I introducing something new or reviewing?	
What mathematical concept(s) do I want to highlight?	





## Handout 3B.1b (Continued)

When selecting the mathematical skill or topic	Participant Answer
Am I introducing something new or reviewing?	
What mathematical concept(s) do I want to highlight?	
What background knowledge do my students already have (i.e., what do my students already understand)?	



















## Handout 4A.2 (Continued)

### The Rate Problem and Anticipatory Questions – Part B

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#### Anticipatory Questions:

1.

2.

3.









## Handout 4B.3

### Fruit Strips Problem – Comparing Solutions Framework and Graphic Organizer

Features of the Solution Strategies	Solution 1	Solution 2
How was the problem solved? (e.g., visual representation, algebraic equation, table, etc.)		
Which operation(s) were used in each solution?		
Did one of the solution methods rely on a pattern?		

Use the table above to write some ways the two solution methods are similar and/or different. Remember to focus on how the mathematics skills and concepts underlying each strategy are similar or different.

Similar	Different











## Handout 4B.6 (Continued)

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What do I want the students to learn or notice when comparing these solutions?	What probing questions could be posed to elicit this learning?





























## Handout 5B.6 (Continued)

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**10.** \_\_\_\_\_ **T:** So, what I'm thinking is that you had 30 magenta beads and you knew that you needed the nine more so is this where you showed that this was 30 and the 39?

**S:** *Yah*

**11.** \_\_\_\_\_ **T:** Can you think of a way you could have gotten to this solution of 39 beads with the information you got here? (points to 000 box box box, etc.)

**S:** *I could have counted by 10s for this and then I would have gotten to 30 and then I could have just added 9 to it.*

**12.** \_\_\_\_\_ **T:** And if you take a look at the work you did here, you're thinking  $3 \times 3 = 9$  and also the  $3 \times 10 = 30$ , so you would have arrived at 39 by doing what?

**S:** *Adding*

**T:** You've got it very good.





## Handout 5B.8 (Continued)

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4. \_\_\_\_\_ **T:** How did you know not to stop at 2 tricycles?

**S:** *So, 17 is not an even number. It's an odd number so if I would have divided it by 2, it would be a fraction which you really can't have a fraction of a bike, it needs to be a whole bike.*

**T:** That is true.

5. \_\_\_\_\_ **T:** If we were going to extend this kind of pattern you got going, could we get another answer where we still had more bikes than trikes—if we had a least two of each but we had a different answer than this?

**S:** *Yes. We could because if you subtracted 3 from here (points to 14) that would be 12...no 11 and if you take 3 away from 11 that would be 8 and you could do 8 divided by 2 which is four bikes wait...*

6. \_\_\_\_\_ **T:** And how many tricycles would that be?

**S:** *That would be more tricycles so no you could not do that.*

**T:** Great work and high five!



