

Does the usage of an online EFL workbook conform to Benford's law?

Mikołaj Olszewski¹, Kacper Łodzikowski², Jan Zwoliński³,
Rasil Warnakulasooriya⁴, and Adam Black⁵

Abstract. The aim of this paper is to explore if English as a Foreign Language (EFL) learners' usage of an online workbook follows Benford's law, which predicts the frequency of leading digits in numbers describing natural phenomena. According to Benford (1938), one can predict the frequency distribution of leading digits in numbers describing natural datasets, e.g. river lengths. In such numbers, the digit 1 occurs most frequently, while the digit 9 occurs least-frequently. This counter-intuitive phenomenon attracted the attention of researchers seeking inconsistencies in data, e.g. false tax claims (Miller, 2015). We show that the practical application of Benford's law could extend to detecting abnormal learner behaviour in online EFL products. First, we show that the distributions of leading digits of the number of online activities submitted by EFL learners on an e-learning platform and the time spent on those activities do indeed follow Benford's law. Then, we show that some learners whose behaviour does not conform to Benford's law show online behaviour that is abnormal relative to their peers – in particular, they submit many activities in a few days, which could suggest, for example, poor time management.

Keywords: Benford's law, EFL, e-learning, time on task.

1. Introduction

Benford (1938) stated that it is possible to predict the frequency distribution of leading digits in numbers composed of four or more digits describing such natural

1. Pearson IOKI, Poznań, Poland; mikolaj.olszewski@pearson.com

2. Pearson IOKI, Poznań, Poland; kacper.lodzikowski@pearson.com

3. Pearson IOKI, Poznań, Poland; jan.zwoliński@pearson.com

4. Pearson PLC, Boston, United States; rasil.warnakulasooriya@pearson.com

5. Pearson PLC during this research, now at Macmillan Learning, New York City, United States; adam.black@macmillan.com

How to cite this article: Olszewski, M., Łodzikowski, K., Zwoliński, J., Warnakulasooriya, R., & Black, A. (2016). Does the usage of an online EFL workbook conform to Benford's law? In S. Papadima-Sophocleous, L. Bradley, & S. Thoučesny (Eds), *CALL communities and culture – short papers from EUROCALL 2016* (pp. 351-357). Research-publishing.net. <https://doi.org/10.14705/rpnet.2016.eurocall2016.587>

datasets as river lengths or city populations. In such numbers, the digit 1 is expected to be the most frequently occurring leading digit (about 30% of cases), while the digit 9 is expected to occur least-frequently (fewer than about 5% of cases), even though the chance of occurrence is intuitively expected to be the same for all leading digits. In recent years, Benford's law attracted the attention of researchers because of its practical use, e.g. identifying tax or vote frauds (Miller, 2015).

In education, Benford's law has been applied to evaluating the chance of picking the correct answer among distractors on a multiple-choice test (Slepkov, Ironside, & DiBattista, 2015). We know of no previous work exploring the application of Benford's law to e-learning of EFL, hence the present study.

2. Method

2.1. Data

According to Nigrini (2012, pp. 21-22), numbers in a dataset are expected to conform to Benford's law if they describe *natural* events or facts such as city populations (rather than, say, computer-generated bank account numbers) and if the dataset has no inherent limit (which excludes, say, exam scores).

We focused on the number of online learning activities completed by EFL learners and the time spent on those activities. The data comes from MyEnglishLab for Speakout Pre-intermediate 1st edition (henceforth 'MyEnglishLab'), an e-learning platform with exercises accompanying a textbook. The online activities comprise twelve units, each of which contain about thirty activities. The platform is aimed at institutions, so most learners analysed here were enrolled in a course set up by their teacher or instructor. The anonymised dataset contains 3,218,624 first attempts of MyEnglishLab activities from 35,265 learners from 18 different countries (speaking 12 different languages).

2.2. Analysis

To see if the number of MyEnglishLab activities completed by learners conforms to Benford's law, we counted the total number of activities submitted (i.e. attempted) daily by each learner. Days with no learner activity were not included. Resubmitting the same activity did not increase the count. For example: if learner A submits 11 activities on Monday and three activities on Tuesday, and Learner B submits four

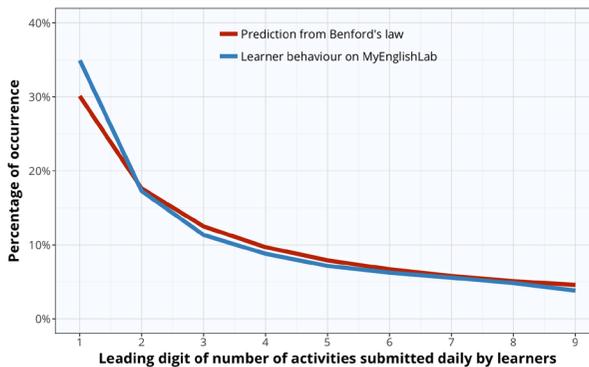
activities on Tuesday and six on Wednesday, the dataset contains the observations {11, 3, 4, 6}. The frequency distribution of the leading digits of these measurements was plotted and compared with the expected trend according to Benford's law.

To see if time spent on those activities conforms to Benford's law, we listed the time (in seconds) that every learner spent on every first submission of a MyEnglishLab activity. Again, the frequency distribution of the leading digits was plotted and compared with Benford's distribution. We ran a Pearson's Chi-squared Goodness-of-Fit test, which is one of several tests used to evaluate if a dataset conforms to Benford's law. Of several such tests available in the BenfordTests R package (Version 1.2.0; Joenssen, 2015), this one was the fastest. Data processing and visualisation were performed in R (Version 3.2.4; R Core Team, 2016) running in RStudio (Version 0.99.893; RStudio, 2016).

3. Discussion

A visual inspection of Figure 1 shows that the distribution of leading digits of the number of activities submitted daily per learner on MyEnglishLab follows the Benford's law curve closely, with the exception of the digit 1. This means there were more cases of learners submitting either one or between 11 and 19 activities per day than predicted by Benford's law. Despite this, it could be stated that the number of submitted activities (roughly) conforms to Benford's law.

Figure 1. Distribution of leading digits of the number of submitted activities compared to Benford's distribution



A visual inspection of Figure 2 shows that the distribution of leading digits of time spent on single activities submitted on MyEnglishLab also closely follows Benford's

distribution. Although the digit 1 is an exception again, the fit is better. A similar result was observed for the first two leading digits of time (not shown in this figure).

Figure 2. Distribution of leading digits of time spent on MyEnglishLab activities compared to Benford's distribution

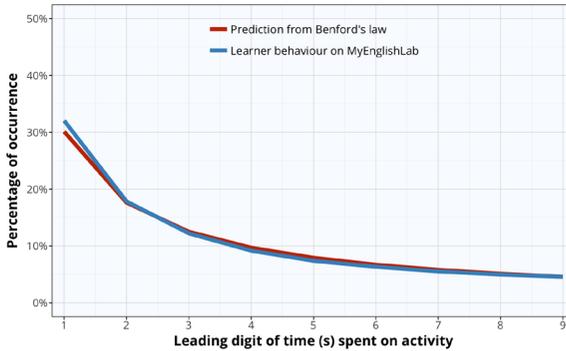
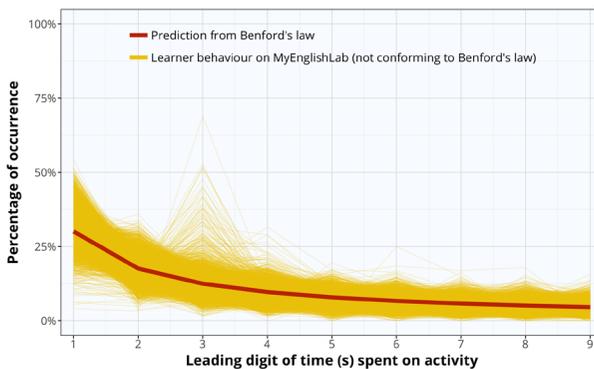


Figure 3 shows learners whose behaviour does not conform to Benford's law. Each thin line represents a learner. Pearson's Chi-squared Goodness-of-Fit test showed that of 12,427 learners who submitted at least 100 MyEnglishLab activities, time on task follows Benford's law for 74% of learners and does not follow Benford's law for 26% of learners ($\alpha = 0.05$).

Figure 3. Distribution of leading digits of time spent on MyEnglishLab activities by learners whose behaviour does not conform to Benford's law

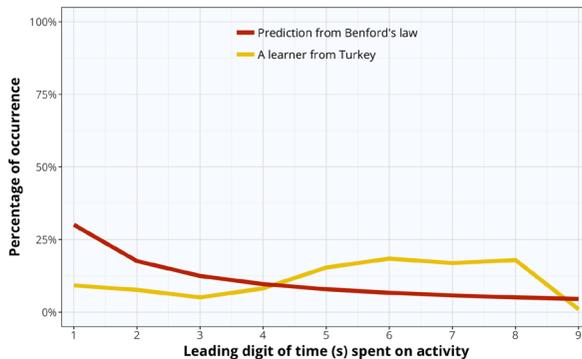


While exploring backend logs of learner interactions with MyEnglishLab, we noticed that some of the 26% of learners whose behaviour does not conform to

Benford's law share three characteristics. First, even if they were enrolled in a course that lasted a couple of months, they used the platform to submit exercises only for a couple of days. Second, on those few days of activity, the learners submitted an unusually high number of activities, often receiving high scores. Third, learners seemed to have worked with these activities simultaneously, i.e. they opened one activity after another in quick succession (probably in separate browser tabs although front-end interactions such as browser focus were not tracked here) and then, after some time, quickly submitted one activity after another. This could be an indication of cramming.

Figure 4 shows an example of one such learner. This learner took part in what seemed to have been an intensive two-month course, judging by the online activity of other participants in that course. While other learners in the course submitted activities relatively frequently, this learner submitted 195 activities on three different days (within a span of 10 days), scoring ~96% per activity, on average. On each such day, the learner opened a number of activities almost at once, spent more time on each following activity, and then submitted them all almost at once. This happened towards the end of the course, so completing online activities might have been a course requirement.

Figure 4. Distribution of leading digits of time spent on MyEnglishLab activities by a learner whose behaviour does not conform to Benford's law



4. Conclusions

We showed that the distributions of leading digits of the number of online activities completed by EFL learners and the time spent on those activities closely

follow Benford's law. The approach used in this paper shows how insights can be revealed in noisy online data, such as the time data, which the standard methods of analysis would not reveal.

Benford's law has been applied for tax fraud detection and our results show that it may also be worth applying it for detection of abnormal learner behaviour. Whereas we do not know if the learners whose behaviour did not conform to Benford's law in this particular study behaved so because of poor time management skills or other factors, Benford's law could help flag such learners to teachers who would then choose the best course of intervention by talking to learners.

Still, our findings are directional and future research should focus on validating such an approach, and its usefulness to teachers. Another strand of research could focus on comparing the computational performance of different tests for evaluating conformity to Benford's law (with operationalising large-scale detection in mind) and comparing this approach to other methods of detection and prediction of learner performance, e.g. those that rely on simpler metrics, such as login frequency.

5. Acknowledgements

We thank Daniel Roe, Category Director of Pearson English, for granting us permission to share the findings broadly. We also thank Claire Masson and the Pearson English MyEnglishLab team.

References

- Benford, F. (1938). The law of anomalous numbers. *Proceedings of the American Philosophical Society*, 78(4), 551-572. <http://www.jstor.org/stable/984802>
- Joenssen, D. W. (2015). *BenfordTests: statistical tests for evaluating conformity to Benford's law* [Computer software]. <http://CRAN.R-project.org/package=BenfordTests>
- Miller, S. J. (Ed.). (2015). *Benford's law: theory and applications*. New Jersey: Princeton University Press. <https://doi.org/10.1515/9781400866595>
- Nigrini, M. J. (2012). *Benford's law: applications for forensic accounting, auditing, and fraud detection*. Hoboken: Wiley. <https://doi.org/10.1002/9781119203094>
- R Core Team. (2016). *The R project for statistical computing* [Computer software]. <https://www.R-project.org>
- RStudio. (2016). *Integrated Development for R* [Computer software]. <http://www.rstudio.com>

Slepkov, A. D., Ironside, K. B., & DiBattista, D. (2015). Benford's law: textbook exercises and multiple-choice testbanks. *PLoS ONE*, *10*(2), 1-13. <https://doi.org/10.1371/journal.pone.0117972>

Published by Research-publishing.net, not-for-profit association
Dublin, Ireland; Voillans, France, info@research-publishing.net

© 2016 by Editors (collective work)
© 2016 by Authors (individual work)

CALL communities and culture – short papers from EUROCALL 2016
Edited by Salomi Papadima-Sophocleous, Linda Bradley, and Sylvie Thouéšny

Rights: All articles in this collection are published under the Attribution-NonCommercial -NoDerivatives 4.0 International (CC BY-NC-ND 4.0) licence. Under this licence, the contents are freely available online as PDF files (<https://doi.org/10.14705/rpnet.2016.EUROCALL2016.9781908416445>) for anybody to read, download, copy, and redistribute provided that the author(s), editorial team, and publisher are properly cited. Commercial use and derivative works are, however, not permitted.



Disclaimer: Research-publishing.net does not take any responsibility for the content of the pages written by the authors of this book. The authors have recognised that the work described was not published before, or that it is not under consideration for publication elsewhere. While the information in this book are believed to be true and accurate on the date of its going to press, neither the editorial team, nor the publisher can accept any legal responsibility for any errors or omissions that may be made. The publisher makes no warranty, expressed or implied, with respect to the material contained herein. While Research-publishing.net is committed to publishing works of integrity, the words are the authors' alone.

Trademark notice: product or corporate names may be trademarks or registered trademarks, and are used only for identification and explanation without intent to infringe.

Copyrighted material: every effort has been made by the editorial team to trace copyright holders and to obtain their permission for the use of copyrighted material in this book. In the event of errors or omissions, please notify the publisher of any corrections that will need to be incorporated in future editions of this book.

Typeset by Research-publishing.net
Cover design by © Easy Conferences, info@easyconferences.eu, www.easyconferences.eu
Cover layout by © Raphaël Savina (raphael@savina.net)
Photo "bridge" on cover by © Andriy Markov/Shutterstock
Photo "frog" on cover by © Fany Savina (fany.savina@gmail.com)
Fonts used are licensed under a SIL Open Font License

ISBN13: 978-1-908416-43-8 (Paperback - Print on demand, black and white)
Print on demand technology is a high-quality, innovative and ecological printing method; with which the book is never 'out of stock' or 'out of print'.

ISBN13: 978-1-908416-44-5 (Ebook, PDF, colour)
ISBN13: 978-1-908416-45-2 (Ebook, EPUB, colour)

Legal deposit, Ireland: The National Library of Ireland, The Library of Trinity College, The Library of the University of Limerick, The Library of Dublin City University, The Library of NUI Cork, The Library of NUI Maynooth, The Library of University College Dublin, The Library of NUI Galway.

Legal deposit, United Kingdom: The British Library.
British Library Cataloguing-in-Publication Data.
A cataloguing record for this book is available from the British Library.

Legal deposit, France: Bibliothèque Nationale de France - Dépôt légal: décembre 2016.