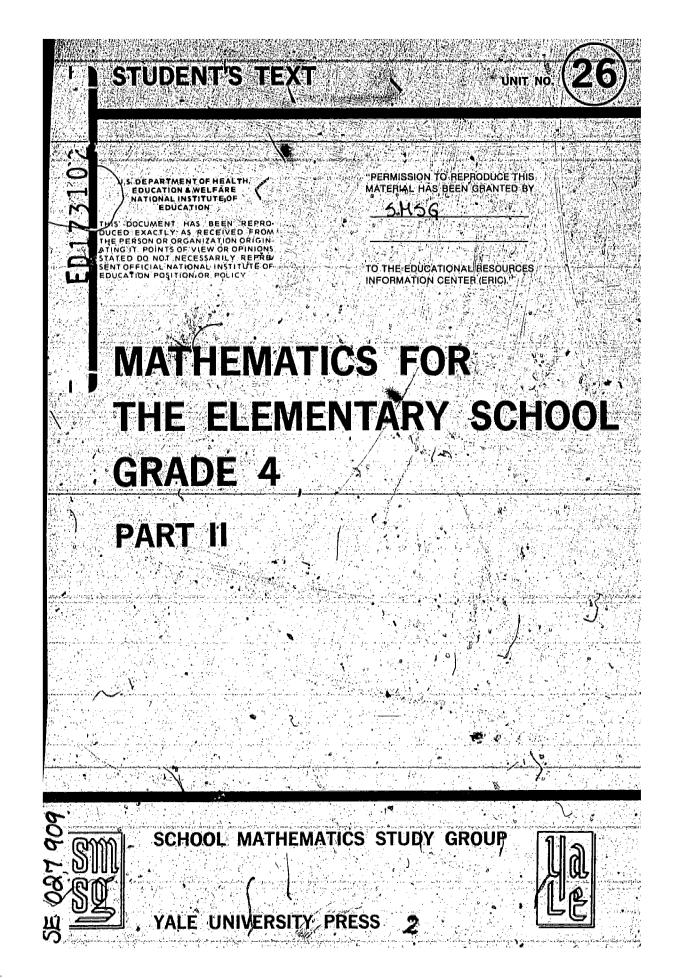
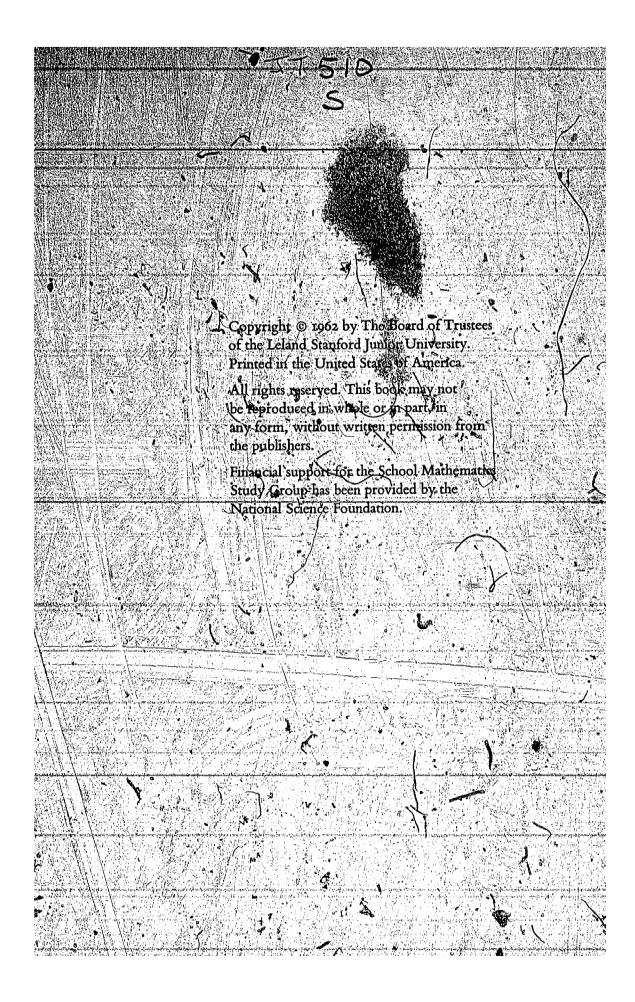
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Leslie Bearty	Chula Vista City School District, Chula Vista, California
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chapter 6 EROPERTIES AND TECHNIQUES OF ADDITION AND SUBTRACTION II IOPRIERENTENAMES TOREWIE SAME NUMBER There are many ways of naming a number. The decimal numeral for 40 + 2 is 42. It may also be named in other ways. Nan sales that all the names below are for the same number Do you agree? 27 - 3; 24 + 0; 10 + 14; 25 - 1; 2 tens and 4; 1 ten and 14. What is the decimal numeral for 40 + 15? State five other names for 40 + 15. (a) Is $234 = 200 + 30 + 4^{\circ}$ (c), Is $234 = 200 + 20 + 14^{\circ}$ Is 234;= 200 + 10 + 247; (d) Is 234 = 100 + 130 + 47 You may think of 67 as 6 tens and 7 ones or as 5 tens and 17 ones. What are other names for 67? May we think of 726 as 700 + 20 + 6? as 700 + 10 + 16? as 600 + 120 + 6? Different names for a number 34 as 3 tens and 4 ones are often shown on an abacus. How is 34 named on each abacus at the right? 5. Tell two different names for each of these numbers. Show each on the abacus. (a) 46 (b) 97 and 14 ones

Copy the numerals 1 - 10. on your paper. Next to each write the correct answers to complete this chart.

Decimal Numeral"

Another Name for the Number

	的。 第一个时间,他就是一个一个一个一个一个一个一个一个一个一个一个一个一个一个一个一个一个一个一个	
	1	. 120 + 17
	2 	1200 + 160 + 18
		6 tens + 18
	5 96	4 hundreds + 15 tens + 8
	7 238 8 49	15 hundreds + 23 fens + 19
area ana	10 1,526	

For each of exercises 11 - 13 write > or < so each mathematical sentence will be true. In exercise 11, is 1000 + 300 + 60 + 16 another name for 1376?

11. 1,378 1000 + 300 + 60 + 16

12. 2,874 1 thousand + 17 hundreds + 16 tens + 4 ones

13. 4,926 3 thousands + 18 hundreds + 11 tens + 6 ones

- 2. The salesman traveled 230 miles in March, 310 miles in April, and 345 miles in May. How many miles did he travel in the three months?
- 3. From January through June the salesman traveled 2;010 miles.

 From July through December he traveled 1,854 miles. How
 far did he travel during the year?
- 4. You found how far the salesman traveled in one year in exercise 3. During another year he traveled 4,013, miles

 What was his mileage during the two years?
- 5. On an automobile trip, Fred and Carol played a game by counting station wagons and trucks they saw on the highway.

 Fred counted 234 station wagons and Carol counted 205

 trucks. How many station wagons and trucks did they count
 in all?
- 6. Jack and Tim have been gathering rocks for the new walk their father is making. Jack has gathered 172 rocks and Tim has gathered 213. How many rocks have the two boys gathered altogether?



MORE ADDITION What number is n if 423 + 345 + 214 First, place beads on the abacus to show 400 + 20 + 移 the addends so that each addend is 300 + 40 + 5 200 + 10 4 4 separated from the others. Next, show the result of adding the ones, 400 + 20 + 3 Show the result of adding the tens. 300 + 40 + 5 200 + 10 + 4 Show the result of adding the 900 + 70 + 12 hundreds. Now 423 + 345 + 214 = 900 + 70 + 12. 900 + 70 + 12 is thought of as 900 + 70 + (10 + 2). 900 + 70 + (10 + 2) = 900 + (70 + 10) + 2.What is the decimal numeral for 900 + 80 + 2? Now try to add 342, 124 and 418 without the abacus. 342 = 300 + 40 + 2See Box A. 124 = 100 + 20 + 4 418 = 400 + 10 + 8What numbers were added 800 + 70 + 14 = 884first? b. What decimal numeral is.

3. Find n if 375 + 278 = n. You might try the method on

page 306 In Box B, the decimal

numeral 653 was obtained

from adding 500, 140, and 13.

375 = 300 + 70 + 5 278 = 200 + 70 + 8500 + 140 + 13 = 653

Ъ٠

375

4:/ Sometimes 375 and 278 are.

added as in box)C:

What numbers were added

Sto get 13? How do you get the 140? How do you

get 500? How is the

653 obtained? The method of Box C may be more convenient for you.

- 1. Use the method of Box. B to find each sum.
 - 43
- 167
- 346
- 558
- 1287

- 29
- <u>254</u>
- <u>186</u>
- <u>645</u>
- 3648
- 2. Use the method of Box C to find each sum.
 - 429
- 697
- 1278
- 8296
- 6278

- 41<u>93</u>

ANOTHER METHOD FOR ADDING

Addition is an operation on two numbers. When we operate on 15 and 3 and get 18, we have added. (15 + 3 = 18) Eighteen is called the sum. Fifteen and 3 are called addends.

An addition exercise is written in columns to make it easy to add.

Columns help to keep the ones together, the tens together, the hundreds together, and so on.

In column addition the ones are added first, the tens next, the hundreds next, and so on.

Part of the sum of the ones' column is sometimes remembered. It is then added in with the tens.

Part of the sum of the tens! column is sometimes remembered. It is then added in with the hundreds.

329 146 948

To add I think: 9 and 6 are 15 and 15 and 8 are 23. Think of 23 as 2 tens and 3 ones. Record 3 and remember 2 tens.

Two tens and 2 tens are
4 tens; 4 tens and 4 tens
are 8 tens; and 8 tens and
4 tens are 12 tens. Think
of 12 tens as 1 hundred and
2 tens. Record 2 tens and
remember 1 hundred.

One hundred and 3 hundreds are 4 hundreds; 4 hundreds and 1 hundred are 5 hundreds and 9 hundreds are 14 hundreds.

Record 14 hundreds.



	Find the	e stams	for exercises	1 thr	ough 5.	4	Ž
1.	(a)	(́b)	(c)	(d)	(e)	(f)	
	43	57 °	19	76	. 68	53 17	nativitation and or successive
Alexandra (<u>29</u>	<u>38</u>	<u>46</u>	<u>15</u>	<u>28</u>		
2.	126 <u>246</u>	348 <u>629</u>	167 <u>726</u>	239 <u>43</u>	468 504	2 82 509	est,
	<u></u> 563	 635	447	 563	. 	647	· · · · · · · · · · · · · · · · · · ·
	128	<u>406</u>	129	129	<u>257</u>	39	
4.	17₩	88	489	179	266	593	
	<u>138</u>	<u>543</u>	272	<u>658</u>	<u>698</u>	<u>248</u>	
5.	347	256	1591	1876	8976	1762	1
	897 304	1297 540	8643 9275	7235 8544	1235 7142	4391 3065	
		<u>698</u>	<u>5873</u>	<u>6718</u>	6473	<u>8572</u> .	

- Find n for each of exercises (a) through (d).
- (a) n = 697 + 384
- (c) n 559 = 2476 (d) 362 = n 875

- 1. List the number of days in each of the first six months of this year. How many days are there in the first six months of this year?
- 2. List the number of days in each of the last six months of this year. How many days are there in the last six months of this year?
- 3. John went to a book store. He found 5 magazines which he wanted. Their prices were 75¢, 20¢, 25¢, 55¢, and 95¢. He bought the three which were cheapest. How much did they cost?
- 4. There were 135 books borrowed from the library on Monday, 140 books on Tuesday, 168 books on Wednesday, 174 books on Thursday, and 147 books on Friday. During these five days, how many books were borrowed?
- The Jackson family took a trip by_car from New York City
 to Boston. The trip took five hours. This is how far
 they traveled each hour: 36 miles, 44 miles, 47 miles,
 41 miles, and 38 miles. How many miles did they travel
 in the five hours?





- 6. John s mother bought him a new coat, cap, shoes, and boots. The cost of the coat was \$18, the cap \$3, the shoes \$8, and the boots \$6. How much did she pay for them all?
- 7. There are 65,761 Indians in Arizona, 53,769 Indians in Oklahoma, and 41,901 Indians in New Mexico. How many Indians live in these three states?
- 8. There are 629 boys and 587 girls in Longfellow School.

 How many children attend Longfellow School?
- 9. In 1940 there were, 172,172 people in Miami, Florida.

 In 1950 there were 87,063 more people living there than
 in 1940. How many people lived in Miami in 1950?
- During a candy sale Mary sold 232 boxes of mints. Sue sold 472 boxes, and Jane sold 143 boxes. Find the total number of boxes sold by the three girls.
- The pupils of Oak School collected gifts for poor children at Christmas. They collected 433 books, 316 toys, 252 games, and 164 puzzles. How many gifts were collected in all?



Copy the numerals 1 through 8 on your paper. Next to each numeral write the words and numerals to complete this

Numbers \ Result Operation -Operated On Used

1. 15, 289 addition
2. 139, 76 215 addition

3. n addition $\frac{674 + 879 = n}{674 + 879}$

Mathematical

Sentence

5. 641, (379+81) addition

6. 162, 69 addition

7. 345, 1877 532 8. 647, 387 addition

Write = or \neq so each of exercises 9 through 15 will be true mathematical sentences.

9. 372 + 499 ____ 773

10. 312 + 184 _____ 128

11. 346 + n = 179, if n = 177

12. n + 156 394, if n = 328

13. n - 341 159, if n = 500

14. If n = 379, then n + 172 _____ 308 + 233

15. If jn = 473, jn = 473

REVIEW OF SUBTRACTION

<u>Exercise</u> <u>Set 7</u>

- 1. George had 524 for the answer to an exercise. It should have been 639. How much too small was his answer?
- 2. The zoo keeper told Jim that the big gorilla weighed 572 pounds, and the small one weighed 361 pounds. How much more does the large gorilla weigh?
- 3. In 1950, the population of a city was 6,478. By 1960, it had increased to 9,699. What was the increase in population during the ten-year period?
- 4. The Boy Scouts had a paper drive: Troop 51 collected 8,200 pounds of paper. They wanted to collect 9,600 pounds. How many more pounds of paper do they need to collect?
- 5. Subtract

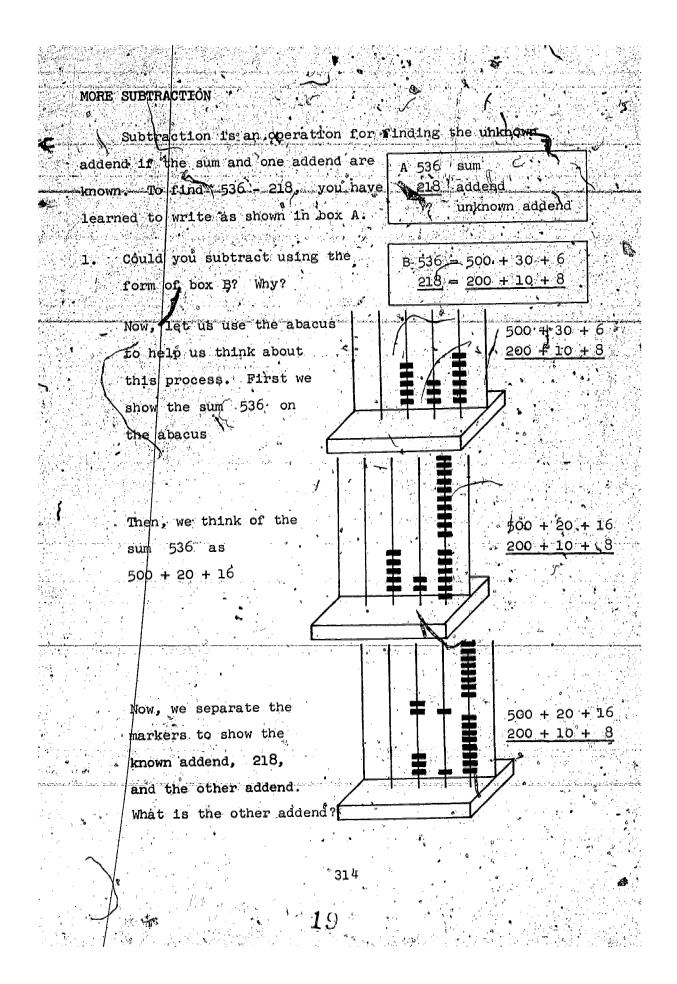
6. Find n so each mathematical sentence will be true.

(a)
$$n + 395 = 697$$

(c)
$$863 + n = 1175$$

$$(b)$$
 $n = 1158 - 737$

(d)
$$2378 - 2163 = n$$



The written record of the above subtraction is

$$\frac{218}{9} = \frac{200}{10} + 10 + 8 = \frac{200}{10} + 8$$

Sometimes, finding the unknown addend is more difficult.

For example, what is
$$n$$
, if $2687 + n$ = .932?

We may write:

$$268 = 200 + 60 + 8 = 200 + 60 + 8 = 200 + 60 + 8$$

. Explain how we may think when subtracting in this way.

What is the other addend?

Now let us look for a shorter way of writing the steps in a subtraction problem. Notice how this form corresponds to the one above. We begin with 932 9 hundreds, 3 tens, 2 ones - 268 2 hundreds, 6 tens, 8 ones.

We cannot subtract in the ones column so we regroup

9 \ 9 hundreds, 2 tens, 12 ones

We cannot subtract in the tens! column so we regroup again

8 hundreds, 12 tens, 12 ones

$$12 - 8 = 4$$
, 4 ones

$$12 - 6 = 6$$
, 6 tens

ANOTHER METHOD FOR SUBTRACTING

Subtraction is an operation on numbers. When we operate on 15 and 3 and get 12, we have subtracted. 15 - 3 = 12. And, 12 is called the unknown addend.

A subtraction exercise is written in columns to make subtraction easy. Columns help to keep the ones together, the tens together, etc.

In column subtraction the ones are subtracted first, the tens next, etc.

Renaming the sum in a subtraction exercise may help us to subtract.

5576 - <u>1</u>328

To subtract I think:

There are not enough ones in the ones place in 5,576.

I will think of 5,576 as

5 thousands, 5 hundreds,

6 tens, and 16 ones.

16 - 8 = 8. 6 - 2. = 4.

5 - 3 = 2. 5 - 1 = 4. The unknown addend is 4,248.

Exercise Set 8

Find the unknown addend in each of 1 and 2.

1. (a)	(b)	(c)	(d)	(e)
93	187	817	852	598
3 <u>38</u>	99	<u>748</u>	<u>575</u>	<u>378</u>
Continue to the property of				
2. 5634	2876	8421	3124	5672
.1256	259	5167	<u> 2674</u>	148 <u>9</u>



- 1. One week a factory assembled 2,640 trucks and 1,582 automobiles. How many more trucks than automobiles were
- 2. In 1950 there were 3,500 people in Woodside. In 1960 there were 9,400 people in Woodside. How many more people were there in 1960 than in 1950?
- 3. We planned a 455 Mile trip. The first day we traveled 266 miles. How many miles were left to travel?
- 4. The Mississippi River is 2,348 miles long and the Ohio River is 981 miles long. How many miles longer is the Mississippi River?
- 5. What is the total length of the Mississippi and the Ohio
- 6. In New York City, the Empire State Building is 1,472 feet high. The Chrysler Building is 1,046 feet high. How much higher is the Empire State Building?

317

- 7. There were 435 children at Whittier School and 379 children at Edison School. How many children attend both schools?
- 8. A sign on a foot bridge reads, "Not safe for over 200 pounds." Jerry weighs 62 pounds, Dick weighs 57 pounds, Tom weighs 68 pounds. Can the three boys safely walk across the bridge together?
- Another bridge holds two tons safely. A cement truck that weighs 2,165 pounds is on the bridge. How many more pounds could safely be on the bridge at the same time?
- 10. Susan's grandmother was born in 1908. How old will she be on her birthday this year?

SUBTRACTION WITH ZEROS

- Which of these are other names for 8,000?
- (a) 8,000 ones (d) 7,000 + 1,000 (g) 8 thousands
 - (b) 8021 .21
- (e) 800 hundreds (n) 8,000 0

- (c) 800 tens.
- (f) 10,000 2,000
- 2. CSuppose you are to find n when 8,000 - 1,732 = n. You can write the example as in Box A. Finding the 🔩 unknown addend is easy if you rename 8,000 as 799 tens and 10 ones or 7990 + 10.
- Α 8000
- (a) Look at the example given in Box B.
 - (b) Tell how to get the unknown addend, 6260 + 8.
 - (c) What decimal numeral names the unknown addend?
- 8000 = 7990 + 101732 = 1730 +6260 +

Exercise Set 10

Find the unknown addend for each of these.

(a)

(b).

(c)

804

602

- 102
- 3001

267

536

- 85
- 1467

6000

- 4803



- 1. John is 52 inches tall; his father is 70 inches tall.

 How many inches must John grow to be as tall as his father?
- At Glenn School there are 500 boys and 375 girls. How many more boys are there than girls?
- 3. Don has 1,500 stamps. He pasted 323 in his album.

 How many are left to put in the album?
- 4. Sue has \$25. She is saving to buy a bicycle which costs \$42. How much more money must she save?
- 5. A high school stadium has 5,200 seats. 3,482 tickets have been sold for a game. How many tickets are left?
 - 6. An elephant in a zoo weighs 5,000 pounds. A bear weighs 746 pounds. How much less does the bear weigh than the elephant?
- 7. West Virginia became a state in 1863. Hawaii became a state in 1960. How many more years has West Virginia been a state than Hawaii?



RELATION OF THE TECHNIQUES OF ADDITION AND SUBTRACTION

Exercise Set 12

Copy the chart below. Add or subtract each exercise and then undo each.

	<u> </u>
, Do	Undo
1. Add 725 , <u>342</u>	1.
2. Subtract 1629 817	2.
3. Subtract 5232 768	3.
4. Add 5287 9388	.4.
5. Add 26534 12986	5•

6. Show that each of these mathematical sentences about doing and undoing is true. The first one is done for you as an example.

(b)
$$(841 + 368) - 368 = 841$$

(e)
$$(384 + 769) - 769 = 384$$

7. Column addition may be checked by using the commutative and associative properties of addition. In this example, first "add from the top down." Then "add from the bottom up." Are the sums the same? Add: 43 32 57	Maria (Ida Maria Antana Maria (Ida Maria Antana Maria (Ida Maria Antana Maria (Ida Maria Antana)		el Chipron por entre in requestro description	e podrukania stanje v podruka povenica ne v podruka povenica i podruka sa povenica i konsuperana podruka. Podruka si se podruka sa podruka		
first "add from the top down." Then "add from the bottom up." Are the sums the same? Add: 32 57 Add and check the sums in each of the following exercises: 8. 72	which desired later	.Column additic	on may be	checked by using	the commu	tative
#3 32 57. Add and check the sums in each of the following exercises: 8. 72 324 3286 17208 19 964 9246 15363 36 322 3078 42630 42 508 5000 88 12. 13, 14, 15, 15, 1492 687 15618 61429 3876 941 29832 78503 9547 600 75490 59268 3841 817 61078 68107 2056 932 70201 91030 16. ERAINTWISTER: Try to find the sum for exercise 8 by adding down the column once.		and associativ	/e propert	les of addition.	In this	example,
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Copy the numerals 1 through 7 on your paper. correct words or numerals to complete this chart.

	Numbers ? Operated On	Result	Operation _©	Mathematical Sentence
1.	394, 869		addition	
2.	and a second of the second A second of the		a kanana sana di jangan pengangan kanana sana pengangan kanana sana pengangan pengangan pengangan pengangan p Pengangan pengangan	762 = 575
3.	1498,	1-277	addition	
Manage Har	_(297_+_356),495	erikan andara ingga kanala anga kanala	subtraction .	
5.	2000, (156 + 354)		subtraction	er og en fra til en en goderne skriver, i der en delet fra til en de de en en en en en en en en en de de de en en en en en en en en en en de en
6.	(392 + 867), 201		subtraction	
. 7.				384 + 979' =
	Control of the second of the s			

In exercises 8 to 16, what is n so each mathematical sentence will be true?

8.
$$n = 67 + 48$$
 9. $n = 204 - 157$ 10. $n = 4000 - 1963$

10.
$$n = 4000 - 1963$$

11.
$$n + 42 = 89$$

12.
$$102 - n = 3$$

13.
$$n - 128 = 568$$

14.
$$n + 392 = 691$$

15.
$$\sqrt{601 - n} = 39$$

6.
$$893 - n = 256$$



C; D and E are to be replaced by one of the digits 0, 1, 2, 3, 4, 5, 6, 7, 8 or 9. They may be replaced by different digits in different exercises: A symbol such						
	g hair, and a facility on the \$1 to \$5. Petrony (Ay Ababa).		2-place numer	ali de la companya d		
	- 14	63 <u>- A</u> B8	47 <u>+ D</u> CC	DD <u>+ E</u> 80	- cč <u>+ c</u> 60	
	ABC <u>- 42</u> 153	Е4 <u>+ 30</u> -87./	1988 - 182 - 14	7A <u>- 入B</u> 14・	CD + D3 79	
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					A. A	
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THE LANGUAGE OF SUBTRACTION PROBLEMS

- 1. Family A traveled 323 miles and family B traveled.

 289 miles on a weekend trip. How many more miles did

 family A travel than family B?
- 2. Family A traveled 323 miles and family B traveled 289 miles on a weekend trip. How far did the two families travel?
- 3. Family A traveled 323 miles and family B traveled 289 miles on a weekend trip. How much farther would family B have to travel in order to travel as far as family A?
- 4. Families A and B are together on a trip of 323 miles.

 They have traveled 289 miles. How many miles do they have left to travel?

- 1. A notebook costs 15¢, a pencil 27¢, and an eraser 5¢.

 How much will it cost to buy a set of one of each?
- 2. Four children put their savings together to help buy a riding horse. Mary had \$35, Jerry had \$48, Diane had \$123, and Frank had \$97. How much money did the four children have?





- 3. A football playing field is 300 feet long and 160 feet wide. How far will you have walked if you walk along the four edges of the field?
- 4. John has 268 postage stamps. He received some for Christmas. Then he had 323. How many stamps did he receive for Christmas?
- 5. At Fairview, the temperature was 58° at moon and 23° at midnight. How much had the temperature changed?
- 6. Tom wanted to buy a radio which was priced at \$72. He had \$56 saved. How much did he still have to save?
- 7. On a page in a catalog the following prices were given:

 soft ball, \$1; bat, \$5; fielder's mitt, \$3; catcher's

 mitt, \$12; first baseman's mitt, \$9; catcher's mask,

 \$4; and baseball uniform, \$6. What will it cost

 Mr. Thompson to buy a ball, a bat, and three uniforms

 for his sons?
- 8. In one year the Acme Motor Company made 969,732

 automobiles, 95,060 trucks, and 17,747 motor scooters.

 Find the number of vehicles made by the Acme Motor Company
 in that year.

IF-THEN THENKING We often use "If-then" reasoning. For example, you may think: "II- Frun-home, then I will get there quicker." or "<u>Fr</u>it rains, then we cannot play baseball." In our 1f-then statements we want the second part to be true because of the first part. We use "if-then" thinking when we reason: "If "7 + n = 15, then n + 7 = 15" or "lf 7 + n = 15, then n = 8". --- We-would not think "If 3 + 6 = 9, then 3 + 6 = 10, since the "then part is not a result of the "if" part. -We-could think, "If 3 + 6 = 9, then 3 + 7 = 10." Complete this statement in other ways, If 3 + 6 = 9, 4. (a) Is it true that "If n + 6 = 15, then n = 15 - 6"? (b) Is it true that "If n - 6 = 10, then n = 10 + 6"?

	<u>Exercise Set 15</u>
Agricultural de la company Special de la company Street de la company	. Complete these statements. Use some different ways to
All the second s	complete each as you can.
Appendix and the second	(a) If $15-9=n$, then (d) If $11+n=25$, then
The second secon	(b) = If 13 + n = 21, then (e) If $12 + n = 19$, then
	(c) If $33 = 17 + n$, then (f) If $n - 15 = 14$, then
political production and the control of the control	Appropriet to the second secon
2.	Use =, > or < so each of these statements will be true:
	$(a) \mathbf{L} \mathbf{n} + 6 = 17, \text{then} \mathbf{n} = 17.$
6	(b) If $2\hat{i} - n = 19$, then $n _{n} 21$?
manufacture (1) and the second	(c) If = n+27, then n 44.
	(d) If $n - 16 = 31$, then $n = 16$.
	(e) If n + n = 40, then n 40.
	(f) If $n + 0 = 178$, then $n _{} 178$.
A STATE OF THE STA	(g) If $0 - n = 0$, then $n = 0$.
PARTIES ENGLISHED TO THE PARTIES OF	(n) If $(6 \mp 8) + n = 19$, then $n = 19$.
Sparite Maria or processors that a second a few or a set that	
**************************************	BRAINTWISTER. Remember: x, y, and z represent whole
	numbers. Suppose $x + y = z$.
Part of the Control o	(a) Are you sure that $x < z$ and $y \le z$?
	(b) Give an example for x = z
	(c) Give an example for $x < z$.
5 (2) Att phin sein – de to €, et o ou, en	(d) Give one example for $x < z$ and $y < z$.
e Principal and the second	(e) could x > z?
And processing the March Street Street	328
م سيود الراق البادل المراجع	
Part And Annual Control of the Contr	after an teach between the complete to the complete of the complete of the complete of the complete of the comp The complete of the complete o

The arrangement of numbers in the square at the right is called a magic square:

6		10.7	
D	4	3	.8
R	_وــ	<u>-5</u> =	
55.4	3		127-93
F'	2	7	6

- 1. What is the sum of the numbers in column A? in column B?
- 2. What is the sum of the numbers in row D? row E? row F?
- 3. The 4, 5, and 6 are said to be on a diagonal. What is their sum? What three other numerals are on a diagonal?

 What is their sum?
- 4. Are all eight sums the same? The square is said to be "magic" because the sums of all rows, columns, and diagonals are equal.
- 5. Make a new square by adding 19 to each number in the above square. What is the sum of the numbers in: each row?

 each column? each diagonal? Is the new square a magic square?
- 6. Is the square on the right a magic square? What is the sum of the number's on each row, column, and diagonal?

71	57	58	68
60	66	65	63
64	62	61	67
-59-	69	_7o_	56_

7. Make a new square by subtracting 49 from each number in the square in exercise 6. Is it a magic square?

REVIEW

Exercise Set 17

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	4.7	215		8	4	111	5		All be		4:1	T	2	6				47		10	P. 11.	5	3 C	2	190	67.4		aid.			Լተ	41	11.3		100		10		4.14	v.		3	Ţ
721	1.00	100		=1	17	11.7	115	14.5	21.1	$I^{*} \leftarrow \iota$	1341		133	41611	100		4.3	3-1		10	100	15. 16	Ť., :	7		7.77		1.11	F 111		1 110		400		rafty.		100	F.5. **	2 E (13.7	1	1,000	100	20
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Find n so each mathematical sentence will be true.

(a)
$$81 = 46 = n$$
 (c) $n + 126 = 253$ (e) $359 - n = 284$

(b)
$$n = 76 + 49$$
 (d) $n - 87 = 123$ (f) $283 + n = 481$

(a)
$$81 + 69 = 160$$

(b)
$$124 + 238 = 362$$

- BRAINTWISTER. What whole number, if any, can be used for
 - n so each mathematical sentence will be true?
 - (a) 192 + n = 168
- (e) n = 12 = 26
- (b):/-192 + n = 268 ----
- (f) 12 n = 26
- (c) 312 n = 314 (g) 26 21 = n
- (d) 312 n = 310 (h) 21 26 = n

BRAINTWISTER.

- (a) The two numbers you operate on are n and n. The operation you use is addition. The result is 200. What number is n?
- (b) Follow the directions of exercise (a) but replace 200 with 582.
- 8. ERAINTWISTER. What is wrong with this problem? The two numbers you operate on are n and n. The operation you use is subtraction. The result is 10. What number is n?
- 9. BRAINTWISTER. Two numbers operated on are n and 376. The result is 593. Write two true mathematical sentences using n, 376, and 593. In each mathematical sentence n will be a different number.
- 10. BRAINTWISTER. Two numbers operated on are n and 376. The result is 89. Can you write one or two true mathematical sentences using n, 376; and 89? Why?

- 1. Ammodel plane costs \$2.15. Joe had some money and then

 he earned \$1.58. Then he had exactly enough to buy the

 plane; How much did he have before earning \$1.58?
- 2. The fourth grade class collected 287 more pounds of old newspapers than the fifth grade class. The fourth grade class collected 512 pounds. How much did the fifth grade collect?
- 721 is the largest 3 digit number that can be written using each of the digits 7, 2, and 1. What is the smallest number that can be so written? What must be added to the smaller number to get the larger?
- 4. Mary went to the store to buy one loaf of bread and one dozen eggs. Bread is 29¢ a loss and eggs 65¢ a dozen using only the above information which of these questions can you answer?
 - (a) What is the cost of Mary's purchases?
 - (b) How much in all did Mary pay for bread?
 - (c) How much change did she bring home?
 - (d) If she gave the clerk a \$5 bill, how much change did she receive?

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- 5. The East School had a newspaper and magazine drive. Room

 A collected 1,546 pounds, Room B collected 2,875

 pounds, and Room C collected 5,324 pounds. How many

 pounds of paper did these three rooms collect in all?
- 6. BRAINTWISTER. Use the numbers 2, 3, 4, 5, 6, 7, 8, 9

 and 10 to make a magic square. Hint: the sum of each

 row, column, and diagonal is 18.
- 7. BRAINTWISTER. (a) What number is n if (6 n) + 4 = (6 + n) 4
 - (b) How many counting numbers are there between 194 and 275?
- 8. BRAINTWISTER. Each mathematical sentence below is true.

 In which is n not a whole number?

$$(a) n - n = n$$

(6)
$$(3 + 2) + 2 = n$$

(d)
$$(3 + 2) + n = 2$$

9. BRAINTWISTER. Find n so each mathematical sentence is true.

(d)
$$n < 12$$
 and $n > 10$

Exercise Set 19.

At Jordon school, the cafeteria served lunch to:

Act of the Street and	9-51-10-6 (4-6)	Above the back to	
∵195 o	hildnan	On Mo	MOD W.
エフフ	*******	, 4 11.1114	

218 children on Tuesday

198 children on Wednesday

203 children on Thursday

194 ohildren on Friday

Use the above information to solve problems 1-8.

- . How many children were served lunch during the week?
- 2. How many more than 1,000 lunches were served during the
- 3. Find the two days on which the most lunches were served.

 The total number of lunches for these two days was how many less than 500?
- The total number of lunches served the first three days of the week is how many more than the number served the last two days of the week?

The mathematical sentences in exercises 5 through 8 answer what questions about the number of lunches served?

5.
$$\frac{195}{195} + n = 218$$

$$x = 198 + 19^{4}$$

"The prices of some card games are: Old Maid 26g; Hearts 192, Play Your Hunch 176, and Rummy, 24g. Which of the mathematical

sentences in the box can be

used to answer exercises 9=

through 11?

(c)
$$(24 + 19) + 26 = n$$

(d)
$$n = (19 + 24) = .26$$

 $(f) \cdot (24 + 19) - n = 26$

Play Your Hunch and Hearts?"

The mathematical sentences in exercises 12 through 17 answer what questions about the cost of the card games?

15.
$$n + 26 = 19$$

17.
$$17 + n = 2$$

Meaning of Operation

You have been studying addition and subtraction, two of the operations of mathematics. They are operations on two numbers. The symbols that indicate these operations are + and -. Now we are going to "make up" some operations. They are "make-believe" operations and are not found in mathematics books. They have been invented to see if you can discover their meaning.

One make-believe operation is named "circ." The symbol to indicate circ is ① . 2 ① 4 is read, "Two circ four." Circ means add 3 to the first number and then subtract the second number from that sum. Thus 2 \bigcirc 4 = 1. Find n for each of these.

- (b) $8 \odot 1 = n$
- (d) $4 \odot 4 = n$ (f) $9 \odot 2 = n$

Another make-believe operation is named, "bow." The symbol to indicate bow is T . 3 T 4 is read, "Three bow four." Bow means choose the smaller number. Thus

8 T 5 = 5. Find n for each of these.

- (d) 9 T 10 = n

Another operation is named, "wob." The symbol to indicate wob is 1 . 3 1 4 is read "Three wob four." Here are some results of the operation, wob, on two numbers. Try to find the meaning of wob. .

(a)
$$4 \cdot 1 \cdot 6 = 6$$
 (c) $8 \cdot 1 \cdot 1 = 8$ (e)

(b) 8
$$\pm$$
 0 = 8 (d) 2 \pm 6 = 6

(d)
$$2 L_{x}6 = 6$$

(f)
$$7 \stackrel{\checkmark}{\mathbf{L}} 7 = 7$$

Find n for each of the following:

(g)
$$5 1 6 = n$$

$$(1)$$
, $7 \perp 10 = n$

(k)
$$2 \perp 0 = n$$

(h)
$$1 + 9 = r$$

(j)
$$6 1 8 = n$$

(1)
$$9 \perp 2 = n$$

The symbol ** is to be a sign of operation. 3 * 4 you to operate on 3 and 40 in a certain way. It is read, "Three star four." Here are some results of the operation, star, on two numbers. Try to find the meaning of star.

(a)
$$3 * 4 = 8$$

(c)
$$2 * 6 = 9$$

(e)
$$1 * 1 = 3$$

(d)
$$3 * 7 = 11$$

(f)
$$5 * 4 = 10$$

Find n for each of the following:

$$(1)$$
 3 * 6 = n

$$(k) 1 * 0 = n$$

$$(h) - 8 * 7 = n$$

$$(1) 5 * 9 = n$$

(1)
$$1 * 6 = r$$

5. Another operation is called, "pick." The symbol for pick is . Try to find the meaning of . from these examples.

- (a) 3 15 = 4 (c) 2 14 = 3 (e) 7 15 = 6

6. Another operation is called, "alpha." The symbol for alpha is $\mathcal{L}_{m{a}}$. It is an operation on one number. Try to find the meaning of & from these examples. "

- (a) $\mathcal{L} \ 3 = 6$ (b) $\mathcal{L} \ 0 = 0$ (c) $\mathcal{L} \ 5 = 10$ (d) $\mathcal{L} \ 8 = 16$

What is n in each of the following?

- (e) $\mathcal{L} = n$ (f) $\mathcal{L} = n$ (g) $\mathcal{L} = n$ (h) $\mathcal{L} = n$

SUPER BRAINTWISTER: Another operation is called, "beta." The symbol to indicate beta is B . Try to find the meaning of beta from these examples:

- (a) 3 B 4 = 5
- (c) 2 B 8 = 2 (e) 6 B 1 = 5
- (b) 1 B 2 = 9 (d) 7 B 5 = 0 (f) 3 B 3 = 6

Find n for each of the following: "

- (g) 2 B 3 = n
- (i) $5 \cdot 8 \cdot 6 = n$ (k) $1 \cdot 8 \cdot 0 = n$

- (h) 8 B 4 = n
- (j) 4 B 2 = n , (1) 5 B 5 = n

8. SUPER BRAINTWISTER. For which of the operations in exercises 1-7 does the commutative property seem to hold?

ENRICHMENT

Exercise Set 21

UNION OF SETS

Pretend you have Set A and Set B.

Call Set C the intersection of Set A and Set B.

Call Set D the union of Set A and Set B.

Copy and fill in this table. (You may need to draw some pictures.)

Number of members in Set A	Number of members in Set B	Number of members in Set C (Intersection) .	Number of members in Set D (Union)
(1) 7	. 8	0	15
is (2) mais and of six and is in the six and is		farman 200 an an	13
(3) 7	9	4	98 7
(4) 8	3	0	
(5) 8	3	n	
(6) 8	m	0 *	
(7) P	r	2	<u></u>
(8) p	r	5	

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Chapter 7

TECHNIQUES OF MULTIPLICATION AND DIVISION

OPERATTONS

We think of addition, subtraction, multiplication, and division as the four basic operations of arithmetic.

We have learned that an operation on numbers is a way of thinking about two numbers and getting one number as a result.

When we think about 12 and 3 and get 15, we are adding. When we think about 12 and 3 and get .9, we are subtracting. When we think about 12 and 3 and get 36, we are multiplying. When we think about 12 and 3 and get 4, we are dividing.

MULTIPLICATION

We express multiplication like this:

We read the sentence like this:

- 9 times 4 is equal to 36.
- 9 times 4 equals 36.

We know that:

- 9 is a factor of 36.
- 4 is a factor of 36.
- 36 is the product of 9 and 4

DIVISION

We express division like this:

$$36 \div 9 = n$$

$$36 = n \times 9$$

or

$$36 = 9 \times n.$$

We read the sentence like this:

- 36 divided by 9 is equal to n.
- 36 is equal to what times 9?
- 36 is equal to 9 times what number?

We know that:

- 36 is the product of 9 and n.
- 9 is a known factor of 36.
- n is an unknown factor of 36.

THE DISTRIBUTIVE PROPERTY OF MULTIPLICATION OVER ADDITION

Methods of multiplication depend on expressing one factor as a sum and then using the distributive property of multiplication over addition.

To multiply 48×6 , you can think of 48 as (40 + 8). Then we multiply each number by the factor 6. We use the distributive property.

$$6 \times 48 = 6 \times (40 + 8)$$

 $6 \times 48 = 6 \times (40 + 8)$ Rename 48 as (40 + 8).

=
$$(6 \times 40) + (6 \times 8)$$
 FDistribute the 6 over

$$(40 + 8).$$

The product of 6 and 40

is 240. The product of

6 and 8 is 48.

The sum of 240 and 48

is 288.

THE DISTRIBUTIVE PROPERTY DIVISION OVER ADDITION

"we express '75 as To divide 75 by 5 Then we divide both numbers by

$$75 \div 5 = (50 + 25). \div 5$$

Rename 75 as (50 + 25).

5) Distribute the 5 over

50 + 25).

vide 50 by 5. Divide

The sum of 10 and 5

Write the numerals from 1 to 20 on your paper. If a statement is true, write <u>true</u>. If a statement is false, write <u>false</u>.

- 1. Using the set of whole numbers, you can multiply any pair of numbers and always get a whole number for their product.
- 2. Using the set of whole numbers, you can divide any pair of numbers and always get a whole number for the unknown

3.
$$273 \times 846 = 846 \times 273$$

factor.

5.
$$69 + 3 = 3 + 69$$

6.
$$17 = 17$$

7.
$$6 \times 0 = 6$$

8.
$$1 \times 9 \neq 9$$

10.
$$6 \times 9 < 7 \times 9$$

$$\pm 1.58 \times 69 > 69 \times 58$$

12.
$$48 + 4 = (40 + 4) + (8 + 4)$$

13.
$$(20 + 4) \times 7 = (20 \times 7) + (4 \times 7)$$

14.
$$2 \times (3 \times 17) = (3 \times 17) \times 2$$

15.
$$2 \times 34 = (2 \times 30) + (2 \times 40)$$

16.
$$(21 \times 7) + 7 = (21 + 7) \times 7$$

17.
$$(48 + 6) + 2 = 48 + (6 + 2)$$

18.
$$(5 \times 30) + (5 \times 6) = 5 \times 36$$

19.
$$(47 \times 18) + (47 \times 12) = 47 \times 30$$

Find a decimal numeral for n in each sentence.

1.
$$10 \times 18 = n$$

$$11. \quad 10 \times 47 = n$$

2.
$$17 \times 10 = n$$

$$12.89 \times 10 = n$$

3.
$$27 \times 10 = n$$

13.
$$54 \times 10 = n$$

14.
$$10 \times 98 = n$$

5.
$$10 \times 107 = n$$

15.
$$10 \times 125 = n$$

6.
$$12 \times 10 = n$$

$$-16. \quad 314 \times 10 = n$$

7.
$$120 \times 10 = n$$

$$17.412 \times 10 = n$$

8.
$$10 \times 19 = n$$

18.
$$842 \times 10 = n$$

BRAINTWISTERS:

10.
$$300 \times 10 = n$$

19.
$$17 \times 20 = n$$

20.
$$12 \times 30 = n$$

MULTIPLYING BY MULTIPLES OF TEN

We have learned how to multiply two numbers when one of the numbers is 10.

Now we want to learn to multiply two numbers when one of the numbers is a multiple of 10. Multiples of 10 are 10, 20, 30, 40, 50, and so on. Can you name some other multiples of 10?

Suppose we find the product of 7 and 20. To multiply 7 and 20, we can think of 20 as (10 + 10). Then,

$$7 \times 20 = 7 \times (10 + 10)$$
 Rename 20 as $(10 + 10)$.

= $(7 \times 10) + (7 \times 10)$ Distribute 7 over $(10 + 10)$.

= $70 + 70$ Multiply 7 and 10.

= 140 Add 70 and 70.

Too, we can think of 20 as (2×10) . Then,

$$7 \times 20 = 7 \times (2 \times 10)$$
 Rename 20 as (2×10) .

$$= (7 \times 2) \times 10$$
 Use the associative property.

$$= 14 \times 10$$
 Multiply 7 and 2.

$$= 140$$
 Multiply 14 and 10.

Is it easier to find the product of 7 and 20 by the first way or the second way? Let us find the product of another pair of numbers using the second way. One of the factors is a multiple of 10. Give reasons for each step in the following example.

$$8 \times 40 = 8 \times (4 \times 10)$$

$$\stackrel{\checkmark}{=} (8 \times 4) \times 10$$

$$= 32 \times 10$$

$$= 320$$

The product of 8 and 40 is 320. $8 \times 40 = 320$. 346

Find the decimal numeral for each product in exercises 1 through 12. In exercises 1 through 4, write each step as in the example.

Example:
$$7 \times 30 = 7 \times (3 \times 10)$$

= $(7 \times 3) \times 10$
= 21×10

- 1. 5×80
- 2.: 70 × 7
- 3. 50 x 8
- 4. 6 x 30

In exercises 5 through 12, find the decimal numeral for each product without writing all the steps. In exercise 5, can you think that 7 multiplied by 4 is 28 and that 28 multiplied by 10 is 280?

- 5. 7 × 40
- 6.5×60
- 7. 6 x 70
- 8.7×80

- $9,60\times9$
- 10.3×600
- 11. 30×8
- 12. 9 x 90

Use mathematical sentences to help solve each of the solve following problems. Express each answer in a complete sentence.

- 1. The beads on an abacus may be arranged so that there are 20 beads on each of 4 wires. How many beads are on this abacus?
 - ... Some land will be divided into 7 blocks. 40 houses will be built on each block. How many houses will there be on the land?
- 3. In one section of a plane there were 20 rows of seats with 5 seats in each row. How many seats were there in this section of the plane?
- 4. At an assembly the chairs were arranged in 30 rows.

 There were 10 chairs in each row. How many chairs were set up for the assembly?
- 5. Bob bought 3 season tickets to the Basketball games. Each ticket costs \$3.20. How much void Bob spend for the tickets?
- 6. On the family room floor there were 660 tiles. 304 tiles were used on the kitchen floor. How many more tiles were used on the floor of the family room than on the floor of the kitchen?





MULTIPLYING BY MULTIPLES OF ONE HUNDRED

We have learned how to multiply two whole numbers when one of the numbers is 10. We have learned how to multiply two whole numbers when one is a multiple of 10. What are some multiples of 10?

Look at this example for finding the product of 6 and a multiple of 10 (30).

$$6 \times 30 = 6 \times (3 \times 10)$$

= $(6 \times 3) \times 10$
= 18×10

We now want to learn to multiply two whole numbers when one of the numbers is 100. We also want to learn how to find the product of two numbers when one factor is a multiple of 100. What are multiples of 100? Is 200 a multiple of 100? is 300? Is 400? Can you name some other multiples of 100?

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```
See if you can understand these examples.
                                          6 \times 100 = 6 \times (10 \times 10)
= (6 \times 10) \times 10
= 60 \times 10
              Example 1:
                                                       = 600
                                        18 \times 100 = 18 \times (10 \times 10)
= (18 \times 10) \times 10
= 180 \times 10
             Example 2:
                                                      = 1800
                                          6 \times 300 = 6 \times (3 \times 100)
= (6 \times 3) \times 100
= 18 \times 100
= 1800
                                          50 \times 30 = (5 \times 10) \times (3 \times 10)
= (5 \times 3) \times (10 \times 10)
= 15 \times 100
           Example 4:
                                                       = 1500
      Example 5:
                                         16 \times 200 = 16 \times (2 \times 100)
= (16 \times 2) \times 100
= 32 \times 100
                                                        ₹ 3200
                                         4 \times 2000 = 4 \times (20 \times 100)
= (4 \times 20) \times 100
= 80 \times 100
= 8000
                                                        = 8000
Can you name the product just by looking at the two numbers
to be multiplied? Try these.
                                                     30
                                             12 \times 400
How many could you do?
 Now you can use what you have learned about multiplying
by 10 and 100 and their multiples.
```

$$7 \times 500 =$$

6. 10 × 7 = _

7. 500 × 5 ≡ ____

8. 600 ×,3 =

10. 50 x 6 = <u>*</u>

```
MORE ABOUT MULTIPLYING
     We now learn to multiply two numbers like these:
                   4, and 32
     This array helps us to think about 4	imes 32.
  . We can make smaller arrays.
     How many rows does each have? How many columns does each
               We can use one of these ways too.
      \frac{\times 4}{120 + 8} = 128
```

Exercise Set 6 Find the decimal numeral for each product in the following exercises. Tuse two forms as in the example. Example: $3 \times 12 = 3 \times (10 + 2)$ "= (3 × 10) + (3 × 2) = 30 + 6 = 36 -<u> 30</u>. 36 3. 6 × 34

	Exercise Set 6	(Contra)
6. 5 × 87	87 × × 5	
7. 7×34	Berginsulse Bergering and American State of the State of	
8. 8 × 37	37 × 8	
9. 4 × 36	36 1 × 4	사람들은 이 그들은 아들이 들어가는 수 가는 것 같아 물었다.
10. 8 × 89	89 × 8	시간 사람들은 경기를 가지 않는 바다를 받는 것이다.
	354 - 58	



MULTUTELYING DARGER NUMBERS We know how to find the products of numbers like 3 and 46, 7 and 39, 6 and 45, What number must n represent in each of these sentences if the sentence is a true statement? 3°× 46 ≡ n 7 × 39 = n The products are 273, 138, and 2270. Now match the products and the product expressions. We now want to find the product of numbers like 3 and 312. We write $3 \times 312 = 3 \times (300 + 10^{\circ} + 2)$ " = (3 × 300) + (3 × 10) + (3 × 2)

There are several ways that we might use the vertical form for multiplication. Here are some of them. 300 + 10 + 2 900 + 30 + 6 = 936 In the last example, how did we get 900, 30, and 6? You do not need to use all of these ways. Use the one that you like best. You may even like a short form like 312 · 936 Can you discover a way to find the product of

Exercise 8et 7 Find the decimal numeral for each product in the following exercises. Show the partial products. 5 x 601 3. 4×322 . 4 × 3002 7 × 5101

	The section of the later of the section of the sect	Exerc	<u> 18e Set 8</u>		And the second s
fon	Work these n=if;you can. Example:		311	ple. Úse	the vertical
Application of the Control of the Co	Provide de Autorial de Santa de Constante de Carres y Carres de Carres de Carres de Carres de Carres y Carres de Carres de Car	algorithms (the great of the second of the second	<u>× 5</u> 555		un galan de la cerca de la companya de la companya La companya de la co
7.	243	6. 800 ≢ <u>× 6</u>	11.	134 × 2	16, 1010 × 9
2.	.210 () / ;	7, 7 821 × 4·	12.	612 × 4	17. 1023 <u>× 3</u>
3. 	. 203 <u>× 3</u>	8. 3020 <u>× 3</u>	13.	723 ∵ <u>× 3</u>	18; 2332. × 3
4.	202 <u>× 4</u>	9. 3002 <u>× 4</u>	14.	<u>× 3</u> 632	19. 8212 ×4
5.	420 <u>× 2</u>	10: 502 \(\times \)	15.	734 × 2	. 20. 9111 <u>× 8</u>
Age to the control of		6 2	358		



A SHORTER METHOD OF MULTIPLYING In our last lesson you saw how to shorten the form at the reft so that you could multiply 312 by 3 in the way shown at the right: 900 Were you able to tell what you had to think to use this way? . We want to think some more about these shorter ways. Suppose we need to find the product of 4 and 23. already know how to find the product in this way: Now let us see if we can find a shorter form for doing this. We can think $4 \times 3 = 12$. Think of $12 \times as$ 1 ten and 2 ones. Let us write the 2 in the one's place. We will remember the 1 ten. $4 \times 20 = 80$. 80 is 8 tens 8 tens and 1 ten are 9 tens. How can we write the numeral for 9 tens and 2 ones? What is the product of 4 and 23? We can write

Andrews and the second	The state of the s	e de la companya de La companya de la co La companya de la co	
Here E	re some problems. (an you fill in the b	anka?
And the second s	And the Control of th		
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Voll m	av wish to use this	short method to do th	e problems
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Use the way you like best to find the number represented

by n in each of these.

$$3. \quad 9 \times 62 = n$$

. 8.
$$3 \times 89 = n$$

10.
$$8 \times 78 = n$$

Copy and complete. (Note: Each blank must be replaced by one digit.)

MULTIPLYING NUMBERS LESS, THAN 100 BY MULTIPLES OF 10

We new want to learn how to multiply numbers like 20; and

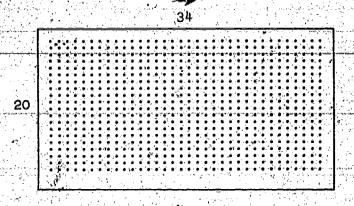
34, 40 and 46, 50 and 23, 60 and 31.

Is one number of each pair a multiple of 10? Name the multiples of 10 in these pairs.

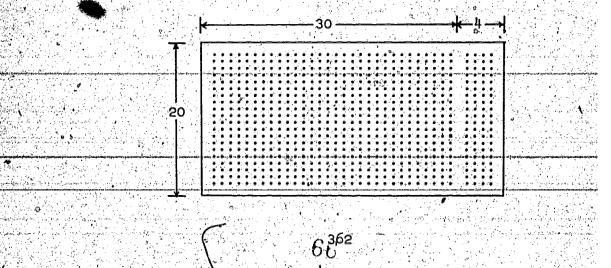
Is the other number in each pair less than 100?

Let us learn a way to find the product of 20 and 34.

Does 20 x 34 name the number of dots in this array? How can
you tell?



Here Is another array just like the one above. Let us separate it into smaller arrays.



Does (20 × 34) describe the first array? Does (20 x 30) + (20 x 4) describe the second array? Do the two arrays show that $20 \times 34 \neq (20 \times 30) + (20 \times 4)$? Does this help you to find the number of dots in the big We can write: 20 × 34 = 20 × (30 + 4) (20 × 4) <u>(20 × 30)</u> (20 × 34) Can you think of other ways of finding the product of these two numbers?

Exercise Set 10 .20 🗴 43 ≢ n 1. 30 x 30 = n .3. 10 x 80 = n 4. 30 × 40 = n 50 × 32 = n. 18. $.70 \times 83 = n$ % 6. . 60 × 90. = n 19. 90 × 65 = n 20. 80 × 87 = n $8. 80 \times 40 = n$ ž1. 90 x 38 = n + 9. 30 x 90′≌ n $22. 70 \times 57 = n$ $10. \quad 50 \times 70 = n$

FINDING PRODUCTS OF NUMBERS GREATER THAN 10 (AND LESS THAN 100)

We have learned to find the product of pairs of numbers. We made some choices in the numbers we selected.

We learned to find products of pairs of numbers like these:

$$\frac{3 \text{ and } 45}{3 \times 45 = 3 \times (40 + 5)}$$
 $= (3 \times 46) + (3 \times 5)$
 $= (3 \times 46) + (3 \times 5)$
 $= (8 \times 10) + (8 \times 6)$
 $= 120 + 15$
 $= 80 + 48$
 $= 135$
 $= 128$

120

 (3×40)
 $\frac{15}{15}$
 (3×5)
 $\frac{15}{135}$
 $\frac{5 \text{ and } 24}{5 \times 24 = 5 \times (20 + 4)}$
 $= (5 \times 20) + (5 \times 4)$
 $= 120$
 $(5 \times 4) + (5 \times 20)$
 $= 120$

We can use the same way for all of these examples. We can use different ways to find the product of numbers like these.

We learned to find products of numbers when one of the humbers was a multiple of 10. What numbers less than 100 are multiples of 10? Can you find the product for each of these pairs? Why can we change order The products are 170, and 740. Did you get them right? " * Now we wild learn how to find the products of any two numbers greater than low we will still make a choice. will be numbers less than 100.

Ann was cutting a Targe cake.

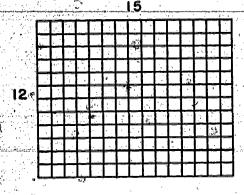
She cut 12 long pieces (rows) of cake.

She cut each long plece into 15 pieces.

How many pieces of cake did she have?

Is this mathematical sentence a correct one for this problem?

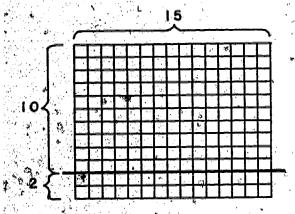
Does this picture give us an idea of the cake? Explain.



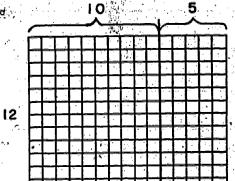
Let us separate this array anto smaller arrays.

What product expression does each array suggest to you?

Find the array each of these describes.

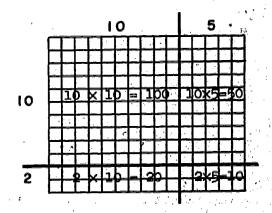


10 x 15 = 150 2 x 15 = 30 There are other ways we can separate the array. Look at this



This vertical form helps us to find the product.

Let us see still another way of separating the array. Now we can write the product in vertical form in this way.



Use the way that you like best to find the products in the exercises in Exercise Set 11. (The more we can learn to remember, the less we need to write.)

Exercise Set 11

Find the decimal numeral representing n.

$$1. \quad 12 \times 23 = r$$

7.
$$21 \times 78 = n$$

2. $11 \times 42 = n$

8.
$$31 \times 66 = n$$

3.
$$14 \times 52 = n$$

9.
$$32 \times 59 = n$$

4.
$$15 \times 32 = n$$

10.
$$45 \times 45 = n$$

5.
$$32^{k} \times 41 = n$$

11.
$$37 \times 48 = n$$

6.
$$23 \times 63 = r$$

12.
$$29 \times 54 = r$$

(Optional)

Sometimes properties of multiplication can be used to make short cuts in multiplication. See if you can explain these short cuts.

13	3	: 50					$A_{i,j}(x)$					<i>1.7</i> 8	3. , ,
		× 78		hort	cut:	rewri	te or	retr	iink	as	1	%[2¢)
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	**************************************	x 29	, 9	hort	cut:	Write	or t	hink	as	0		<u>- 33</u>	<u>'</u> ''

16. 480
$$\times 370$$
 short cut: find 37×48 , then multiply by 100 \times

Try to find a short cut in these exercises. If got gamet,

USING MULTIPLICATION IN PROBLEM SOLVING

You have solved problems before.

Do you remember how you solved problems?

Let us use this problem to help us remember.

Problem: At the tircus, the children of Madison School sat in a section of 15 rows. Eighteen children were seated in each row. How many children from Madison School were seated in this section?

Bits of Information: There are 15 rows and there are

Mathematical Sentence: $15 \times 18 = n$

orke

×.15

-- C

....

100

Answer Sentence; .270 children were seated en this

In solving problems you need to:

Understand question that is to be answered

Find the information given in the problem that will help you.

Write a mathematical sentence that relates this information to

the guestion.

Find the number that is not known.

Write an answer to the problem question.

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Exercise Set 12

- 1. The children of Madison School went to the circus in 6 buses. Forty-five children rode in each bus. How many children rode in the 6 buses?
- 2. There were 424 boys and girls enrolled in Madison School.

 If 270 children went to the circus and the other children went to the zoo, how many children went to the zoo?
- 3. One day at the zoo there were 154 children from Madison School and 168 children from Adams School. How many children visited the zoo that day from the two schools?
- 4. A crossword puzzle had 15 squares across and 12 squares down. How many squares were there in the puzzle?
- 5. There were 360 dots in one part of an array and 24 dots in the other part. How many dots were there in the whole array?
 - 6. The score of a football game is 35 to 17. How many points does one team need to tie the score?
 - 7. Mrs. Smith buys 14 gallons of milk each month. How many gallons does she buy in a year?
- 8. Fifteen gallons of ice cream were bought for the Halloween party. If one gallon served 26 children, how many children did the . 15 gallons serve?





- 9. There were 12 tables in the cafeteria. If 16 children sat at each table, how many children could be served at one time?
- 10. 36 boxes of crayons were ordered for a class. Each box contained 24 crayons. How many crayons were there altogether?
- 11. In the parking lot at the ball park there were 24 rows with spaces for 35 cars in each row. How many cars may be parked in this lot?
- 12. It took 191 seconds for the children in Lowell School to Leave the building during a fire drill in March. In April the time was 186 seconds. How much longer did it take the children to leave the building in March?
- 13. Mrs. Wood made 27 jars of jam. If each jar held 16 ounces, how many ounces did she make?
- 14. There are 53 boys and girls in the morning kindergarten class and 48 in the afternoon class. How many children are in the two classes?
- 15. Each of the 32 children in Miss Park's class made 18 name tags for open house, How many name tags did they make?

FINDING UNKNOWN FACTORS

Try to find the unknown factors in these sentences. Use multiplication facts to help you.

A

B

$$4 \times n = 36$$

$$4 \times n = 360$$

$$n \times 8 = 6$$

$$n \times 8 = 640$$

$$n \times 7 = 42$$

$$n \times 7 = 420$$

$$2 \times n = 12$$

$$2 \times n = 1200$$

$$5 \times n = 30$$

$$5 \times n = 3000$$

What multiplication fact did you use for each?

In what way did finding the unknown factors in \underline{A} help you to find the factors in \underline{B} ?

How can each of the sentences in A and B be rewritten using the division symbol?

Many problems are solved by dividing one number by another. Here is an example.

Paul has 52 stamps. He can put 4 stamps in one row in his book. How many rows will he need if he puts all 52 stamps in his book?

We want to find the number of rows of stamps.

There are 4 stamps in each row.

There are 52 stamps in all.

Is the mathematical sentence for this problem $n \times 4 = 52$, where n represents the number of rows?

Think of an array.

The stamps in his book might be arranged as in the picture at the right. The way the array is separated shows that

$$52 = 20 + 20 + 12$$
.

4

We write:

$$52 + 4 = (20 + 20 + 12) + 4$$

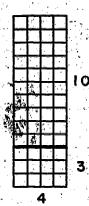
$$= (20 + 4) + (20 + 4) + (12 + 4)$$

$$= 5 + 5 + 3$$

$$= 13.$$

There are 13 rows of stamps.

The stamps in his book might also be arranged as in this picture at the right.



The way the array is separated shows that 52 = 40 + 12.

We write

The number 52 can be renamed so that each addend is a multiple of 4. These numbers are multiples of 4:

.Can you name some others?

Try some other ways of renaming 52

Find the unknown number in each of these exercises.

10

n x 10 = 40

3. 1200 + 3 = n

Rename each product using multiples of the known factor as addends.

Example 1:

$$5. \quad 48 + 2 = 1$$

$$5. \quad 42 + 2 = k$$

$$8. \cdot n = 55 + 5$$

12.
$$91 + 7 = 1$$

13.
$$112 + 8 = t$$

14.
$$217 + 7 = W$$

15.
$$333 + 9 = m$$

16.
$$400 \div 5 = n$$

17.
$$639 \div 3 = 1$$

18.
$$420 \div 4 = m$$

19.
$$-770 \div 7 = 1$$

20.
$$630 \div 6 = t$$

EXCYPLE (USE) 115

Write mathematical sentences to help you solve the following problems. Solve them. Write an answer sentence for each problem.

- 1. At the air show 40 planes flew in formation. There were 10 rows. How many planes were in each row?
- 2: A class of 36 children was divided equally into 3 committees to plan a party. How many children were on each committee?
- 3. The grocer put 60 carrots in bunches of 5. How many bunches did he make?
- 4. How many days are there in 7 weeks?
- 5. Bob received an allowance of 50%. Jim's allowance was 75%. How much more money does Jim receive than Bob?
- 6. 50¢ is how many times as much money as 5¢7
- 7. The 80 men in the marching band were divided into rows. . How many men were in each row?
- 8. A jet plane carried 42 passengers in one section and 102 passengers in another section. How many passengers were aboard the jet?

379

A WAY OF DIVIDING TWO NUMBERS We have learned that we can rename the product and divide to find the unknown factor. , jh = 225 + 9 = (180 + 9) + (45*+ 9) Here is another way to show division Mathematical Sentence: Form I: Form LI: 9 **)**225

. You may use either form shown above.

Now we know: "' '

380

Exercise Set 16 Use Form I or Form II to find the unknown number in each 60 ÷ 12 = n 376 + 8 = q

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USING DIVISION IN PROBLEM SOLVING

There are 108 fruit trees in an orchard. There are 9 rows of trees with the same number of trees in each row How can you find the number of trees in each row?

The information in the problem is: (*)

There are 108 trees.

There are 9 rows:

Each row has the same number of trees

Let us form a mathematical sentence to show how the bits of information in the problem are related. Let an represent the number of trees in each row.

 $9 \times n = 108$, or n = 108 + 9.

In the mathematical sentence, 108 is the product, 9 is the known factor, and n is the unknown factor. We can find by dividing 108 by 9. Your answer should be (2°) so that $9 \times 12 = 108$.

We now write an answer sentence:

There are 12 trees in each row.

In this problem about the trees, there are 108 trees in the set. The set of 108 trees is divided in 9 wets, with the same number in each group. You found the number of trees, in each of the 9 sets, This number was 12. You used division to find the number of trees in each set.



wew let us think of another problem. Suppose there are 822 dogs in a large dog show. An official tells us that there are cocker spandels, poodles, collies, Irish setters, boxers, and German shepherds. Also, he tells us that in each breed there is the same number of dogs. How many dogs of each breed are in the show? The information in the problem is: There are 822 dogs in the show. There are 6 breeds of dogs in the show. Each breed has the same number of dogs. The question we want to answer is: How many dogs are there of each breed? /Let us form a mathematical sentence. Let n represent the number of each breed of dog. $6 \times n = 822$, or n = 822 + 6. In the mathematical sentence, 822 is the product, 6 is the known factor, and n is the unknown factor. We can find n by dividing 822 by 6. We show the division in either one of these 30° 6)822 6 822 100 600 222 180 42 dogs of each breed The answer sentence is: There are 137 in the show. In this problem about dogs, there are 822 dogs in the set. There are 6 sets with the same number in each group. We found the number of dogs in each set by dividing 822 by 6.

Exercise Set 18 e mathematical sentences to help you so we the following problems: Solve them. Write an amswer sentence for each problem. The Jackson family is planning a 510 mile trip. If they have 5 days to travel, about how many miles must they tratel each day? Seven jets left the airport one day. Each had 128 passengers aboard. How many people left the airport by jet that day?: 4 In Cub Scouts, John made a collection of 144 small shells. He put the same number in each of 6 boxes. How many did he put in each box? Fran collected 126 leaves for a project in school. mounted them, on 9 large posters. How many leaves did she mount on each poster? There are 189 Boy Scouts in 9, troops. If each troop has the same number of members, how many boys are in each troop? Peggy's mother baked)186 cookies for a picnic. She packed the same number in each of three boxes. How many did she pack in each box?

7.	Dick and Tom offered to make tickets for the puppet show.
Free Programme (St. 1997) Programme (St. 1997) Programme (St. 1997)	They made 139 tickets on Tuesday, 125 on Wednesday, and
ng Palesylesi.	127 on Thursday. How many tickets did the boys make
	togethen?
8.	The restaurant had 2 dining rooms. One held 220 people,
	the other had room for 175 people. How many more people
	could eat in one dining room than in the other?
erenium en	
⁄"∵9:.·	If 27 visitors are taken through a state capital building
	in one group, how many visitors are taken through in 13
Ange of Louis and the	groups?
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10	If one-case of canned soup weighs 24 pounds, how much
	will 48 cases weigh?
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11.	A committee of 7 pupils collected 455 rocks while
Service of the servic	working on a class project. If each pupil of lected
ky staniskanta is sinch od o kilosofia sinch od od od od od sinch od od od od od	the same number of rocks, how many rocks did each pupil
	find?
	There are 9 boys in our Cub Scout den. The boys
12.	collected 477 toys during their yearly toy drive.
	If each boy collected the same number of toys, how
	many toys did each boy collect?
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	387
	o operation in the contract of
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BECOMING MORE SKILLFUL IN DIVIDING NUMBERS The fourth grade class had 1720 inches of string. wanted to cut it into pieces, each 8 inches long. How many pieces_will_they_have? Mathematical sentence: 1720 + 8 = n or We can work this problem in several ways. Here are three ways. 100 10 100 200 100 400 920 1320 800 (c) the shortest one of the 3 ways? There are 215 pieces of string.

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Exercise Set 19 Find the missing factor. 1. 340 + 4 = n 12. 8280 + 9 = t' 1435 + 5 = n 13.. 3616 + 8 = m 14. 3560 + 2 = n 1056 + 8₁ = n 16. 8960 + 8 = s 17. 5761 + 7 = m 10. 2240 4 4

Exercise Set 20 write mathematical sentences to help you solve the following problems. Solve them. Write an answer sentence for each problem. If a plane travels 1675 miles in 5 hours, about how far does it travel in one hour? How many doughnuts are there in 17: dozen? For the school carnival the mothers put 600 pieces of homemade candy into bags. They put 5 pieces of candy in each bag. How many bags did they pack? 720 loe cream bars were bought by the Dad's Club to treat the children of Baker School. There were 669 children present that day. How many extra bars were there? A motorcycle traveled 234 Jmiles on 6 gallons of gas. How far did it travel on one gallon? A market put 1744 onions into bunches of 8 onions each. How many bunches were there? A grocer ordered 726 bottles of soft drinks. They were defivered in cartons that held six bottles each. How. many cartons were delivered?



FINDING QUOTIENTS AND REMAINDERS

We can use the division process to solve problems like this one:

There are 306 people at the exhibit. There are to be 4 tours. How many people should go in each tour to have about the same number of people in each group?

Mathematical sentence: $306 = (4 \times n) + r$.

You may use either form: ...

Form I.

<u>76</u>

Form II

70

)306 <u>280</u> 26

<u>. 2</u>

306 = (76 × 4) + 2

Each group should have 76 people. There are 2 people to join one or two of the groups.

In a mathematical sentence like

we say that

306_is_the_dividend

76 is the quotient.

4 is the divisor.

2_1s the remainder

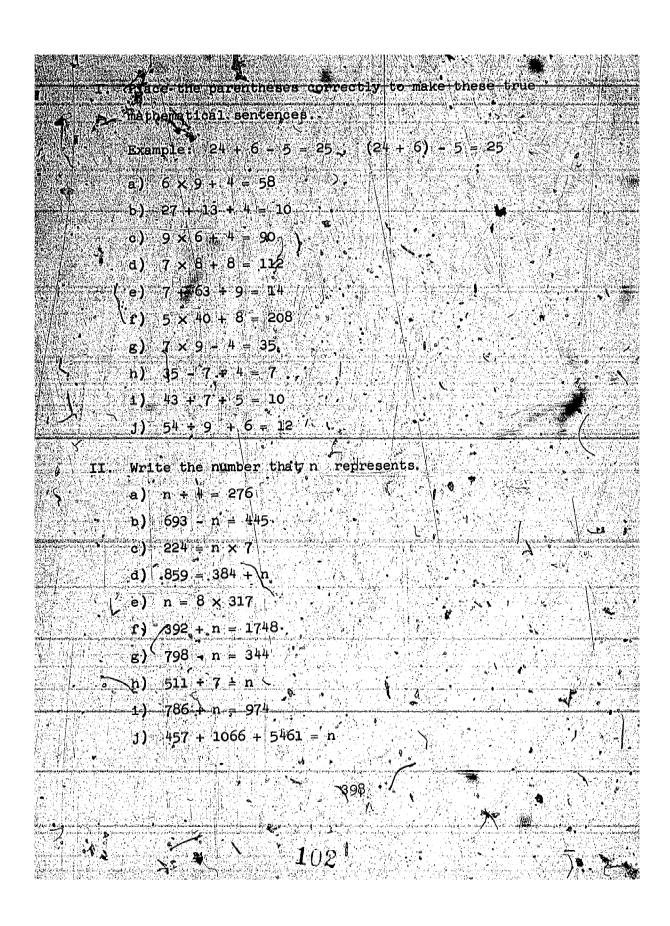
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tind the numbers of and r must represent to make each sentence
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   1242 = (q \times 8) + r
   943 = (q \times 7) + r
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数据的证明的证明和证明的证明的	mathematical sentences to help you solve the Following
probl	ems. Solve them. Write an answer sentence for each problem.
	29 boys want to organize teams of 5 boys for a relay race;
	How many teams can be organized? How many boys will not race?
of Property was a second secon	
, 2.	If the school oustodian put 80 chairs into rows of 10
elist program trap between a district tra- cing program trap between transporters and the second	chairs each; how many rows could he make? Would there be any
	chairs not used?
3.	Longfellow School bought 25 new bounce balls. Each of 6
	classrooms are to share the balls equally. Any that are left
	will be kept for next year. How many ball's will each room
	get?
	"Polka for Three" is a dance done in groups of 3. How many
	groups can be made in a class of 32 children? How many
Andrew Commence of the Commenc	children will not dance?
	Mary is asking 30 girls to her party. How many yables
Section Land and the section of the	must she have if she serves 4 at a table? How many girls
establishment for a series for the series of	will have to sit on the sofa to eat?
egin men kumun satur kanala satur kanala Manada satur kanala satur kanal Manada satur kanala satur kanal	271 reservations were made for a luncheon.
b.	271 reservations were made for a luncheon. ** would have to be set if # people were to be seated at each
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	198

A baken is to pack 1250 cupcakes for a school picnic. He
will put 8 in each box. How many boxes will he order?
2) Each of 15 Girl Scouts sold 24 boxes of cookies. How
many boxes were sold?
3. / Six sheets of colored paper are needed for a booklet. How
/ many booklets can be made from 500 sheets of colored paper?
4. The-Parent-Teacher Association of a school had 324 members
last year and 296 members this year. How many more
memberships are needed to reach last year's record?
In a school library there were 23 sets of readers. There
were 75 books in each set. How many books were there in
the 23 sets?
6. Bill planted 12 rows of tomatoes. There were 15 plants
in; each row. How many plants did Bill set out?
7. The children of Miller School are raising money to buy a television set which costs \$350. They have collected
\$179. How much more money do they need?
A PERCONAL SECTION OF THE PROPERTY OF THE PR

white beads, 720 red beads, 1801 green beads, and
in 5 hours?
10. There were 385 tickers to be put in buildes of 8. How many bundles will there be? Will any times be left?
11. On a reading test, Mary read 284 words in 3 minutes. About how many words did she read in one minute?
12: A farmer packed 360 boxes of apples for shipping Each box weighed 45 pounds. What was the weight of all the
boxes?
13. 573 scouts who attended the Jamboree slept in tents which
had 4 beds. How many tents would 573 scouts need?
14. 630 dancers attended the Folk Dance Festival: Into how
many groups of 8 could they be divided for square. dencing?
396

i 147.994 ≒ (q × 8) + r 2.= 889= (q × 7),4°r' $7449 = (q \times 8) + r$ 290 ⊌ (q × 9) + r 14. $3636 = (q \times 8) + n$ "**493 = (**(q. ×, 5) + r 15. $2390 = (q \times 6) + r$ 5. + 389 ≡ (q ¾ 4) + x. 16. 1235 = (q.x.5) + r 534.**?= \(q × 5)**\+\r 7:7:1:954 = (q:x-4) + r' 17. $2770 = (\mathbf{q} \times 3) + \mathbf{r}$ 588 = (q × 6) + r 18. $477' = (q \times 9) + r$ 19. 6792 = (q x 7) + r 6769 = (q × 9) + r $3626 = (q \times 4) + r$



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a:):::386 **b)**....633... VI. Solve the following: a) $85 \times 27 = n$ f) f) $126 \div 3 = n$ b) n + 5 = 405 g) 600 - n = 568c) $9 \times 847 = n^{1/2}$ h) 876 + 889 = nd) 352 + n' = 900 1) 726 + 8 = ne) 27.+5.+8 = n j) 9000 - 3492 = n VII. Solve: -a) net 9-= 97 . $f) \quad 6 \times 7008 = n$ g) 108 ÷ 5 = n b) 89 + 95 + 96 = n h) 65 + 54 + 51 + 70 + 33 = h c) 10 x 85 = n d) 671 + 9 = n 1) n + 7 = 96 e) 6040 - n = 2159 j) 422 + 6 = n VIII. Solve the following: f) 680 + 807 + 739 = a) 393 + 8 = nb) $67 \times 36 \neq n$ g) n + 279 = 871c) 64 + 48 + 9 + 85 = n · h), 542 - 498 = n d) 29 + n = 861) 547 + 9 = nj) n + 5 = 5030e) $8 \times 1321 = n$

e)- 574 30 4 91. = \n f(): 278 + 7 = n - g) .19 × 69 = n ' h) 357 + 249 + 610 + 8 **1)** / 338 + 5' = n j) 201 $\div 4 = n$ Braintwisters, 1. Here is an imaginary operation called "cut". The symbol for cut is A . Try to find the meaning of A from these examples. a) $8 \wedge 4 = 1$ c) 10 5 = 1b) 9 A 3. = 2 d) 20 A 4 = 4 What is n in each of the following? 1) $63 \land 7 = n$ k) 36 A 6 = n g) $35 \land 7 = n$ 1) $49 \wedge 7 = \hat{n}$ h) $32 \land 8 = n$ j) $56 \land 8 = n$ Another imaginary operation is called "ler". The symbol for ler is \int . Try to find the meaning of \int from these examples. a) 6 f 2 = 3 c) $10 \int 2 = 7$ e) $5 \int 1 = 3$ b) $12^3 \int 3 = 8$ \ d) $8 \int 7 = 0$ What is n in each of the following? 1) 152 ∫ 151 = n

Part A Use = , > , or < to make these true statements. Example: if n + 2 = 7, then n < 7a) If $27 \div n = 9$, then n =b) If n+12=17, then n-17c) If $n \times 15 = 45$, then n = 1d) If 50 - n = 50, then $n _{-}$ e) If $128 \div n = 32$, then n = 4If $n \times 33 = 132$, then $n \underline{} 33$ g) If $n \div 7 = 4$, then n = 4n) If 1407 + n = 2989, then n $\frac{1}{1}$ 1407 1) If $143 = (2 \times 71) + n$, then $n _{--} 2$ j) If n = 6357 = 653, then n = 6357Write a mathematical sentence to "undo" the following. Example: 7 + 2 = n / (7 + 2) - 2 = na) 31 + 4 = nb) 12 × 6 = n c) 15 ÷ 3 = n $a) \quad 423 + 172 = n$ 3592 - 1782 = ne) 72 - 13 = nFor each multiplication fact write two division facts. Example: $2 \times 6 = 12$, $12 \div 6 = 2$, $12 \div 2 = 6$ $8 \times 6 = 48$ a) $6 \times 7 = 42$ 7 × 8 = 56 j) 9 x 7 = 63

Number Pair	:Result	Operation	Résult	Operation
a) 40, 25	65	Addition -	15	Subtraction
b) [72, 8			576	
e) 96, 8		Subtraction	12.	
d) 84, 23	1932 . <			Addition
e) 369,9	378	Aggregate and developed to extension a secondarial policy of the secondarial secondaria seco	man a su prancada aprofe	Division
f) 80, 12		Addition		Subtraction
g) 45,5	225		9	
h) 90, 9	81			multiplication

5. BUE = (red, blue, white, green, purple)

 $\mathbf{B} \bigcap \mathbf{E} = \{ \dots \}$

E = {green, purple}

What operation could you use to find the number of

members in Set B? Name the members of Set B.

6. A
$$\bigcup G = \pi_2, 4, 5, 6, 3, 7$$

$$A \cap G = \{5, 6, 7\}$$

$$G = (5, 6, 7)$$

Could you use subtraction to find the number of members

in Set A? Name the members of Set A.

$$7.1 c = (2, 4; 6, 8)$$

Name the members of the Set C U O.

-What-operation-could-you-use-to-find-the-number-of

members in CUO?

	a) 2 line segments
	b) 3 line segments \
	d) 6 line segments
	e) 1 10 line segments
Manager State of the Control of the	How many vertices has each polygon in Problem 8 ?
9.	How many versices has each polygon in 110010m
10.	Find the number that n represents in each of these.
	Example a is done for you.
	a) $53 + 22 + n = 89$, $53 + 22 = 75$, $89 - 75 = 14$, $n = 14$
Michigan (1996) Panggan ang Panggan (1996) Panggan ang Panggan (1996) Panggan ang Panggan (1996)	b) 24 + 30 + n = 79
ke dan	c) #3 + n + 25 = 87 d) n + 9 + 30 + 27 = 152
	(a) $11 + 9 + 30 + 21 = 1504$
	f) 59 + 497 + n + 7 = 1069
	g) $34 + n$ $+ 11 = 68$
	h) 275 + 596 + n = 1716
	1) $16 + n + 66 = 96$
Stock to the second state of the second state of the second secon	j) $n + .669 + .352 = .1021$
project and a major or day of grade has a	k) $88 \pm 7 + \hat{n} = 174$
Antina is a section of the section o	anakaning na promon natahan kanasan mengan bermalik seri pengan dalam mengan bermalik natahan bermalik natahan Mengan pengan natahan pengan
	The second secon
	404
angle and the agreement of the grant of the	the strength of the second sec

Idea	* Model*
1) Point	a) My path when I walk all the
2) Line segment.	way around the block and
3) Line	return to my starting point.
i ing ji sain sa di sa ji 🔻	b) A stretched piece of string
လည်း ကြောက်သောကြသည်။ သို့သည်။ သည် သည် သည် သည် သည် သည်။ နိုင်ကျားသော ကြောက်သည် သည် သည် သည် သည် သည် သည် သည်။	c) The rim of a drinking glass
5) Plane	d) A Tootball field
6) Simple Closed Curve	e) The tip of a compass
7) Polygon	f) The edges of a piece of
8) Circle	floor tile
9) Plane region	g) The surface of a calm lake
	whose shores cannot be seen
engan kanan di kanan di kanan di k anan di kanan di kanan Kanan di kanan di ka	h) The light from a distant star
	1) A straight narrow road with
	no ends in sight
Part B	
	· ·
production of the control of the con	e (or two sentences if necessary)
Write a mathematical sentence for each problem and solve.	
for each problem and solve.	Write an answer sentence.
for each problem and solve. 1. The Polk Street bus makes	Write an answer sentence. three round trips every hour. How
for each problem and solve.	Write an answer sentence. three round trips every hour. How
for each problem and solve. 1. The Polk Street bus makes many minutes should one r	Write an answer sentence. three round trips every hour. How
for each problem and solve. 1. The Polk Street bus makes many minutes should one r	Write an answer sentence. s three round trips every hour. How round trip take? rges 25 cents for lunch. How much
for each problem and solve. 1. The Polk Street bus makes many minutes should one records. 2. The school cafeteria characteria characteri	Write an answer sentence. s three round trips every hour. How round trip take? rges 25 cents for lunch. How much for lunches all week?
for each problem and solve. 1. The Polk Street bus makes many minutes should one record to the school cafeteria charmoney will a student need.	Write an answer sentence. s three round trips every hour. How round trip take? rges 25 cents for lunch. How much for lunches all week?
for each problem and solve. 1. The Polk Street bus makes many minutes should one record to the school cafeteria charmoney will a student need.	Write an answer sentence. s three round trips every hour. How round trip take? rges 25 cents for lunch. How much if for lunches all week?
for each problem and solve. 1. The Polk Street bus makes many minutes should one record to the school cafeteria charmoney will a student need.	Write an answer sentence. s three round trips every hour. How round trip take? rges 25 cents for lunch. How much for lunches all week?
for each problem and solve. 1. The Polk Street bus makes many minutes should one record to the school cafeteria charmoney will a student need.	Write an answer sentence. Is three round trips every hour. How round trip take? Trips 25 cents for lunch. How much if for lunches all week?
for each problem and solve. 1. The Polk Street bus makes many minutes should one record to the school cafeteria charmoney will a student need.	Write an answer sentence. s three round trips every hour. How round trip take? rges 25 cents for lunch. How much if for lunches all week?



- 4. A dairy cow requires three acres of grazing land. How much land is needed for 175 dairy cows?
- 5. Mary's baby sister drinks 8 ounces of milk six times a day. How much milk will the baby drink in one week?
- 6. The class in Room 15 invited their parents to a puppet show.

 There were only forty-five chairs in the room and 72

 parents came. How many parents had to stand?
- 7. One scout troup delivers 364 hand bills, another troop has 37 less to deliver. How many hand hills do both troops deliver?

Group Activities

Multiplication Quiz

child (leader or quiz master) stands in front of the class and says, "I am thinking of two factors whose product is 42."_____
Then he calls on class members.

Child in class group called on asks, "Are you thinking of and 7 ?"

The leader replies yes or no as the case may be. A record is kept on the board of all combinations of numbers correctly given for review later.

If the leader passes a wrong combination he must sit down and a new leader is chosen.

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1. Using the symbols >, true sentençes. a) 747 319 x 3 • f) $343 \div 7$ 49 x 6 g) 3148 _____232 x 14 ь) 83, × 7 ____ 73 × 8 c) $576 \div 9$ 32×2 h) $(7 \times 8) \times 2$ $(12 \times 9) + 4$ d) 914 - 326 22×25 1) 25×25 30×20 __c)_576 ÷ 9___32 × 2 e) 34 x 19 - 799 - 153 J) (40 + 4) x 4 4 2. Tell whether each of the following is true or false. f) $(16 \div 2) \times 2 = 16 \div (2 \times 2)$ a) 6 + 3 = 3 + 6g) 7 × 6 < 156 - 112 b) 12 - 8 \(2 + 2 h) $29 = 8 \neq 4 \times 7$ c) 36 + 7 < 35 + 8 **(1)** 16 + 12 + 9 = 52 - 15 1) $4 \times 6 > 2 \times 11 \times 1$ e 3 × a is always > 3 × 2 j) $6 \times 5 \times 2 \neq 30 + 30$ 3. Tell what operation is used and find r. Example: $7 \times r = 42$, division, r = 6f) $24 \times r = 120$ g) 56 ÷ r = 8

Value of the state	Example: Of - C = II, C X II = OT , II - OC
A Control of the Cont	a) 832 ÷ 4 = n
	b) $273 \div 3 = n$
	c) 568 ± 8 = n
	d) $4207 \div 7 = n$
	e) $355 \div 5 = \hat{n}$
	r) 602 ÷ 7 = n
	g) $664 \div 8 = n^{2}$
	$\mathbf{n}) 111 \div 3 = \mathbf{n}$
5	Complete these to make them true sentences using words from
	this set of words: division, operation, multiplication,
	addends, subtraction, factor, addition, product.
	a) We operate on two factors and get a
	b) The operation of undoes subtraction.
anga dana barawa bagisand Marawa barawa bagisand	c) We operate on two and get a sum.
The state of the second of	d) The operation of subtraction undoes
	e) To find an unknown addend we use
	f) We use division to find an unknown
•	g) The operation of produces a sum.
	h) An on numbers is a way of thinking about
	two numbers and getting one and only one number.
Anglio All Company	1) A product is the result of the operation of
Hiller Handler of the Berkelman Legisla, Co	en la composition de la composition de La composition de la
	408
	112

(c)
$$9 \times 32 = (9 \times _) + (_ : \times 2)$$

h)
$$32 \times 4 = (16 \times 4) + (- \times 4)$$

7. Write each of the following using symbols.

Example: The number 8 increased by y,

- a) The sum of y and 6 5
- b) The number y added to 6
- c) The number y increased by six
- d) Six more than the number y

Find the number represented by each of the above if

8. Write each addition sentence as a subtraction sentence.

Find what number n represents

a)
$$40 + n = 68$$

c)
$$n + 54 = 90$$

d)
$$102 + n = 256$$

e)
$$n + 69 = 534$$

f)
$$452 + n = 931$$

g)
$$384 + n = 731$$

h)
$$465 + n = 53$$

	Column I	Column TI
	vertex	a) the union of a simple closed
	triangle	curve and its interior
3)	intersection	b)
* 4)	ratius	
	quadrilateral	d) the study of space and location
	plane-region	e) the set of points that is the
0	oircle -	triangle and its thterior
8)	triangular region	f), $\left(\begin{array}{c} - \\ - \end{array}\right)$
(9)	çay	g) the short way to name a line
		h) the polygon that is the union of three line segments
		2/2
		J) the common endpoint of two rays
		that are not on the same line
		Signal Commence of the Commenc
Part B		
Write a	mathematical senter	nce (or two sentences if necessary) for .
	سست برده و سند مستند مدانت معاون با معاون با معاون با معاون المعاون و المعاون و المعاون و المعاون و	rite an answer sentence.
	*	
		ents each for school softballs. How
mucl	n does he pay for t	wo dozen softballs?
9 How	many ice cream cup	s can be bought for 90 cents if each
	costs 6 cents?	Os seitus periminen as antigan et en antigan kan periminen kan territorial en antigan internet et en en en en e
cup	GORDS O' CELTOR!	
		410
		114
→ 1 転員 「同所等等等等等。	ZZ - ZTNOS BO BOOT 編 - Nago J Costor C	

- 4. For his model plane convection, Mark pays \$1.29 for one model, \$2.25 for another and \$1.46 for another. What is the total cost of the models?
- 5. In the problem above, Mark had saved \$3.29 and borrowed the remainder from his father. How much did he borrow?
- 6. Barbara can swim 120 yards in 5 minutes. How far ean she swim in 20 minutes?
- 7. A sign in the bakery reads; cookies 30 cents a dozen, donuts 60 cents a dozen, chocolate cakes 80 cents each. How much does it cost for two dozen cookies and a cake?
- 8. In the problem above, find the cost of two dozen cookies, two dozen donuts and a cake.

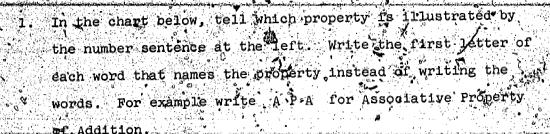
Individual Projects

- 1. Make up some operations and their symbols. Work at least.

 8 problems with each of your make-believe operations. Then
 put some examples on the board to see if your class can
 discover their meanings.
- least 79 other kinds. Name five or more other kinds of mathematics. Make a chart for your classroom of the kinds you can find.







	보험하는 경상 사용을 보면 해결합하는 물을 받아 보면 보다 보다 보는 사용을 <u>보는 것 같다. 그리는 것으로</u>	(,
	Number Sentence	Property
	a) $320 \times 7 = (300 \times 7) + (20 \times 7)$	
	b) 643 x 29 = 29 x 643	
	(e) $287 \div 7 = (280 \div 7) + (7 \div 7)$	•
	a) $381 + (546 + 9) = (381 + 546) + 9$	
	e) 250 ÷ 5 = (200 ÷ 5) + (50 ÷ 5)	
- 24 - 24 - 3	r) 37 + 504 =/37 + 504	1
	g) 46 × 6 = (40 × 6) + (6 × 6)	
e. Li,	(a) $(23 \times 7) \times 18 = 23 \times (7 \times 18)$, V

Fill in the symbol = or # which makes each of the following a true sentence

Example: 324 + 415 / 748

- a) 47 + k/X 2 = T<2
- b) > 14 + 2 × 3 = 21
- c) $30 7 + 3 \neq 20$
- d) $(6.x)^2 5 = 7$
- e) \ 5 ≠ 3 × 5 ≠ 20
- $6 + 2 \times 3 \neq 12$
- g) $16 \div 2 \times 4 \neq 2$:
- h) 135 ÷ 5 + 3 = 30
- 1) 232 x 6 5 = 282
- $1) \quad 123 \times 3 3 = 0$

Write each of these sentences using numerals and the symbols for "less than" and "greater than".

- a) Three is less than five
- b) Fifty-eight is greater than thirty
- c) Eighteen is less than nineteen
- d) Four hundred five is greater than five
- e) Three tens are greater than twenty
- f) one thousand twelve is less than two thousand
- g) —Seventy is greater than sixty-two
- h). Nine hundred ten is less than ten hundred
- 1) Three hundred thousand is greater than three thousand
- J) Forty-six is greater than twenty-six.

	Example: $4 \times 364 = 1.456$, so $40 \times 364 = -14.560$
	a) 80 x 117 = 9,360 , so 800 x 117 =
	(δ) 5 × 766 = 3,830 , so 50 × 766 =
ant a Rhannevolution excluse	c) 9 × 36 = 324 , so 900 × 36 = _
	d) 30 × 592 = 17,760, 80 300 × 598 =
4	, e) 8 x 125 = 1,000 , so 800 x 125 =
	f) $3 \times 987 = 2,961$, so $30 \times 987 = \frac{1}{2}$
	g) 12 × 91 = 1,092 , so 120 × 91 =

	11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27
	Using the number line above find how many whole numbers are
Marie and the second second	between these numbers.
	a) 13 and 17 . e) 27 and 23
	b) 12 and 13 f) 21, and 20
Control of the Contro	c) 19 and 11 g) 15 and 17
	d) 19 and 25 h) 12 and 26
ST OFF THE STATE OF THE STATE O	. Copy and complete these sentences.
	a) A ray has endpoint(s).
and the second s	b) A triangle is the union of line segment(s).
	c) A line has endpoint(s).
	d) Space is the set of point(s).
100	e A line segment has endpoint(s).
A service of the serv	f) A radius is a line segment with endpoint(s)
P. Harris arrival to 1970 or exist of 1	on the circle:
	g) A quadrilateral is the union of line segment(s)
The same of the sa	

Column II

Column II

Column II

AB

Cope

Part B

Write a mathematical sentence (or two sentences if necessary)
for each problem and solve. Write an answer sentence.

- 1. The Clark family traveled 387 miles in 9 hours. How many miles did they average each hour?
- 2. During Public Schools Week, 1,162 people visited Pine Grove School, 1,219 visited Sleepy Hollow School, and 1,094 visited Thrand Valley School. How many people visited the three schools?
- 3. Dean and Gail have stamp collections. Dean has 364 stamps.

 He needs 37 more to have as many stamps as Gail. How many stamps does Gail have?



children would need to make two pictures?

- 51 A jet liner averages 449 miles an hour between Los Angeles
- and St. Louis. The trip takes four hours. How many air
- . miles is it between the two cities?
- 6. How much more do I pay for two shirts that cost \$2:15 each than for one shirt that costs \$3.29?
- 7. The price of potatoes is 5 pounds for 29 cents. What is the cost of twenty pounds of potatoes?

Group Activity

Tic, Tac, Toe

The objects of the game are speed and accuracy in addition. This is a racing game. Each child draws intersecting line segments as shown. The sum is announced by the teacher. The children put single digit addends in squares so that each row gives the sum. $6 \mid 5 \mid 2$

Example: Sum is 13. 4 3 3 6

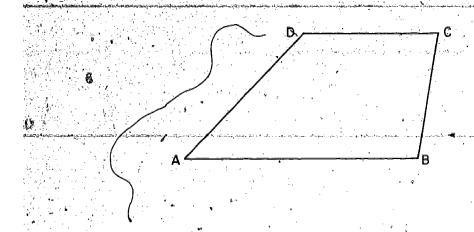
Individual Project

Use only polygons to make an interesting drawing. See how many polygons your classmates can identify.



RECOGNITION OF COMMON GEOMETRIC FIGURES REVIEW OF TRIANGLE AND QUADRILATERAL Thinking Together 1) a) What name is given to a polygon, which is the union of three line segments? The three line segments are called the sides of the triangle. b) What is the common endpoint of any two sides of a triangle called? c) What are the endpoints of the line segments of a triangle called? d) How many sides and vertices does a triangle have? What is a polygon which is the union of four line segments called?

with sides \overline{AB} , \overline{BC} , \overline{CD} , and \overline{DA} .



Let us recall that <u>quad</u> suggests four. In the figure shown above four angles are formed. They are \(\textstyle DAB, \textstyle ABC, \)
BCD, and \(\textstyle CDA. \) There are some points of these angles that are not points of the quadrilateral because angles are made up of rays.

The vertex of one of the angles is called a <u>vertex</u> of the quadrilateral.

The vertices of these four angles are called the vertices of the quadrilateral.

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Andrew Marine Committee Co
Exercise Set 1
i. a) Four points are marked below. Trace these points on a
sheet of paper and label them as shown.
• F
• G
H•
b) Draw EF, FG, GH, HE.
2. On the sheet of paper on which you drew the figure for exercise 1 write answers to the following questions:
a) Do these segments form a quadrilateral?
b) Name the sides of this quadrilateral.
c) Name a vertex of the quadrilateral.
d) Name the vertices of this quadrilateral.
e) Color the interior of the quadrilateral.
3. Go back to exercise 1. Trace the 4 points again on a
sheet of paper and label them as shown:
a) Draw EG, FH, EH, and FG.
b) Do these segments form a quadrilateral? Why?
419

4.	a) Four points are marked below. Trace these points on a
ENGLISHED TO THE THE PROPERTY OF THE PROPERTY	sheet of paper and label them as shown.
The Later Control of the Control of	Section of the Control of the Contro
	The state of the s
	Kanada kanad Kanada kanada kanad
Palitina Palitini Palitini	
	h) Draw IJ, JL, IK, and KI.
	And the second of the second o
5. ************************************	On the sheet of paper on which you drew the figure for
Maria de la companya	exercise 4, write answers to the following questions.
And the special bulk and the special s	(a) Is your figure a union of four line segments?
in this continue to the second	b) Do TK and KL lie on the same line?
The second secon	c) Is your figure a quadralateral? Why or why not?
And the second s	d) Is your figure a polygon?
	I that to a name for your figure?
ggi Kahlifi Kahung persentah caming signasi sari in me	e) What, is a name for your figure?
Marian Land	Mark three points (not all on the same line) on your
tige to the second of the seco	paper. Label them P, Q, and R. Draw \overline{PQ} , \overline{QR} , and
	a) Is your figure a polygon?
	b) Is your figure the union of three line segments?
	b) Is your figure the union of three line segments?
organism in the second	c) What is a name for your figure?
And the second of the second o	d) What is a triangle?
proprietable profit the service type and the servic	420
	t de la companya del la companya de la companya

COMPARING LINE SEGMENTS

Thinking Together

- 1) Henry says he thinks the line segment represented by the edge of his desk is longer than the line segment represented by the bottom edge of the door. Bill thinks differently. They have only a long piece of string. How can they find out which segment is longer?
- 2)—Bill says; "I can take this long piece of string and hold it at one corner of your desk. Then we can extend the string along the edge to the other corner. Let us hold this string so that it represents the edge of the desk."

"Henry, you hold your end of the string at one corner of the bottom edge of the door. I place the string along the edge leading to the other corner. Suppose the string does not reach the other corner. Then the segment represented by the bottom edge of the door is longer than that represented by the edge of your desk. If the string goes beyond the other corner, then the edge of the door is shorter than the edge of the desk. If the string matches exactly the bottom edge of the door from the string matches exactly the bottom edge of the door from the corner, the line segments represented are congruent.

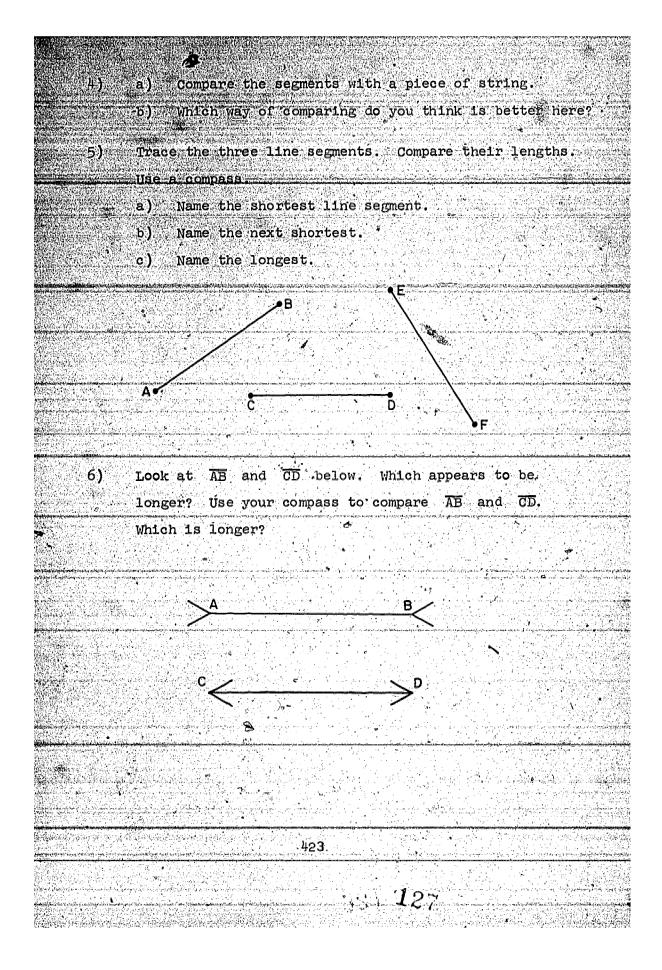
Bill says the line segment represented by the edge which runs from the top to the bottom of the door is longer than the line segment connecting the corner of his desk to the teacher's desk. How can Bill decide which is longer?

You can always compare line segments which are represented by objects if you have a piece of string that is long enough.

Another way to compare line segments is to use a compass



If you had only a compass and you wished to decide which of the represented line segments below is the longer, how would you do 1t? Follow the directions and you will learn how a compass may be used to compare the line segments represented above. a separate sheet of paper trace the above figure a) $\overline{ ext{CD}}$ is part of $\overline{ ext{CD}}$. Extend $\overline{ ext{CD}}$ to the edge of the sheet of . paper. Set the metal tip of the · b.) compassion A and the pencil tip of the compass on B. Without changing the setting of your compass, place the metal tip at C as if you were going to draw the circle with center at C. Draw just enough of the circle to intersect CD. Label the intersection T. If T is between C and D, then \overline{AB} is shorter than \overline{CD} . If D is between and T, then \overline{AB} is longer than \overline{CD} . If the point of intersection is D, then AB is congruent to CD (or AB and CD are congruent segments).



7) Compare AB and CD
Which is longer?
A C B
Exercises 6 and 7 shows us that sometimes we must use
an instrument to compare segments. We cannot trust our eyes
alone .
8) The line segments represented below are congruent.
a) Show that they are congruent by using your
compass.
b) Place a sheet of thin paper over AB and
trace 1t.
c) Move the tracing so that the dot marked A
covers point C. Can you make the dot marked
B cover D? The tracing of AB matches the
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drawing of CD exactly, endpoint for endpoint.
Butter Market Market and the control of the control
A
The state of the s
Of course, we have not actually moved AB:
We have moved a drawing of it.
・ 一般では、一般では、「は、「は、「は、」というないでは、これが、「は、」というないが、「は、」というないできます。 「は、」というないが、「は、」」というないが、「は、」というないが、「は、」」というないが、「は、」」というないが、「は、」」というないが、「は、」」というないが、「は、」」というないが、「は、」」というないが、「は、」」というないが、「は、」」というないが、「は、」」というないが、「は、」は、「は、」」というないが、「は、」」といいは、「は、」は、「は、」」というないが、「は、」」というないが、「は、」は、「は、」」といいは、「は、」は、「は、は、は、は、
9) If someone asked you to compare segments, which
method would you use?
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ISOSCELES AND EQUILATERAL TRIANGLES	
Thinking Together	
A triangle which has at least two sides congruent to each	
other is called an isosceles triangle.	
A triangle which has three sides congruent to each other	
is called an equilateral triangle.	
1. Which of the triangles below is an isosceles ,	
trlangle? Which is equilateral?	PART OF THE PART O
With the control of t	-14
Section residual description of the formation of the control of th	
Figure 1 Figure 2	-
Figure 1 Figure 2	
2. Are there any isosceles triangles suggested by	enen Ante
the edges of the models in your classroom?	
7. Are there any equilateral triangles suggested by	4
the edges of the same models?	
4. Name some things on which you see isosceles	
triangles represented.	رديد
5. Name some things on which you see equilateral	
f striangles represented.	i di Naj
425	
129	· 电阻
Spirit (Particle) was an always for the property of the proper	



	Exercise Set 2	
	Draw an isosceles triangle using only	
	a compass, pencil, and a straightedge. This picture may help you follow the directions of your teacher.	
		Service that general sections are also as a service section and the section an
	y c	
b)	Is AC congruent to AB?	*
	er for a minute, and a mortal demonstrated and a constraint of the	med i grande given gerina gerina eta garan eta gar Garan eta garan eta g
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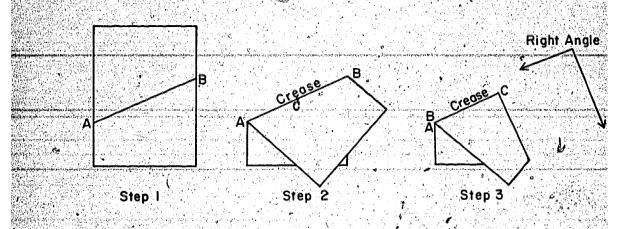


Draw an equilateral triangle using only a (a) compass, pencil, and a straightedge. This picture may help you follow the directions of your teacher. b) Is AB congruent to BC and to AC? Draw an isosceles triangle which is not also an equilateral triangle. Make one of its sides congruent to DE. 4. Draw an equilateral triangle. Make each of its sides congruent to DE of exercise 3.

Thinking Together

We have learned that an angle is the union of two rays which are not on the same line. The two rays must have a common endpoint. By folding paper we are going to represent an angle which is called a right angle.

Fold a sheet of paper. It is not necessary to have the edges even. The crease represents a line segment. Now fold the paper again so that the edges of the first crease line up exactly. The intersection of the two creases is the vertex of an angle. The creases represent part of the rays of an angle. Show these rays. The angle that is represented is called a right angle.



Does this page itself suggest a model of a right angle?

Name some other models of right angles in your classroom.



We shall use the right angle model to draw a right angle having a chosen ray as one of its rays. Let the ray represented below be the chosen ray. Draw a ray like this on a sheet of paper.

- 1. a) Label the endpoint of the ray as A.
 - b) Place the folded paper model of the right angle so that the vertex is at A and one of the creases lies along the ray.
 - c) Trace along the other crease from the vertex.
- There are two possible right angles which can be represented on the paper if the instructions above are followed. Draw both of these.

We shall use our model to compare angles with a right angle. Suppose we wish to compare /BAC, represented in Figure 1, with a right angle. On another sheet of paper copy /BAC. Then draw the right angle /BAD with AB as one of its rays. Draw it so that D is on the same side of AB as C. /Notice that AC falls between AB and AD. We shall say, therefore, that /BAC is smaller than /BAD. So /BAC is smaller than a right angle:

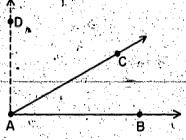
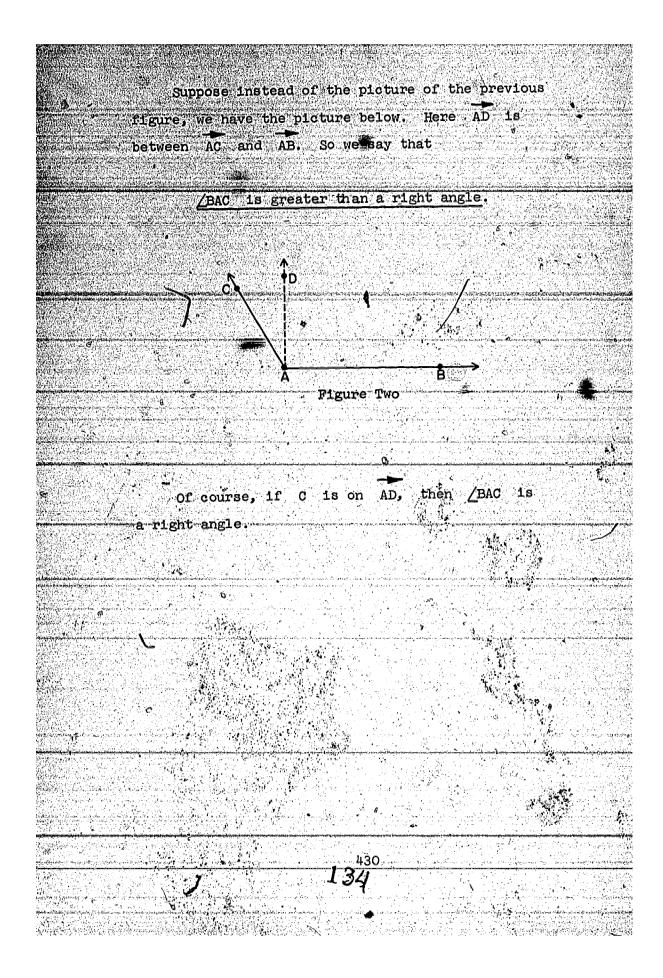
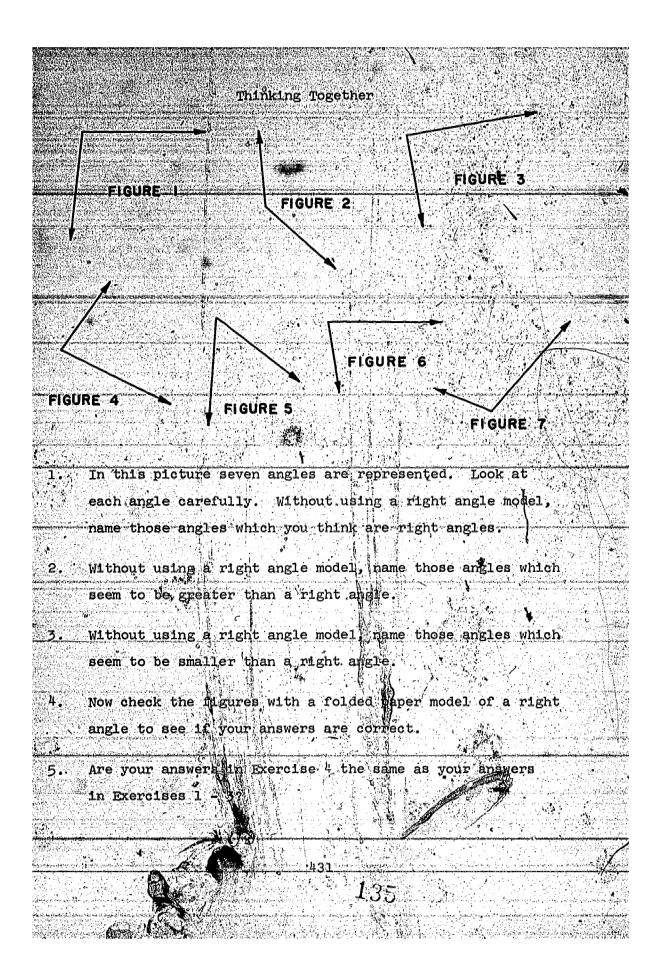


Figure .









6.	you see how an angle may be compared with a right angle if
ender de transporter de la companya	the angle has been represented by a drawing. Suppose an
	"object suggests an angle. How would you compare this angle
Property of the second	with a right angle? Find some object in your classroom
Territorial Company (1994)	which suggests an angle and compare it with your model of
	a right angle.
The state of the s	
elektronista eriteta eriteta en Utakina eta farrila (h. 17. augusta	Fare the angles represented by the edges of your desk right
	angles?
Aller 8	a) Do the hands of a clock ever suggest right angles?
All parties and the second of	
	b) Name a time when they suggest an angle less than a
7.0	right angle.
	c) Name a time when they suggest an angle greater than i
Productive to the state of the	a right, angle.
	Sue wants to know if the angle the hands of the clock
Transfer of the control of the contr	suggest when the time is 12:10 is larger or smaller
	than a right angle. She has a tracing of a right angle
The second secon	on thin paper. How might she use this tracing to decide
	whether or not the angle is larger or smaller than a
	right angle?
10.	Name some other objects which suggest right angles.
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RECTANGLES AND SQUARES

Thinking Together

If each of the four angles of a quadrilateral is a right. angle, we say that the quadrilateral is a rectangle.

- can you find edges of your book which represent a rectangle? Check with your right angle model.
- 2. Do the edges of this sheet of paper represent a rectangle? Check with your right angle model.
- 3. Can you find any models in your classroom which represent a rectangle? Check with your right angle
- 14. Name some objects at your home which suggest rectangles.
 - 5. How could you draw a rectangle using your right angle model?



Exercise Set

1. a) Is the quadrilateral represented below with vertices

A, B, C, and D a rectangle? Use your model of a right angle.



- b) Is AB congruent to BC?
- c) Is AB congruent to DC?
- d) Is BC congruent to AD?
- e) Is BC congruent to CD?
- 2. Which of these statements is true?
 - a) A rectangle has two pairs of congruent sides.
 - b) All four sides of every rectangle are congruent.
 - c) A rectangle has four right angles.
- 3. Make a copy of AD of exercise 1. Using AD as one side, see if you can draw another rectangle which looks different from rectangle ABCD of exercise 1.

Thinking Together

. A rectangle with all its sides congruent to one another is called a square.

1. Below is a representation of a square. Check the angles with your right angle model and the sides with your compass.



- b) Are all the angles right angles?
- 2. Name some objects in your classroom which suggest squares.
- 3. Name some objects in your home which suggest squares.
- 4. Is every square a rectangle?
- 5. a) Is every rectangle a square?
 - b) Are some rectangles also squares?

BRAINTWISTER

Draw a square using only the folded paper model of a right angle, a compass, and a pencil.



SURFACES

Thinking Together

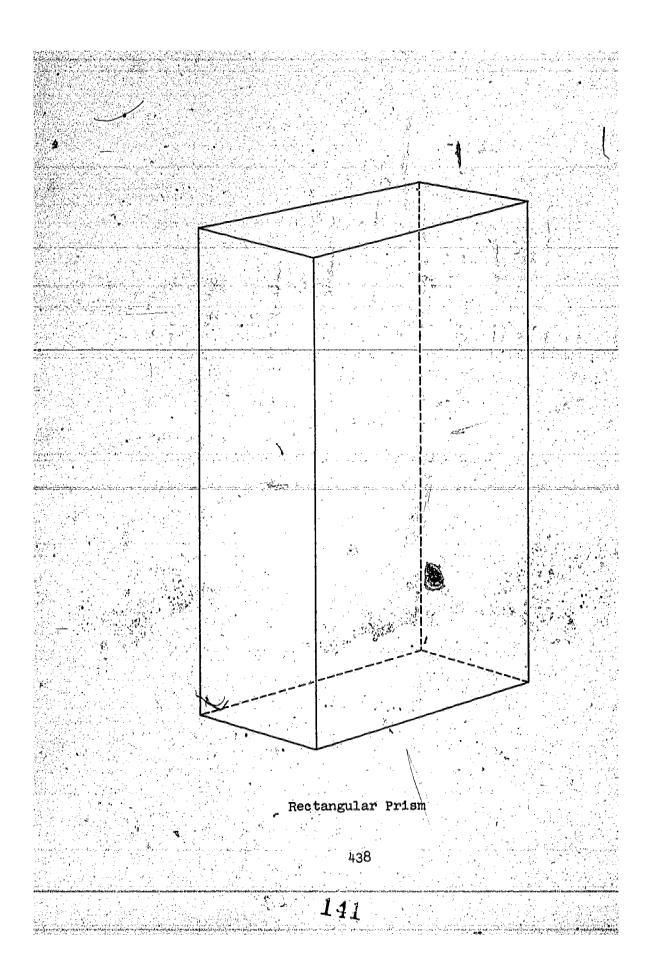
We are going to look at some objects. The surfaces of these objects represent sets of points in space. These sets have names which you will find below the pictures of the objects.

The objects are called models because they represent sets of points. Parts of the surface of some of these objects remind us of parts of planes because they are flat.

A closer look at these flat parts shows that one suggests a triangular region (a triangle and its interior). Another flat part of a model suggests the union of a quadrilateral and its interior. Still others remind us of circular regions (circles and their interiors).

Not all parts of the surfaces are flat. For example, the sphere, the cylinder, and the cone have parts of surfaces which are not flat.







Thinking Together

Let us look closely at this model of a rectangular prism.

Any one of the flat parts of the surface suggests a quadrilateral and its interior. The set of points on the flat part is called a <u>face</u>. The union of all the faces is called a <u>rectangular</u>.

prism. A rectangular prism consists of the entire surface of the model but not the inside of the model.

- 1. Look at a face.
 - a) Trace with your finger the edge of a face. The edges represent the sides of what figure?
 - b) Show with your finger the vertices of the rectangle.
 - c) Mark with your pencil three points in the interior of the rectangle.
- 2. How many faces does the rectangular prism have?
 The edges of the model represent line segments.
 These line segments are the intersection of two different faces and are called edges of the rectangular prism.

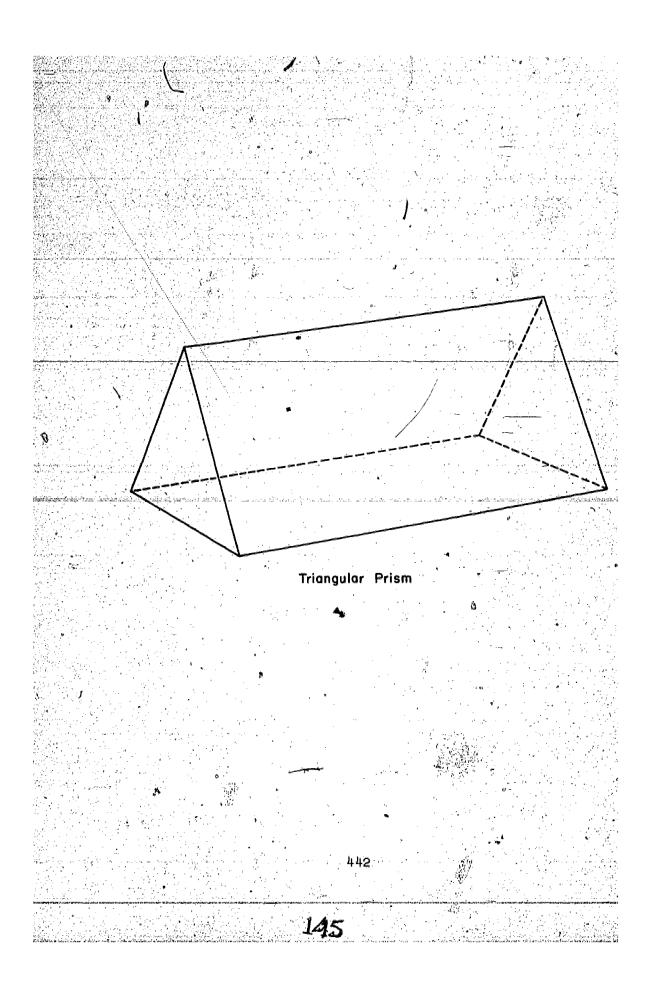
- 3. a) Trace an edge with your finger.
 - b) Show two faces whose intersection is this edge.
 - c) Count the number of edges of the rectangular prism. How many are there?

The corners of the model represent points. Each such point is called a vertex of the prism; it is also a vertex of each of the three quadrilaterals which come together at the corner. The plural of the word "vertex" is "vertices", so we can speak of one vertex and several vertices.

- a) Mark a vertex of the rectangular prism
 - b) What three quadrilaterals have this point as a vertex?
 - c) 'How many vertices does the rectangular prism have?
- 5. Name some other object which represent a rectangular prism.
- 6. If a wooden folgok were hollow, would it still represent a rectangular prism?

	Exercise Set 2
1.	Complete the following sentences, using a
	separate sheet of paper.
gade had englysi ferdilikket (af 1944 - englysiski af tradition of figure, in 1945 - englysiski af tradition of the second of th	Obligation (Control of the Control o
	a) A rectangular prism has faces.
	Each face represents a rectangular
	region.
	Tegion.
Bank the state of	b) The rectangular prism has
<mark>e de la desta de la desta de la desta de la composición de la desta de la desta de la defenda de la desta de la dela de la desta de la defenda del defenda de la defenda </mark>	edges andyertices.
機能 (A) (A) A (A) A (A	
2.	Is a rectangular prism hollow?
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Triangular Prism

Thinking Together

The model we will study next represents a triangular prism.

As in the rectangular prism, the flat parts of the model will represent plane regions which are called faces. The triangular prism is the union of the faces. (Notice that a triangular prism, as we have defined it, is "hollow".)

- 1. Are all the faces of the triangular prism the 'union of rectangular regions?
- 2. Indicate a face which does not represent a rectangular region.
- 3. What does this face represent? We call a face which represents a triangle and its interior a triangular face or a triangular region.
- 4. How many triangular faces are there?
- 5. How many rectangular faces are there?

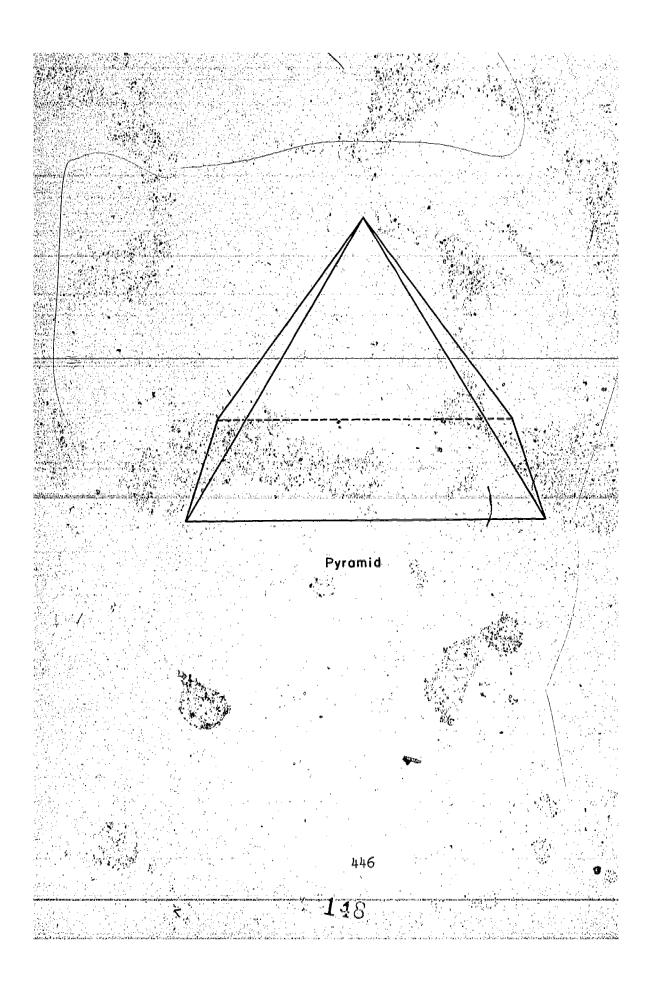
The triangular prism also has line segments which are the intersections of two faces and are called edges. The endpoints of the edges are called vertices of the prism. They are represented by the corners of the model.

- 6. How many edges does a triangular prism have?
- 7. How many vertices does a triangular prism have?
- 8. Name some objects which represent a triangular prism.



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	<u></u>	kerdise <u>Set 3</u>	
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	look at your mode	and write on a	separate piece
And the second of the second o	of paper the word	that complete	the following
and the grant state on the state of	sentences.	Andrew Broken	
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		N. W.	
	a) A triangular	prism has	triangular
	faces.		
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	b) A triangular	prism has	faces.
	*		,
		en e	
	c) A triangular	prism has	edges.
		34	***
	d) A triangular	prism has	vertices.
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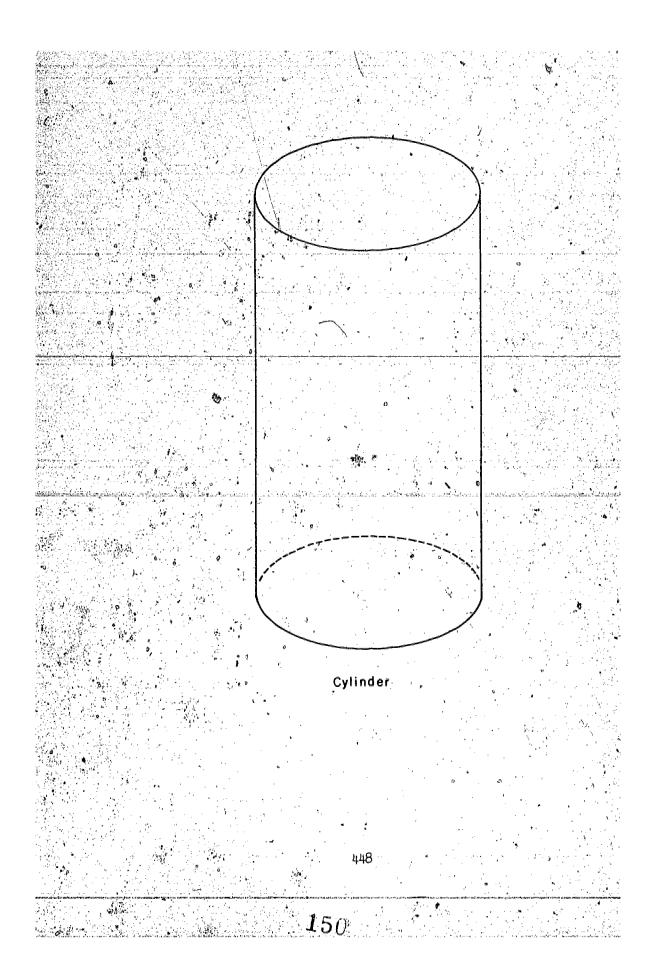
Pyramid

Thinking Together

Look at the model of the pyramid pictured on page 446. It is made up of flat parts only, like those of a prism. These suggest parts of planes, and as in the case of the prism, they will be called faces. The pyramid is the union of these faces. (Notice that a pyramid, as we have defined it; is "hollow":) Faces next to each other intersect in a line segment which has endpoints called vertices.

- i. a) How many triangular faces does this pyramid have?
 - b) Are there any faces on this pyramid which are not triangular? Trace this face with your finger.
 - c) How many faces are there on this pyramid?
 - d) How many vertices are there on this pyramid?
 - e) Put your finger on a vertex which is the intersection of three faces.
 - f). Show a vertex which is the intersection of four faces.
 - g) . How many edges does this pyramid have?
 - h) Trace with your finger four edges which intersect at a vertex.
- 2. Name some objects which suggest a pyramid.

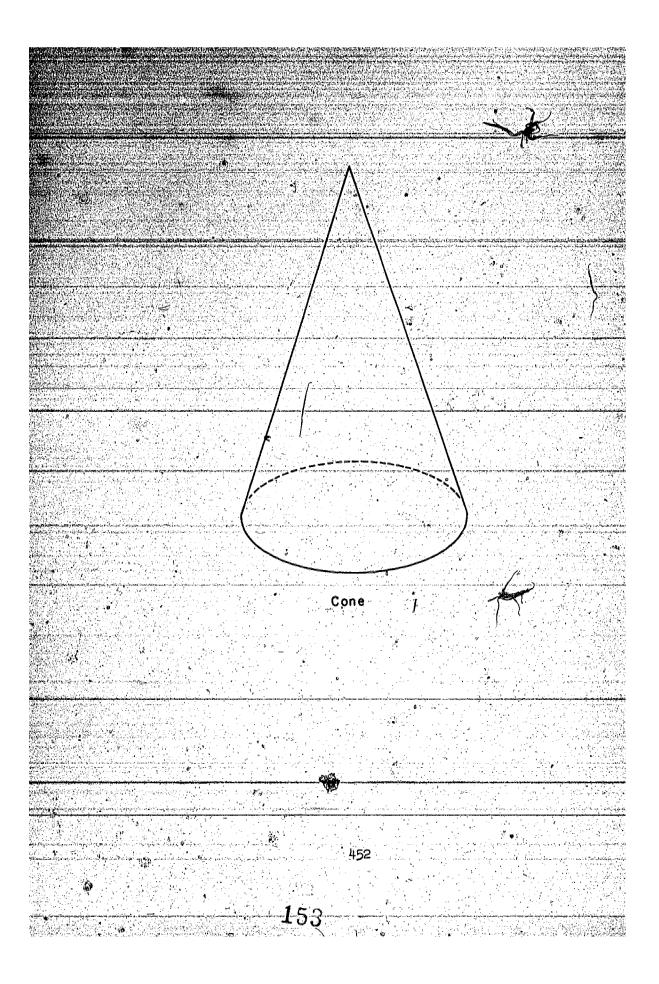






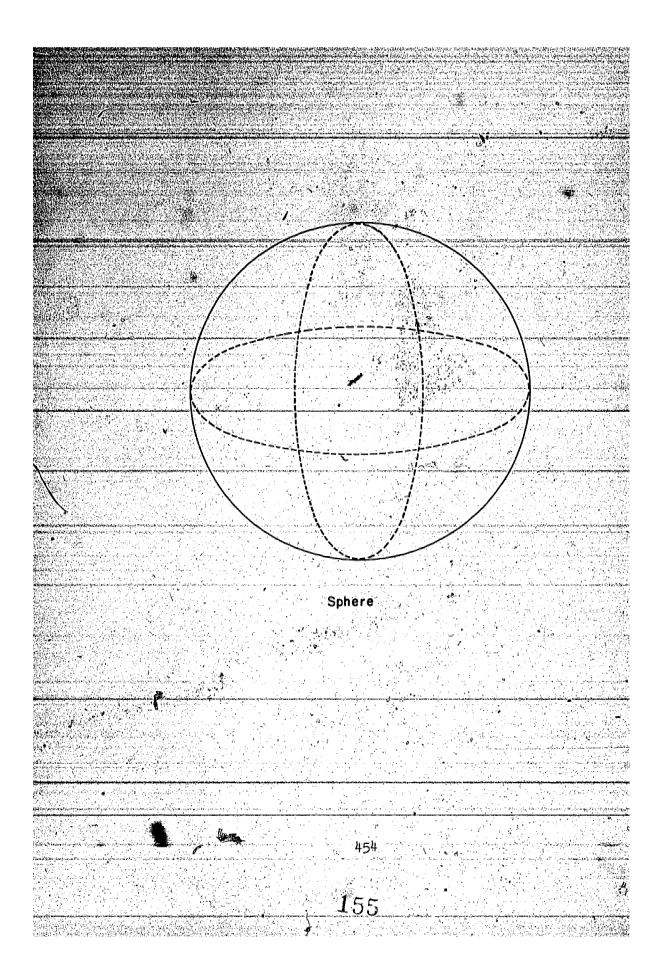
	And the state of t
Let us look at the model of the cylinder which you he brought to class.	ave
1. a) Are all parts of the surface of the	
model flat?	
b) What do the flat parts represent?	and the common production of the common produc
c) Are the circular regions the same size?	
Remove the top and bottom of a	
box which is the model of a	
cylinder. Make one straight	
cut as shown in the picture.	makey searces profit trade for their
Spread out the part just cut	
so that it lies flat on the desk:	and the state of t
2. a) What geometric figure is represented?	
b) Does this suggest how you might construct	
a model of a cylinder?	
c) Fut the parts of the box together/again	, i
so that it is a model of a cylinder.	
3. Name some objects which represent cylinders or	
parts of cylinders.	
449	رسيده مو ايون د خط دورگرده دد. د از د در دورگرد کرد در فورد د از در
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Not all cylinders are like the oatmeal boxes or the cans that you brought. Your models are examples of a special kind of cylinder called a circular cylinder. Circular cylinders have circular regions for bases. Many cylinders do not have circular regions for bases. Look at this picture of a culmder. Its bases are not dircular Take a can which is a model of amircular cylinder. Take out both bases. Press it down like this: Think of bases that are oval regions being put on the can. Now we have a model of a cylinder which is not a circular sylinder. Try to find a model of a cylinder which is not a circular cylinder. Sometimes toothbrushes come in this kind of container. Would part of the front or the back fork of a bicycle be an example of a cylinder?





one:	Thinking Together	
	can see from the photographs that the model of a cone cent from that of a cylinder.	
1.	Describe ways in which the model of the cone	
	differs from that of the cylinder.	Direct surface and
2.	a) What geometric figure does the flat part suggest?	and the state of t
Marken de la come de Antique Marken de la come de la come Marken de la come de Marken de la come de	b) Place the model of the cone so that the	
	flat part is on a sheet of paper and trace .	and trights 🖺 gift with g
	around the edge. What is represented?	
3.	What is represented by the tip of a model of a cone? The point represented by the tip is called the vertex of the cone.	
hairmanni mara	Suppose the model of a cone is	a tagan ya sa ku yana dagan da sa ya Kanasak sa garan da sa sa kana kana kana Baran
Anton Appelline in the St.	cut in half so that the cut	
	passes through the vertex and drvides the circular region into parts of equal size. What will the cut edge represent? The cut edge is	
	shown as the heavy line segments in this drawing.	No.
5.	Name other objects which suggest comes or parts of co	nes.
6; *	Ts a cone-hollow?	
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mhe	surface of a ball or a globe is a model of a sphere	
		Alter Comments of the Comments
1.	Look at the shadow of a ball on the sidewalk when	
	the sun is directly overhead, or look at the shado	N
	made by a ball with a light directly over it.	
	What does the edge of the shadow look like?	
- 2	Cut a model of a sphere into two pieces of equal	(a) income y reportal through
ence (nec	size.	is all the grant grant of the con-
	What geometrical figure do the edges of each half	
	of the sphere represent?	
3.	Place one of the halves of the sphere on a flat	
and the second section of the sectio	surface so that the cut edge is against the flat surface. Trace around this edge.	n train, com soli ancie dos ligidos plantas. A como esta de la como esta de
	What does the drawing represent?	
		المراجع المراجع المراجع المراجع
4.	Do you think that all the points of the half	
	sphere are the same distance from the center of	
	the circle that is represented by the edge?	
5.	Does this suggest that there is a point inside	
	the sphere that we might call the center?	
		nd in English was in the control of
energy is the second	Control of the Contro	A Secretary of the Secretary



6.	Think of a tetherball, when the rope	1/8 -t1e	htly.
	stretched, the ball is always the sa	证的现在分词	and the state of t
	from the point where the rope is atta As the ball moves around	ioned 	The second secon
	into different positions; do you think the point		tightly stretched
	where the rope is	pomijos (Bunis I. 1886) Pomijos (Bunis I. 1886)	rope
	attached to the ball;		
	goes through points on a sphere?		
The property of the control of the c		eigesteiskaan kirja aa olima 1 maart – 1 maar	
7.	How would you describe a sphere?		
	and the state of t	nada ang magalika kanana ang maga	
8.	Would the description of the sphere	as ^{II} the	set of
	all points in space that are the sam from a chosen point called the cente	· · · · · · · · · · · · · · · · · · ·	An all a shared have
MAN CONTROL AND CONTROL OF THE CONTR	description?		
946	How does this description differ fro	m that	of an circle
10.	Ta a sphere hollow?		
			The second secon
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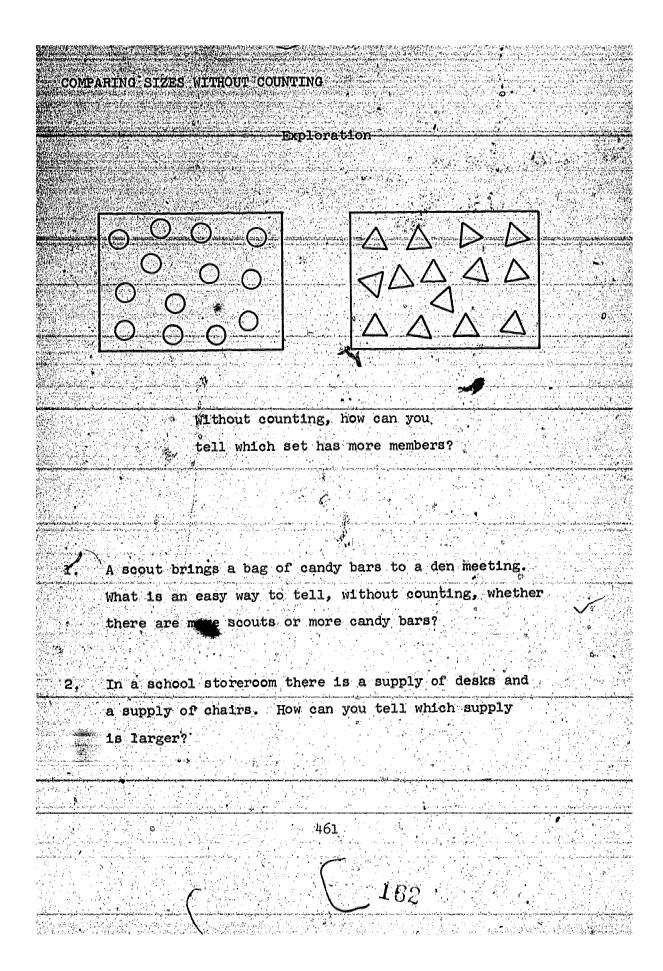
EDGES AND	FACES					
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	and an experience of the second	AND THE PERSON OF THE PERSON O	triangular p with your ri	arabita /		entre Control
2.	Do any e	dges of a	pyramid form	n a rectang	le?	
Mark Line and Property Pro-	Check wi	th your ri	ght angle mo	del.	property in a second control of the	
<u>**</u>	How many	faces of	the rectangu	ılar prism	have	-College and Artist
	edges wh	ich form a	rectangle?	arta artifica a parta un tega an especial tripid under comme		
programme and the second	How many	faces of	the triangul	lar prism h	ave	alan ayan saki
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5.		faces of	the pyramid	have edges	which.	
6.	triangul	ar prism.	of a rectar	ld. Copy t	De la constantina de la constantina en la constantina de la constantina del constantina de	
		g table on lank space	, a sheet of s.	paper and		
		Number of Faces	Number of Vertices	Number of Edges	Number of faces plus number of vertices minus number of edges	
Rectangul	ar prism					
Triangula	r pr‡sm					
Pyramid		A THE RESERVE OF THE PARTY AND A PARTY OF THE PARTY OF TH	Anna and a second	- Adding and the second second		
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The state of the s	The William Control of the Control o
	vertices of the rectangular prism. Subtract
	the number of edges from this sum. What is
	your answer?
SECTION OF THE PROPERTY OF THE	
And the state of t	
Principality and the principal of the probability of the principality of the principal	Do the same for the triangular prism and the
	pyramid. What is your answer in each case?
	Look at other geometric figures made up-of
	portions of planes. Is the number of faces
	이 시마스의 등 전기 때에서 이 사는 사람들은 아이를 살고 있다. 그녀야만 하고 마음이나요? 인경을 가져갔다.
	plus the number of vertices minus the
	number of edges the same for these geometric
	figures ?
godinistrature minimum i suntaturi mana per un di	Do you think you will always get the same
	answer if you add the number of faces and
	the number of vertices, then subtract the
Parlicipies of comprehensive and an analysis of the state of the comprehensive and the c	number of edges of any geometric figure
	which is the union of parts of planes?
e)	Write a mathematical sentence for your
	answer of 6d.
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Chapter 9		
LINEAR MEASUREMENT		
COMPARING SIZES		
Greations About Size		
Exploration		
How_many_of the questions you ask and other	people ask	
begin, "How much?" "How many?" "How far?"		Andrew Commission of the Commi
We say: "How many pupils are there in your "How long is/the hall outside your		
"How far is it to New York?"	e militarian rapidagai erikiren pakemaan militaria 1900 - Parin Pa	
Andrew Market Control of Control	and the second s	and American Agram a major of program of the American property and the American program of the American Agram
To answer these questions, we use numbers.		
There are 32 pupils in the class		
The half is 320 feet long.		
/it is 750 miles to New York.		
Answers to some of these questions can be of		ners gener hers general en els stapens et familie de la se
other answers can <u>not</u> be found just by counting.	新祖 医墨门克特氏层	
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1. The size of your class	
2. The height of the tallest boy in your	class کیرُ
3. The size of your family	
4. The size of your classroom	
5. The length of a book shelf	
7. The size of the smallest fock in the	collection
8. The population of your town	
9. How hard the wind is blowing	
10. The size of a bloycle wheel	nes riconos colos de resumente de proceso en escarca de desentación de desente de desente de consecuente de co
Think of a rock collection. What can you	tell about the
rock collection by counting. Is there somethin	ng you cannot
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rock collection by counting. Is there somethin	ng you cannot
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Which rope do you think is longer, A or B? To compare dirves like those in the pictures, lay a string along each ourve. Then straighten out the strings. What geometric figures do the stretched-out strings represent: 462		How can you tell how the attendance at a movie compares :
you can compare the sizes of single objects whose size can not be found by just counting. 5. Here are pictures of two pisces of rope. A B Which rope do you think is longer, A or B? If you had the ropes instead of the pictures, how could you tell which is longer? To compare curves like those in the pictures, lay a string along each curve. Then straighten out the strings. What geometric figures do the stretched-out strings represent?		
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If you had the ropes instead of the pictures, how could you tell which is longer? To compare curves like those in the pictures, lay a string along each curve. Then straighten out the strings. What geometric figures do the stretched-out strings represent?		
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Suppose you wish to compare AB and CD. To prove to someone that CD is longer than AB, stretch a string on AB ... With your fingers, hold the points of the string that fall on A . and B. Move the string and place At on CD with one endpoint on C. Is the other endpoint on D? Since it is between C and D, $\overline{ ext{CD}}$ is longer than AB. How is comparing segments, to see which is the longer, something like matching groups of separate objects to compare the sizes of the groups without counting? There are many things which are enough like our idea of 7. a line segment so that we can think of them as line segments; for example, a stretched string; some pencil marks on paper, the edge of a table, a pencil. Name several other things which we might think of as line segments.

8. Remember that between any two points in space there is just one line segment. If we have any two objects which we think of as points; we can also think of them as endpoints of a line segment. This is what we mean when we say:

the distance between the two tips of a compass, the distance between the earth and a star, the distance from home plate to second hase the height at which an airplane flies.

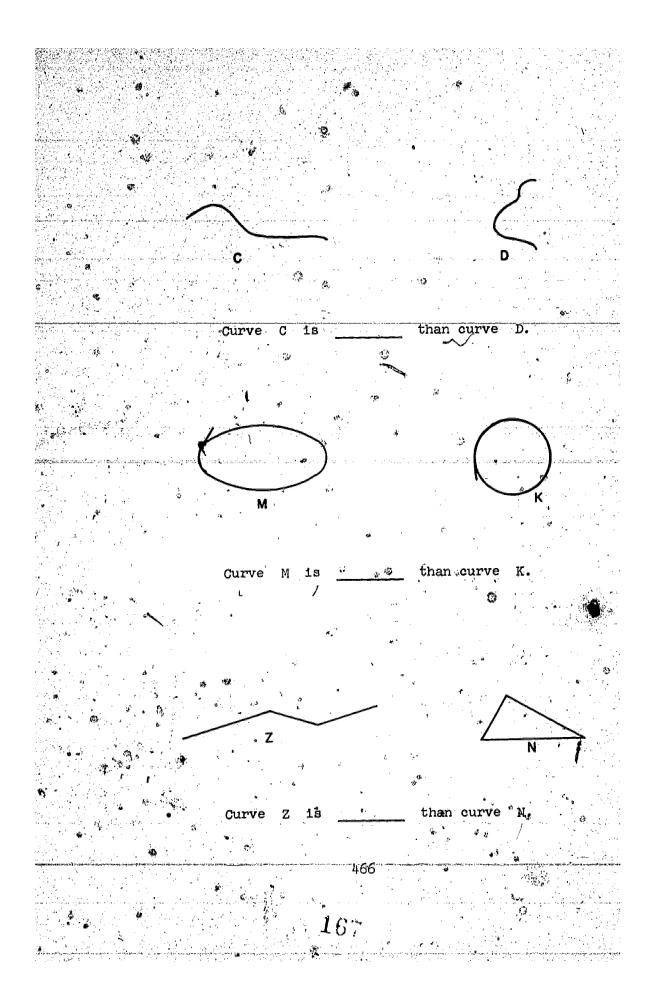
Name several other ways we think of line segments by

9. The way you go to school is probably not much like a line segment. A picture of it might look like this:



We can still talk about the distance you travel in going to school. Your path can be thought of as a curve, but not as a line segment. What does distance or length mean for curves? We think of the curve as represented by a piece of wire or string. Then we imagine straightening out the wire or string to represent a line segment.

Use strings to compare the line segments and other curves. Copy each sentence below the figures and write "longer" or "shorter" in the space.

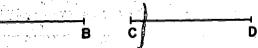




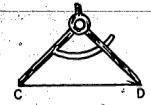
USING A COMPASS TO COMPARE SEGMENTS

Exploration

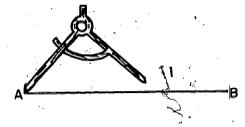
Is AB longer than , CD?



Recall how you have used a compass to compare segments.
Place the points of your compass on C and D.

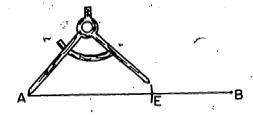


Without changing your compass, place the sharp point on A.



Draw a small part of a circle which intersects AB.

Label the intersection E.



E is between A and B, so \overline{AB} is longer than \overline{AE} . \overline{AE} has the same length as \overline{CD} , so \overline{AB} is longer than \overline{CD} .

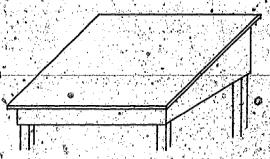
Exercise Set 2 Trace the following figures on your paper. Use your compass or string to help you compare segments. Copy and answer the question for each exercise. Color the unmatched part of the longer segment. Which is longer, AB orWhich is longer, Which is longer,

MEASURING SEGMENTS
Measuring a Segment

Exploration,

You know that you cannot tell the size of a segment by just looking at it and counting. You can tell how long it is by comparing it with some other segment.

How can you tell how long
your desk is?
What-geometric-figure-does
the edge of your desk
represent?



Take your pencil.

Lay it along the edge of your desk, with one end on the corner

Put your finger on the desk at the other end of the pencil.

Lay the pencil down again from that point.

How many pencils long is the edge of your desk?

Give your answer to the nearest whole number.

2. People often use their hands to tell how long a segment is.

Spread your right hand so the fingers are as far apart as possible. Place your right hand with your thumb on the left corner of your desk. See how many hand-spans long your is.

The segment represented by your pencil of your hand-span is called your unit of measure.

The number of pencil-lengths or hand-spans it took to cover the edge of your desk is the measure of your desk. A measure of your desk may be 7.

To name a flength, we use beat the measure and the unit of measure. A length of your desk may be 5 hand-spans

		Exercise Set 3
and the head for	Сору	and complete each of the sentences.
	1.	Our family drinks -3. quarts of milk each day.
		a. The unit of measure is
ktorikaja die karalija selepa setem Karalija die karalija die karalija Karalija die die karalija die ka		b. The measure is
		c. The amount of milk is
	2.	My dog weighs 18 pounds.
		a. The unit of measure is.
		b. The measure is
		c. Its weight is
) salah sala	My desk is 9 chalk-pieces long.
10	3	a. Its length is
	elil erkeyelika	in kalada je najveli plitanja i troja, monio postava i roka in popera kao koje je zavelna i pojekti koje proje
		o. The unit of measure is
	3 - 1	
		In Exercises 4-9 use the words length, measure, or
	3.	of measure, so that each sentence will make senee
	420	It takes 6 chalk-pieces to cover the edge of the desk.
		Its 1s 6.
	5.	My desk is 4 pencils long. Its 4 pencils.
	6.	My desk 1s M hand-spans long
		The is the hard-syan
	7.	The in hand-spans is 5.
	8.	The I used is a segment.
		represented by one pencil.
	9,	The edge of my desk has a of 4 pencils.
	and the desired	470
		171.



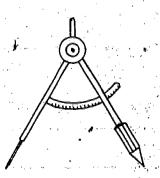
USING A COMPASS TO MEASURE LINE SEGMENTS

Exploration

We want to find the measure of \overline{CD} .

We use our compass to help us

measure a line segment.



Our unit of measure is \overline{AB} .

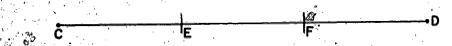


We lay off the unit \overline{AB} on \overline{CD} .

We lay off \overline{AB} on \overline{CD} three times.

We label the intersections E and F.

See the picture below.



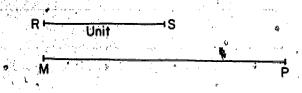
We write: $m \overline{CD} = 3$

What is the measure of \overline{CE} ?
What is the measure of \overline{CF} ?
What is the measure of \overline{ED} ?

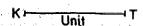
Exercise Set 4

Copy each of the segments in exercise 1 and 2 Find the measure of each segment.

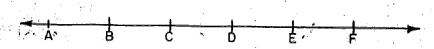




2



3. Tell the measures of the segments in the figure.



$$m \overline{AE} =$$

$$m \overline{BE} =$$

$$m \overline{BF} =$$

4. Write the name of any segment which has the measure given.
Use the unit and figure for Exercise 3.

MEASURING TO THE NEAREST UNIT

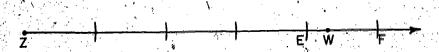
Exploration

We want to find the measure of \overline{ZW} .

We use AB as the unit of measure.

Å É

This picture shows how we can find the measure of \overline{ZW} , using \overline{AB} as unit.



How many times can you lay off the unit on \overline{ZW} ?

m \overline{ZE} = 4. Is m \overline{ZW} larger than 4? Why?

m \overline{ZF} = 5. Is m \overline{ZW} smaller than 5? Why?

The measure of \overline{ZW} is between 4 and 5 units.

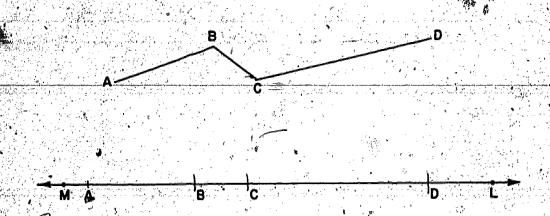
Since W is nearer to E than F, we say

m $\overline{ZW} = 4$, to the nearest unit.

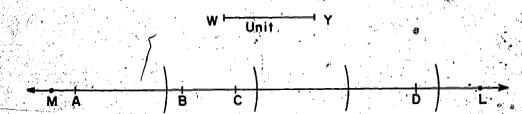
			des Cat F		le:
		Exerc	eise <u>Set 5</u>		
Tra	ce the figures	in each of	the following	exercises.	
Fin	d the measures	s of the segm	ments to the ne	earest unit.	
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				And the second s	
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7		en e			
	R	LE.	s s	• Unit	
		en .			
	The length	of RS is g	reater than _	units but	
	less than	units.			
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			75.		9)

BRAINTWISTER:

On ML draw a segment whose length is the length of the curve ABCD.



Now find the measure of curve ABCD. Use WY as unit.



The length of curve ABCD is greater than ____ units but less than ____ units.

m ABCD = _____, (to the nearest unit)

USING STANDARD UNITS OF LENGTH

Exploration

Suppose a team of boys from your school were going to play a game of baseball with a team from another school. If the other team brought a baseball so large and heavy you could hardly lift it, what would you say? You would probably say, "We will not play with that baseball. It is not the standard size and weight." What does that mean? Can you find out the standard size of a baseball?

You have been using units of measure which were not of "standard" size. Now we shall use standard units, which are used by a great many people and which always mean the same amount. The size of a standard unit is set by law.

Your encyclopedia contains information about the National Bureau of Standards in Washington, D. C.

In which of the following sentences are standard units used?

- 1. He is as strong as an ox
- 2. Put in a pinch of salt.
- 3. We get $\frac{1}{2}$ pint of milk for tunch.
- 4. The corn is knee high.
- 5. I used to live a day's journey from here,

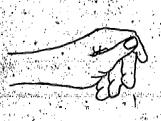
You are familiar with many standard units. Name some of these units.



Primitive people had little need for standard units. If the caveman liked the size of his neighbor's spear, he could borrow the spear and copy its length. Or, he could think, "When the spear is held with one end on the ground, the other end reaches my shoulder." Then, he could make a spear with that same length.

Many of the standard units which we use came from units which were not standard. These were used by people long ago.

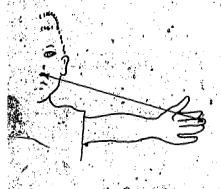
Many of them came from using parts of the body.



An inch came from the use of a part of a finger as a unit of length. Can you find a part of your finger which is about an inch long?



A foot came from the length of a person's foot. Is your foot shorter or longer than a foot ruler?

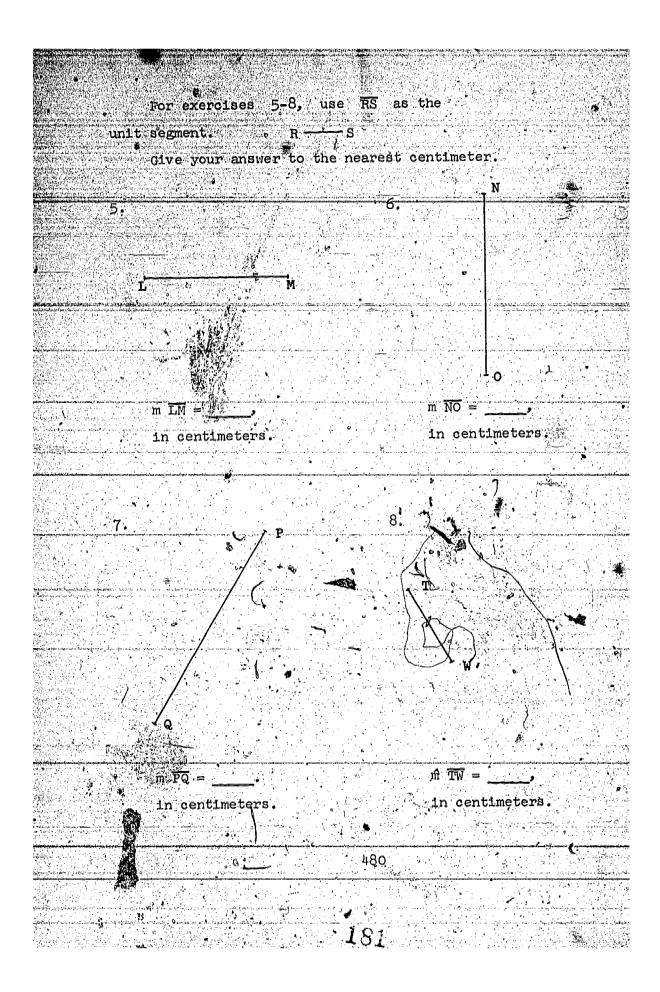


A yard was at one time thought of as the distance from the tip of a person's nose to the tip of his middle finger, when his arm was held straight out from the shoulder. Is the distance from your nose to the tip of your finger as long as a yardstick?



projects	Here is a model of a standard with
	You have often used this unit
	A B
Experience makes a second of the second of t	Inch
	Tt 1s the inch.
And the state of t	Name some objects you measure in inches.
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	page of the control o
The state of the s	ere is a model of another standard unit.
	This unit may be new to you.
Make the provider relating to the control of the co	The state of the s
Allen and Allen	It is the centimeter.
And the second s	
	If you lived insFrance, or in many other countries,
	you would use this unit segment instead of the inch.
	Scientists in all countries use this unit.
And the state of t	
And the second s	478
The first of the f	

Exercise Set 6 Trace each figure in exercises 1-8 on your paper. Use your compass or string to find the measures of the segment. Copy and complete the statement for each exercise. For exercises 1-4, use AB as the 👪 1't segment. Give your answer to the 🥻 nearest inch. in inches





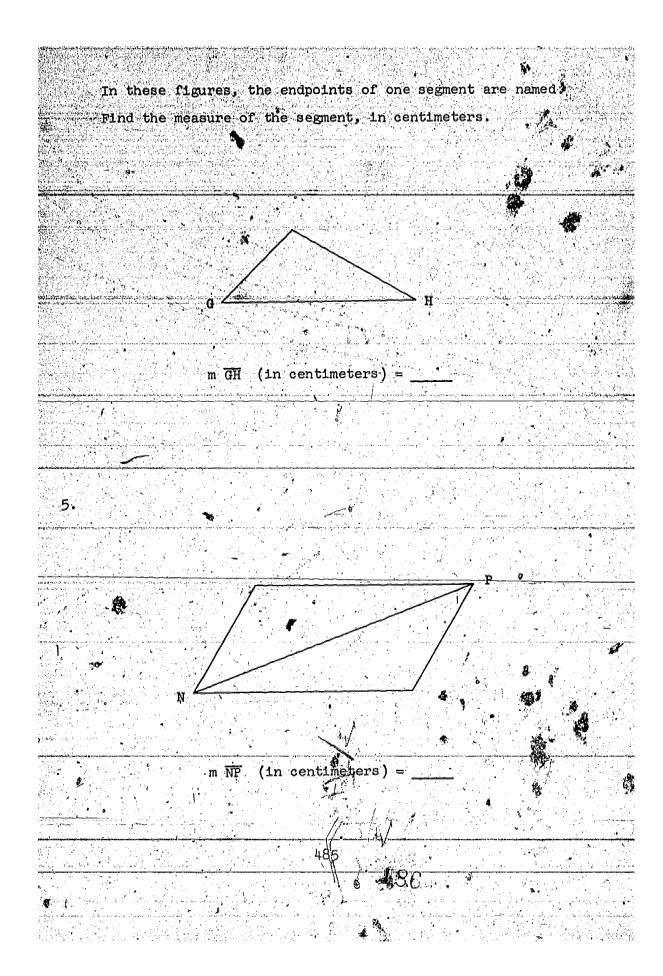
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	m \overline{ZW} (in centimeters) =				
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	a <u>scale</u> . Follow these dire		an inch scale	
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	1. Write zero below	and the state of t	和军事 海绵	your compass
Historia Services	to copy the inch	ાને અનું કું કું કોન્સિનો ફ્રેક્ટ્રિક માટે મહામાનું કે કહા	beginning #1	Label-the
destal in all refress to the second	other endpoint			
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s, make a centimeter scale. What is the largest number on your centimeter some? What is the largest number on your inch scale? Does your centimeter scale look like this one? centimeter Save your centimeter scale, too. You dan use your scales to find the measure of a segment Win inches and in centimeters. Copy and find the measure of KW, in inches. Place your compass with the points on K and W. without changing your compass, place the sharp point of the zero point of the inch scale and the pencil point on the ray. What point on the scale is nearest the pencil point? What is its number? What is the measure of KW in inches? Find the measure of KW in centimeters. Use your compass and scale.

```
Exerclse Set 7
using your fach scale and your centimeter scale, find the
measures of these segments.
Find the measures in inches and in centimeters.
                      (in inches)
                  m AB
                       (in centimeters)
                        (in inches)
                        (in centimeters)
                  m EF (in inches)
                  m EF (in centimeters)
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	THE INCH SCALE AND THE CENTIMETER SCALE	
	Exploration (
Agrical Control of the Control of th	You have made an inch scale and a centimeter scale you have used these scales to find measures of lin	and the same of th
	You have found measures of line segments in other	a a digitation and the state of the designation of the state of the st
	Now we will use only the scales of measure.	
	We find the length of \overline{AB} .	
bilanii princesto de Literatura	edistribution manufacture and structure for Artist in Annal Artist in the Artist in the Artist in Artist in An Landaus and Artist in Art	And the second s
		(o
	i. We can place our scale along AB like this:	. T. V.
	A B	
	0	4
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in the same of the same of	2. Here is another way of placing our scale.	
Garage Control on a most	Why would you place the ruler in this way?	to the second se
	Ą	and the second s
	0 1 2 3 4	5
	3. Are there other ways to place the ruler to f	ind the
Programme Company	length of AE?	
	The length of AB is 3 inches.	
	We write $m \overline{AB} = 3$.	
4	We read: The measure of AB is 3.	
	486:	
All and the second seco	magnetic many policies and service of the property of the property of the control	The art of the second s

When you used the scale to find the measure of AB you used it as a <u>ruler. A ruler</u> is a straightedge with a scale on it. Which of these drawings shows the correct way to place a ruler to measure a segment? Why? inch Find the length of CD, to the nearest inch. Place the scale along $\overline{\mathtt{CD}}$ as in the picture. What point on the scale is below C? ____ Point D lies between what two points on the scale? Is D closer to 3 or 4 on the scale? What is the length of CD, to the nearest inch? Give two other ways to use the scale to measure CD.

6	Here are plots Find the lengt Then; find the	th of each s e length of er.	egment to	the neare	信息 高铁铁路	
	The abbreviat. Write your ansone. a) c				in the f	irst
		gth of <u>CD</u> gth of <u>CD</u>				47. 星乳层型槽
	b) /E -		F	4 В ж		
	d) x	y		X		
	e) þ.					R
7.\ 8.	Draw a segmen	alan da	length.			
			488 189			de tra de destada de la compansión de la

	Exercise: Set: 8	
1,	Find the length, to the nearest inch, of one of your pencils.	
2.	Find the length of the same pencil in centimeters.	
5.	What is the length of AB; in inches? What is its length in centimeters?	***************************************
54.	CD is 4 inches long. What is its length in centimeters?	
Marie Calego	Company of the second s	
*5.**	Draw a segment that has a length of 5 inches.	9
6.	Draw a segment whose measure, in inches, is 4.	
7.	Draw a segment whose measure, in centimeters, is 10.	a for fairness top of the fair
8.	Draw a segment that has a length of 14 centimeters.	agen met en
9.	Copy the sentence and white the words <u>inches</u> or	
	A segment which is 5 in length is longer than a segment which is 5 in length.	
	489	
Annahin Marinda dan	190	



OTHER STANDARD UNITS Exploration. The inch unit and the centimeter unit are too small to be used for measuring long distances. As you know, larger units thre used for this purpose. Three which you know are named the foot (ft.), the yard (yd.), and the mile (mi.). Recall what you know about these unit segments. Draw a segment 1 foot long. Draw a segment 1 yard long Draw other segments 2 ft., 3 ft., and 4 ft. long. Measure each of the segments in inches, List your results like this: Length in feet Length in inches inches inches inches inches Which of these segments was one yard in length? Draw a line segment 18 inches long. Name it AB. Mark a point C on \overline{AB} so that \overline{AC} is 1 ft How long is CB? The length of AB

Draw a line segment 29 in. long. Name it AB. Find a point Con AB so that AC is 1 ft. long. Then find a point D on $\overline{ ext{CB}}$ so that $\overline{ ext{CD}}$ is 1 ft. How long is AD? How long is DE? Draw-segments-with these lengths in inches-Then tell the length in feet and inches. Length in inches Length in feet and inches Segment .15 in. ~20 1n. On m mark of AB whose length is 1 foot. Then mark off BC whose length is 3 inches so that C is not on AB. What is the length of AC in feet and inches? What Mis the length of AC in inches? On ki mark off RS whose length is 2 feet. Then mark off ST whose length is 7 inches, so that T is not on RS. What is the length of RT in feet and inches? What is the length of RT in inches?

A PARTY SANCTON	<u>Segment Length in feet and inches</u> Length <u>in inche</u>
parting partition of the state	AB 2 ft. 1 in.
ericky (S. P. Aregennous) - Commission (M. Aregennous) - Commission (M. Aregennous)	元 Tift. 7 in
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BRAI	NTWISTERS
Appendix Berta Branch (Stage Special Stage Special Spe	After the second of participation of the second of the sec
1.	A mile is a distance of 5.280 feet. About how many
	steps would you take to walk agmile?
	If a car is traveling 60 miles an hour, how far will
	How long does it take you to walk a mile?
	An analysis for the second sec
3 • • • • • • • • • • • • • • • • • • •	Suppose someone ran a mile in 238 seconds. How many minutes and seconds did he take?
pater should have provided a major of the short	ing the trade of the property of the state o
egylegies 4. 4. 4. am terppe file (Carlo de princip de	Suppose the four men in a mile relay event ran their
	"quarter" mile in the times of 45, seconds, 47 seconds
	relay team to run the mile?
all the second forms by the second se	the first constraint of the graph and graph an

If segments have these lengths, which is longer?
a) (10 inches on 1 foot?
principle of the princi
c) 1 inch or 1 centimeter?
ty (d) l foot or 10 centimeters?
e) 1 ft. 7 in. or 2 ft.?
f) 28 inches or 2 feet?
2. Look at each segment and its measure, then write the unit.
Segment Length
A B 3 3
D \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \
\mathbf{E}
G. H
CH A
3. Complete:
Length in feet and inches Length in inches
$\overline{\mathbf{x}}$ 3 ft. 1 in.
MV
DE 1 ft: 10 in.
FG
493
A second of the
294



	reasonație. Use <u>centim</u>	eters, inches, fest, ya	rds, or miles.
	g) The seat of the te	acher's chair is/,16	aboye
de l'estevant est est au partir de la company de la compan	the fleor. b) Helen is in the fo	urth grade. Her height	18
	130		
	(e)): The Take 1s +		
	d) The height of a ta e) A crayon is about	把新越级的人们的人们的人们的 医二氏病	
	f) It is 2	from Bob's house	to the park.
1 5i	If segments have these	lengths, which is longe	
And State of the S	How much longer?	· 是一个一个一个一个一个一个一个一个一个一个一个一个一个一个一个一个一个一个一个	How much
		Longer?	Longer?
	b) 18 inches or 2		
	c) 4 feet or 1 ye		
	d) 1 ft. 8 in. or e) 1 yd. 4 in. or		
Whotepool Emerican Allocations are seen as	f-)====122ft.,.		
ham and high property in the first party of the fir	g) 1 mile or 3,49	5 feet	
6.	You know/that 1, mile	13 5,280 feet. How.n	any yards
Complete Sea of the Se	La Bhat?		
7		mile in 12 minutes 1 ow many miles can he go	产生。實際的關係的可能的人們的問題的問題
	the Boy Scout pace, He hour?	JW milety miles can	
and freed the public formulation above the company		494	
and the first of the second traces and	and a constant of the control of the		The state of the s
The second secon	we can be a considered to the considered and a positive for the considered by the considered and a considered to the considered and a consider		The control of the section of the se



Learning to combine Lengths . Pupil Height	
Prolocation Bill 4 ft. 8	
The teacher made a record of the Jim 5 next	Vonesse
heights of children in his Helen 4 ft. 6.4	
fourth grade class. The children knew that he meant Bill's height was 4 /rest	
and 8 inches. Betty s height was 4 feet and 2 inches:	
Jim's height was 5 feet and 0 inches. How many feet and	
inches is Helen's height?	
We often use more than one unit to tell sizes.	
How would you use more than one unit to measure the door	
in your classroom?	
2. /Now we will/learn how to combine lengths.	
Sue, Patty, and Janet are decorating a room-for a party.	
They plan/to put crepe paper around the Windows.	· ·
The girls had strips of paper with these lengths:	
Patty 4 ft: 5 in:	
Janet 3 rt. 2 in.	
Janet, 3 ft. 2 in.	
the light and the first of the control of the contr	
Janet 3 ft 2 in a) If they put their strips of paper endy to end it would look like this:	
Janet 3 ft. 2 in. a) If they put their strips of paper end to end it.	A Company of the Comp
Janet 3 ft 2 in a) If they put their strips of paper endy to end it would look like this:	
Janet 3 ft 2 in. a) If they put their strips of paper end to end it. would look like this: Sue's Patty's Janet's	
Janet 3 ft 2 in. a) If they put their strips of paper end to end it. would look like this: Sue's Patty's Janet's	The second secon
Janet 3 ft 2 in. a) If they put their strips of paper end to end it. would look like this: Sue's Patty's Janet's	
Janet 3 ft. 2 in. B) If they put their strips of paper end to end it would look like this: Sue's Patty's Danet's 6 ft. 3 in. 4 ft 5 in. 3 ft. 2 in.	The second secon



measures so that we use only one unit, the inch.
How many Inches of paper did Sue have? How many Inches of paper did Patty have?
How many inches of paper did Janet have? Now we can add the measures: 75 + 53 + 38 = 166.
The length of the paper was 166 inches.
Express this length in feet and inches. (b) We can show the combined strips by another sketch like this:
ار غال (5in. 3ft. 2in) غال (5in. 3ft. 2in)
c) Now let us think about the combined strips in a different order. We can show our thinking by this sketch:
6 // 4 // 3 // 3 5 2 // in in. in. in.
The answer could be found by adding the measures which go with the same unit.
6 / 6 / 6. 3 in. 6 / 4 / 4 / 3 = 13 $^{\circ}$ 4 ft. 3 + 5 + 2 = 10 5 in.
3 ft., 2 in.
Usually-we write:
6 ft. 3 in. 4 ft. 5 in. The girls have 13 ft
<u>3-ft.2-ip.</u> 10-in. of one paper
And the second s
496



Patryls - Janet's.
4.ft. 50in. 7. 3. Ct. 2 in.
The length of Janet's paper, in inches . 38 in:
We subtract the measures: $-53 - 38 = n$. 53
- 15 - 15 - 15 - 15 - 15 - 15 - 15 - 15
Patty's strip is 15 inches longer than Janet's. How many feet and inches is this?
b) We can work the problem another way. We subtract the measures which go with the same unit.
$4-3=1$ $3 \text{ ft.} 5 \text{ in.} 5-2=3$ $\frac{3 \text{ ft.}}{2 \text{ in.}} \frac{2 \text{ in.}}{2 \text{ in.}} \frac{3 \text{ ft.}}{2 \text{ in.}} \frac{3 \text{ in.}}{2 \text{ in.}} $
The work is usually written like this:
<u>3 ft. 2(in.</u>
The length of Patty's paper is 1 ft. 3 in more
than the length of Janet's paper.
:497

a football the farthest. See John 17 yd. 2 ft. the record of their distances. a) How much farther did Martin throw than Charles? b) How much farther did Martin throw than John? c) How many feet did Charles throw the ball? d) How far was the football thrown in three tries? Can we add the three measures? We can add only the measures which have the same unit
the record of their distances a): How much farther did Martin throw than Charles? b) How much farther did Martin throw than John? c) How many feet did Charles throw the ball? d) How far was the football thrown in three tries? Can we add the three measures?
b) How much farther did Martin throw than John? (c) How many feet did Charles throw the ball? . (d) How far was the football thrown in three tries? . Can we add the three measures?
c) How many feet did Charles throw the ball? : d) How far was the football thrown in three tries? . Can we add the three measures?
d). How far was the football thrown in three tries?
Can we add the three measures?
We can add only the measures which have the same unit
18 2
$\frac{1}{2}$
17 2
5 1 . (5)
The football was thrown 51 5
// // // // // // // // // // // // //
51 vd.
1 yd. 2 ft.
52 ya. 2 ft.
51 yd. %5 ft. is the same measure as 52 yd.
498
Constitution of the consti



1.	Dick has two pencils. One pencil is 7 inches long and	7
per la prima de la companya de la co	one is 6 vinches long. When put end to end his two pencils show a segment which measures ft. in:	one de la companya de
2.	Jane has a piece of ribbon 2 ft. 8 in. in length; Sara 8 ribbon is 3 ft. 9 in. long.	
	(a) How much shorter is Jane's ribbon than Sara's? (b) The two ribbons, when put end to end, make a piece 7 ftin.long.	
3.	Add these measures. (Write the lengths in the answers in two ways, as shown in exercise a).	de l'approprie
	ra) 6 yd. 2 ft. d) 11 yd. 2 ft. 37 yd. 1 ft.	
	9 yd. 2 ft. 22 yd. 5 ft. ≟-23 yd. 2 ft.	
	b) 23 ft. 8 in e) 24 ft. 2 10.	
	35 ft. 2 in	The Control of the Co
	c) 38 yd. 2 ft. f) 8 in.	
	23 yd. 2 ft. 5 in. 4 in.	es de la contra del la contra de la contra de la contra del la contra del la contra de la contra de la contra del la contra del la contra de la contra del la co
	#99 2///	
de Chi	We consider the control of the contr	Para a managanan Managanan Managanan

		rd. 1 ft.			8 yd. 2 ft	
		ft. 11/(in. ft. 8 in.			26 ft. 9 in 9 ft: 4 in	19 - Marie 1971 (1971)
5.	for a plant of the second	e the names classroom.	and heig	hts (in in	ches) of 3	O pupils
		John 56	Mary	Jeannie 53	,Ro y rce 63	Tom
And the second s	grant on the state of the state	Denise	Paul 61	Jack 63	. Phyllis 52	Helen \ 52
	RWS	Pran	Fred 59	Martha 54	- Walter 61	Viola 60
		:B111 52	Glen 52	Lenore 61	qary 56	Boyd 65
		Sarah 52	Greg 52	Valaree 63	Jake 56	Gerry 65
	And Completed Colonians Service Colonians Colo	Edna 52	W111 54	James 52	н111 [—] 65	Jo 64
on 100 pp. Languages or a section of the con-	a) Wh	ich row of p	oupils ha	s the grea	test total	height?
The state of the s	a para palamente al la serie de la como de l La como de la como de l	w much is the	and the second of the second	Control of the second of the s	ignere ingen er en nicht er in der geben die gestellt der geben der der	
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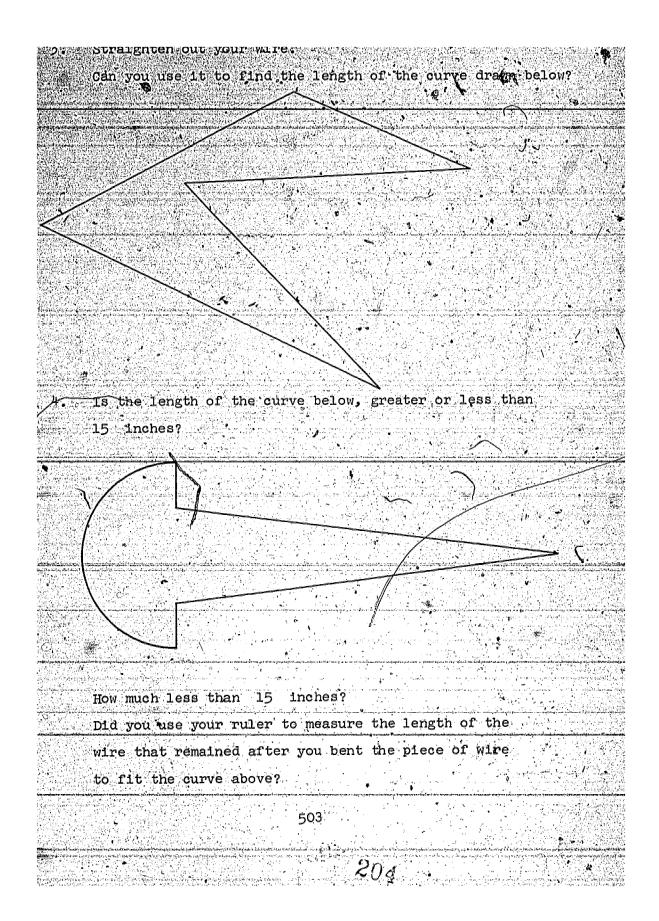


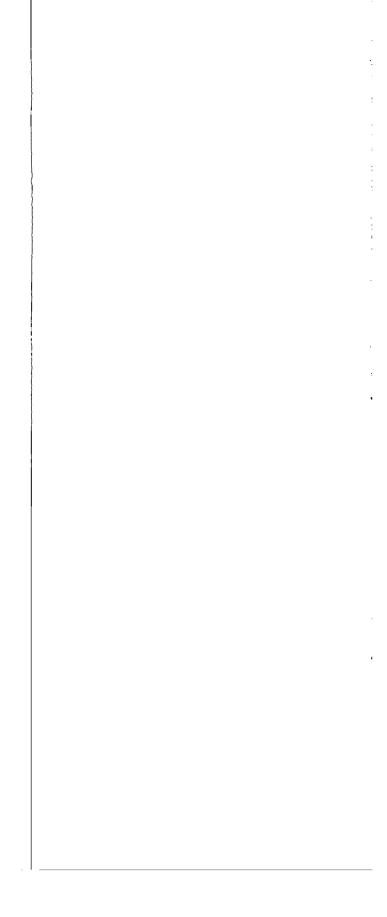
. Use	the table of exercise 5 to answer the following
er desertate in a lever de Constitution de la constitution Distriction de la constitution de Lever de la constitution de la con	AND CONTROL OF THE PROPERTY OF
a.	: Which column of pupils has the least total
	How much is the least total height?
A Company of the Comp	Statistics of the hypothetic program with the program of the progr
D.	Which row of pupils has the least total height?
	How much is this total height?
c.	Is there one pupil who is sitting both in the column of least total
	height? Who?
	Approximate to the second of t
distribution de la companya de la co	
4	
<i>数</i> 数5.50 平均管理区	
	and the state of t
A control of the cont	501



1. Take applece of wire, 15 inches long. Bend it to make a simple closed curve, like this: What is the length of the wire when it is bent in the shape of this curve? 2. Straighten out the wire, and hend it to form a different closed curve. What is the length of the new curve? What happens to the length of the wire when you change the shape of the simple closed curve?	Len	ngths of Simple Closed Curves Exploration
What is the length of the wire when it is bent in the shape of this curve? 2. Straighten out the wire, and hend it to form a different closed curve. What is the length of the new curve? What happens to the length of the wire when you change		
What is the length of the wire when it is bent in the shape of this curve? 2. Straighten out the wire, and bend it to form a different closed curve. What is the length of the new curve? What happens to the length of the wire when you change	And the second s	See the state of t
shape of this curve? 2. Straighten out the wire, and hend it to form a different closed curve. What is the length of the new curve? What happens to the length of the wire when you, change		
2. Straighten out the wire, and hend it to form a different closed curve. What is the length of the new curve? What happens to the length of the wire when you, change		What is the length of the wire when it is bent in the
closed curve. What is the length of the new curve? What happens to the length of the wire when you, change	The state of the s	de se de la companya del companya de la companya de la companya del companya de la companya del com
## 프로그램 # 1916 ## ## ## ## ## ## ## ## ## ## ## ## ##	2.	closed curve.
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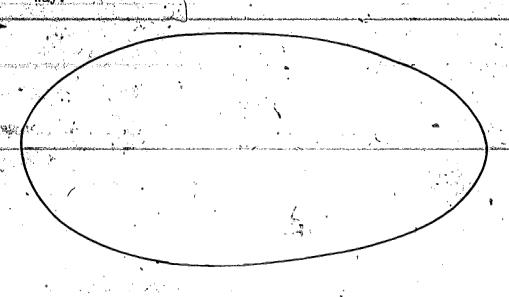




5. Take another piece of wire whose length you do not know.

Bend it to fit the curve below.

If there is wire left over, bend it back and out of the



Can you think of some way of using the wire outline to find the length of the curve?

If you straighten the wire out, will the length of the part of the wire that outlined the curve change?

Straighten out the wire.

Measure it with a ruler.

What is the length of the chaver





Use pieces of wire and a ruler to find the lengths of the curves.

Remember that this simple closed curve is called a polygon because it is the union of line segments.

505

20e



Take a plece of wire. Bend it, using the whole piece of wire, so that you make an equilateral triangle.

What is the length of the triangle?

Bend a piece of wire so that, using the whole piece of wire, you have a polygon with four sides of the same length.

Find the length of the polygon.

5. Use the same piece of wire as in exercise 4 and make a different polygon with four sides of the same length.

- 5. Use the same piece of wire as in exercise 4 and make a different polygon with four sides of the same length.

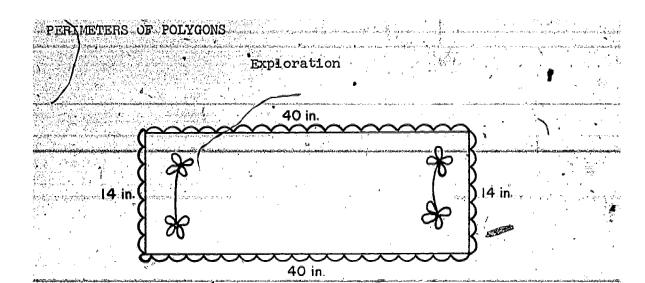
 Without straightening the wire, do you know the length of this polygon?
- 6. Find a model of a circle in your home.
 Use a piece of wire or a piece of string to help you find the length of the circle.
 Did you need a ruler?
- 7. Cut a model of a triangle with its interior from a piece of cardboard.

Can you find the length of the triangle?

Did you use a piece of wire?

Could you have found the length of the triangle using the ruler only?

500 207



Joan wished to buy some lace edging to trim a scarf.

The scarf was 40 inches long and 14 inches wide.

How much edging does Joan need?

The number sentence which tells the measure of the length of the edging Joan needs to trim all four edges of the scarf is:

$$40 + 14 + 40 + 14 = 108$$

The length of the edging that Joan must buy is 108 inches.

How many yards of edging does she need?

The perimeter of the rectangle in this example is 108 inches.

You have found the length of many simple closed curves.

When the curve is a polygon whose sides are line segments, we call the length of the polygon its perimeter.

The perimeter gives a number and a unit of measure.

507

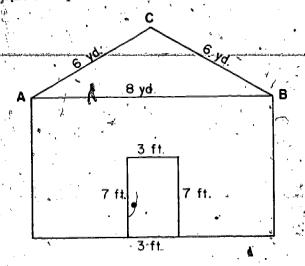
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2. The Jones family decided to decorate the front of their home for the Christmas season.

Johnny wanted to put a string of colored lights on the house along the triangle ABC. Mary wanted to put a string of colored lights around the doorway.

Mr. Jones said he would buy lights for the door or the roof He would not buy lights for both. Also, he would decorate the one, which required the shorter string of lights.



Johnny measured the 3 sides of the triangle.

Mary measured the 4 sides of the rectangle around the door

Each reported that the sum of the measures of the sides

of the figure he measured was 20.

Johnny said: "6 + 6 + 8 = 20"

Mary said: "3 + 7 + 3 + 7 = 20"

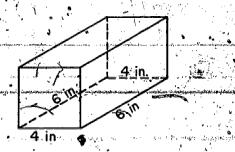
What other fact did Mr. Jones need to know before he could make a decision about which part of the house to decorate?

Did the Jones family decorate the door or the roof?

Exercise Set 12

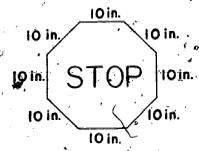
Joe made a cardboard model of a chalkbox. He wished to tape the edges of the bottom of the box with-scotch tape. How much scotch tape did he need?

(There is no overlap at the corners.)

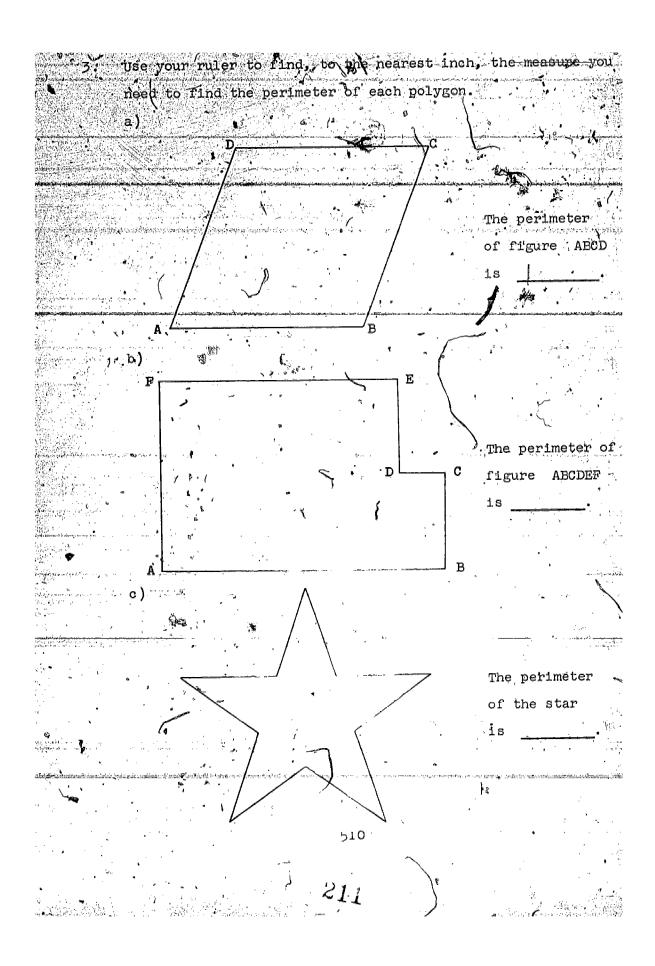


Did you find the sum of the measures of the sides of the rectangle, or did you find the perimeter of the rectangle?

2. The police department of a town is painting a thin black border around the edge of the STOP signs. How many inches of border must be painted on each sign?



The edge of the STOP sign represents a polygon. What 4s the perimeter of this polygon?





FINDING+PERIMETERS

Exploration

Here is a plan for the floor of a rectangular room.

What is the perimeter of the edge of the floor?

12 ft. 3 in.

7ft. 2in

7ft. 2 in.

2ft. 3in.

The we place a piece of wire around the edge of this floor plan, then straighten out the wire, we are picture the wire like this:

12 ft. 3 in.

7 ft. 2 in.

12 ft. 3 in.

7 ft. 2 in.*

Imagine that we cut the vire into eight pieces.

We put them together again, as shown in this picture,

, 12 ft.

7 ft.

12 ft.

7 ft

3 2 3 2 Min in ir

Has the length changed?

We add the measures which have the same unit. -

$$12 + 7 + 12 + 7 = 38$$

$$3 + 2 + 3 + 2 = 10$$

The length, or the perimeter, of the rectangle is 38 ft.

10 in. Remember we add the measures. We do not add the units.

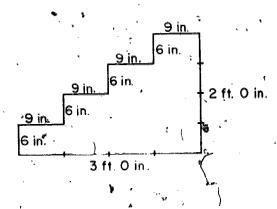
We add only those measures that were made using the same unit.

<u>Exercise</u> <u>Set 13</u>

Find the perimeter of a corner piece of land in the shape of a triangle if the lengths of its sides are 50 feet inches, 80 Feet 7 inches, and 50 feet 4 inches.

A yardstick is)1 inch wide. Find the perimeter of the face of the yardstick that shows the scale. Give your answer in yards and inches. Give your answer again in feet and inches.

3. Find the perimeter of the polygon pictured below:



- a) Can your answer the written using only one unit?

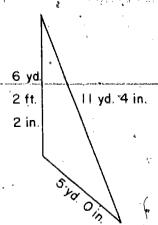
 Write your answer in inches only, in feet only.
- b) Can your answer be written using yards only and what we have learned, so far?

In France, a baseball diamond is a square, each of whose sides is 27 meters 70 cm. long. Pierre hits a home run. What is the length of the shortest path he can take, if he tauches each base on his way back to home place? You will need to know that 100 centimeters equals 1 meter.

b)

Which curve is longer? How much longer?

2 yd. 2 ft. 8 yd. 2 ft.



3RAINTWISTERS

- A man wants to put a fence all around his land. He knows that the boundary of his land can be thought of as a square. He measures one side and finds that it is between 125 and 126 ft. Long. How much fencing should he buy?
 - In Jim's house a piece of glass in a window was broken. His father measured the frame where the glass went. He found that it was a rectangle with 14 Inch and 24 inch sides, to the nearest inch. He bought a new piece of glass 14 inches wide and 24 inches long. When he went to put it in the frame he found that it was too long to fit. Can you give a possible reason?

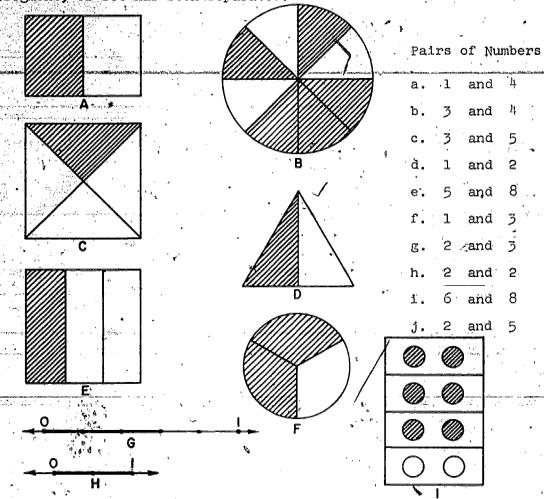
CONCEPT OF RATIONAL NUMBERS IDEA OF RATIONAL NUMBERS

Exploration

Look at each of the figures on this page.

For each figure, choose a pair of numbers at the right which can be-used-to-talk-about-the number of parts-that are shaded and the number of congruent parts into which each unit region, unit

segment, or set has been separated.



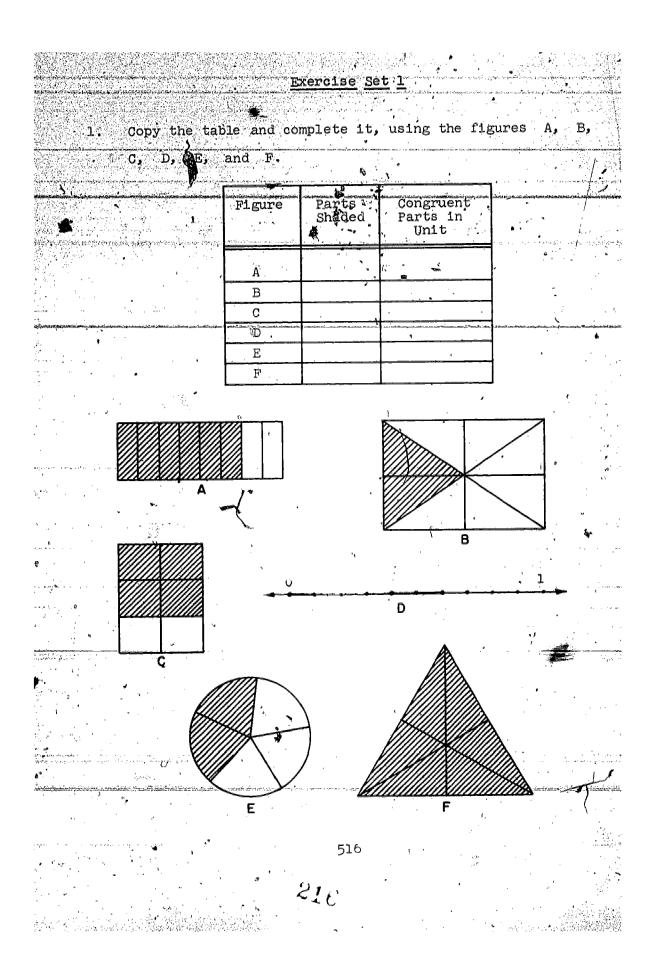
Were you able to find a pair of numbers for each? Did you find these -- A-d; B-e; C-a; D-d; E-r; F-g; G-c; H-h; and

I-b?

515

215





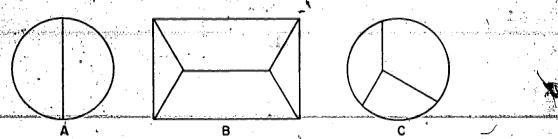
2. Write on your paper the letters from A to G.

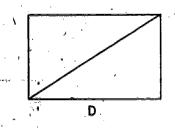
After each, write <u>Yes</u> if the figure <u>has been</u>

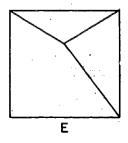
partitioned into congruent regions. Write <u>No</u> if

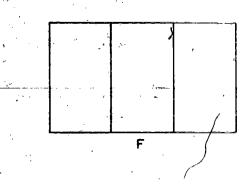
the figure <u>has not been</u> partitioned into congruent

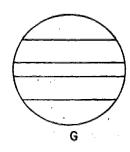
regions.





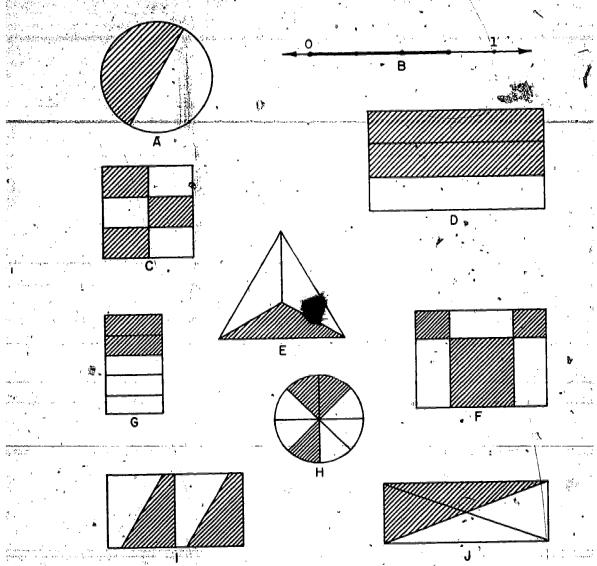








3. What pair of numbers can be used to talk about the shaded region in each figure? Remember we will let the first number of the pair tell how many parts are shaded. We will let the second number of the pair tell into how many congruent parts the unit region has been partitioned.



into congruent regions? Which ones were they?

518

218

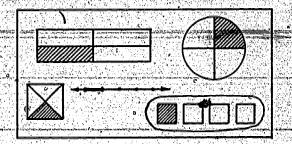


ANEW KIND OF MUMBER

Exploration

When a region is partitioned into congruent parts and some of these parts are shaded, we use a new kind of number to describe what we see: These new numbers are called rational numbers, 2, 1, and 8 are rational numbers. They are read, "one-half," "one-fourth," and "three-eighths."

Each of these figures at the right suggests the same rational number. The rational number is one-fourth. The symbol, $\frac{1}{\pi}$, which names the rational



number one-fourth is called a <u>fraction</u>. Fractions are written using two numerals. The two numerals are separated by a horizontal bar.

For example:

The numerals are 1 and 4.

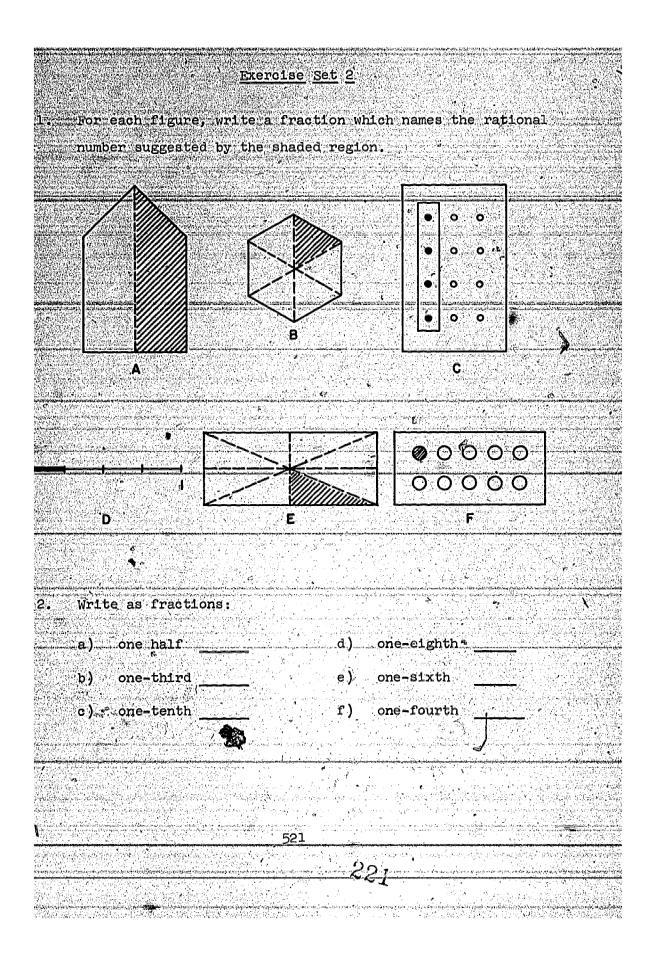
The numeral above the bar tells the number of congruent parts of equivalent subsets described. The number is called the numerator.

The numeral below the bar tells the number of congruent parts into which the set of objects, unit region, or unit segment has been partitioned. The number is called the denominator.



5].0

What rational number is suggested by each of these figures below What rational number does each of these figures suggest? Figure A suggests the rational number, $\frac{2}{\pi}$, read three-fourths Figure B suggests the rational number, $\frac{2}{3}$, read two-thirds. Figure C suggests the rational number, $\frac{2}{2}$, read two halves.





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On your pa	per, make 6 copies of	
On your pa	per, make 6 copies of ke the unit regions the s that suggests each of the	same size. Then show
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n your pa elow. Ma picture	ke the unit regions the s that suggests each of the	same size. Then show rational numbers named



		Exercise : Cfgures to complete en done for you.		
The second secon	A milds p	B B	Z C	Carlot State
Project Control of Con	New York of the Right Section Colors of the Property of the Colors of th	Control Contro	F	
	Figure	Number of Congruent Parts in Figure	Number of Shaded Parts	Rational Number Suggested by Shaded Part
	A	4		2 1 1
And appropriate to the second	, B			
Alexandra de la companya de la comp	Ď			
	E	Santa Asserting Asserting		
		524		The second secon
and personal confidence for the first of the second		in the second se		on the second of



22. Using figures A, B, C, D, E, and F of exercise l, write the name of the rational number suggested by the
unshaded part of each figure.
3. Use these figures to complete the sentences below
X M N O Y Set C= {1,2,4,6,8,10,12,14} Fig. B Fig. C
Fig.B Fig.C Fig.A a) Figure A has been separated into
congruent regions. region has been shaded. The shaded region is best described by the rational number named by the fraction
b) Points M, N, and O separate \overline{XY} into
c) Set C has members member names an odd number. This member is
of all the members of Set C.
525 225



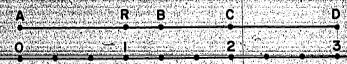
	Study your answers to exercises 1, 2, and 3.
	Copy and then write "above" or "below" in each blank.
A state of the sta	a) The numeral the bar names the number of congruent parts into which the unit has been
	b) The numeral the bar names the number. of congruent parts which are described.
Baltimote and remaining and re	Ann watched 5 television programs. Each was $\frac{1}{\pi}$ of an hour long.
aggregation is a series of the	a) How long did Ann watch television?
	b) How much longer would she need to watch TV. to make her total time 1 hour?
· ·	
6.	A figure like the one pictured below was made by laying toothpicks, each the same size, end-bo-end. What
	fractional part of the perimeter is the "roof" / ?
Company of the Compan	
	526
	226



RATIONAL	NUMBERS GREATER THAN ONE
	Exploration (
rin the pi	cture below, the line segment AB is l. unit fong.
ō	
	B
C.	
E o-	
Ge	√ Jana 1
10	
And the second s	
1 (a)	On the number line the unit segment is separable into congruent segments.
(b)	Use a fraction; Each small segment is of
	the unit segment.
(c)	The measure of $\overline{\rm AB}$ is 1. The measure of $\overline{\rm AB}$ is
Property and pure and property and a second control of the control	also (Use a fraction.)
(d)	Is $rac{8}{8}$ the measure of line segment AB?
(é)	
· 遊園集員公司2000年11月2日(日本	Is $\frac{2}{8}$ the measure of line segment CD?
(f)	Is $\frac{5}{8}$ the measure of line segment CD? Is $\frac{5}{8}$ the measure of line segment EF?
(f) (g)	
	Is 등 the measure of line segment EF?
(g)	Is $\frac{5}{8}$ the measure of line segment EF?
(g)	Is $\frac{5}{8}$ the measure of line segment EF? Is $\frac{2}{8}$ the measure of line segment GH? Is $\frac{9}{8}$ the measure of line segment IJ?
(g)	Is $\frac{5}{8}$ the measure of line segment EF? Is $\frac{2}{8}$ the measure of line segment GH? Is $\frac{9}{8}$ the measure of line segment IJ?
(g) (h)	Is $\frac{5}{8}$ the measure of line segment EF? Is $\frac{2}{8}$ the measure of line segment GH? Is $\frac{9}{8}$ the measure of line segment IJ?



2. Fach unit segment of the number line below has been separated into 3 congruent segments. AR is the same the length as the unit segment.

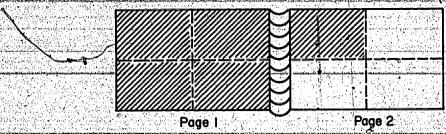


Use this number line to answer the questions.

(a) What fraction names the measure of $\overline{
m AR} ?$

(b) What fraction names the measure of AB? AC? AD?

3. Bill has a photograph album. Each page is separated into congruent parts. On each page he can place 4 pictures.



If Bill pastes 5 pictures in his album, he will cover $\frac{4}{4}$ of one page and $\frac{1}{4}$ of another page. What rational number describes the number of pages covered?

Fractions like $\frac{2}{8}$, $\frac{5}{8}$, $\frac{3}{8}$, $\frac{1}{2}$, $\frac{1}{3}$, $\frac{2}{3}$, $\frac{1}{4}$, $\frac{3}{7}$, $\frac{4}{5}$ tell us that the measure of a segment on a region is less than 1.

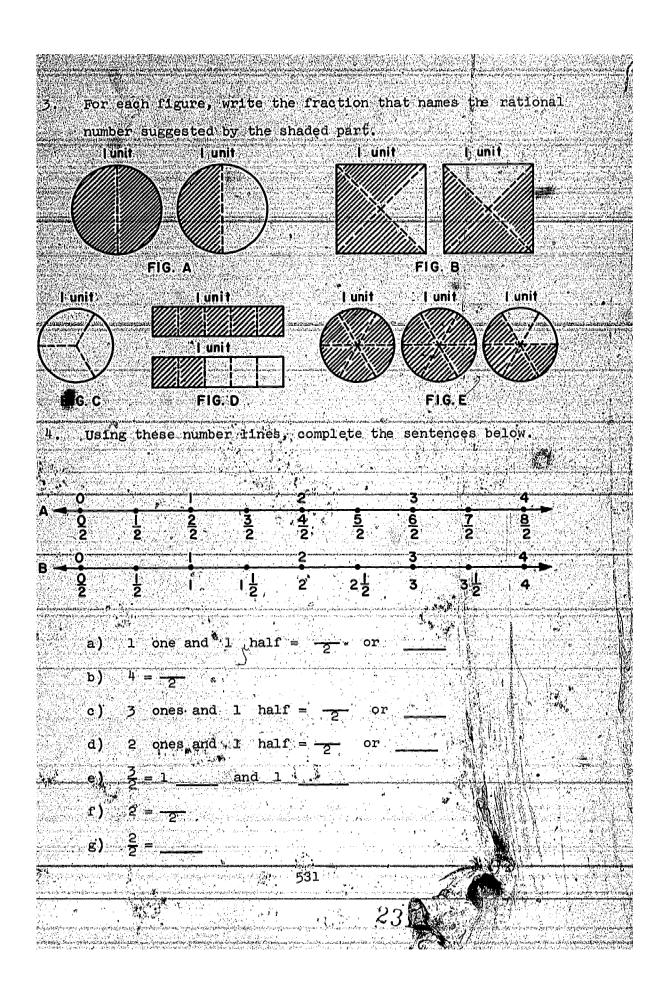
Fractions like $\frac{8}{8}$, $\frac{2}{2}$, $\frac{3}{3}$, $\frac{4}{4}$, $\frac{5}{5}$, $\frac{6}{6}$ tell us that the measure of a segment or region is exactly 1.

Fractions like $\frac{9}{8}$, $\frac{11}{8}$, $\frac{3}{2}$, $\frac{4}{3}$, $\frac{5}{4}$, $\frac{5}{2}$, $\frac{5}{2}$ tell us that the measure of a segment or region is greater than 1.

Exercise Set 4 Copy the unit segments below. The dots separate each unit segment into smaller, congruent segments. Label each dot correctly. Each of the figures below represents a unit region or unit segment. Study these diagrams. Then answer the questions on the next page.



Magazi (1 magazi) a sa s	
a)	How many, thirds are there in A?
Control of the Contro	How many thirds are there in B?
	flow many thirds are shown in A and B together?
	What rational fraction is suggested by the shaded region of A and B together?
	What rational number is suggested by the unshaded
The second secon	region of A and B together?
b)	What rational number is suggested by tage shaded region
	What rational number is suggested by the unshaded region in C? in D? in E?
	What rational number best describes the shaded regions in C, D, and E altogether?
	What rational number best describes the unshaded regions in C, D, and E altogether?
Control of the Contro	Advisory from the second second surface we transfer to the second
, a)	What rational number is suggested by the shaded region
	of F and G together?
eserven sinten en Tillia	What rational number is suggested by the unshaded
	region of F and G together?
. a)	In Figure H, what rational number is the measure of
And the second s	$\overline{ ext{AB}}$? of $\overline{ ext{AC}}$?
	530
	230

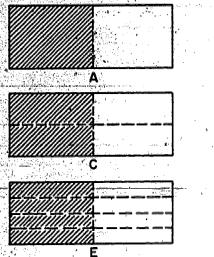


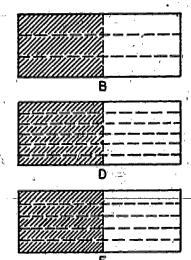
5. Copy the line segment shown below on your paper.
B A Company of the Co
AB is a unit segment.
a) Mark a point D so that \overline{AD} is $\frac{1}{2}$ unit long.
b) Mark a point E so that \overline{AE} is $\frac{3}{2}$ units long.
c) Mark a point F so that AF is $\frac{5}{2}$ units long.
6. Copy the line segment perow. Notice each unit segment has
been separated into β congruent segments.
/2 3 3
Using a certain unit, the measure of \overline{XY} is $\frac{4}{3}$.
Mark new points U. V. and W so that
a) XU is 1 unit long.
b) \overline{XV} is $\frac{2}{3}$ unit long.
The state of the s
7: Mark is 4 feet tall. What number gives his height in
yards?
8: Ellen watched 5 television programs. How many hours did she watch TV if each program was:
a) ‡ of an hour long?
b) 🖫 of an hour long?.
532
Application of the programment of the contract

DIFFERENT NAMES FOR THE SAME NUMBER

Exploration

1. The pictures of unit regions below suggest some ways of thinking of one-half.





In A, what fraction names the measure of the shaded region?

In B, what fraction names the measure of the shaded region?

In C, what fraction names the measure of the shaded region?

In D, what fraction names the measure of the shaded region?

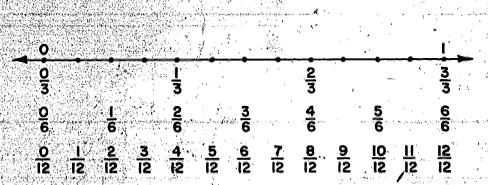
In E, what fraction names the measure of the shaded region?

In F, what fraction names the measure of the shaded region?

In F, what fraction names the measure of the shaded region? $\frac{1}{2}$, $\frac{3}{5}$, $\frac{2}{7}$, $\frac{6}{12}$, $\frac{1}{8}$, and $\frac{5}{10}$ are all ways of naming the rational number $\frac{1}{2}$.

We can write: $\frac{1}{2} = \frac{3}{6} = \frac{4}{8} = \frac{5}{10}$.

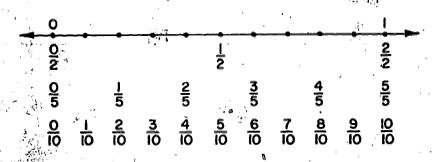
What are some other fractions that this same number? We say that $\frac{1}{2}$ is the simplest name, or simplest form, for this rational number. Can you tell why?



2. Make true statements by writing a fraction in each blank
Use the number line above to help you.

b.
$$\frac{10}{12} =$$

d.
$$\frac{4}{5} = \frac{1}{100} = \frac{1}{100}$$



3. Use the number line above to help you write the missing numerator or denominator.

a.
$$\frac{1}{2} = \frac{n}{10}$$

$$b \cdot \frac{2}{10} = \frac{1}{n}$$

$$c. \quad \frac{4}{5} = 10$$

d.
$$1 = \frac{10}{2} = \frac{8}{2}$$

4 . Using one number line, we can show many different names

for a rational number.

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We see that some fractions are names for the same rational number. What other fractions are names for the rational number $\frac{1}{2}$?

What other fraction is a name for the rational number $\frac{1}{4}$?

What other fraction is a name for the rational number $\frac{3}{4}$?

Can you find other fractions that name the same rational number on this line?

One rational number may be named by many fractions.

The rational number $\frac{1}{4}$ may be named by: $\{\frac{1}{4}, \frac{2}{8}, \frac{3}{12}, \frac{6}{24}, \dots\}$ The rational number $\frac{9}{3}$ may be named by: $\{\frac{2}{3}, \frac{4}{6}, \frac{6}{9}, \frac{8}{12}, \dots\}$ The rational number $\frac{2}{5}$ may be named by: $\{\frac{2}{5}, \frac{4}{10}, \frac{6}{15}, \frac{8}{20}, \dots\}$ The rational number $\frac{1}{10}$ may be named by: $\{\frac{1}{10}, \frac{2}{20}, \frac{3}{30}, \frac{4}{40}, \dots\}$

Can you think of other fractions which would name each of these numbers above?

Many fractions can be used to name the same whole numbers.

For example, "1 may be indicated by

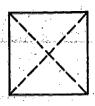
$$\frac{2}{2}$$
, $\frac{3}{3}$, $\frac{4}{4}$, $\frac{5}{5}$, $\frac{6}{6}$, and so on.

Can you name three other fractions that belong to this set?

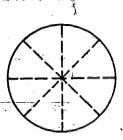
Exercise Set 5

Copy each of these figures.

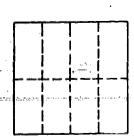
l.

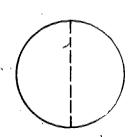


2

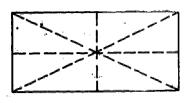


3.





5



Color $\frac{2}{4}$ of this figure.

 $\frac{2}{4}$ is another name for _

Color $\frac{6}{8}$ of this figure.

6 is another name for ___.

Color $\frac{2}{8}$ of this figure.

is another name for ____.

Color $\frac{2}{2}$ of this figure.

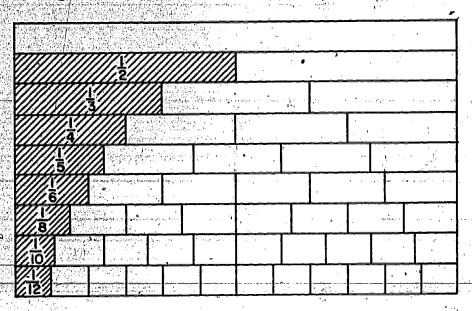
C₂

 $\frac{2}{2}$ is another name for ____

Color $\frac{4}{8}$ of this figure.

 $\frac{4}{8}$ is another name for ____.

.6. Using this chart, write as many names as you can for



a)

d) $\frac{1}{5}$

b) $\frac{1}{3}$

e) 4/5

c) $\frac{1}{\pi}$

 $f = \frac{6}{8}$

7. Write at least three other fractions which name each of the following rational numbers. If you can write more than three, do so.

a) $\frac{1}{4}$

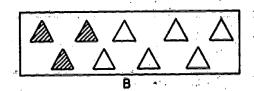
c) 5/2

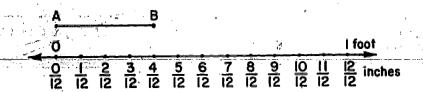
b) <u>2</u>

- a) $\frac{2}{3}$
- $e) \frac{3}{\pi}$

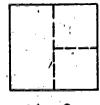
8. The diagrams below suggest three other names for 🕏. What are they?







9. Draw 5 boxes like the ones below. Separate each box to show the mathematical sentence written below. The first one is done for you.



$$\frac{1}{2}=\frac{2}{4}$$



$$\frac{4}{8} = \frac{1}{2}$$



$$\frac{1}{4} = \frac{2}{8}$$



$$\frac{6}{8} = \frac{3}{4}$$



$$\frac{2}{6} = \frac{1}{3}$$

538

10. Complete:

$$a \int_{0}^{\infty} 1 = \frac{1}{2}$$

(b)
$$\frac{2}{6} = \frac{1}{3}$$

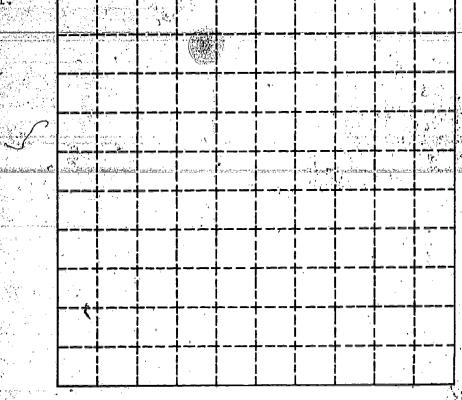
g),
$$\frac{1}{3} = \frac{1}{9}$$

h)
$$\frac{2}{4} = \frac{8}{8}$$

1)
$$\frac{6}{8} = \frac{4}{4}$$

$$(1)^3 \quad \frac{1}{3} = \frac{1}{12}$$

11.



The unit square shown on the preceding page has been the separated into 100 congruent square regions.

- a) Each small square region is what part of the unit square region?
 - -b) Each small square region is what part of 1 row or 1 column of square regions?
 - c) Each row or each column of square regions is what part of the unit square region?

d)
$$\frac{4}{10} = \frac{?}{100}$$

e)
$$\frac{7}{10} = \frac{?}{100}$$

(f)
$$\frac{90}{100} = \frac{?}{10}$$

g)
$$\frac{30}{100} = \frac{?}{10}$$

h) How many small square regions should you color if you are to color 1700 of the unit square region?

$$\frac{83}{100}$$
 ? $\frac{100}{100}$? and $\frac{10}{10}$?

in how many different ways can you cover the unit square using the fractional pieces shown? Each piece may be used more than once. You may wish to trace, cut out, and make several copies of each . model region before you work your puzzle. Square 4 ż 8 8 541 241

Here are a few solutions to the puzzle on page 541. How many more did you discover? ŀ 8 8 8 İĕ 4 4 2 - 112 91 *) . 1 14 4 4 |8|8 1818181818 . trocking designation of ... 1 | 1 4 | 8 14 <u>|</u>4 111 ខៀន 8 8 8 8 4 12 <u>|</u> <u>|</u> <u>|</u> 8 8 8 8 <u>|</u>|8 8 | | <u>|</u> | | 8 542 212 ..

ORDERING THE RATIONAL NUMBERS

Exploration

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	2							2.			1 (4) 1 (4)	N y	2	•			2			2	
	0			Ţ	1/2			2 ″	Topics Spiritory	Vijera <mark>.</mark>	3	· .	4		<u>5</u>		<u>6</u> .	Z		<u>8</u>	; • , , ;
	4		e de la companya de l	4	100	Signalis Ngjarja Ngjarja	7				}	:	4		4		4	4	ماريد	4	يورد :
	<u>c</u>	Ī		2		3		<u>4</u>	5	· (<u> </u>	7	<u>8</u> ,	<u>9</u> 8	10	π	12/	3 14	<u>15</u>	<u>16</u>	<u> </u>
	8	8	12	В		8	. 3	ٿ ي.	8	. ¢	5	8	Ø,	8	8	8.	8	8 7 8	. 6	8	, ,

Look at the number line.

Is $\frac{1}{2}$ to the right of $\frac{1}{4}$? Is $-\frac{1}{2} > \frac{1}{4}$?

Is $\frac{3}{\pi}$ to the right of $\frac{3}{8}$? Is $\frac{3}{\pi} > \frac{3}{8}$?

Is $\frac{5}{4}$ to the right of $\frac{4}{2}$? Is $\frac{5}{4} > \frac{4}{2}$?

Is 0 to the left of $\frac{1}{4}$? Is $0 \leqslant \frac{1}{4}$?

Is $\frac{2}{4}$ to the left of $\frac{4}{2}$? Is $\frac{2}{4} < \frac{4}{2}$?

Is $\frac{5}{8}$ to the left of $\frac{6}{8}$? Is $\frac{5}{8} < \frac{6}{8}$?

It is easy to see that $\frac{1}{4}$, $\frac{3}{4}$, $\frac{6}{4}$, and $\frac{8}{4}$ are ordered from least to greatest.

Are $\frac{1}{2}$, $\frac{5}{8}$, $\frac{5}{4}$, and $\frac{4}{2}$ ordered from the least to greatest?

It would be easier to decide if we used other fractions for these numbers.

Using other names for these same numbers, we can write them as

$$\frac{4}{8}$$
, $\frac{5}{8}$, $\frac{10}{8}$, and $\frac{16}{8}$.

Now we see the numbers are named in order from least to greatest?

As you move to the right along a number line, the rational numbers become greater. As you move to the left, they become less.

Exercise Set 6

1. Use this chart and the symbols > and < to complete the sentences below.

	10			<u> </u>	16.	<u>. [</u>	<u> </u> 6	16	1 <u>e</u> T	16	16	16	16	1 <u>e</u>	ыF	<u>– 6</u>
	 8	100	<u>!</u>	3		<u> </u> 	<u> </u>			<u>!</u> 8	<u> </u>	<u>l</u> 3	, , , , , , , , , , , , , , , , , , ,	L '', B	<u> </u>	3
- E		i 4		en de la company	الله الله الله الله الله الله الله الله		<u> </u> 	, 2	المهار	2				<u>. </u>	r + s not (FM
	•			<u> </u>					4	1	13 % . 1		2	- 		

- a) ½ ‡
- c) $\frac{3}{8} \frac{1}{4}$
- e) #______

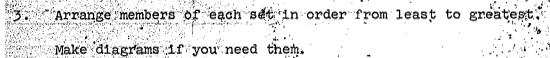
- b) $\frac{1}{8}$ _____ $\frac{1}{4}$
- a) $\frac{1}{2}$ $\frac{3}{8}$
- f) $\cdot \frac{3}{8}$ --- $\cdot \frac{2}{4}$

2. Write the correct answer. The fraction chart above may be used, if heeded.

- a) Which number is less: $\frac{17}{8}$ or $\frac{16}{8}$?

 Which is farther to the left on the number line?
- b) Which number is less: $\frac{10}{8}$ or $\frac{12}{8}$?
 Which is farther to the left on the number line?
- which number is less: $\frac{17}{8}$ or $\frac{15}{8}$?
 Which is farther to the left on the number line?
- d) Which number is less: $\frac{11}{4}$ or $\frac{4}{2}$?

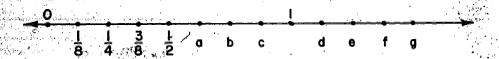
 Which is farther to the left on the number line?



$$A = \{ \frac{7}{2}, \frac{3}{2}, \frac{11}{2}, \frac{13}{2}, \frac{5}{2} \}$$

$$B = \{ \frac{7}{4}, \frac{3}{4}, 2, \frac{9}{4}, \frac{11}{4} \}$$

4. Associate a rational number with points a, b, c, d, e, f, and g in the diagram below.



- 5. List in order the numbers used in counting by two-thirds from $\frac{2}{3}$ to 4.
- 6. List in order the numbers used in counting by three-halves from $\frac{3}{2}$ to 9.
- Write two other names for each of the following numbers:
 - a) $\frac{12}{8}$

c) 10

b) 5/2

ر (د

- 8. Copy and complete by writing the symbol > or < in

 - o) 1

- d) $1 \frac{1}{2}$
- $\frac{1}{8}$
- f) $\sqrt{\frac{1}{6}}$ $\frac{1}{\sqrt{1}}$
- 9. Rearrange these numbers in order from least to greatest.
 - a) \(\frac{5}{8}, \quad \frac{3}{8}, \quad \frac{1}{4}, \quad \frac{1}{8}, \quad \frac{1}{4}

 - $\frac{2}{5}$, $\frac{1}{6}$, $\frac{1}{3}$
 - a) $\frac{3}{2}$, $\frac{1}{2}$, $\frac{3}{4}$, $\frac{5}{2}$
- 10. Arrange in order the numbers in each set below. Begin with the greatest.
 - $A = \left\{ \frac{2}{4}, \frac{3}{4}, \frac{1}{4} \right\}$
 - $B = \left\{ \frac{1}{4}, \frac{1}{2}, \frac{1}{8} \right\}$
 - $C = \left\{ \frac{1}{2}, \frac{3}{8}, \frac{3}{4} \right\}$
- 11. Arrange these numbers from least to greatest.
 - $\frac{1}{2}$, $\frac{1}{10}$, $\frac{1}{4}$, $\frac{1}{8}$, $\frac{1}{3}$, $\frac{1}{6}$

Supplementary Exercises Copy and write > , < , or = in each blank to make a true sentence. The number line above will help

Which fraction of each pair below will be farther to the right on the number line? Put members in order from least to Copy and fill in each blank with the symbol $\stackrel{?}{.}>.$ Look at exercise 4. Which fraction in each pair labels a point farther to the right on the number line?

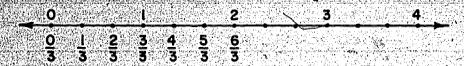
NEW KIND OF NAME hese pictures help us think about the numbers, $\frac{3}{2}$ and Unit Unit $=\frac{4}{7}$ and $\frac{4}{7}$ and $\frac{3}{4}$ l one and l one and 3 fourths ones and fourths Another way of naming $\frac{3}{2}$ Another way of naming $\frac{11}{4}$

	Rational numbers named by fractions like $\frac{1}{2}$, $\frac{3}{4}$, $\frac{2}{3}$, and
	ell us that the measure of a region, segment, or set is <u>le</u>
than	
ini kanada (a. 6. 6. 6. 6. 6. 6. 6. 6. 6. 6. 6. 6. 6.	Rational numbers named by fractions like $\frac{2}{2}$, $\frac{8}{8}$, $\frac{4}{7}$, and
<u>ネ</u> ッセ	ell us that the measure of a region, segment, or set is
equa	1 60 1.
	published named by fractions like T 2 and 5
tell	Rational numbers named by fractions like $\frac{7}{4}$, $\frac{3}{2}$, and $\frac{5}{3}$ us that the measure of a region, segment, or set is great
than	#####################################
para di Prima ann	Other names for 1 are $\frac{4}{1}$, $\frac{2}{5}$, and $\frac{3}{5}$.
Antiques (Solution of Edward Court one	Since this is true, $\frac{2}{4}$, $\frac{2}{2}$, and $\frac{1}{3}$ may be renamed $1\frac{2}{4}$.
1 <u>2</u> ,	and $1\frac{2}{3}$.
	$1\frac{3}{4}$, $1\frac{1}{2}$, and $1\frac{2}{3}$ are read, "one and three-fourths,"
	and one-half; and one and two-thirds. Fractions ten in this way are said to be in mixed form.
WIT O	
teller og ger og til af i gligger forskaller og den en forskaller og den en forskaller	All Market Control of the Control of
Angelia (Tambula) Angelia (Tambula) Angelia (Tambula)	550
e kelaku ya ke menasi Kabupatèn Pangkatèn Kabupatèn	Alleger and the second of the

Exercise Set 8

Copy and finish the number line below. Then use it to complete the mathematical sentences so that each will be

a true sentence.



a) $\frac{4}{3} = \frac{1}{3}$ and

d) $2\frac{2}{3} = 2$ and $\frac{2}{3}$

4 5 $2\frac{2}{3} = \frac{6}{3}$ and $\frac{2}{3}$

b) $\frac{6}{3}$ is $\frac{3}{3}$ and $\frac{3}{3}$

25 = -3-

6 _ ____

e) 4 = 3

(c) $\frac{11}{3} = 3$ ones and $\frac{1}{3}$

f) $3\frac{1}{3} = \frac{9}{3}$ and $-\frac{1}{3}$

33 =

2. Arrange the numbers in each of the following sets in order from least to greatest. Use diagrams if you need them.

 $A = \{\frac{2}{4}, 0, \frac{7}{4}, 2, \frac{9}{4}, 1\}$

 $B = \left\{ \frac{5}{3}, 1, \frac{10}{3}, 4, \frac{7}{3}, 2, \frac{2}{3}, 3 \right\}$

3. Peter has 13 blocks to walk to school. Each block is $\frac{1}{10}$ mile long. How many miles does he have to walk to school?

A pound of butter is usually divided into four bars of the same size. Vicky found 7 bars of butter in her refrigerator. To How many pounds of butter were in the refrigerator? Can you do these without any help? Try some of them. Write the mixed form for each of these numbers. 6. Which is greater write the name of the greater number in each pair. You may use a number line to help you decide. e) <u>12</u> or 37 7. Copy and complete. Use diagrams if you need them. Between what two whole numbers on the number line would the following fractions be?

) and					野野 1945年	7. 7. 2. 1.	.1 .2			3	entarialisti and H. 1990 Heperiya Alsa, 1980 Jawa	ang dan Tanggan Sanggan Tanggan Sanggan	2.	
			₹.							2			-2	
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) F		7	2 4		3 T		4 4	t gang belang ang di pertugan dan pengantan selapan dan pengantan selapan dan pengantan selapan dan pengantan	\$	<u>6</u> 4	7	the state of the s	2 8 4	
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) '' 5 :	<u>-</u> 1	2	3. 	4 5		5	<u>6</u> 6	- 7 -	8/1 5/1	<u>9</u>	<u>10</u>	11 6	12	
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7	***********	0 0	. B	8	<u>6</u> ਲ	7 8	<u>용</u> 8	8	10 11 8 8	1 <u>2</u> 8	13 14 8 8	1 <u>5</u>	16 8	erie erie erie erie erie erie erie erie
					at management of	ederyo Maria e Maria e			e martini minipalina di Radio di Martini di Para di Para di Martini di Para di		13 14 8 8	ten jandra franc		(colored to experiment)
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	Use sen	the nu	mber - Wr	line Ite nce	as a	bove symi	· •̀C	opy t	he fol	low1:	ng math	emati	cal	Section of the sectio
	Use sen make	the nu tences:	mber Wr ente	line Ite nce	as a	bove symi	· •̀C	opy t	the fol	low1:	ng math	emati	cal	
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	Use sen make a) b)	the nu tences:	mber Wr ente	line Ite nce	as a	bove symi	· •̀C	opy t	the fol	low1:	ng math	emati	cal	
	Use sen make a)	the nu tences:	mber Wr ente	line Ite nce	as a	bove symi	· •̀C	opy t	the fol	low1:	ng math	emati	cal	
	Use sen make a) b)	the nu tences:	mber Wr ente	line Ite nce	as a	bove symi	· •̀C	opy t	the fol	low1:	ng math	emati	cal	

- 2. Starting at zero, list in order the numbers used in
 - a) counting by one-half to $\frac{4}{2}$
 - b) counting by two-thirds to $\frac{6}{3}$
 - c) counting by three eighths to $\frac{15}{8}$
- 3. Write 2 other names for each of the following.

 - b) 1 = ...,

 - d) 22 = _____
 - 4. Match each rational number in Column 1 with a fraction that names the same number from Column 2.

Column 1 Column 2

- a)
- 1 2
- f)
- g

c)

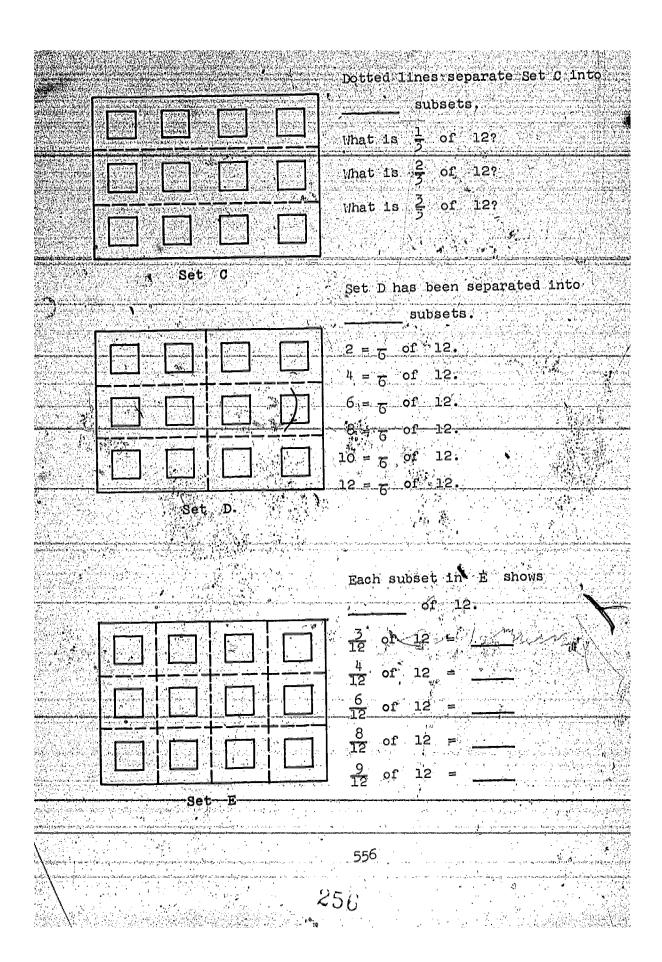
b)

- . h
- -1-)-

- e)
- I I may Market any (1)
- · 28

Below are pictures of sets of 12 objects Dotted lines separate the picture of Set A into 2 subsets. How many objects are there in 1 subset?
Dotted lines separate the picture of Set A into 2 subsets. How many objects are there in 1 subset?
subset?
How many objects are there in 2
subsets? Is ½ of 12 objects equal to // Objects?
Is $\frac{2}{2}$ of 12 objects equal to
Set B has been separated into
4 subsets. How many objects are in each
subset? $\frac{1}{\pi} \text{ of } \mathbb{12} = \frac{2}{\pi} \text{ of } 12$
$\begin{array}{cccccccccccccccccccccccccccccccccccc$
And the second s
555 255





Exercise Set 10 A, B, C, and D are unit square regions. Copy them on your paper. Separate each one into four equal regions. Color $\frac{1}{11}$ of A red. b) Color 🔓 of B blue. q): Color 倉 of C green. Color $\frac{4}{1}$ of D green. $rac{4}{\pi}$ is another name for Write the fraction that best describes the uncolored regions of each unit square region above. Points B and C separate the unit line segment AD 1nto 3 congruent segments. m AB

	Exerdise Set 11
7.2	
	0 0 0
e de la companio de l	O O O
Application of the state of the	It has been partitioned into 4 subsets./
	The same number of objects is in each subset.
	What is $\frac{1}{4}$ of 16? What is $\frac{3}{4}$ of 16?
	What is $\frac{2}{7}$ of 16? what is $\frac{\sqrt{4}}{7}$ of 16?
2	Here is another picture of a set of objects. It has been
	partitioned into five subsets. The same number of objects
tig tender green in de service de le conservation de la conservation d	1s In each subset.
	What is $\frac{1}{5}$ of 20?
· 有待的是连接的的特别的。例如《《门语	
	What is \(\frac{2}{5}\) of 20?
	What 1s 5 of 20?
	What is \(\frac{2}{5}\) of 20? What is \(\frac{4}{5}\) of 20?
	What is $\frac{3}{5}$ of 20? What is $\frac{4}{5}$ of 20? What is $\frac{5}{5}$ of 20?
	What is \(\frac{2}{5}\) of 20? What is \(\frac{4}{5}\) of 20?
	What is 5 of 20? What is 5 of 20? What is 5 of 20?



3.	Complete the following. Use sets of objects if you need them.
	(a) $\frac{1}{2}$ or 6 is $\frac{1}{2}$
	: b) = \frac{1}{2} : \text{of} \tau \tau = \frac{1}{2} : \text{of} \tau \tau = \frac{1}{2} : \text{of} \tau \tau \tau \tau \tau \tau \tau \tau
	(c) $\frac{1}{7}$ of 8 1s (g) $\frac{2}{3}$ of 9 is
	(d) $\frac{1}{2}$ of 10 is h) $\frac{2}{5}$ of 10 is
the state of the s	Jane bought six doughnuts. She ate $\frac{1}{5}$ of them. How many doughnuts did Jane eat? How many doughnuts did Jane have left?
4-5•	Bill had twenty marbles. He lost $rac{1}{4}$ of them. How many
	marbles did Bill lose? How many did he have left?
	Alice had 36 Jacks. She traded Tof them to Mary: How many Jacks did Alice trade? How many Jacks did Alice have left?
7.	On the way from the store, Bob dropped a dozen eggs. He
	looked inside the carton. He found $rac{ar{ar{J}}}{\Pi}$ of the eggs broken.
	How many eggs are there in a dozen? How many eggs were
estuden en ignere.	broken? How many eggs were not broken?
BRAI	INTWISTER
A STATE OF THE STA	John gave Bill sixteen Jelly beans. This was 💆 of the
report of 777 of	number John had. How many did John have at the beginning?
Branch Romania	and the second s
Service to the service of the servic	259

	Exercise Set 12
17.	There were "20 problems on an arithmetic test. John worked
	all but 具 of them. How many problems did John fthish?
2.	1 of a string of 12 Christmas tree lights had burned out. How many lights had to be replaced?
3.	At a sale, books that had been 50% were selling for 2
4.	
	full. How many candy bars were in the box?
	of actual playing time to play a game. How many minutes of
6.	actual playing time are gone at the end of the third quarter There were 6 boys and 3 girls on a softball team. What part of the team was boys?
6.	actual playing time are gone at the end of the third quarter There were 6 boys and 3 girls on a softball team. What part of the team was boys?
6. 7.	actual playing time are gone at the end of the third quarter There were 6 boys and 3 girls on a softball team. What
	There were 6 boys and 3 girls on a softball team. What part of the team was boys? The year is separated into four seasons of equal length. What part of the year is each season?
	actual playing time are gone at the end of the third quarter. There were 6 boys and 3 girls on a softball team. What part of the team was boys? The year is separated into four seasons of equal length.
	There were 6 boys and 3 girls on a softball team. What part of the team was boys? The year is separated into four seasons of equal length. What part of the year is each season? Mary has a collection of 15 dolls, 2 of them represent children from other countries. How many of the dolls represent children from other countries?
7.	There were 6 boys and 3 girls on a softball team. What part of the team was boys? The year is separated into four seasons of equal length. What part of the year is each season? Mary has a collection of 15 dolls. 2 of them represent children from other countries. How many of the dolls represent children from other countries? Jim was making a model of a plane. He needed a single piece of wood 2 of a foot long. He had a piece of wood 8
7.	There were 6 boys and 3 girls on a softball team. What part of the team was boys? The year is separated into four seasons of equal length. What part of the year is each season? Mary has a collection of 15 dolls, 2 of them represent children from other countries. How many of the dolls represent children from other countries?



- Place parentheses correctly to make each of the following
 - a true statement. Example a is shown...
 - $(6 + 4) \times 3 = 30$
 - ···b) -8 ×-3 +-5 < 64
- (c) $6 + 3 \times 6 > 24$
 - d) 2 x 5 + 4 = 18
 - e) 4 × 16 + 4 > 68
- f) 9 + 6 ÷ 3 = 11
- g) 8 x 5 + 3 ≠ 43
 - h) $6 \div 3 \times 4 = 8$
 - 1) $18 \div 6 + 3 \neq 2$

- (k) 5 x,8/ $\frac{1}{2}$ 2 > 30
 - 1) $25 \div 5 + 8 = 13$
 - m) $19 + 8 \div 2 > 14$
 - n) $45 \div 5 + 4 < 13$
 - 6) 27 + 3 ÷ 6 = 5 h
 - (a) 28 7 × 3 ₹ 63.
 - q) $46 + 8 \div 9 = 6$
 - r) 28 + 21 ÷ 7 ≠ 7
 - s) $17 \pm 4 \times 3 < 39$
- 1) $14 \div 7 + 7 > 1$ t) $49 \div 7 + 6 = 13$
- 2. Mixed Addition and Subtraction
 - a) 327 + 54
 - b) 457 + 218
 - c) 384 + 291
 - d) 384 156
 - e) 995 768
 - f) 870 418
 - g) 2384 1963
 - h) 1066 883
 - 984 + 168
 - 700 362

- , k) 1478 + 2388
 - 1) 400 + 583 + 324
 - m) 1037 537
 - 11) 709 **-** 368
 - (3) + 31 + 36
 - رم 801 513
 - y) 145 508
 - r·) 678 + 254
 - 2900 1256 ა)
 - 590 , 303 + 81

3. Write the number narepresents.

o)
$$43 \times 6 = r$$

a)
$$43 \times 6 = n$$

d) $587 - n = 369$

e)
$$77. \pm 99. + n = 237$$

$$f$$
) $p \times 6 = 3708$

$$n), n = 127 \times 5$$

1)
$$746 - n = 413$$

$$1) \cdot 624 + n = 1141$$

k).
$$n = 737 \times 8$$

1)
$$n + 304 + 488 = 1640$$

m)
$$.4767 = x \times 7$$

n)
$$719$$
 - n = 285

n)
$$719^n - n = 285$$

o) $8789 + n = 12497$
p) $707 - \times 6 = n$

p)
$$70.7 \times 6 = n$$

3
s) $n \times 9 = 7857$

t)
$$n = 658 = 758$$

Addition, Subtraction, Multiplication, and Division

a)
$$367 \times 6$$

5. Wrlte the number n represents

a)
$$\frac{1}{2}$$
 of $12 = n$

g)
$$\frac{2}{3}$$
 of $9 = n$

b)
$$\frac{1}{3}$$
 of $15 = n$

h)
$$\frac{3}{4}$$
 of $48 = n$

$$(c) \frac{1}{\pi} \text{ of } 8 = n,$$

1)
$$\frac{2}{5}$$
 of $10 = n$

(a)
$$\frac{1}{9}$$
 of $9 = n$

$$\frac{1}{8}$$
 of $16 = n$

(e)
$$\frac{1}{5}$$
 of $20 = n$

k)
$$\frac{4}{5}$$
 of $15 = n$

f)
$$\frac{1}{6}$$
 of $18 = n$

1)
$$\frac{83}{8}$$
 of $16 = n$

Find the unknown addend by regrouping.

Example:

$$462 = 400 + 60 + 2 = 400 + 50 + 12$$

$$-157 = 100 + 50 + 7 = 100 + 50 + 7$$

$$300 + 00 + 5 = 305$$

503 +

 $\gamma_{s,r}$ Multiplication and Division

$$h) 496 \times 6$$

8. Write the numeral for each blank that makes a true sentence. Example a is shown.

a)
$$(14 \div 2) \times 9 = 10$$
 k) $(1 \times 4) + 8 = 44$

$$\kappa$$
) (\sim 4) + 8 = 44

c)
$$(8 \times 8) - \dots$$
 m) $(7 \times 8) + 16 = \dots$

$$(7 \times 9) + 12 =$$

q)
$$(\underline{} \times 9) - 6 = 48$$

1)
$$(11 - 5) \times 9 =$$
 s) $(\times 6) - 7 = 29$

s)
$$(\times 6) - 7 = 29$$

$$(8 + 20) - _ = 14$$
 $(7 \times 9) + _ = 72$

t)
$$(7 \times 9) + \underline{\hspace{1cm}} = 72$$

1. Using the symbol > , = , or < make each of the following

a true sentence.

a) $\frac{2}{3}$ foot 12 inches f) 12 inches

b) 24 inches $\frac{1}{2}$ yard

g) $\frac{1}{2}$ quart ____ 2 pints

c) i pint ___ ; quart

h) 15 minutes $\frac{1}{\pi}$ hour

d) 1 hour 30 minutes

1) 4 feet _____ $1\frac{1}{2}$ yards

e) $\frac{2}{3}$ yard ____ 2 feet

j) 9 inches $\frac{1}{3}$ yard

Arrange in order of size from smallest to largest.

f) 1 ft., 6 in., $\frac{3}{4}$ ii.

g) 45 min., $\frac{1}{2}$ hr., 60 min., $\frac{1}{4}$ i.e.

h) 1 ton, 1 lb., $\frac{1}{2}$ lb., 1 oz.

1 pt., 1 qt. '1 cup., 1 gal .

- 3. N = {The named points A, B}

 What is the greatest number of line segments that can have endpoints in Set N?

 Name the segment(s).
- 4. M = {The named points C, D, E}

What is the greatest number of line segments that can have endpoints in Set M?

Name the segment(s).

- 5. R = (The named points G, F, H, I)

 What is the greatest number of line segments that can have endpoints in Set R?

 Name the segment(s).
- 6. Draw two line segments to make three quadrilaterals and five new triangles out of Δ XYZ.
- A B
- 7. Draw two line segments (make (wo new triangles and three quadrinaterals out of △ ABC.
- 8. 4 < 5 < 8 means 4 is less than 8 write these sentences the shorter way.
 - a) 32 < 34 and 34 <,40 ·
 - b) $\frac{1}{4} < \frac{2}{4}$ and $\frac{2}{4} < \frac{3}{4}$
 - c) 112 < 115 and 115 < 11/
 - d) $\frac{1}{2} < \frac{3}{4}$ and $\frac{3}{4} < \frac{7}{8}$

- 9. Find the number that n represents in the following:
 - a) 14 < n < 16

d) $\frac{3}{8} < n < \frac{5}{8}$

b) $\frac{1}{3}$ < n < $\frac{3}{3}$

- e) $9 < n < \frac{20}{2}$
- c) ,786 < n < 788
- f) $\frac{1}{2}$ $\langle n \langle 1\frac{1}{2} \rangle$

- 10. What is it?
 - a) A model that has 3 rectangular regions and 2 triangular regions for faces.
 - bi A model that has four triangular regions for faces.
 - c) A model that has six rectangular regions for faces.
 - d) A model that has one rectangular region and two circular regions for faces.
 - e) A model whose edges form right angles only.
 - f) A model that has a circular region and a half circular region for facés.
- 11. These statements are comparing the length of line segments.
 - Complete these to make them true statements.

Examples a and b are done for you.

- a) 4 ft. is 2 times as long as 2 14
- b) 2 t. is 2 as long as 4 t. It.
- c) 19 in. 1s ___ times as aug as 3 in)
- al) 3 in. is __ as long as 9 ir.
- yd: is 2 times as long as 6 yd
- g) 6 yd. is as long as 12 /4
- the Smin. As Meas long as 45 min
- 1) 45 min. Is ____times as long as 15 min.

- 12 :	Match the Standard Unit of Measure from Column I with the
	Item you would use 1t to measure from Column II
hard survey and progress or	alat, kajas ka
	A COLUMN III
	a) cup Length of your pencil
The state of the s	b) feet Bottle of milk
	c) seconds Distance between cities
And the state of t	d) hours Length of a football field
Transport of the state of the s	e') days Timing a running race
- 1	f) quart Time at recess
	g) yards Time until a birthday
and the second	h) minutes Time for sleeping
	i) miles Height of a tree
	j) inches Sugar for a recipe
ligadisan opain al 3 com	Write 4 different fraction names for each of the points
	labeled on this number line
	O A B C D
14.	Find the perimeter of the religious;
	a) A polygon with slues whose measures are 16, 28, and
	32 in inches
	b) An equilateral triangle with the measure of one of
. 4	its sides 14 in recomp
¥y	c) A polygon with 6 congruent sides, the measure of
	one side is 35 1 centimeters.
k.	d) A square, one size of which has the measure of 7 in meters
	e) A polygon with 2 sides whose measures have the sum
	of 8 yards and 3 sides whose measures have the sum
The global state of the state o	of 15 in yards.
	-568
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Management of the second of th	268

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Part B

Write a mathematical sentence (or two sentences if necessary)

for each problem and solve. Write an answer sentence.

- 1. The Davis family uses, 8 eggs for breakfast. What part of a dozen eggs is left?
- 2. Eddie earns 75 cents on Monday, 50 cents on Wednesday, and 75 cents on Friday mowing lawns. How much will he earn in six weeks?
- 3. The school bus runs 7 miles on a gallon of gasoline.

 Each week the bus goes an average of 882 miles. How
 much gasoline will the bus use in four weeks?
- her horse. She bought 5 bales of hay at \$1.75 a bale and 100 lb. of oats at \$5.30. How much will this month's feed bill be?
 - 5. Tom hit a softball 135 ii Randy hit the ball 25 ft. farther than Tom. How har and mandy hit the ball?
 - 6. It is 347 air miles from San Francisco to Los Angeles, 1240 air miles on to Dallas, 443 air miles from Dallas to New Orleans, then 669 air miles on to Miami. How many air miles is it by this route, from San Francisco to Miami?



- 7. The nurse found Janice to be 4 ft. 4 in. tall, Linda ... 4 ft. 11 in. tall, and Maria 4 ft. 9 in. tall. How much taller than Janice is Linda?
- 8. In the standing broad-jump Pat's best jump was 5 ft. 3in.
 while Roy's best jump was 6 ft. 2 in. Roy's jump was how
 much better than Pat's?
- 9. For his birthday Tom received a new baseball bat that is 24 inches long. The bat's length is what part of a yard?
- 10. Joe delivers 56 papers each day. How many papers does he deliver in 28 days?
- 11. Susan buys 2 dozen cookies for 30 cents a dozen and a cake for 80 cents. How much does she pay the clerk?

Braintwisters

The state of the s

- pieces, each 6 inches long it takes five minutes to make each cut. How man, minutes will it take you to cut the 5 pieces?
- 2. An inchworm was slimbling a tree 5 feet high. He climbed three inches every day and slipped back two inches every night. How many days will it take him to reach the top?



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