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ABSTRACT

This material, organized in a workbook format, was developed to be used with the non-college bound, lower one-third of the ninth-grade student population. Topics covered are flowcharts, set theory, number systems (natural numbers, whole numbers, integers, and rationals), number operations, percentage, measurement, finance, geometric constructions, statistics, and number bases. For the teacher's manual, see SE 016 407. (DT)

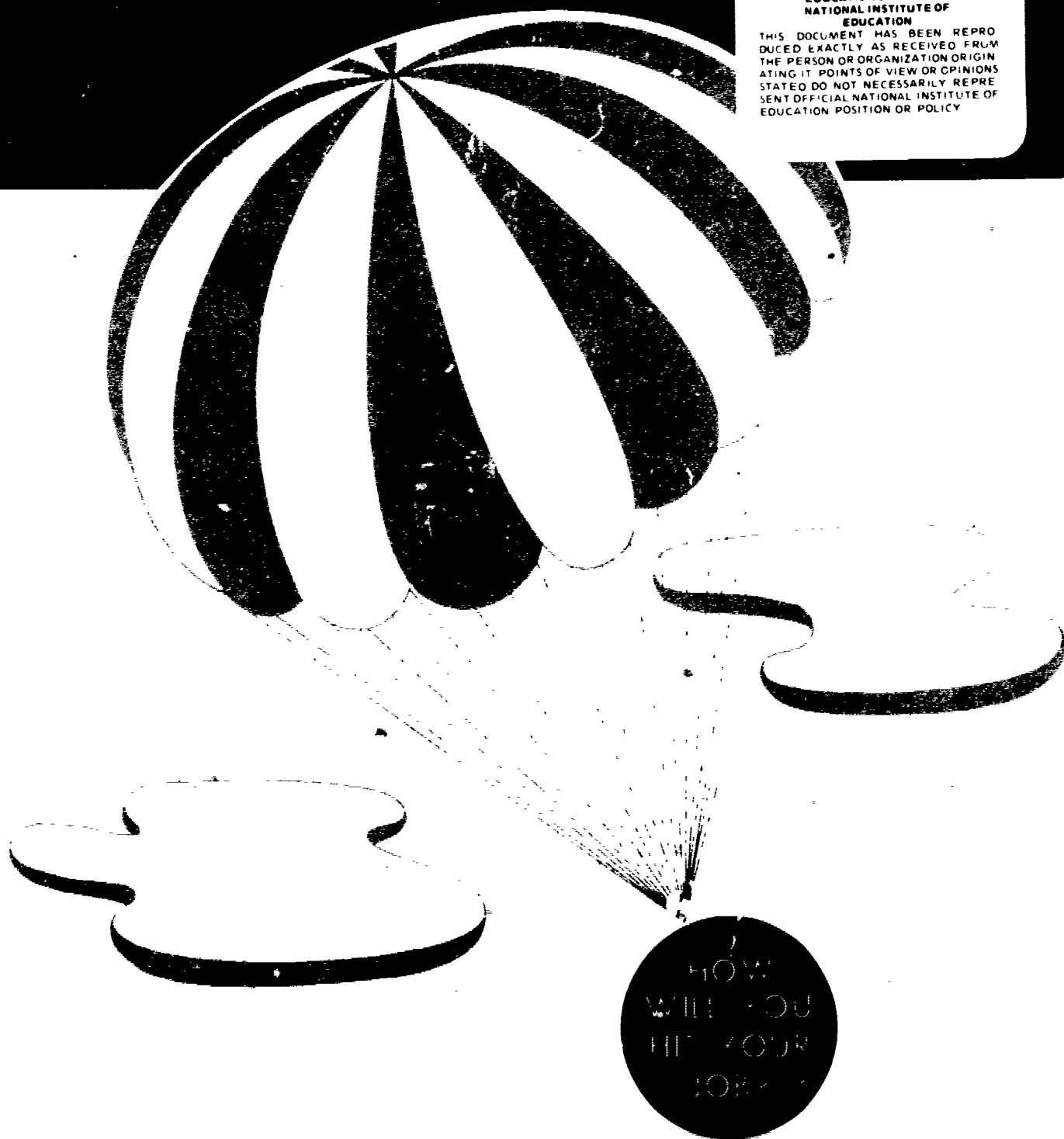
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DROP-IN MATHEMATICS

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PREFACE

The basic material in this book was developed by eight teachers of mathematics in Arkansas Schools working on a grant to Wynne Public Schools under Title III of the Elementary and Secondary Education Act in the summer of 1966. The material was classroom tested in 1966-67, revised in the summer of 1967 and again in the summer of 1968. The material was edited for printing by Mrs. Evelyn Underwood, Mr. Ed White, Mrs. Wanda Lacy, Mrs. Judy Ahart and Mr. Gene Catterton. The editing and printing was financed by the State Title III Program.

The material was developed to be used with the non-college bound student in general and the lower one third of the ninth grade student population in particular. The material develops our number system starting with counting numbers and proceeding through rationals. As the different ideas of numbers are developed, real life problems are used to illustrate the use of the ideas. The authors believe that any teacher who uses this material will enjoy greater success if he will acquire problems from his own local area to use in addition to the ones in this book.

We wish to express appreciation to Dr. Cecil McDermott, of Hendrix College; Mr. Terry Shoemaker of the Jefferson County School in Colorado; Mr. Truett Goatcher, Supervisor in the Department of Education, and Mr. Charles Watson of the State Title III staff, who served as consultants during the revision and editing of the material.

This material was originally prepared under a grant authorized by the U. S. Office of Education through Section 301-308 of Public Law 88-10 Title III. The original project entitled "Calculators in a General Mathematics Laboratory" was sponsored by the Wynne, Arkansas, Public Schools and was directed by Mr. Gene Catterton. Six Arkansas school districts: Hope, Pine Bluff, Lewisville, Wynne, Jonesboro and Fort Smith made up the original experimental sample.

During the summer of 1971 a committee, directed by Gene Catterton and funded under section 303 of the Elementary and Secondary Education Act 91-230 by Title III section of the Arkansas Department of Education revised, up-dated and prepared the original material for printing. The committee was composed of the following teachers who used the materials: Mrs. Evelyn Underwood, Mrs. Wanda Lacy, Mr. Ed White and Mrs. Judy Ahart. Mathematics consultants to the committee were Dr. Cecil McDermott and Mr. Truett Goatcher.

Printing of these revised materials has been made possible through section 303 funds of the Elementary and Secondary Education Act which are administered by the Title III section of the Arkansas Department of Education.

The project presented herein was performed pursuant to a grant from the U. S. Office of Education, Department of Health, Education and Welfare. However, the materials presented do not necessarily reflect the position or policy of the U. S. Office of Education and no official endorsement by the U. S. Office of Education should be inferred.

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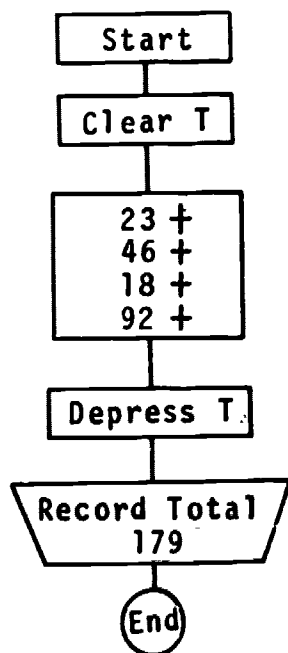
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UNIT I
FLOWCHARTS

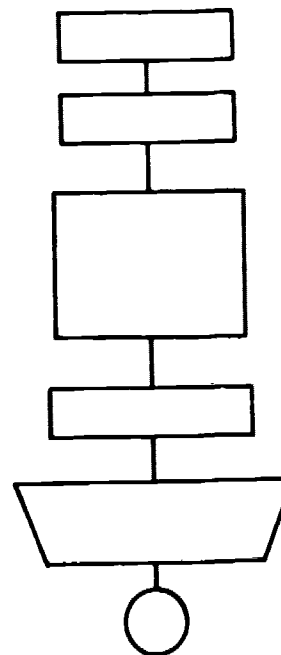
Example 1

$$\begin{array}{r} 23 \\ 46 \\ 18 \\ +92 \\ \hline \end{array}$$



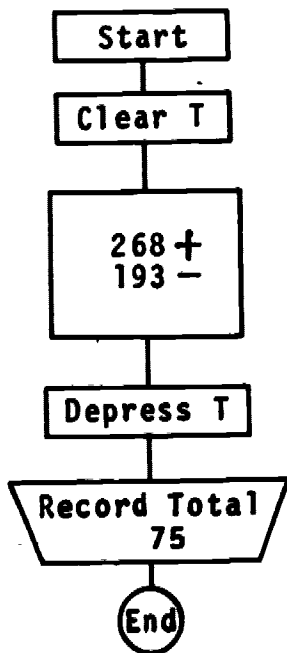
Exercise 1

$$\begin{array}{r} 98 \\ 192 \\ 471 \\ +64 \\ \hline \end{array}$$



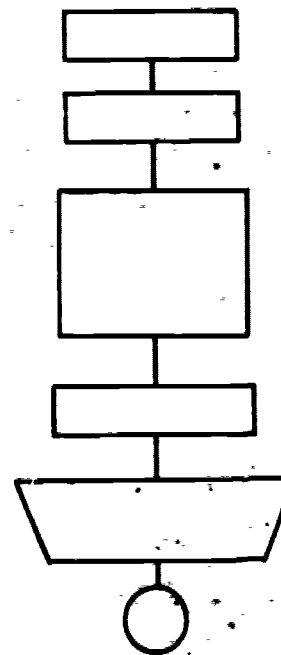
Example 2

$$\begin{array}{r} 268 \\ -193 \\ \hline \end{array}$$



Exercise 2

$$\begin{array}{r} 541 \\ -267 \\ \hline \end{array}$$



Calculator Practice

Add:

1. 567	2. 349	3. 1398	4. 5610	5. 3480
350	764	9871	2345	1156
910	610	6070	3387	2595
590	444	6767	4353	5687
56	600	674	7008	76
<u>542</u>	<u>876</u>	<u>9876</u>	<u>7654</u>	<u>62</u>

6. 2765	7. 9874	8. 7190	9. 1000	10. 98,709
1133	1138	1117	9999	38,470
4756	3889	3030	9510	10,489
9876	1098	1819	9722	45,901
7364	9485	5867	9206	60,007
4685	9874	9765	2094	98,764
<u>1980</u>	<u>1010</u>	<u>9001</u>	<u>1037</u>	<u>76,347</u>

Subtract:

11. 9087	12. 7865	13. 890,765	14. 90,876
<u>-4580</u>	<u>-1098</u>	<u>-91,081</u>	<u>-9,871</u>

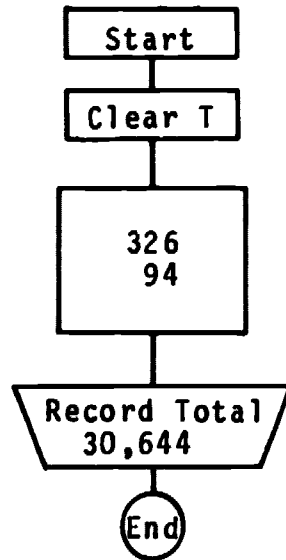
15. 100,098	16. 1,098,765,432	17. 9,080,705,050
<u>-8,761</u>	<u>-78,965,190</u>	<u>-98,765,430</u>

18. $983,765 - 18,765 =$ _____

19. $9,876,543,210 - 123,456,789 =$ _____

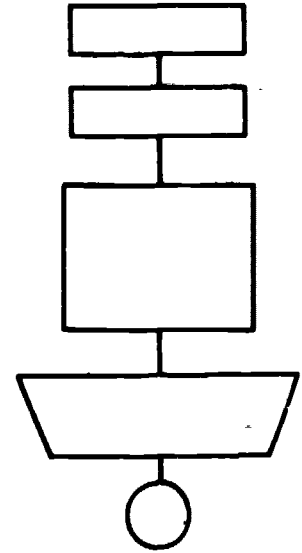
Example 3.

$$\begin{array}{r} 326 \\ \times 94 \\ \hline \end{array}$$



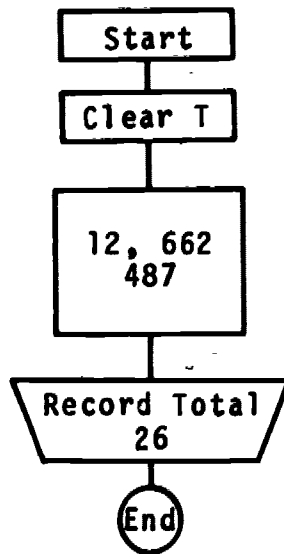
Exercise 3.

$$\begin{array}{r} 492 \\ \times 87 \\ \hline \end{array}$$



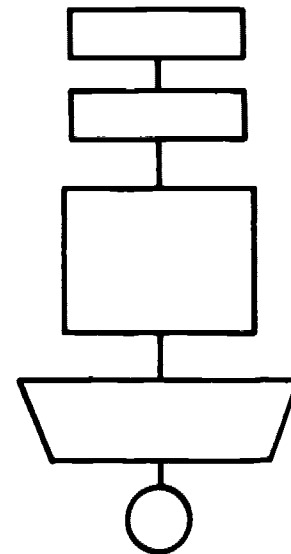
Example 4.

$$12,662 \div 487 =$$



Exercise 4.

$$8473 \div 37 =$$



Calculator Practice

Multiply:

1. $\begin{array}{r} 4657 \\ \times 431 \\ \hline \end{array}$

2. $\begin{array}{r} 6780 \\ \times 328 \\ \hline \end{array}$

3. $\begin{array}{r} 1098 \\ \times 19 \\ \hline \end{array}$

4. $\begin{array}{r} 675,478 \\ \times 49,761 \\ \hline \end{array}$

5. $\begin{array}{r} 9776 \\ \times 57 \\ \hline \end{array}$

6. $\begin{array}{r} 98,765 \\ \times 76 \\ \hline \end{array}$

7. $\begin{array}{r} 90,100 \\ \times 107 \\ \hline \end{array}$

8. $\begin{array}{r} 3,456,789 \\ \times 567 \\ \hline \end{array}$

9. $76,610,987 \times 1,098 =$ _____

10. $98,761,000 \times 5,678 =$ _____

Divide:

11. $10,600 \div 25 =$ _____

12. $952 \div 56 =$ _____

13. $9408 \div 112 =$ _____

14. $3375 \div 15 =$ _____

15. $5951 \div 11 =$ _____

16. $14,518 \div 17 =$ _____

17. $350,027 \div 541 =$ _____

18. $128,388 \div 823 =$ _____

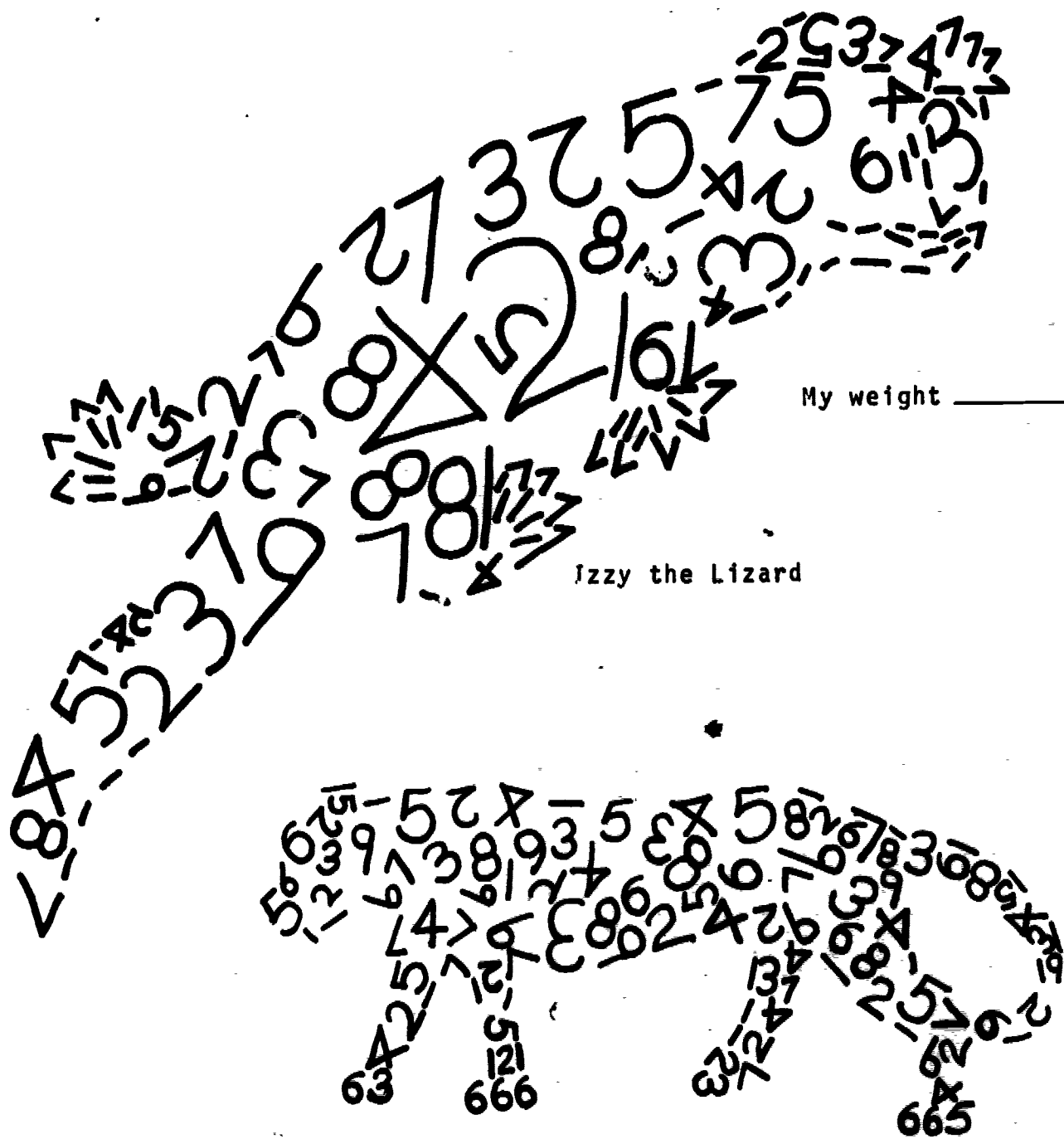
19. $666,000 \div 150 =$ _____

20. $99,661 \overline{) 219,254,200}$

Which Is Heavier?

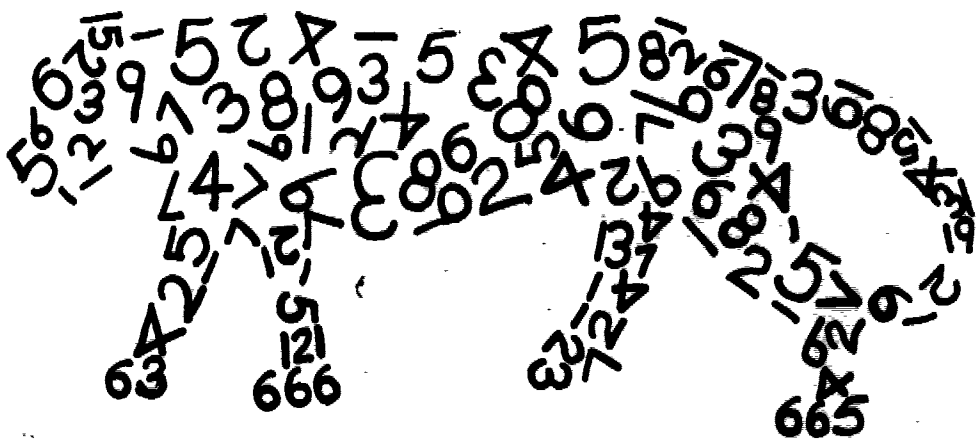
Every line segment is a one digit numeral.

The 6's are curved;
the 9's are straight.
Add all of my numbers
to find my weight.



My weight _____

Izzy the Lizard



Bengy the Tiger

My weight _____

UNIT II

SETS

A. Set: A set is a collection of objects or ideas.

Examples:

1. Set of dishes
2. Pupils in this room
3. Leaves on a certain tree
4. Symbols for making flowcharts
5. Grains of sand on the earth
6. Stars

Exercises

1. Give 3 examples of sets in this room. _____

2. Give 3 examples of sets in your home. _____

3. Give 3 examples of student groups in
your school. _____

B. Elements: Elements are the members belonging to a set. Elements may be described or listed.

Exercises

Description	Listed Elements
1. Set A = {Starter set of dishes}	= {Plates, cups, saucers, bowls}
2. Set B = {Teacher of this class}	= {_____}
3. Set C = {The set of letters in my name}	= {_____}
4. Set D = {_____}	= {Dimes, nickels, pennies}
5. Set E = {_____}	= {I, V, X, L, C, D, M}
6. Set F = {Favorite record}	= {_____}
7. Set G = {The pupils in this room}	= {(List on another paper)}

C. Finite Set: A finite set is a set in which all the elements can be counted. (There is a last element).

Exercises

Description	Listed Elements
1. Set J = {The counting numbers}	= {1, 2, 3, 4, ..., 49, 50}
2. Set K = {The odd numbers less than 100}	= {_____}
3. Set L = {The letters of the alphabet}	= {_____}
4. Set M = {_____}	= {3, 6, 9, ..., 30, 33}
5. Set N = {_____}	= {1, 3, 5, 7, ..., 27, 29}
6. Set O = {Set of even counting numbers between 10 and 1000}	= {_____}

- D. Infinite Set: An infinite set is a set in which all the elements cannot be counted. (There is no last element).

Examples:

- | | |
|---------------------|---------------------|
| 1. Counting numbers | 4. Odd numbers |
| 2. Even numbers | 5. Rational numbers |
| 3. Multiples of 3 | 6. Whole numbers |

Many infinite sets can be listed by pattern.

Example:

Set Z = Set of all counting numbers = $\{1, 2, 3, 4, 5, \dots\}$

Exercises

1. Set Y = Set of all even counting numbers = $\{\underline{\hspace{2cm}}\}$
2. Set X = Set of all counting numbers which are multiples of three = $\{\underline{\hspace{2cm}}\}$
3. Set W = $\underline{\hspace{2cm}}$ = $\{4, 8, 12, 16, 20, \dots\}$
4. Set V = $\underline{\hspace{2cm}}$ = $\{4, 9, 16, 25, 36, \dots\}$

- E. Empty or null sets: A set having no elements is the empty or null set. This is written $\{\}$ or \emptyset

Examples:

1. Set U = The students in this class who are college graduates. $\underline{\emptyset}$
2. Set T = The people in this class who ride tricycles to school. $\underline{\{\}}$

Exercises

1. Set S = $\{\text{Women who have been President of the United States.}\}$
2. How many elements are the set of Jolly Green Giants in this class room? $\underline{\hspace{2cm}}$

- F. **Subset:** A set whose elements are also members of another set is called a subset.

Examples:

1. Set A = {1, 2, 3, 4, 5, 6, 7}
- Set B = {1, 2, 3, 4}
- Set C = {1, 2, 3, 4, 5, 6}
- Set D = {1, 2, 3, 4, 5, 6, 7}
- Set E = {1}

Sets B, C, D, and E are all subsets of Set A.

2. Set A = {=, -, X, ÷}
- Set B = {=, X}

Set B is a subset of Set A.

3. Set S = {1, 2, 3}
- Set T = {1, 2, 3, 4, 5, . . . }

Set S is a subset of Set T.

The null set is a subset of every set.

Every set is a subset of itself. (Set S is a subset of Set S)
(Set T is a subset of Set T)

Exercises

1. Set N = {Sunday, Saturday, Friday}
 - a. List all the subsets of one element.
 - b. List all the subsets of two elements.
 - c. List all the subsets of three elements.
 - d. List all the subsets of four elements.
 - e. Is the null set a subset of this set? _____
 - f. How many subsets did you obtain from Set N? _____

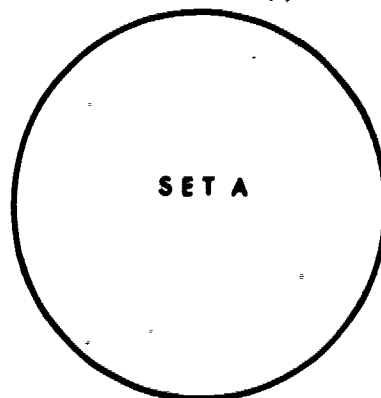
2. Given Set $N = \{\text{Mary, Jane, Joe}\}$
 - a. List all subsets in Set N.
 - b. What kind of a set is Set N?
3. Given Set $S = \{3, 7, 6, 1\}$
 - a. List all subsets of one element in Set S. _____
 - b. List all subsets of two elements in Set S. _____
 - c. List all subsets of three elements in Set S. _____
 - d. List all subsets of four elements in Set S. _____
 - e. List the elements of a set of which S is a subset. _____
4. How many subsets are possible:
 - a. from a three element set? _____
 - b. from a four element set? _____

G. Venn Diagrams: Venn diagrams are drawings that show the relation of sets and subsets.

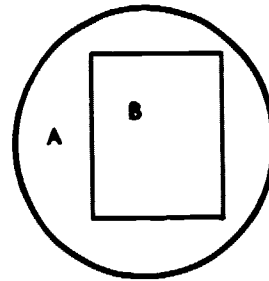
Example.

1. Set A = {All students in school}
- Set B = {All students assigned to this room this hour}
- Set C = {All boys assigned to this room this hour}

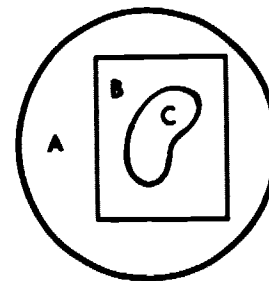
Let Set A be pictured as a geometric figure such as a circle.



Since Set B is a subset of Set A, it may be pictured as a smaller figure inside the larger figure.



Since Set C is a subset of Set B, it may be represented by an even smaller figure.



Is Set C a subset of Set A?

Exercises

Use Venn diagrams to show the relationship between the following sets.

1. Set A is the set of all boys in our state.

Set R is the set of all boys in our school.

Set S is the set of all boys in our mathematics class.

2. Set T is the set of counting numbers less than 50.

Set G is the set of even counting numbers less than 50.

Set M is the set of counting numbers less than 50 which can be divided by three.

H. Intersection of Sets: The intersection of two or more sets is a set containing all elements that are common to the individual sets.

Example:

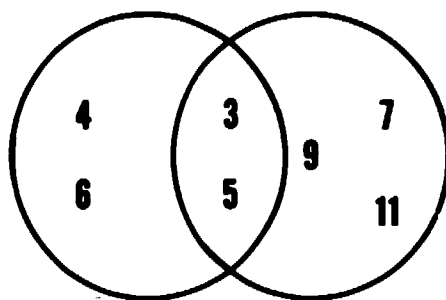
1. Set A = {3, 4, 5, 6}

Set Y = {3, 5, 7, 9, 11}

List the set of elements which belong to both Set A and Set Y.

Set N = {3, 5}

Set N is formed by the intersection of Set A and Set Y. The following Venn diagram shows this intersection.



Exercises

1. Set A = {1, 2, 3}

Set B = {3, 4, 5}

Set C = {Set A intersection Set B} = {_____}

Draw a Venn diagram of these sets. Shade only the intersection. (Set C)

2. The set of even numbers 1 through 20 = {_____} = Set K.

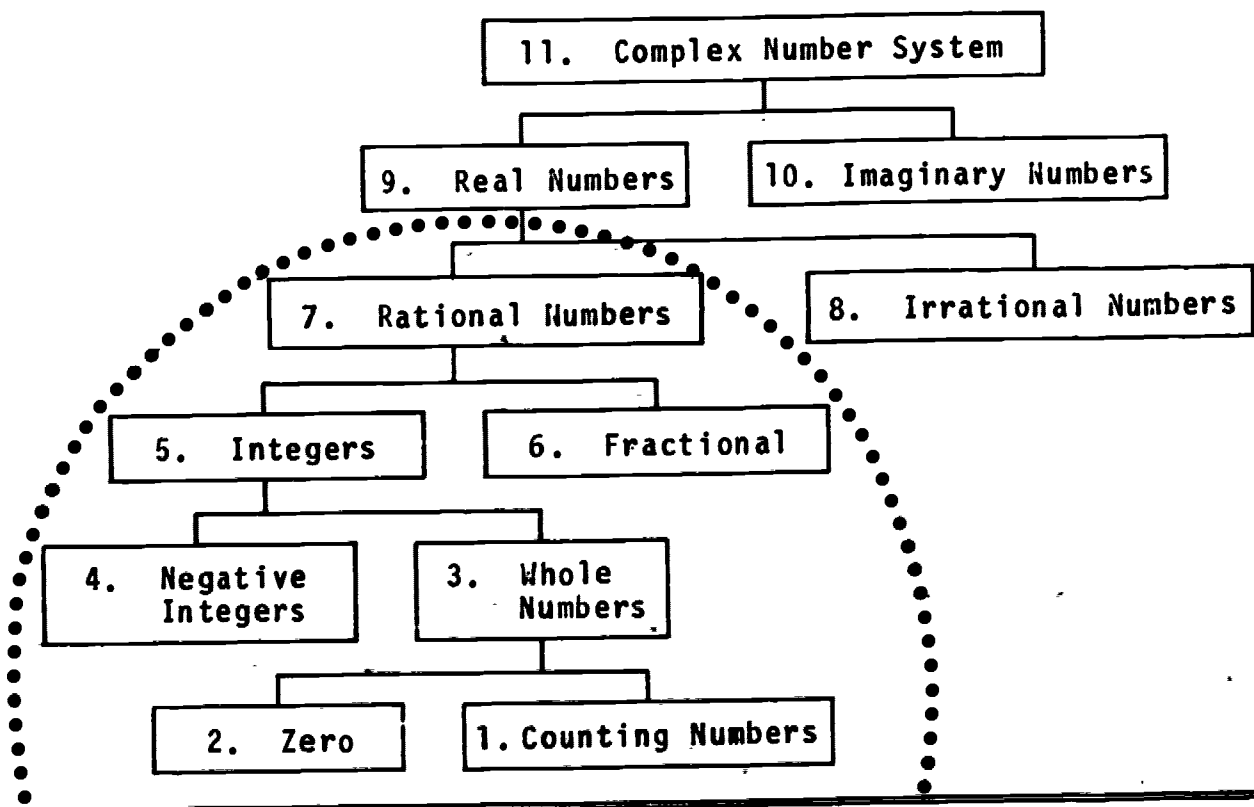
The set of numbers 1 through 20 which can be divided by three = {_____} = Set J.

The intersection of Set K and Set J = {_____} = Set D.

Show these sets using a Venn diagram.

I. Number System: A set of numbers that obeys a definite set of laws when added, subtracted, multiplied or divided.

Infinite sets play an important role in the study of mathematics. The outline of our number system involves several infinite subsets.



What is the only subset above which is not infinite? _____

Our study will be mainly about the sets in the dotted line. We will see why we need these sets of numbers and what they are.

Can you give an example of a number from each subset in the outline?

- Set Number: 1. _____ 7. _____
 2. _____ 8. _____
 3. _____ 9. _____
 4. _____ 10. _____
 5. _____ 11. _____
 6. _____

J. Renaming Numbers: Every number has many names.

Exercises

1. List ten names for the number (10).



2. Draw lines from 6 to all other names for 6 that you can find in this box.

$(8 \div 2)$	$(7 + 3)$	$(5 + 1)$
$(3 + 3)$	6	$(11 - 6)$
$(1 + 11)$	$(10 - 5)$	$(4 + 2)$

3. Draw a loop around all those number names which tell how many



's you see in the picture.

	$2 + 2 + 1$	$7 - 3$
	$5 + 0$	$3 + 2$
$6 - 3$	$8 - 4$	$9 - 2$
$1 + 1 + 1 + 2$		
$4 + 1$	$2 + 2 + 2$	
	$3 + 3 - 1$	

UNIT III

COUNTING NUMBERS

A. Investigation of Counting Numbers

Exercises

- _____ 1. How many members are in your family?
- _____ 2. How many mathematics books do you have in your home?
- _____ 3. What is the use of the black cable you often find laid across a highway or street?
- _____ 4. How many windows are in your home?
- _____ 5. How many desks are in this mathematics classroom?
- _____ 6. How many students are there in this mathematics class?
- _____ 7. How many words do you count on this page?
- _____ 8. What is the total number of letters used in writing the words on this page?
- _____ 9. What is the average number of letters used per word?

Exercises

From one counting number to the next counting number

1. $13 + \bigcirc = 14$ 2. $6 + 1 = \bigcirc$
3. $\bigcirc + 1 = 124$ 4. $1256 + \bigcirc = 1257$
5. a. $\bigcirc + \bigcirc + \bigcirc = 3$
b. $\bigcirc + \bigcirc = 3$
6. a. $\bigcirc + \bigcirc + \bigcirc + \bigcirc = 4$
b. $\bigcirc + \bigcirc = 4$
c. $3 + \bigcirc = 4$

7. If any counting number is chosen how do you find the next counting number? _____
8. a. What are the different names for the number four in exercise 6?
b. Is there a difference between "b" and "c" in exercise 6?
c. Can you write exercise 6 in still another way?

Calculator Practice

$$\begin{array}{r} 1. \quad 21 \\ \quad 3 \\ \quad 52 \\ \hline \quad 61 \end{array}$$

$$\begin{array}{r} 2. \quad 6 \\ \quad 9 \\ \quad 8 \\ \quad 7 \\ \hline \quad 34 \end{array}$$

$$\begin{array}{r} 3. \quad 243 \\ \quad 257 \\ \quad 672 \\ \hline \quad 979 \end{array}$$

$$\begin{array}{r} 4. \quad 18 \\ \quad 142 \\ \quad 675 \\ \quad 79 \\ \hline \quad 9 \end{array}$$

$$\begin{array}{r} 5. \quad 3 \\ \quad 476 \\ \quad 259 \\ \quad 8 \\ \hline \quad 21 \end{array}$$

$$\begin{array}{r} 6. \quad 454 \\ \quad 7 \\ \quad 782 \\ \quad 7869 \\ \hline \quad 5 \end{array}$$

$$\begin{array}{r} 7. \quad 454 \\ \quad 32 \\ \quad 4876 \\ \quad 6 \\ \hline \quad 25 \end{array}$$

$$\begin{array}{r} 8. \quad 13 \\ \quad 723 \\ \quad 9 \\ \quad 72 \\ \quad 889 \\ \hline \quad 92 \end{array}$$

$$\begin{array}{r} 9. \quad 98 \\ \quad 8 \\ \quad 345 \\ \quad 87 \\ \quad 7652 \\ \hline \quad 56 \end{array}$$

$$\begin{array}{r} 10. \quad 86,456 \\ \quad 24,514 \\ \quad 18,632 \\ \quad 97,543 \\ \quad 12,543 \\ \quad 67,892 \\ \quad 14,897 \\ \quad 64,523 \\ \quad 18,324 \\ \hline \quad 65,889 \end{array}$$

$$\begin{array}{r} 11. \quad 2432 \\ \quad 6719 \\ \quad 8547 \\ \quad 1357 \\ \quad 6429 \\ \quad 8165 \\ \quad 4321 \\ \quad 9658 \\ \quad 4231 \\ \hline \quad 6614 \end{array}$$

Calculator Practice

1.
$$\begin{array}{r} 334 \\ 346 \\ \hline 532 \end{array}$$

2.
$$\begin{array}{r} 567 \\ 876 \\ \hline 545 \end{array}$$

3.
$$\begin{array}{r} 891 \\ 819 \\ \hline 918 \end{array}$$

4.
$$\begin{array}{r} 156 \\ 348 \\ \hline 763 \end{array}$$

5.
$$\begin{array}{r} 245 \\ 631 \\ \hline 893 \end{array}$$

6.
$$\begin{array}{r} 872 \\ 134 \\ \hline 576 \end{array}$$

7.
$$\begin{array}{r} 865 \\ 544 \\ \hline 322 \end{array}$$

8.
$$\begin{array}{r} 218 \\ 422 \\ \hline 553 \end{array}$$

9.
$$\begin{array}{r} 871 \\ 992 \\ \hline 332 \end{array}$$

10.
$$\begin{array}{r} 321 \\ 654 \\ \hline 798 \end{array}$$

11.
$$\begin{array}{r} 161 \\ 385 \\ \hline 369 \end{array}$$

12.
$$\begin{array}{r} 893 \\ 568 \\ \hline 432 \end{array}$$

13.
$$\begin{array}{r} 354 \\ 786 \\ \hline 825 \end{array}$$

14.
$$\begin{array}{r} 319 \\ 813 \\ \hline 457 \end{array}$$

15.
$$\begin{array}{r} 562 \\ 137 \\ \hline 689 \end{array}$$

16.
$$\begin{array}{r} 154 \\ 632 \\ \hline 987 \end{array}$$

17.
$$\begin{array}{r} 654 \\ 321 \\ \hline 811 \end{array}$$

18.
$$\begin{array}{r} 635 \\ 274 \\ \hline 862 \end{array}$$

Practical Application

Date 5-26 1971
 M. Sharon Long

Reg. No.	Clerk	ACCOUNT FORWARDED	
1	Jung		44
2	Beans		18
3	Bunch		41
4	Olives		42
5	Cheese		41
6	P. Chips		39
7	Pasta		29
8	P + Beans		18
9	P. Chops		24
10	Cookies		24
11	Envelopes		5
12			

Date 6-4 1971
 M. Sharon Long

Reg. No.	Clerk	ACCOUNT FORWARDED	
1	Pasta		29
2	P. Chips		25
3	P. Chops		36
4			
5			
6			
7			
8			
9			
10			
11			
12			

44+
 18+
 41+
 42+
 47+
 39+
 29+
 18+
 24+
 24+
 5+
 29+
 35+
 36+
 48+
 41+
 29+
 15+
 59+
 31+
 44+
 15+
 24+
 84+
 22+
 843 T

Date 6-10 1971
 M. Sharon Long

Reg. No.	Clerk	ACCOUNT FORWARDED	
1	Potatoes		48
2	Bunch		41
3	Bread		29
4	Lemons		15
5	Crisps		39
6			
7			
8			
9			
10			
11			
12			

Date 6-18 1971
 M. Sharon Long

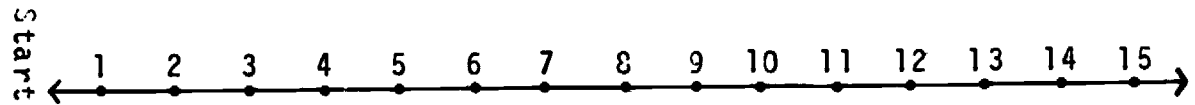
Reg. No.	Clerk	ACCOUNT FORWARDED	
1	Bread		31
2	Cheese		44
3	Tomatoes		15
4	Potatoes		24
5	Ham		84
6	P. Chops		22
7			
8			
9			
10			
11			
12			

Does the addition tape at the right agree with the tickets? If there are mistakes, circle them and correct them. Also, correct the total.



3. Addition of counting numbers on a number line

Example:



Think of the distance between the points as a unit of measure.

Problem $4 + 7 =$

Begin at "start" and count 4 units to the right. (positive)

Beginning at 4 count 7 units to the right.

Which counting number did you reach?

Exercises

Make number lines for the following problems:

1. $8 + 3$

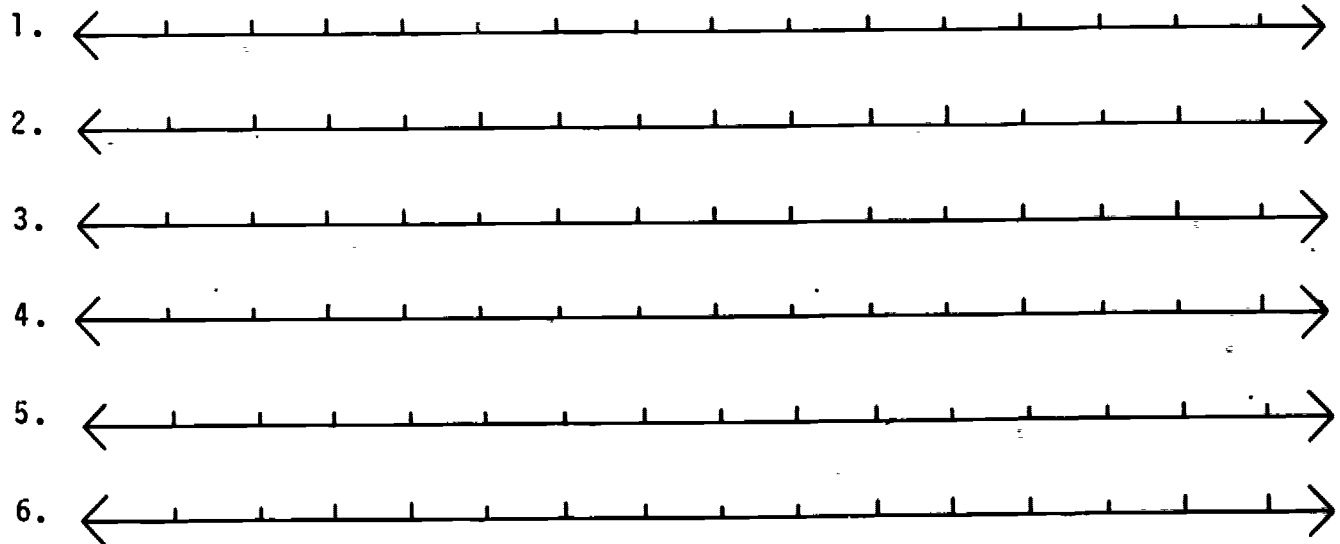
2. $7 + 2 + 4$

3. $1 + 7 + 3$

4. $5 + 1 + 3$

5. $8 + 1 + 3 + 2$

6. $6 + 1 + 1 + 2$



7. Mary has 5 shades of Revlon lipstick and Sue has 9 shades.
- Make a number line.
 - Number 15 units from start.
 - The two girls have how many shades in all?
 - What counting numbers were used in this problem?
 - What was the greatest counting number obtained?
 - What operation was used in this problem?
8. Joe hit 2 home runs, Jim hit 3 home runs, and John hit 4 home runs.
- Make a number line.
 - Number the units.
 - How many home runs were hit altogether?
 - What counting numbers were used in this problem?
 - What was the greatest counting number obtained?
 - What operation was used in this problem?
9. During library reading period, Mary read 22 pages, Jane read 11 pages, and Joe read 16 pages.
- Make a number line.
 - Can you find another idea (or number) to use in place of the word "start"?
 - How many pages were read by Mary, Jane and Joe?
 - Perform the operation using the number line.
 - What was the greatest counting number obtained?
10. John has 5 nickels, Jim 3 nickels, Al 1 nickel and Bob 2 nickels.
- Make a number line.
 - Number the units.
 - How many nickels do all the boys have?
 - What counting numbers were used in this problem?
 - What was the greatest counting number obtained?
 - What operation was used in this problem?

Magic Squares: A magic square is a square which is divided into a number of smaller squares called cells. By following a few simple rules, consecutive counting number may be placed in these cells so that the sum of each row, column, and diagonal is the same.

Magic squares with an odd number of cells:

1. Begin by placing any counting number in the center cell of top row.
2. Proceed diagonally upward to the right.
3. If you stop outside the large square, go to the bottom cell in that column or the extreme left cell in that row.
4. If you stop in a full cell, go back to the last number and place the next number in the empty cell below.
5. Small cell at top right with X should be treated as full cell.

Example:

			X
8	1	6	
3	5	7	
4	9	2	

Exercises

1.

			X

2.

						X

3.

						X

Magic squares with an even number of cells:

1. Begin by drawing in the diagonals.
2. Start in top left corner and count consecutively placing only the numbers that fall in cells through which a diagonal passes.
3. Put the first consecutive number not written in the next to the last cell and count back to the beginning placing numbers in the empty cells.

Example:

1	15	16	4
12	6	7	9
8	10	11	15
13	3	2	16

Exercises

1.

3.

2.

4.

C. Closure Property for Addition

Exercises

1.

X	X
X	X

 How many X's do you see in the box? _____

2.

X	X
X	X

 How many X's are in this box? _____

3. How many X's are in both boxes? _____

4. Is your answer a counting number? _____

5. a. How many girls are in this class? _____

b. How many boys are in this class? _____

c. How many students are in this class? _____

6. What type of number is answer "c"? _____

7. Add the following:

$\begin{array}{r} 22 \\ 15 \\ \hline \end{array}$	$\begin{array}{r} 33 \\ 12 \\ \hline \end{array}$	$\begin{array}{r} 8 \\ 13 \\ \hline \end{array}$	$\begin{array}{r} 162 \\ 221 \\ \hline \end{array}$	$\begin{array}{r} 142 \\ 97 \\ \hline \end{array}$
---	---	--	---	--

8. Can you give an example of adding two counting numbers, where your answer is not a counting number?

9. If you add any two counting numbers, what type of number is your answer?

10. Add:

$\begin{array}{r} 7 \\ 9 \\ \hline \end{array}$	$\begin{array}{r} 12 \\ 41 \\ \hline \end{array}$	$\begin{array}{r} 13 \\ 8 \\ \hline \end{array}$	$\begin{array}{r} 14 \\ 7 \\ \hline \end{array}$	$\begin{array}{r} 51 \\ 6 \\ \hline \end{array}$	$\begin{array}{r} 32 \\ 42 \\ \hline \end{array}$
---	---	--	--	--	---

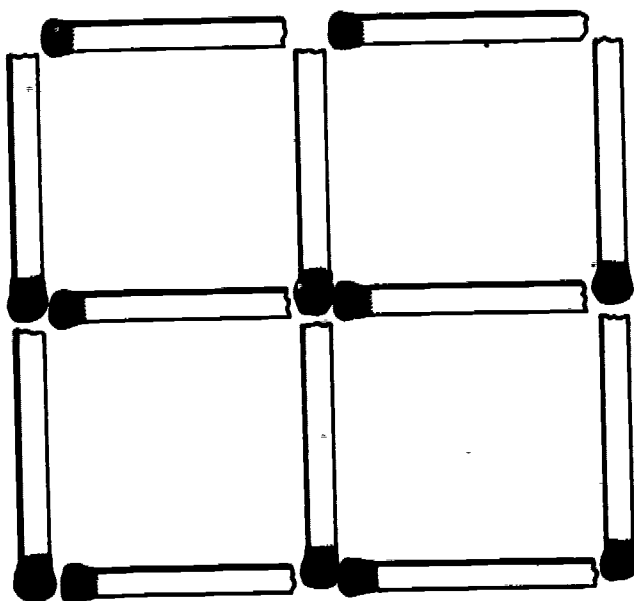
Note: Another way of stating problem 9 is to say the set of counting numbers is closed under the operation of addition.

Practical Application

Use the chart on the following page to find the number of seeds needed.

Crops to be planted	Distance between rows	Distance between plants	No. of seeds per acre	No. of acres	Total number of seeds
Cotton	30"	4"	_____	100	_____
Corn	30"	24"	_____	56	_____
Watermelons	42"	50"	_____	25	_____
Soybeans	30"	2"	_____	150	_____
Cantaloupes	36"	36"	_____	12	_____
Potatoes	30"	4"	_____	5	_____

Did you strike out?



In the arrangement of matches at the left, there are four small squares and one large square, making five squares in all. Can you change the position of three matches to reduce the number of squares to three?

Plant Population Per Acre At
Various Row and Hill Spacings

One Plant Per Hill

Row Width

Spacing In Row	30"	32"	34"	36"	38"	40"	42"
2"	104,538	98,002	92,238	87,114	82,529	78,420	74,670
4"	52,269	49,001	46,119	43,557	41,264	39,201	37,335
6"	34,846	32,667	30,746	29,038	27,510	26,134	24,890
8"	26,134	24,501	23,060	21,778	20,632	19,600	18,667
10"	20,908	19,600	18,448	17,423	16,506	15,680	14,934
12"	17,423	16,334	15,373	14,519	13,755	13,067	12,445
14"	14,934	14,000	13,177	12,445	11,790	11,200	10,667
16"	13,067	12,250	11,530	10,889	10,316	9,800	9,334
18"	11,615	10,889	10,249	9,679	9,170	8,711	8,297
20"	10,454	9,800	9,224	8,711	8,253	7,840	7,467
22"	9,503	8,909	8,385	7,919	7,503	7,127	6,788
24"	8,711	8,167	7,687	7,259	6,877	6,533	6,222
26"	8,041	7,539	7,095	6,701	6,372	6,031	5,744
28"	7,467	7,000	6,588	6,222	5,895	5,600	5,334
30"	6,969	6,533	6,149	5,808	5,502	5,227	4,978
32"	6,534	6,125	5,765	5,445	5,158	4,900	4,667
34"	6,149	5,765	5,426	5,124	4,855	4,649	4,392
36"	5,808	5,445	5,125	4,840	4,585	4,356	4,149
38"	5,502	5,158	4,855	4,585	4,344	4,126	3,930
40"	5,227	4,900	4,612	4,356	4,126	3,920	3,733
42"	4,978	4,667	4,392	4,148	3,930	3,733	3,536
44"	4,752	4,455	4,193	3,960	3,751	3,564	3,394
46"	4,545	4,261	4,010	3,788	3,588	3,409	3,247
50"	4,182	3,920	3,690	3,485	3,301	3,136	2,987
54"	3,872	3,630	3,416	3,226	3,057	2,904	2,766
58"	3,605	3,379	3,181	3,004	2,846	2,704	2,575
62"	3,372	3,161	2,975	2,810	2,662	2,529	2,409
66"	3,168	2,970	2,795	2,640	2,500	2,376	2,263
70"	2,987	2,800	2,635	2,489	2,358	2,258	2,133
74"	2,825	2,649	2,493	2,354	2,231	2,119	2,018
76"	2,751	2,579	2,427	2,292	2,172	2,063	1,965
78"	2,680	2,513	2,365	2,234	2,116	2,010	1,915
80"	2,613	2,450	2,306	2,178	2,063	1,960	1,867

D. Commutative Property for Addition

Exercises

1.
$$\begin{array}{r} 17 \\ 36 \\ \hline \end{array}$$

$$\begin{array}{r} 36 \\ 17 \\ \hline \end{array}$$

Observe your results.

2.
$$\begin{array}{r} 8 \\ 15 \\ \hline \end{array}$$

$$\begin{array}{r} 15 \\ 8 \\ \hline \end{array}$$

What seems to be true of the results?

3.
$$\begin{array}{r} 29 \\ 45 \\ 37 \\ 13 \\ \hline \end{array}$$

$$\begin{array}{r} 13 \\ 37 \\ 45 \\ 29 \\ \hline \end{array}$$

Check your results and compare.

4. Could you find another arrangement of the numbers in the last problem that will give the same results?
5. Tommy has 15 rock-and-roll records, Joe has 12, and Bill has 2.
- a. What is the total number of records? _____
- b. Could the order be rearranged? _____
- c. How many different ways? _____
- d. List these ways. _____
6. Johnny pushes his grocery cart to the checkout stand and unloads the groceries onto the counter. Does the clerk have to check his items in the order in which they are placed on the counter? Why?
7. Check the groceries on the following page and compare tapes and totals with other members of the class.

Note: Since numbers can be added in any order with the same results being obtained, addition then is said to be commutative.

Purnell's Pride U.S. Inspected Grade 'A'

FRYERS

Cut Up,

Lb. 37c

Whole

Lb.

31c

JOY
LIQUID
 GIANT
 SIZE
 22 oz
 bottle

45c

Wagner
**ORANGE
 DRINK**
 Quart **25c**

YOUNG TENDER

Yellow Squash

lb.

19c

CALIFORNIA
STRAWBERRIES
 Qt

89c

Coca Cola, Pepsi, Dr. Pepper

Qt. Drinks 3 for 89c

BETTY CROCKER

Cake Mix

WITH OUR
COUPON
OFFER

3

1-lb.
2-oz.
pkgs.

79c

E. Identity Element for Addition

Exercises

1. How many times does the letter "p" appear in the word "apple"? _____
2. How many times does the letter "p" appear in the word "grape"? _____
3. How many times does the letter "P" appear in the word "banana"? _____
4. Can you write a symbol for the answer in exercise 3?
5. Give this symbol a name? _____
6. Is this newly named number a counting number?

7. In addition, the number zero has a special property. $5 + 0 = 5$, $7 + 0 = 7$, $0 + 21 = 21$. Since zero is "special" in addition, we call it the identity element for _____.
8. Add:
 - a.
$$\begin{array}{r} 330 \\ 207 \\ \hline \end{array}$$
 - b.
$$\begin{array}{r} 40 \\ 607 \\ \hline 90 \end{array}$$
 - c.
$$\begin{array}{r} 43 \\ 9 \\ 10 \\ 8 \\ \hline 30 \end{array}$$
 - d. $7 + 8 + 10 + 12 + 20 + 17 =$
 - e. $13 + 30 + 27 + 14 + 26 =$
9.
 - a. What purpose does the zero serve in each numeral of problem 8? _____
 - b. Zero is the _____ element for addition and also a place holder in numerals.

NOTE: The identity element for addition is a number that can be added to any given number and the sum is that given number.

10. The following items were bought for Mrs. Smith's new kitchen:

Teflon griddle	\$1.88
Storage set	1.33
Electric can opener	7.77
Dish drainer	1.14
6 Tumblers	<u>1.05</u>
Total	

The clerk was given \$20.00.
What change should be returned? _____

11. The following supplies and food freezer were purchased by Mrs. Smith:

Home freezer	\$198.88
Plastic freezer bags	.88
1 roll freezer paper	1.28
1 package plastic containers	.87
1 roll tape	<u>.90</u>
Total Purchase	

Is the cost more or less than \$210? _____

How much more or how much less? _____

12. Mr. Russell purchased the following extras for his car:

Mirror muff	\$.39
Letter basket	1.41
Auto Compass	3.33
Fender flaps	1.55
Dash fence	.29
Seat belt retractor	<u>1.59</u>
Total Cost	

Change from \$10.00 bill _____

Practical Applications

1. A purchase amounted to \$7.56.
The clerk was given a ten dollar bill.

Count the change as the clerk would count it out to the customer. Begin with \$7.56 and count 7.57, 7.58, 7.59, etc.

2. A purchase amounted to \$3.24.
The clerk was given a five dollar bill.

Count the change.

3. A purchase amounted to \$.32.
The clerk was given a half-dollar.

Count the change.

4. A purchase amounted to \$12.21.
The clerk was given a twenty dollar bill.

Count the change.

5. A purchase amounted to \$34.75.
The clerk was given a fifty dollar bill.

Count the change.

Calculator Practice

Add:

1. 91.35
34.11
22.33
883.22
11.99
90.46
34.94
14.64
82.55

2. 45.234
45.459
65.365
975.098
3.967
.214
90.666
6.890
8.543

3. 47.09
78.09
9304.33
675.43
3456.23
34.87
9098.67
23.23
3757.09

4. 987,564.98
475,667.98
388,641.53
49,586.90
98,876.98

5. 3.987
765.937
28.984
2,736.958
37,465.987

6. 3.9
37.4
87.9
364.9
364.3

7. 4758
3746
4657
0987
8765
7654
9876
3985

8. 4758
3645
9087
5432
8765
5432
3245
7865

9. 378,542
3,986
7
346
2,976
38,675
2,987
23



You have gone to work as a route salesman for Dr. Pepper Bottling Company. During the first day you drove a truck that carried 194 cases of drinks. You made only four trips to the plant that day.

Number of cases checked out:				Full cases brought back at the end of day.	
Dr. Pepper	18	18	18	10	3
Cartons:	17	5	10	7	7
K.S.D.P.	18	18	15	17	2
K.S.D.P. Ctns.	17	4	11	18	9
Dietetic:	18	7	9	11	11
Cartons:	17	9	16	7	12
Soda:	18	15	12	5	6
Nugrape:	18	14	16	4	2
Sun Drop:	18	15	13	9	1
Tin Cans:	17	10	15	12	3
Glass Cans:	18	3	8	6	4

Using the above information fill in your daily sales report on the following page. Get the price per case from your local dealer and compute the extensions.

Be sure to find the

- a. total cases you checked out of each type drink.
- b. total cases you checked out of all drinks on all four trips.
- c. total full cases you brought back.
- d. net cases sold of each type drink.
- e. total of the net cases sold of all drinks.

DAILY SALES REPORT

SALESMAN _____ DATE _____ 19__

	BRT. FOR'D	CASES OUT	CASES OUT	CASES OUT	CASES OUT	CASES OUT	CASES OUT	TOTAL CASES OUT	FULL CASES BACK	NET CASES SOLD	PRICE	AMOUNT
DR. PEPPER												
CARTONS												
K. S. D. P.												
K. S. D. P. Cms.												
DIETETIC												
CARTONS												
SODA												
NUGRAPE												
SUN DROP												
TIN CANS												
GLASS CANS												
EMPTIES RETURNED												
BOTTLES												
SHELLS												
TOTAL NET SALES												

UNIT IV
WHOLE NUMBERS

A. Investigation of Whole Numbers

1. How many digits are in the number '238'? _____
What does the digit 2 mean? _____ The digit
3? _____ The digit 8? _____

2. Another name for the number 45,653 is (40,000 + 5,000 +
600 + 50 + 3). There are _____ ? sets of:
_____ ten thousands _____ hundreds
_____ thousands _____ tens
_____ ones

This number written in expanded notation is $4(10,000) +$
 $5(1,000) + 6(100) + 5(10) + 3$.

3. $33,333 = 3(10,000) + 3(1,000) + 3(100) + 3(10) + 3$

Written in multiples of 10 this number is equal to
 $3(10 \times 10 \times 10 \times 10) + 3(10 \times 10 \times 10) + 3(10 \times 10) +$
 $3(10) + 3$

How does each group compare with the group to its right?

NOTE: 100 can be written as 10×10 but it also can be
written 10^2 . The small 2 placed to the upper right of a
numeral is called an exponent. An exponent tells us how
many times a number is used as a factor.

The number above can also be written with exponents as:

$$3(10^4) + 3(10^3) + 3(10^2) + 3(10^1) + 3(10^0)$$

Our number system is based on the number we know as "ten"
and is called the decimal number system.

Exercises

Write the following numbers:

1. 564 Using multiples of 10 _____
 Using exponents _____
2. 7,032 Using multiples of 10 _____
 Using exponents _____
3. 230,156 Using multiples of 10 _____
 Using exponents _____

Acrostic

There are twenty mathematical terms in this puzzle. There are no extra letters; they may be upside down or diagonal; but they are in order. Circle them and list them.

			E	S	R	E	V	N	I		
N	U	L	L			D					
		M	U	L	T	I	P	L	Y		
I	I	S	R			V			T		R
I	N		Q			I			I	O	E
E	F	T		U		D			T		B
S	I	L	E		A	E		A	N		M
B	N		O	G		R	L	D	E	E	U
U	I			W	E	U	E	D	D	S	N
S	T				C	R			I	R	
	E			L	W	H	O	L	E	E	
			A			A			I	V	
		C	L	O	S	E	D	R		N	
		S	U	B	T	R	A	C	T	I	E

Cross Number Puzzle

	1	2	3		4	5	6	
7					8			9
10			11	12			13	
14		15			16	17		
		18				19		
20	21		22		23		24	25
26			27	28			29	
30		31			32	33		
	34				35			

Across

1. Twice fifty-six
4. CXXXII
7. Half of 3864
8. Half of 12,012
10. No. of years in decade
11. No. of pounds in one-tenth of a ton
13. No. of letters in alphabet
14. A dozen more than a thousand
16. III, IV, V, VI
18. No. of elements in a null set
19. $0 + 5$
20. MDCCIX
23. 1027 times two
26. $5 \times 2 + 4 - 2 + 9$
27. Ninety tens
29. 2 score plus 4
30. MDCCXCIX
32. 4 to 1 backwards
34. $33 \times 30 + 9$
35. CCII

Down

1. MCM
2. Lucky (or unlucky?) number
3. MMCCXXII
4. MDCIII
5. $5^2 + 5$
6. 452
7. CXI
9. DCLXVI
12. Cipher
15. No. of years in a century
17. No. which refers to high society
20. 112
21. 3046 plus 5133
22. One less than ten thousand
23. Twice MVI
24. 9,8,7,6,_____,_____,_____,_____,
_____,
_____1
25. $21^2 + 3$
28. 8 times 0
31. $10^2 - 1$
33. Half of forty

B. Associative Property of Addition

Example:

The result of $5 + 7$ is 12. If we then add 9, the final result is 21. The result of $7 + 9$ is 16. If we then add the result to 5, the final result is 21. These combinations can be written as follows using parentheses:

$$(5 + 7) + 9 = 21$$

$$5 + (7 + 9) = 21$$

Exercises

In the following exercises see if the associative property holds true:

1. a. $(18 + 39) + 27 =$

b. $18 + (39 + 27) =$

2. a. $(276 + 345) + 467 =$

b. $276 + (345 + 467) =$

3. a. $3208 + (1609 + 876) =$

b. $(3208 + 1609) + 876 =$

4. Use 13, 45 and 32 and give an example of the associative property.

a. _____

b. _____

A Cardless Card Trick

Ask someone to think of any card in the deck giving the value of 11 to a Jack, 12 to a Queen, 13 to a King, and 1 to an Ace; add the number of the card next higher in sequence. (If he's thinking of a King, add 14.) Multiply the result by 5. Add the value of the suit (clubs 6, diamonds 7, hearts 8, spades 9) to his total; ask for this result. Mentally deduct 5, and tell him the card he thought of. The last number shows you the suit and the rest tells the number of the card.

C. Closure Property for Multiplication

Exercises

1. What is the result in each of the following problems?
 - a. $4 \times 8 \times 6 =$
 - b. $144 \times 12 =$
 - c. $1,859 \times 76 \times 54 =$
 - d. $7 \times 9 \times 8 =$
 - e. $34 \times 746 \times 2,100 =$
 - f. $39 \times 1 =$
 - g. $49 \times 94 =$
 - h. $9,876,432 \times 32,587 =$

2. What kind of number is each answer above?

3. Is there any case of multiplying whole numbers in which the product is not a whole number?

4. Multiply manually and then check on the machine.
 - a. $7 \times 9 =$
 - b. $8 \times 12 =$
 - c. $17 \times 4 =$
 - d. $18 \times 21 =$
 - e. $64 \times 83 =$
 - f. $79 \times 81 =$
 - g. $83 \times 126 =$
 - h. $764 \times 34 =$
 - i. $273 \times 142 =$
 - j. $69 \times 4,782 =$

NOTE: The product of two or more whole numbers is a whole number. Therefore, the whole numbers are closed under multiplication.

Calculator Practice

Multiply:

- | | | | | |
|----|---|---|--|--|
| 1. | a.
$\begin{array}{r} 4,038 \\ \underline{56} \end{array}$ | b.
$\begin{array}{r} 8,492 \\ \underline{354} \end{array}$ | c.
$\begin{array}{r} 9,765 \\ \underline{253} \end{array}$ | d.
$\begin{array}{r} 344 \\ \underline{90} \end{array}$ |
| 2. | $\begin{array}{r} 4,657 \\ \underline{82} \end{array}$ | $\begin{array}{r} 8,762 \\ \underline{752} \end{array}$ | $\begin{array}{r} 48,027 \\ \underline{9,084} \end{array}$ | $\begin{array}{r} 5,862 \\ \underline{906} \end{array}$ |
| 3. | $\begin{array}{r} 8,375 \\ \underline{45} \end{array}$ | $\begin{array}{r} 654 \\ \underline{57} \end{array}$ | $\begin{array}{r} 98,762 \\ \underline{75,243} \end{array}$ | $\begin{array}{r} 47,624 \\ \underline{9,073} \end{array}$ |
| 4. | $\begin{array}{r} 524,903 \\ \underline{35} \end{array}$ | $\begin{array}{r} 759,372 \\ \underline{21} \end{array}$ | $\begin{array}{r} 75,903,613 \\ \underline{243} \end{array}$ | |
| 5. | $\begin{array}{r} 81,065,432 \\ \underline{36,789} \end{array}$ | $\begin{array}{r} 8,196,432 \\ \underline{65,432} \end{array}$ | $\begin{array}{r} 63,826 \\ \underline{432} \end{array}$ | |
| 6. | $\begin{array}{r} 890 \\ \underline{46} \end{array}$ | $\begin{array}{r} 8,476 \\ \underline{374} \end{array}$ | $\begin{array}{r} 5,762 \\ \underline{7,364} \end{array}$ | $\begin{array}{r} 462 \\ \underline{75} \end{array}$ |
| 7. | $\begin{array}{r} 87,302 \\ \underline{3,628} \end{array}$ | $\begin{array}{r} 729,137 \\ \underline{\quad,087} \end{array}$ | $\begin{array}{r} 8,931,876 \\ \underline{87,907} \end{array}$ | |

D. Commutative Property of Multiplication

Example:

$$\begin{array}{r} 23 \\ \times 15 \\ \hline \end{array}$$

$$\begin{array}{r} 15 \\ \times 23 \\ \hline \end{array}$$

What do you observe to be alike in these problems?

What do you observe about these problems that is not the same?

Is order important in multiplication?

Exercises

1.
$$\begin{array}{r} 37 \\ \times 96 \\ \hline \end{array}$$

Can you write the answer to this problem without computing?

$$\begin{array}{r} 96 \\ \times 37 \\ \hline \end{array}$$

2.
$$\begin{array}{r} 58 \\ \times 72 \\ \hline \end{array}$$

$$\begin{array}{r} 72 \\ \times 58 \\ \hline \end{array}$$

3.
$$\begin{array}{r} 246 \\ \times 183 \\ \hline \end{array}$$

$$\begin{array}{r} 183 \\ \times 246 \\ \hline \end{array}$$

4. a. $(78 \times 43) \times 64 =$

b. $64 \times (78 \times 43) =$
Write this answer without computing.

c. What principle of multiplication works here?

"Smart Work"

Arrange the numbers 1, 2, 3, and 4 in the 4 x 4 square so that the sum of each row, column and diagonal will be 10.

Calculator Practice

Multiply:

1. a.
$$\begin{array}{r} 324 \\ \underline{25} \end{array}$$

b.
$$\begin{array}{r} 632 \\ \underline{56} \end{array}$$

c.
$$\begin{array}{r} 843 \\ \underline{72} \end{array}$$

d.
$$\begin{array}{r} 985 \\ \underline{43} \end{array}$$

2. a.
$$\begin{array}{r} 3738 \\ \underline{37} \end{array}$$

b.
$$\begin{array}{r} 5340 \\ \underline{54} \end{array}$$

c.
$$\begin{array}{r} 54 \\ \underline{5340} \end{array}$$

d.
$$\begin{array}{r} 2454 \\ \underline{62} \end{array}$$

3. a.
$$\begin{array}{r} 1227 \\ \underline{324} \end{array}$$

b.
$$\begin{array}{r} 14,724 \\ \underline{654} \end{array}$$

c.
$$\begin{array}{r} 57,138 \\ \underline{257} \end{array}$$

d.
$$\begin{array}{r} 257 \\ \underline{57,138} \end{array}$$

4. a.
$$\begin{array}{r} 49,083 \\ \underline{985} \end{array}$$

b.
$$\begin{array}{r} 34,578 \\ \underline{787} \end{array}$$

c.
$$\begin{array}{r} 82,559 \\ \underline{389} \end{array}$$

5. a.
$$\begin{array}{r} 52,000 \\ \underline{309} \end{array}$$

b.
$$\begin{array}{r} 15,476 \\ \underline{137} \end{array}$$

c.
$$\begin{array}{r} 71,389 \\ \underline{908} \end{array}$$

6. a.
$$\begin{array}{r} 28,113 \\ \underline{1,843} \end{array}$$

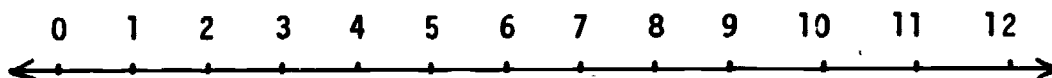
b.
$$\begin{array}{r} 38,564 \\ \underline{1,419} \end{array}$$

c.
$$\begin{array}{r} 42,153 \\ \underline{6,192} \end{array}$$

d.
$$\begin{array}{r} 34,215 \\ \underline{7,281} \end{array}$$

E. Subtraction on the Number Line

Example:



Jim has 5 candy bars and he gave his girl friend two of the candy bars.

- Begin at 0, count 5 units to the right (positive direction).
- Then count 2 units in the opposite direction (negative direction).
- You stop on the whole number 3.

Exercises

1. Make a number line for the following problems:

a. $8-5$ b. $10-4$ c. $7-2$

- What whole numbers were used?
- What whole number was reached?
- What operation was performed?

2. Dooyne weighed 189 lbs. He decided to go on a diet and lost 15 lbs..

- What did he weigh after dieting?
- What kind of number is this?

3. Joe went to Al's Cycle Shop to buy a used Honda. Al had a Super Hawk for \$240 and a Super Sport for \$350.

- a. How much would Joe save if he bought the Super Hawk?
- b. What kind of number is this?

4. NUMBER PUZZLE

ACROSS

- a. 31-7
- c. 861-479
- f. 1246-463
- h. 314-288
- i. 53-47
- j. 2314-1979
- l. 85-36
- m. 111-39
- o. 43,782-37,495
- q. 991-986
- r. 19-2
- s. 2518-1826

DOWN

- a. 543-267
- b. 83-35
- c. 31-28
- d. 17,383-9,126

a	b		c	d	e
f		g		h	
i		j	k		
	l			m	n
o			p		q
r			s	t	

DOWN (continued)

- e. 777-751
- g. 9641-6243
- k. 891-888
- l. 654-227
- n. 1469-1217
- o. 923-862
- p. 79-3
- t. 88,881-88,872

Calculator Practice

Subtract:

1.
$$\begin{array}{r} 84,362 \\ - 76,879 \\ \hline \end{array}$$

2.
$$\begin{array}{r} 98,634 \\ - 82,786 \\ \hline \end{array}$$

3.
$$\begin{array}{r} 64,389 \\ - 24,418 \\ \hline \end{array}$$

4.
$$\begin{array}{r} 18,888 \\ - 9,999 \\ \hline \end{array}$$

5.
$$\begin{array}{r} 46,564 \\ - 22,863 \\ \hline \end{array}$$

6.
$$\begin{array}{r} 34,685 \\ - 24,342 \\ \hline \end{array}$$

7.
$$\begin{array}{r} 18,631 \\ - 2,192 \\ \hline \end{array}$$

8.
$$\begin{array}{r} 62,453 \\ - 1,798 \\ \hline \end{array}$$

9.
$$\begin{array}{r} 91,435 \\ - 68,720 \\ \hline \end{array}$$

10.
$$\begin{array}{r} 23,149 \\ - 6,751 \\ \hline \end{array}$$

11.
$$\begin{array}{r} 19,345 \\ - 6,820 \\ \hline \end{array}$$

12.
$$\begin{array}{r} 78,325 \\ - 64,109 \\ \hline \end{array}$$

13.
$$\begin{array}{r} 39,154 \\ - 26,307 \\ \hline \end{array}$$

14.
$$\begin{array}{r} 58,416 \\ - 32,790 \\ \hline \end{array}$$

15.
$$\begin{array}{r} 81,084 \\ - 79,325 \\ \hline \end{array}$$

16.
$$\begin{array}{r} 98,134 \\ - 76,520 \\ \hline \end{array}$$

17.
$$\begin{array}{r} 89,315 \\ - 20,647 \\ \hline \end{array}$$

18.
$$\begin{array}{r} 73,981 \\ - 45,720 \\ \hline \end{array}$$

Little Goodie

1. Write the year of your birth.
2. Write the year when an important event occurred in your life.
3. Write the number of years since the important event occurred.
4. Write your age this year.
5. Add the four figures.

F. Distributive Property

Exercises

1. By use of separate number lines show the result of each:

a. $2 \times (5 + 3)$

b. $(2 \times 5) + (2 \times 3)$

c. $3 \times (4 + 2)$

d. $3 + (4 \times 2)$

e. $(3 + 4) \times (3 + 2)$

2. Place in the geometrical symbol the correct sign or numeral:

a. $6 \times 32 = 6 \times (30 + \triangle)$

b. $8 \times 47 = 8 \times (\square + 7)$

c. $9 \times 25 = \square \times (20 + 5)$

d. $6 \times 73 = 6 \triangle (70 + 3)$

e. $8 \times 64 = 8 \diamond (60 \triangle 4)$

3. Give an expression on the right that equals the one given on the left. (Do not compute.)

a. $3(13 + 28) =$

b. $(6 \cdot 7) + (6 \cdot 9) =$

c. $(24 + 18 + 31)9 =$

d. $(37 \cdot 13) + (13 \cdot 18) =$

4. Find the results:

a. $6(815 + 346) =$

b. $(86 + 35)3 =$

c. $(7 \cdot 231) + (7 \cdot 154) =$

5. By use of the distributive principle multiply:

a.
$$\begin{array}{r} 68 \\ \times 9 \\ \hline 72 \\ 540 \\ \hline \end{array}$$

b.
$$\begin{array}{r} 57 \\ \times 7 \\ \hline \end{array}$$

c.
$$\begin{array}{r} 325 \\ \times 4 \\ \hline \end{array}$$

d.
$$\begin{array}{r} 4061 \\ \times 3 \\ \hline \end{array}$$

e.
$$\begin{array}{r} 562 \\ \times 13 \\ \hline \end{array}$$

G. Prime Numbers

Exercises

1. A number is circled below if its only factors are 1 and the number itself. These are "special" numbers. Circle all "special" numbers in this list.

2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17
18 19 20 21 22 23 24 25 26 27 28 29 30 31 32
33 34 35 36 37 38 39 40 41 42 43 44 45 46 47
48 49 50 51 52 53 54 55 56 57 58 59 60 61 62
63 64 65 66 67 68 69 70 71 72 73 74 75 76 77
78 79 80 81 82 83 84 85 86 87 88 89 90 91 92
93 94 95 96 97 98 99 100

2. There are _____ "special" numbers.
3. The first special number is _____.
4. The numbers 71 and 73 are pairs of "special" numbers. The first pair of special numbers is _____ and _____.
5. The last special number in this list is _____.
6. The even special number is _____.
7. What is the first counting number that is not special? _____
8. Are 6 and 8 special numbers? _____
9. $2 \times \underline{\quad} = 6$
10. $2 \times \underline{\quad} \times \underline{\quad} = 8$
11. The special factors of 10 are _____ and _____.

NOTE: The "special" numbers in the above exercises are called prime numbers. A prime number is a counting number, other than one, with exactly two factors.

12. $90 = \begin{array}{c} \boxed{9} \\ \swarrow \quad \searrow \\ \boxed{} \times \boxed{} \end{array} \times \begin{array}{c} \boxed{} \\ \swarrow \quad \searrow \\ \boxed{} \times \boxed{} \end{array}$

$90 = \boxed{} \times \boxed{} \times \boxed{} \times \boxed{}$

13. $90 = \begin{array}{c} \boxed{} \\ \swarrow \quad \searrow \\ \boxed{5} \times \boxed{} \end{array} \times \begin{array}{c} \boxed{3} \\ \downarrow \\ \boxed{3} \\ \downarrow \\ \boxed{3} \end{array}$

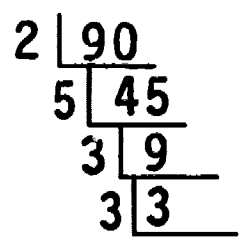
$90 = \boxed{5} \times \boxed{} \times \boxed{3} \times \boxed{3}$

$90 = \boxed{5} \times \boxed{} \times \boxed{} \times \boxed{3}$

14. $90 = \begin{array}{c} \boxed{15} \\ \swarrow \quad \searrow \\ \boxed{} \times \boxed{} \end{array} \times \begin{array}{c} \boxed{} \\ \swarrow \quad \searrow \\ \boxed{} \times \boxed{} \end{array}$

$90 = \boxed{} \times \boxed{} \times \boxed{} \times \boxed{}$

15. Using short division



$90 = 2 \times \boxed{} \times \boxed{} \times \boxed{}$

H. Prime Factors

Exercises

Number	Prime Factors	Pairs of factors
1. 60	$2 \times 2 \times 3 \times 5$	1×60
2. 60	$\bigcirc \times (2 \times 3 \times 5)$	2×30
3. 60	$3 \times (2 \times 2 \times \bigcirc)$	$\bigcirc \times 20$
4. 60	$(\bigcirc \times \bigcirc) \times (3 \times 5)$	$4 \times \bigcirc$
5. 60	$5 \times (\bigcirc \times \bigcirc \times 3)$	5×12
6. 60	$(2 \times 3) \times (2 \times 5)$	$\bigcirc \times \bigcirc$
7. 108	$\bigcirc \times \bigcirc \times \bigcirc \times \bigcirc \times$	$\bigcirc \times 108$
8. 108	$2 \times (\bigcirc \times \bigcirc \times \bigcirc \times \bigcirc)$	$2 \times \bigcirc$
9. 108	$(\bigcirc \times \bigcirc) \times (3 \times 3 \times 3)$	$\bigcirc \times \bigcirc$
10. 108	$\times (\bigcirc \times \bigcirc \times 3 \times 3)$	$\bigcirc \times 36$
11. 108	$(3 \times 2) \times (\bigcirc \times \bigcirc \times \bigcirc)$	$\bigcirc \times \bigcirc$
12. 108	$(\bigcirc \times \bigcirc \times \bigcirc) \times (3 \times 3)$	$\bigcirc \times 9$

A short way to write $2 \times 2 = 4$ is $2^2 = 4$.

13. A short way to write $3 \times 3 = 9$ is $3^{\square} = 9$.

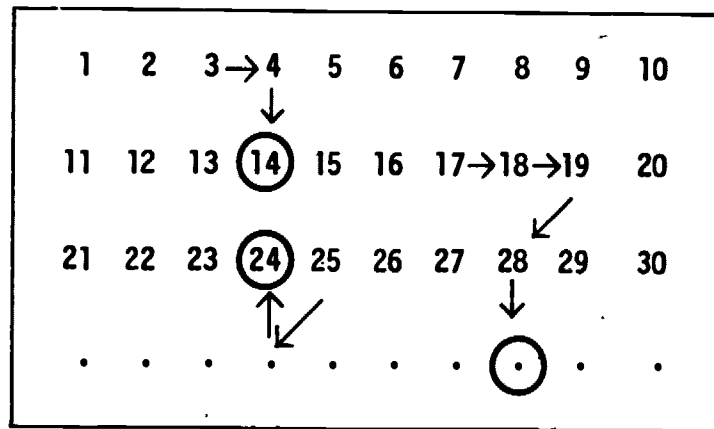
14. $2 \times 2 \times 2 = 8$, $2^{\square} = 8$.

15. $3 \times 3 \times 3 = \square$, $3^{\square} = 27$.

16. Can you show other examples of the renaming of such products?

THINK BEFORE YOU ACT!---

Examples: a. $3 \rightarrow \downarrow = 14$ b. $25 \swarrow \uparrow = 24$ c. $17 \rightarrow \rightarrow \swarrow \downarrow = 38$



Using the vector chart, solve each problem below. Can you do this without any help?

1. $6 \rightarrow \rightarrow = \square$

7. $16 \rightarrow \swarrow \nearrow = \square$

2. $35 \leftarrow \downarrow \downarrow = \square$

8. $47 \swarrow \nearrow \swarrow \leftarrow \leftarrow = \square$

3. $14 \leftarrow \uparrow = \square$

9. $\square \rightarrow \rightarrow \downarrow \downarrow = 44$

4. $5 \rightarrow \leftarrow \uparrow \downarrow = \square$

10. $1 \leftarrow \downarrow \uparrow \swarrow \nearrow = \square$

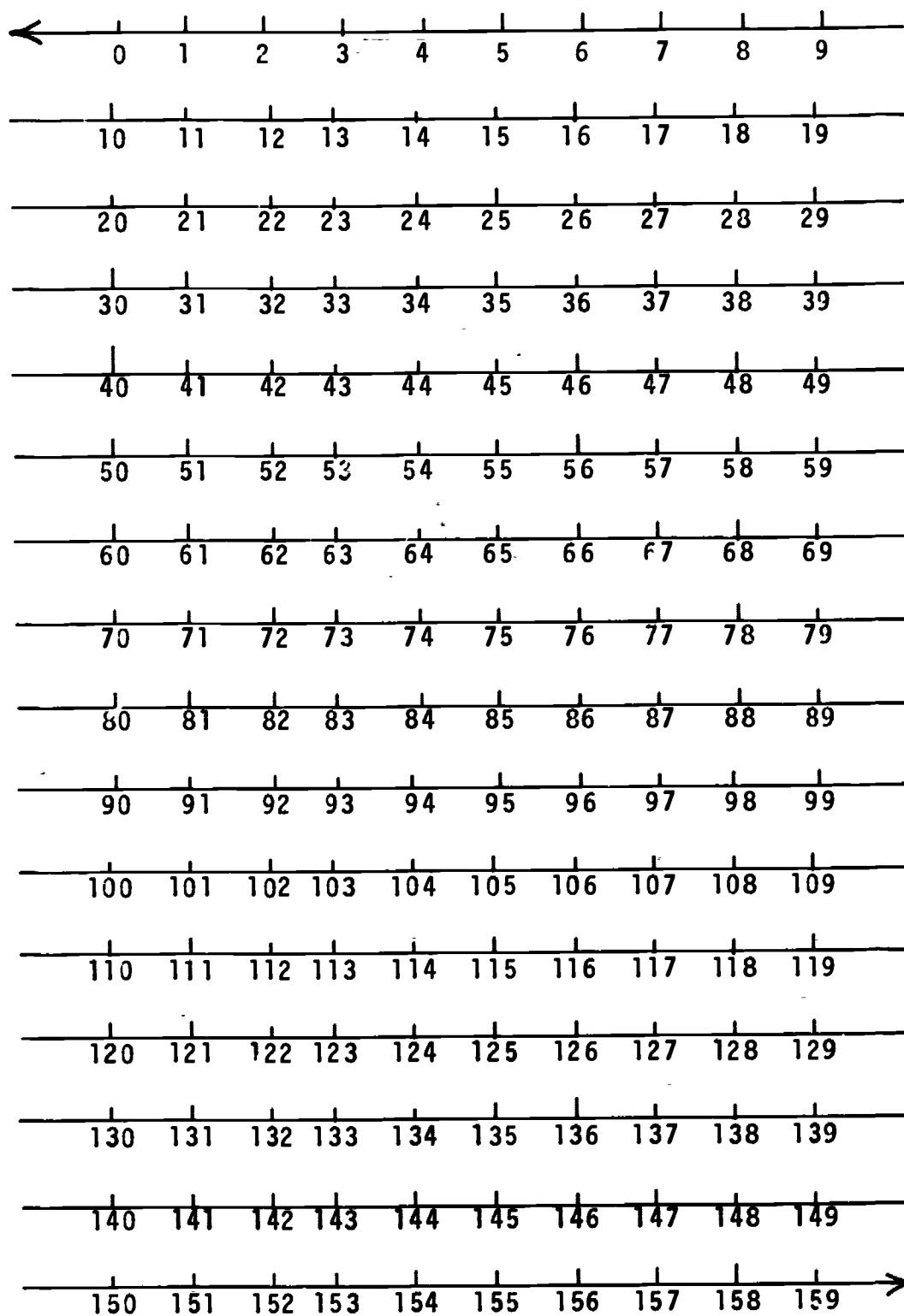
5. $18 \nearrow = \square$

11. $20 \swarrow \swarrow = \square$

6. $10 \swarrow = \square$

12. $6 \downarrow \uparrow = \square$

Vector Chart



I. Common Factors

Exercises

1. is the common factor of
(2 x 7) and (7 x 17)

2. (5 x 11²)
and have for a common factor
(3 x 11²)

3. 5 x 7 x 23
and and have and for common factors
3 x 7 x 23

4. 2² · 3 · 5²
and , and have , and for common factors
2 · 3 · 5³

5. 2² · 7 · 11²
and , and have , and for common factors
2² · 7 · 11
and
2² · 7² · 11

6. Write as products of primes and find the common factors.

$$144 =$$

$$188 =$$

Common factors are

J. Division of Whole Numbers

- Exercises

1. $625 \div 25 =$

2. $1728 \div 12 =$

3. $50,481 \div 237 =$

4. $95,953 \div 793 =$

5. $56,561 \div 347 =$

6. $363 \div 121 =$

7. $627 \div 209 =$

8. $1318 \div 659 =$

9. $747 \div 83 =$

10. $1036 \div 37 =$

11. $19,400 \div 776 =$

12. $58,368 \div 456 =$

13. $500,973 \div 893 =$

14. $299,552 \div 851 =$

15. $186,660 \div 1,220 =$

16. $9468 \div 12 =$

17. $28,075 \div 25 =$

18. 525 shares of a particular stock sold for \$590,625. What was the price per share?
19. Mr. Jones bought 1,125 acres of land for \$365,625. What was the price per acre?
20. Bobby Jones made 581 points on 7 tests. What was his average score?
21. Place the quotient in the correct square:
- a. $65 \div 5 =$
 - b. $72 \div 24 =$
 - c. $527 \div 31 =$
 - d. $102 \div 6 =$
 - e. $24 \div 4 =$
 - f. $784 \div 28 =$
 - g. $354 \div 59 =$
 - h. $70 \div 7 =$
 - i. $5696 \div 365 =$
 - j. $96 \div 8 =$
 - k. $22,712 \div 5,678 =$
 - l. $270 \div 15 =$
 - m. $270 \div 18 =$
 - n. $217 \div 31 =$
 - o. $2277 \div 99 =$
 - p. $100 \div 20 =$

Find the sum of each row.
 Find the sum of each column.
 Find the sum of each diagonal.

diagonal

a	b	c	d		
e	f	g	h		r
i	j	k	l		0
m	n	o	p		w

column

diagonal

Tax Your Brain Power

There is a simple method of checking computation that works in most cases.

Step 1 Add the digits in each number until you get a one digit number. In subtraction the minuend must be larger than the subtrahend even if this means it will contain two digits.

Step 2 Work problem

Step 3 Check

Addition:

435	$4+3+5 \rightarrow 12 \rightarrow 1+2 \rightarrow 3$	
127	$1+2+7 \rightarrow 10 \rightarrow 1+0 \rightarrow 1$	$\rightarrow 3+1+7 \rightarrow 11 \rightarrow 1+1 \rightarrow 2$
295	$2+9+5 \rightarrow 16 \rightarrow 1+6 \rightarrow 7$	
857	$8+5+7 \rightarrow 20 \rightarrow 2+0 \rightarrow 2$	

Subtraction:

4384	$4+3+8+4 \rightarrow 19 \rightarrow 1+9 \rightarrow 10$	
1575	$1+5+7+5 \rightarrow 18 \rightarrow 1+8 \rightarrow 9 \rightarrow 10 - 9 \rightarrow 1$	
2809	$2+8+0+9 \rightarrow 19 \rightarrow 1+9 \rightarrow 10 \rightarrow 1 + 0 \rightarrow 1$	

Multiplication:

187	$1+8+7 \rightarrow 16 \rightarrow 1+6 \rightarrow 7$	
143	$1+4+3 \rightarrow 8 \rightarrow 8 \rightarrow 8$	$7 \times 8 = 56 \rightarrow 5+6 \rightarrow 11 \rightarrow 1+1 \rightarrow 2$
561		
748		
187		
26,741	$2+6+7+4+1 \rightarrow 20 \rightarrow 2+0 \rightarrow 2$	

Division: (Check by multiplication then add remainder)

29	$165 \rightarrow 1+6+5 \rightarrow 12 \rightarrow 1+2 \rightarrow 3$	
165 $\overline{) 4931}$	$29 \rightarrow 2+9 \rightarrow 11 \rightarrow 1+1 \rightarrow 2$	$3 \times 2 = 6 + 2 = 8$
330		
1631	$146 \rightarrow 1+4+6 \rightarrow 11 \rightarrow 1+1 \rightarrow 2$	
1485	$4931 \rightarrow 4+9+3+1 \rightarrow 17 \rightarrow 1+7 \rightarrow 8$	
146		

Divisor x Quotient + Remainder gives check number 8

UNIT V
INTEGERS

A. Integers

Examples:

1. $7 - 11 = \underline{-4}$

2. $15 - 21 = \underline{-6}$

Exercises

1. $34 - 34 = \underline{\hspace{2cm}}$

2. $34 - 35 = \underline{\hspace{2cm}}$

3. $1,436 - 8,561 = \underline{\hspace{2cm}}$

4. $271 - 463 = \underline{\hspace{2cm}}$

5. $1,429,600 - 7,358,547 = \underline{\hspace{2cm}}$

6. $580,575 - 40,580,575 = \underline{\hspace{2cm}}$

7. $968,523 - 1,068,523 = \underline{\hspace{2cm}}$

8. $34 - 107 = \underline{\hspace{2cm}}$

9. $4,267 - 58,462 = \underline{\hspace{2cm}}$

10. $59,576 - 73,856 = \underline{\hspace{2cm}}$

NOTE: The set of whole numbers and their opposites form the set of integers.

11. $48,549 - 568,452 = \underline{\hspace{2cm}}$
12. $46,398 - 84,531 = \underline{\hspace{2cm}}$
13. $6,341 - 8,569 = \underline{\hspace{2cm}}$
14. $94,837,256 - 96,483,725 = \underline{\hspace{2cm}}$
15. $49 - \underline{\hspace{2cm}} = -30$
16. $31 - \underline{\hspace{2cm}} = -19$
17. $\underline{\hspace{2cm}} - 54 = -37$
18. $76,542 - \underline{\hspace{2cm}} = -9465$
19. $\underline{\hspace{2cm}} - 76,534 = -13,268$
20. $\underline{\hspace{2cm}} - 29 = -21$
21. $8 - \underline{\hspace{2cm}} = -1$
22. $35 - \underline{\hspace{2cm}} = -15$
23. $\underline{\hspace{2cm}} - 22 = -5$
24. $\underline{\hspace{2cm}} - 75 = -30$

Figure Me Out

Give the missing numbers so that this will be a magic square.

	$\frac{9}{12}$	$\frac{4}{12}$
		$\frac{11}{12}$
$\frac{10}{12}$		$\frac{6}{12}$

B. Properties of Addition

Exercises

Are the answers to these problems found in the set of integers?

1. $543 + -543$ _____

2. $1,742 + -2,342$ _____

3. $100 + 99$ _____

Work these problems with the calculator.

4. a. $5,432 + 3,780$ _____

b. $3,780 + 5,432$ _____

5. a. $-432 + 358$ _____

b. $358 + -432$ _____

6. a. $-1,540 + -2,544$ _____

b. $-2,544 + -1,540$ _____

Compare the answer in (a) to the answer in (b). What property is illustrated in problems 4, 5, and 6? _____

Work these problems without using the calculator.

7. $475 + -364$ _____

8. $-364 + 475$ _____

9. $-1,643 + 986$ _____

10. $986 + -1,643$ _____

Work these problems using the calculator.

11. a. $(345 + 562) + 792$ _____

b. $345 + (562 + 792)$ _____

12. a. $(-1,184 + 984) + 300$ _____

b. $-1,184 + (984 + 300)$ _____

What do you notice about the answers in problem 11? In problem 12? What property does this illustrate? _____

Calculator Practice

Shade the squares which are not needed for this puzzle.

Across

- a. $124 + ^{-}35$
- c. $576 + ^{-}386$
- f. $12,723 + ^{-}2,720 + 1,175$
- h. $966 + \boxed{} = 990$
- i. $3,796 + 4,732 + ^{-}7574$
- k. $^{-}601 + ^{-}537 + ^{-}989 + 2130$
- l. $^{-}196 + \boxed{} = ^{-}132$
- m. $2,503 + \boxed{} = 196$
- p. $347 + ^{-}341$
- q. $^{-}6,732 + 6,543 + 403$
- r. $^{-}5,130 + 7,598 + ^{-}2,430$

a	b		c	d	e
f		g			
h			i		j
		k		l	
m	n		o		p
q				r	

Down

- a. $1,976 + ^{-}1,164$
- b. $987 + ^{-}73$
- c. $998 + ^{-}416 + ^{-}403$
- d. $^{-}123 + 456 + ^{-}789 + 10,312$
- e. $876 + ^{-}577 + ^{-}299$
- g. $^{-}321 + ^{-}233 + 555$
- j. $^{-}4078 + \boxed{} = 390$
- k. $^{-}9,643 + ^{-}7,653 + 17,600$
- m. $^{-}265 + \boxed{} ^{-}243$
- n. $2,406 + ^{-}1,389 + ^{-}986$
- o. $564 + ^{-}809 + 252$

C. Additive Inverse

Example: $5 + -5 = 0$
 $-5 + 5 = 0$

Exercises

Fill in the following blanks:

1. _____ + 6 = 0

2. $-10 + 10 =$ _____

3. $-3 +$ _____ = 0

4. $-547 +$ _____ = 0

5. $140 +$ _____ = 0

6. $0 +$ _____ = 0

7. $0 + 0 =$ _____

8. In addition, the inverse of zero is _____.

9. In addition, the inverse of -31 is _____.

10. In addition, the inverse of 31 is _____.

NOTE: If the addition of two numbers produces the additive identity element, then one number is the additive inverse of the other.

D. Division of Integers

Exercises

1. $48 \div 6 =$ Is the result an integer? _____
2. $9 \div 3 =$ Is the result an integer? _____
3. $625 \div 25 =$ Is the result an integer? _____
4. $1,246,104 \div 486 =$ Is the result an integer? _____
5. $3,386,955 \div 7,895 =$ Is the result an integer? _____
6. $5,964,959 \div 5,368 =$ Is the result an integer? _____

NOTE: From problem #6 we see the integers are not closed under division. We would like to be able to divide any two integers. Therefore, we must extend the set of integers; or, create a number which will give us the answer to the division of any two integers. (Exception: Dividing by zero)

Example: $9 \div 4$ is not an integer. Therefore we create the number $\frac{9}{4}$ so we can divide.

$$9 \div 4 = \frac{9}{4}$$

The set that includes the integers and all the "new type" numbers needed for division is called rational numbers.



HELPING BUILD ARKANSAS

ARKANSAS POWER & LIGHT COMPANY

NET MONTHLY RATE

Summer Rate*

\$1.45 for the first 15 Kwh or less
3.80¢ per Kwh for the next 40 Kwh
2.70¢ per Kwh for the next 145 Kwh
1.75¢ per Kwh for the next 500 Kwh
1.15¢ per Kwh for all additional Kwh

Winter Rate*

\$1.45 for the first 15 Kwh or less
3.80¢ per Kwh for the next 40 Kwh
2.70¢ per Kwh for the next 145 Kwh
1.75¢ per Kwh for the next 200 Kwh
1.15¢ per Kwh for the next 600 Kwh*
0.80¢ per Kwh for all additional Kw

* Summer Rate will apply for the billing months of May through October and Winter Rate will apply for the billing months of November through April.

**Kwh billed at 1.15¢ shall be reduced to 200 when Customer has an approved electric water heater in regular use.

Electric Water Heating

Customers using an approved electric water heater will be billed 1.0¢ per Kwh for up to 400 Kwh, provided at least 200 Kwh are first billed at the above rates.

Using the above rates work these problems.

1. Find the number of Kwh used if the bill was \$21.75.

2. How many Kwh were used if the bill was \$59.75 ?

3. If the bill is \$173.75 how many Kwh are used?

4. How many Kwh could you get for \$200.75 ?

5. What is the total number of Kwh used in problems 1. and 2. ?

More Goodies

There are 20 mathematical terms in this puzzle. There are extra letters and words which you will not use. The words may be upside down or on a diagonal but they are in order. Circle and list them.

B	R	C	I	F	L	O	W	C	H	A	R	T	E	S	B	U	S	T
Q	W	E	R	E	I	T	Y	A	T	Y	U	U	I	O	P	A	S	D
R	E	G	E	T	N	I	F	L	G	F	H	M	L	J	K	L	F	Z
X	C	A	V	I	E	B	N	C	M	N	U	M	B	E	R	Q	P	W
O	E	I	R	N	U	D	T	U	Y	A	B	L	S	K	C	D	J	F
E	D	I	V	I	D	H	G	L	L	U	N	Z	M	A	X	N	Y	C
L	V	B	T	F	Y	R	U	A	E	I	W	O	D	Q	P	L	T	H
O	G	J	F	N	K	D	L	T	S	A	B	D	V	N	P	O	I	M
H	X	B	Z	I	Q	W	D	O	P	B	R	T	Y	I	U	I	T	O
W	A	S	U	I	N	V	B	R	S	B	D	F	T	G	H	S	N	J
A	B	C	D	E	F	G	H	I	J	Q	R	L	M	N	O	P	E	F
I	J	L	K	M	T	C	A	R	T	B	U	S	T	U	V	W	D	E
M	A	S	D	A	L	E	E	V	E	M	I	A	J	U	D	Y	I	T
M	A	R	Y	C	L	O	E	N	O	R	A	X	R	U	T	H	V	P
W	F	S	P	B	J	L	H	L	R	C	L	O	S	E	D	V	I	P

Think

A man with a five-gallon bucket and a three-gallon bucket went to a well to get exactly four gallons of water. How was he able to get the four gallons of water by using only the two buckets?

UNIT VI

RATIONAL NUMBERS

A. Multiplying Rational Numbers

Rational numbers in fractional form are multiplied by obtaining the product of the numerators and the product of the denominators.

Examples: 1. $\frac{5}{8} \times \frac{1}{4} = \frac{5 \times 1}{8 \times 4} = \frac{5}{32}$

2. $\frac{11}{3} \times \frac{28}{5} = \frac{11 \times 28}{3 \times 5} = \frac{308}{15}$

Exercises

1. a. $\frac{1}{3} \times \frac{4}{5} = \frac{1 \times 4}{3 \times 5} =$

b. $\frac{5}{6} \times \frac{5}{8} =$

c. $\frac{3}{5} \times \frac{4}{7} =$

d. $\frac{3}{7} \times \frac{21}{4} =$

e. Are all the results above rational numbers?

f. Try to think of an example in which the result is not a rational number.

g. Can we conclude that the operation of multiplication is closed under the rational numbers?

2. Multiply: a. $\frac{5}{6} \times \frac{9}{8} =$

b. $\frac{4}{5} \times \frac{4}{13} =$

c. $\frac{9}{8} \times \frac{5}{6} =$

d. $\frac{4}{13} \times \frac{4}{5} =$

e. What do you notice about problems a and c, and b and d?

f. What do you think we can conclude about multiplication of rational numbers?

3. a. $\left(\frac{2}{3} \times \frac{4}{5}\right) \times \frac{5}{4} =$

b. $\frac{2}{3} \times \left(\frac{4}{5} \times \frac{5}{4}\right) =$

c. $\left(\frac{7}{2} \times \frac{3}{2}\right) \times \frac{3}{4} =$

d. $\frac{7}{2} \times \left(\frac{3}{2} \times \frac{3}{4}\right) =$

e. Compare the answers in problems a and b.

f. Compare the answers in problems c and d.

4. a. $\frac{13}{7} \times 1 = \frac{\square}{\square}$ b. $\frac{8}{9} \times 1 = \frac{\square}{\square}$ c. $\frac{7}{8} \times \frac{\square}{\square} = \frac{7}{8}$

d. $\frac{17}{15} \times \frac{\square}{\square} = \frac{17}{15}$ e. $\frac{\square}{\square} \times \frac{1}{1} = \frac{13}{14}$

f. Any number multiplied by 1 produces that same _____.
The identity for multiplication is _____.

5. a. $\frac{4}{5} \times \frac{5}{4} = \square$ b. $\frac{2}{3} \times \frac{3}{2} = \square$ c. $\frac{17}{5} \times \frac{5}{17} = \square$

d. $\frac{7}{8} \times \frac{\square}{\square} = 1$ e. $\frac{24}{91} \times \frac{\square}{\square} = 1$ f. $\frac{\square}{\square} \times \frac{16}{17} = 1$

g. $\frac{7}{12} \times \frac{\square}{\square} = 1$ h. $\frac{8}{1} \times \frac{\square}{\square} = 1$ i. $\frac{\square}{\square} \times 9 = 1$

j. In multiplication, how do you find the inverse of a number? _____

k. The multiplicative inverse of $\frac{7}{8}$ is _____.

l. The multiplicative inverse of 12 is _____.

m. The multiplicative inverse of $\frac{7}{3}$ is _____.

Exercises

Multiply:

1. $\frac{1}{3} \times 4 =$

2. $6 \times \frac{1}{8} =$

3. $\frac{5}{12} \times 5 =$

4. $9 \times \frac{1}{81} =$

5. $\frac{4}{12} \times \frac{2}{4} =$

6. $\frac{1}{2} \times \frac{1}{8} =$

7. $\frac{25}{18} \times \frac{9}{10} =$

8. $\frac{2}{5} \times \frac{1}{8} =$

9. $\frac{5}{12} \times \frac{12}{5} =$

10. $\frac{22}{7} \times \frac{16}{35} =$

11. $5 \times \frac{27}{10} =$

12. $\frac{16}{24} \times \frac{3}{4} =$

13. $48 \times \frac{1}{16} =$

14. $\frac{7}{12} \times 4 =$

15. Fill in the operation and equal signs

3		24		3	=	30
4		2		4		2
12		6		2		4
=						
24		2		5		60

B. Reducing Rationals Using Primes

Exercises

1. Rename these numbers:

$$\frac{5}{3} \times \frac{7}{7} = \frac{5}{3} \times \frac{\square}{\square} = \frac{5}{3} \times \square = \frac{5}{3}$$

$$\frac{35}{21} = \frac{5}{3}$$

2. Find the prime factors of each numerator and each denominator.

a. $\frac{15}{25} = \frac{\square \times 5}{5 \times \square}$

b. $\frac{81}{18} = \underline{\hspace{2cm}}$

c. $\frac{12}{18} = \frac{2 \times \square \times \square}{\square \times 3 \times \square}$

d. $\frac{75}{21} = \underline{\hspace{2cm}}$

e. $\frac{39}{65} = \underline{\hspace{2cm}}$

f. $\frac{4620}{231} = \underline{\hspace{2cm}}$

3. Rename these numbers so that some of the factors will be the identity.

a. $\frac{15}{25} = \frac{\square}{\square} \times \frac{5}{5}$

b. $\frac{81}{18} = \underline{\hspace{2cm}}$

c. $\frac{12}{18} = \underline{\hspace{2cm}}$

d. $\frac{75}{21} = \underline{\hspace{2cm}}$

e. $\frac{39}{65} = \underline{\hspace{2cm}}$

f. $\frac{4620}{231} = \underline{\hspace{2cm}}$

4. Rename these results so that you have a fraction using the smallest numbers possible for numerator and denominator.

a. $\frac{15}{25} = \frac{3 \times 5}{5 \times 5} = \frac{3}{5} \times \frac{5}{5} = \square$

b. $\frac{81}{18} = \underline{\hspace{2cm}}$

c. $\frac{12}{18} = \underline{\hspace{2cm}}$

d. $\frac{75}{21} = \underline{\hspace{2cm}}$

e. $\frac{39}{65} = \underline{\hspace{2cm}}$

f. $\frac{4620}{231} = \underline{\hspace{2cm}}$

5. We can find an easy way to reduce $\frac{153}{102}$ using primes.

$$\frac{153}{102} = \frac{\square \times \square}{3 \times \square} \times \frac{17}{\square}$$

$$\frac{153}{102} = \frac{\square}{3} \times \frac{\square}{\square} \times \frac{17}{\square}$$

$$\frac{153}{102} = \frac{\square}{\square}$$

$$153 \div 102 =$$

6. Reduce

a. $\frac{200}{100} =$

b. $\frac{60}{54} =$

c. $\frac{150}{66} =$

d. $\frac{48}{9} =$

e. $\frac{77}{66} =$

f. $\frac{66}{77} =$

g. $\frac{14}{16} =$

h. $\frac{9}{81} =$

i. $\frac{36}{48} =$

j. $\frac{81}{648} =$

k. $\frac{3}{24} =$

l. $\frac{12}{72} =$

Practical Applications

1. An oil well is drilled in an area that has 80 acres spacing. The oil company pays a $\frac{1}{8}$ royalty interest in the lease. This simply means that the owner or owners get one barrel out of every 8 barrels produced by this well. Mr. Young owns 20 acres of this 80 acre unit. If the well will average 40 barrels per day @ \$2.60 per barrel, how much money should Mr. Young receive in royalty in a 30 day month?

2. John Doe is operating an oil well (#1-A) for Humble Oil Corp.. Materials and labor for May cost \$4783.00. Partners in well #1-A are as follows:

J. Brown - $\frac{3}{32}$

P. Black - $\frac{5}{64}$

J. Lowe - $\frac{3}{8}$

R. Rogers - $\frac{7}{64}$

C. Rogers - $\frac{1}{16}$

B. Franks - $\frac{3}{16}$

D. Young $\frac{3}{32}$

Bill each man for his pro-rata share of cost of operations for May.

C. Multiplying Decimals

Examples:

$$\begin{array}{r} 2.34 \\ 5.64 \\ \hline 13.1976 \end{array}$$

$$\begin{array}{r} 23.4 \\ 5.64 \\ \hline 131.976 \end{array}$$

$$\begin{array}{r} .234 \\ 56.4 \\ \hline 13.1976 \end{array}$$

Exercises

1. The number of digits to the right of the decimal in 13.1976 is _____.

2. Examine the following:

$$97.3 \times 0.125 = 12.1625$$

$$0.0231 \times 836 = 19.3116$$

State in words a rule that will tell where the decimal point should be located.

3. If we multiply $.6 \times .7$ we know that this is the same as multiplying the fractions $\frac{6}{10} \times \frac{7}{10}$. This is equal to $\frac{42}{100}$

which is the decimal .42. If instead it was $.06 \times .7$ we would have $\frac{6}{100} \times \frac{7}{10} = \frac{42}{1000}$; in this case our decimal value is .042.

4. Place the decimal point at the proper place in each products:

a. $\begin{array}{r} 65.84 \\ .45 \\ \hline 296280 \end{array}$

b. $\begin{array}{r} 75.31 \\ 1.28 \\ \hline 963968 \end{array}$

c. $\begin{array}{r} 32.14 \\ 2.3 \\ \hline 73922 \end{array}$

d. $\begin{array}{r} .72 \\ 6.6 \\ \hline 4752 \end{array}$

5. Multiply and place the decimal point correctly:

a. $\begin{array}{r} 56.28 \\ .332 \\ \hline \end{array}$

b. $\begin{array}{r} 326.7 \\ 4.03 \\ \hline \end{array}$

c. $\begin{array}{r} 1.213 \\ 71.2 \\ \hline \end{array}$

d. $\begin{array}{r} 72.3 \\ 60.0 \\ \hline \end{array}$

e. $\begin{array}{r} 700 \\ 2.35 \\ \hline \end{array}$

f. $\begin{array}{r} 36.41 \\ 90.7 \\ \hline \end{array}$

g. $\begin{array}{r} 73.67 \\ 21.2 \\ \hline \end{array}$

h. $\begin{array}{r} .202 \\ .101 \\ \hline \end{array}$

P. O. Box 1280
8th to 9th on LEWIS ST.
OWENSBORO, KY. 42301
Telephone 502-684-2309

Cable Address:
"TAPSCOTT OWENSBORO"

Date 5/14/70

Ship To HOUSE OF FLOWERS

Street Address P. O. Box 366

City LEPANTO, ARK

State _____ Zip Code 72357

ORDER SHEET

Tapscott's
INC.
IMPORTER OF FLORAL PRODUCTS

TERMS
Net 30 Days to those having a favorable rating in Dun and Bradstreet or Florist Credit Guide. If not rated as above, Cash or C.O.D. (25% deposit required). However, you can establish credit with us by furnishing names and complete addresses of three references plus the name of your bank.

MINIMUM ORDER
Service Charge \$2.00
On Orders Less than \$20.00

HOW TO SHIP GOODS
See Back Side of This Page for Cost

QUANTITY SHIPPED	TERMS (SEE ABOVE)		SHIP WEIGHT		MOTOR FREIGHT	RAIL EXPRESS	PARCEL POST	UNITED PARCEL SERVICE	SUB
	QUANTITY ORDERED	IMPORTANT WRITE CATALOG NUMBER	ARTICLE AND COLOR						
		JL-7	LEATHERLEAF				.90	10.80	
		2384	FORGET ME NOT PICK				.60	7.20	
		JR-3	SWEET PEA				.80	4.80	
		JR-728	SUNGOLD				.80	3.20	
		JE-10	DAISEY				.60	7.20	
		MT219	POWDER PUFF ORANGE				4.80	4.80	
		265	POPPY OPIMUM BLUE/GR.				7.20	7.20	
		24223	SILKY MUM - OR./BL./TRK				3.60	10.80	
		2368	BOSTON FERN				4.80	4.80	
		#40 SATIN					3.00	3.00	
		#100 SATIN					3.20	16.00	
		#9	CORSAGE				2.25	25.00	
		#3	CORSAGE T-SS				2.50	12.80	
		MT2152	SCANDASIA EA. COLOR				4.80	14.40	
		G-142	FRUIT + VEGET. ASST				.70	8.40	
		A-149	FINGER GRAPE				2.15	2.15	
		A-148	LG. GRAPE				3.00	6.00	
							TOTALS	175.25	



THE FOLLOWING ABBREVIATIONS ARE USED IN FILLING YOUR ORDER: B O—BACK ORDER
O G D—OUT AND DISCONTINUED O F S—OUT FOR SEASON T O—TEMPORARILY OUT

F-71

CHECK THE EXTENTIONS. MAKE ANY CORRECTION NEEDED.

Calculator Practice

Multiply:

$$\begin{array}{r} 1. \quad 39.34 \\ \quad \quad 4.7 \\ \hline \end{array}$$

$$\begin{array}{r} 398,571.89 \\ \quad \quad 4,758 \\ \hline \end{array}$$

$$\begin{array}{r} 395.8 \\ \quad 47.5 \\ \hline \end{array}$$

$$\begin{array}{r} 2. \quad 586.7 \\ \quad 46,577 \\ \hline \end{array}$$

$$\begin{array}{r} 472.54 \\ \quad 9.08 \\ \hline \end{array}$$

$$\begin{array}{r} 8.6543 \\ \quad 7.86 \\ \hline \end{array}$$

$$\begin{array}{r} 3. \quad 97.67 \\ \quad \quad 8.0 \\ \hline \end{array}$$

$$\begin{array}{r} 685.098 \\ \quad 57.7 \\ \hline \end{array}$$

$$\begin{array}{r} 5,746.8 \\ \quad 87.09 \\ \hline \end{array}$$

$$\begin{array}{r} 4. \quad 47.9 \\ \quad \quad .8 \\ \hline \end{array}$$

$$\begin{array}{r} 84,759.6 \\ \quad \quad .811 \\ \hline \end{array}$$

$$\begin{array}{r} 867.8 \\ \quad .123 \\ \hline \end{array}$$

$$\begin{array}{r} 5. \quad 987.765 \\ \quad 857.96 \\ \hline \end{array}$$

$$\begin{array}{r} 1504,856 \\ \quad .87690 \\ \hline \end{array}$$

$$\begin{array}{r} 475,912.5 \\ \quad 57,697.9 \\ \hline \end{array}$$

$$\begin{array}{r} 6. \quad 47,589.765 \\ \quad \quad .9087 \\ \hline \end{array}$$

$$\begin{array}{r} 69.48475 \\ \quad 64.867 \\ \hline \end{array}$$

$$\begin{array}{r} 1,093.948 \\ \quad 673.57 \\ \hline \end{array}$$

7. In each problem, locate the decimal in the numeral in the box.

a. $.4855 \times 3.03 =$ 14710.5

b. 9546 $\times .02 = 2.00466$

c. $1.5328 \times$ 9776 $= 1.49846528$

d. 7456733 $\times 67.543 = 503.650117019$

Practical Applications

1. Find extensions and total.

BOY CALLISON
Borden Dairy Products
 P. O. BOX 14, WYNNE, ARK. 72396
 Phone BE 8-3802

02352



Borden's

Route No. V207 Date **6-26** 19**71**
 Name **KROGER** V297
 Address _____

QUAN.	SIZE	PRODUCT	UNIT PRICE	AMOUNT
		MIX VAN	%	
	G	MIX CHOC	%	
	A	DISPENSER		
	L	HOMO GLASS		
40	L	HOMO PAPER	1.13	
24	O	HOMO PLASTIC	1.20	
	N	POINSETTIA		
		LOW-FAT		
24		FRUIT DRINKS	.56	
135	1/2	HOMO	.57	
36	G	BUTTERMILK	.50	
36	A	1% - PRO	.54	
	L	POINSETTIA		
		ORANGE JUICE		
16		HOMO	.30	
16	Q	BUTTERMILK	.28	
8	U	SKIM	.58	
20	A	CHOCOLATE	.31	
10	R	BULG.	.32	
	T	1/2 & 1/2		
	S	ORANGE JUICE		
		FRUIT DRINKS		
		EGG NOG.		
10	P	HOMO	.17	
10	I	CHOC.	.17	
10	N	1/2 & 1/2	.38	
28	S	FRUIT DRINKS	.10	
	10	HOMO		
	O	CHOC.		
	Z	BULG.		
44	1/2	HOMO	8.5	
44	P	CHOC.	.09	
	I	BULG.		
10	N	X X CL.	.38	
10	T	DIPS 8 oz.	.37	
20	S	YOGURT 8 oz.	.28	
24	C	SOUR CREAM	.37	
	R	STERILE CREAM		
12	S	PRESSURE CL.	.50	
12	12	OUNCE	.30	
	16	OUNCE		
12	32	OUNCE	.66	
		BULK		
		SUB TOTAL		
70	M	OLEO		
	I	BUTTER	.98	
	C	BISCUITS		
75		TOTAL		



Practical Application

2. Joe, friend of mine for me. Don't forget state sales tax. By the way, if the customer needs time payments, ask for \$10 down and the carrying charge will be 7 1/2 % of unpaid balance. Bal @ \$110⁰⁰ per month. Peter

EXTRA COPY OF:

INVOICE NUMBER: 1836

CASH CHANGE CA
DATE: 5-18-71

GOODYEAR SERVICE STORES
A DIVISION OF THE GOODYEAR TIRE & RUBBER COMPANY
306 No. Washington
Fortrest City, Ark.
#2848 ME 3-2429

PAID STAMP
HERE

NAME: Mrs. Carter
220 N. Taylor Drive
Wynner, LA
LICENSING NO. 4144 691
CUST. ORDER NO. 68- Food
DATE ORDERED: 5-18-71
PHONE NO.

QUAN.	SIZE	DESCRIPTION	WT.	LN	EXTENSION	TOTAL	QUAN.	PRICE EACH	AMOUNT
2	815	X15 AWW Bc Ny	4	45 00			2	1 97	
1		Stag wheels		119					
2		spark plugs		89					
<p style="text-align: center;">Have amount given ready 4 PM</p>									
<p style="text-align: center;">Have ready 4 PM</p>									

ABOVE AMT. RECEIVED IN GOOD CONDITION

CUSTOMER SIGNATURE: _____

TOTAL: 1 97

SALES TAX: _____

TOTAL: _____

THIS IS YOUR EXTRA COPY INVOICE

THIS IS YOUR EXTRA COPY INVOICE

Finish the cash slip. Find the time payment balance. How many months will it take to pay off the balance?

D. Division of Rational Numbers

Example: $\frac{7}{8} \div \frac{3}{4}$

Rename as: $\frac{\frac{7}{8} \times 1}{\frac{3}{4}} = \frac{\frac{7}{8} \times \frac{4}{3}}{\frac{3 \times 4}{3}} = \frac{\frac{7}{8} \times \frac{4}{3}}{\frac{12}{3}} = \frac{\frac{7}{8} \times \frac{4}{3}}{1} = \frac{7}{8} \times \frac{4}{3} = \frac{28}{24}$

Exercises

1. a. $\frac{2}{7} \div \frac{1}{3} =$

b. $\frac{5}{3} \div \frac{1}{5} =$

c. $\frac{5}{6} \div \frac{1}{3} =$

d. $\frac{2}{3} \div \frac{5}{6} =$

e. $\frac{3}{8} \div \frac{1}{2} =$

f. Was the result of each exercise above a rational number? _____

g. Can you think of an example where the result is not a rational number? _____

h. Is the set of rational numbers closed under division? _____

2. $\frac{2}{3} \div \frac{4}{5} = \frac{10}{12}$

$\frac{4}{5} \div \frac{2}{3} = \frac{12}{10}$

Is $\frac{2}{3} \div \frac{4}{5}$ the same as $\frac{4}{5} \div \frac{2}{3}$? _____

Is division commutative? _____

3. $\left(\frac{2}{3} \div \frac{1}{4}\right) \div \frac{3}{5} = \frac{40}{9}$ and $\frac{2}{3} \div \left(\frac{1}{4} \div \frac{3}{5}\right) = \frac{24}{15}$

Is division associative? _____

Exercises

Work each problem and put the answer in the appropriate square in the chart.

1. $\frac{3}{4} \div \frac{5}{4}$

2. $\frac{6}{7} \div \frac{1}{14}$

3. $\frac{12}{13} \div \frac{13}{7}$

4. $\frac{5}{3} \div \frac{6}{9}$

5. $\frac{4}{16} \div \frac{3}{4}$

6. $\frac{15}{20} \div \frac{3}{5}$

7. $\frac{34}{22} \div \frac{13}{11}$

8. $\frac{8}{21} \div \frac{3}{7}$

9. $\frac{27}{35} \div \frac{3}{7}$

10. $\frac{10}{24} \div \frac{5}{12}$

11. $\frac{15}{25} \div \frac{7}{5}$

12. $\frac{136}{238} \div \frac{9}{14}$

13. $\frac{19}{18} \div \frac{5}{6}$

14. $\frac{81}{64} \div \frac{27}{16}$

15. $\frac{125}{169} \div \frac{25}{26}$

16. $\frac{144}{289} \div \frac{36}{34}$

1	2	3	4
5	6	7	8
9	10	11	12
13	14	15	16

Compound Savings

A teenage boy decided to save his money for 30 days. The first day he saved 1¢, the second day 2¢, the third 4¢, and the fourth 8¢. If he continues to save twice as much money each succeeding day, how much will he have accumulated at the end of the 30 day period?

E. Reading decimal numerals:

When reading a mixed decimal, the decimal point is read "and". First read the whole number, then read the word "and" to show the position of the decimal point, and then read the decimal fraction.

ten-thousands	thousands	hundreds	tens	ones	and	tenths	hundredths	thousandths	ten-thousandths	hundred-thousandths	millionths
			2	4	.	5	4				

Twenty-four
and
fifty-four hundredths

EXERCISES

Write the following decimal numerals in words.

1. 8.6 _____
2. 100.43 _____
3. .50062 _____
4. .00009 _____
5. 5.0 _____
6. 225.089 _____
7. 4.1575 _____

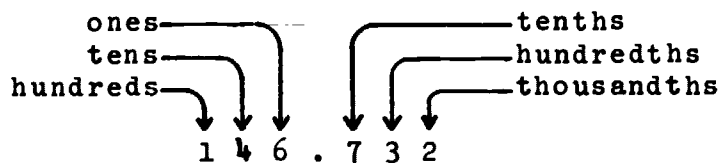
F. Writing decimal numerals:

To write a mixed decimal, write the whole number, place the decimal point after the whole number, and then write the decimal fraction.

EXERCISES

1. eighty hundredths _____
2. five hundredths _____
3. eight thousandths _____
4. one ten-thousandth _____
5. one hundred twenty-eight and two tenths _____
6. two hundred six and twenty-six hundredths _____
7. three thousand and eight hundredths _____

G. Rounding Off Decimal Numerals



Examples:

1. It is 713 miles from New York to Chicago; this distance might be quoted as a distance of 700 miles. We say that 713 has been rounded off to the nearest 100 miles.
2. When 17.462 is rounded off to tenths the result is 17.5.
Why?

Steps to follow in rounding off any decimal number:

- a. Locate the digit that is in the "round off" position. Draw a square around it.

17. 4 62

- b. Draw a circle around the digit to the right of the square.

17. 4 6 2

- c. If the digit in the circle is a 5, 6, 7, 8, or 9, then add one to the digit in the square. Replace all digits to the right of the square with zeros.

17. 5 00 or 17.5

- d. If the digit in the circle is a 0, 1, 2, 3, or 4, then do not change the digit in the square. Replace all digits to the right of the square with zeros.

3. When 13.827 is rounded off to tenths the result is 13.800 or just 13.8.

EXERCISES

1. Round off 7253.483 to:

- a. Hundredths _____
- b. Tenths _____
- c. Ones _____
- d. Tens _____
- e. Hundreds _____
- f. Thousands _____

2. Round off the following numbers to one's place:

- a. 147.2 = _____
- b. 95.68 = _____
- c. 4723.01 = _____
- d. 93.51 = _____
- e. 94.5 = _____
- f. 89.7 = _____
- g. 26.49 = _____

3. Round off the following numbers to hundredths:

- a. 1.255 = _____
- b. 14.314628 = _____
- c. 90.88888 = _____
- d. 33.33333 = _____
- e. 141 = _____
- f. 192.65499 = _____

4. Round off products as indicated:

- a. Hundredths $4.5 \times .16 =$ _____
- b. Tenths $176.9 \times 2.3 =$ _____
- c. Thousandths $2.5398 \times 86 =$ _____
- d. Hundredths $8963.5427 \times 8.36 =$ _____
- e. Ten thousandths $69.5199 \times 56.1 =$ _____
- f. Tenths $4.6 \times 18.5 =$ _____
- g. Ones $100 \times 0.14 =$ _____
- h. Hundredths $123 \times 9 =$ _____
- i. Tens $26.93 \times 14.6 =$ _____
- j. Hundreds $100 \times 14.6 =$ _____
- k. Thousands $236 \times 7.39 =$ _____

CONSOLIDATED BALANCE SHEET

ASSETS

	1966	Round Off
PROPERTY, PLANT AND EQUIPMENT.....	\$413,718,836	
Less: Reserves for depletion and depreciation.....	124,900,411	
	<u>\$288,818,425</u>	hundreds
INVESTMENTS, at cost:		hundred thousands
Municipal bonds.....	\$ 1,033,215	
Miscellaneous.....	3,656,144	
	<u>\$ 4,689,359</u>	
CURRENT ASSETS:		tens
Cash.....	\$ 5,706,685	
Temporary cash investments.....	68,204	
Special deposits.....	215,392	
Accounts Receivable:		
Customers.....	20,925,101	
Others.....	16,798,149	
Notes receivable—including installments due after one year:		
Customers.....	9,051,515	
Others.....	4,651,408	
Inventories:		thousands
Extracted products, chemicals and crude oil, at market or cost.....	1,212,798	
Cement products, at cost.....	684,592	
Materials and supplies, at average cost.....	5,190,541	
Manufactured products, lower of FIFO cost or market.....	11,996,828	
Gas in underground storage, at average cost.....	207,779	
Other current and accrued assets.....	—	
Prepayments.....	600,616	
	<u>\$ 77,302,608</u>	
DEFERRED CHARGES:		millions
Debt discount and expense being amortized over life of outstanding issues.....	\$ 1,564,681	
Other.....	7,984,171	
	<u>\$ 9,548,852</u>	
	<u>\$380,359,244</u>	

THE NOTES TO FINANCIAL STATEMENTS ARE AN INTEGRAL PART OF THIS STATEMENT.

H. Changing Fractions To Decimal Equivalents

To change a fraction to decimal form, divide the numerator by the denominator. The decimal point in the quotient should be located directly above the decimal point in the dividend.

Example: $4 \overline{) 3.00} = .75$ so $\frac{3}{4} = .75$

$$\begin{array}{r} .75 \\ 4 \overline{) 3.00} \\ \underline{28} \\ 20 \\ \underline{20} \\ 0 \end{array}$$

Exercises

Change each of the following fractions to decimal form. Carry out as many decimal places as necessary.

1. $\frac{4}{5}$ 2. $\frac{7}{8}$ 3. $\frac{1}{4}$ 4. $\frac{1}{2}$ 5. $\frac{1}{5}$ 6. $\frac{13}{25}$
7. $\frac{11}{20}$ 8. $\frac{15}{16}$ 9. $\frac{1}{8}$ 10. $\frac{8}{5}$ 11. $\frac{9}{50}$ 12. $\frac{123}{500}$

In division of decimals, change the decimal fraction to a fraction having whole numbers as the numerator and the denominator. Then divide the regular way. Notice the use of 1, the identity for multiplication, in the examples.

Examples:

1. $.3 \times .4$
 $\frac{.3}{.4} = \frac{.3}{.4} \times \frac{10}{10} = \frac{30}{40} = .75$

2. $2.70 \div .6$
 $\frac{2.70}{.6} \times \frac{100}{100} = \frac{270}{60} = 4.5$

3. $3.16 \div .4$
$$\begin{array}{r} 7.25 \\ .40 \overline{) 3.1600} \\ \underline{280} \\ 360 \\ \underline{320} \\ 400 \\ \underline{400} \\ 0 \end{array}$$

Exercises

Change the following fractions to decimals.

1. $\frac{3}{4} =$

2. $\frac{4}{8} =$

3. $\frac{3}{5} =$

4. $\frac{4}{7} =$

5. $\frac{5}{32} =$

6. $\frac{43}{50} =$

7. $\frac{1}{2} =$

8. $\frac{2}{7} =$

9. $\frac{1}{6} =$

10. $\frac{1}{8} =$

11. $\frac{1}{12} =$

12. $\frac{3}{7} =$

13. $\frac{7}{20} =$

14. $\frac{5}{36} =$

15. $\frac{3}{1000} =$

16. $\frac{8}{7} =$

17. $\frac{3}{8} =$

18. $\frac{4}{16} =$

19. $\frac{5}{7} =$

20. $\frac{5}{3} =$

Brain Teaser

In a will, a man leaves \$626.00 to three friends. When the man dies, his friends are 20, 30 and 50. Divide the money among the three in proportion to their ages.

CALCULATOR PRACTICE

Decimal Values Of Rational Numbers < 1
(Save for Reference)

X	1	2	3	4	5	6	7	8	9	10
1/2	.5000	X	X	X			X			X
1/3										
1/4			.7500				X			
1/5										
1/6						X				
1/7									X	
1/8					.6250					
1/9										
1/10										X
1/11										
1/12										
1/13										
1/14				.2857						
1/15										
1/16									.5625	
1/17										
1/18										
1/19						.3158				
1/20										

Complete the chart using four decimal place accuracy.

Mark X in rectangles whose value is not less than one.

Example: $\frac{3}{4} = \frac{1}{4} \cdot 3$ $\left\{ \begin{array}{l} \text{Locate } \frac{1}{4} \text{ on left} \\ \text{Locate } 3 \text{ at top} \end{array} \right\} = .7500$

Decimal Values of Rational Numbers < 1

(Save for Reference)

x	11	12	13	14	15	16	17	18	19	20
1/12	.9167	X	X				X			
1/13										
1/14				X		X				
1/15									X	
1/16										
1/17										
1/18										X
1/19						.8421				
1/20										

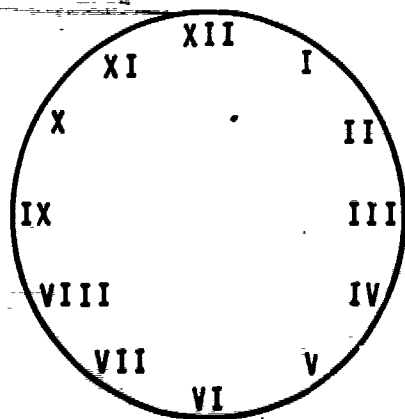
Complete the chart using four decimal place accuracy.

Mark X in rectangles whose value is not less than one.

Challenge Problem

A man drops a clock on the floor and it breaks into four pieces. Each piece shows a sum of 20.

Can you show where the breaks occurred? Is it possible for the breaks to have occurred in more than one way and still show sums of 20?



Exercises

Use machines to check the problems by multiplying.

1. $25 \overline{) .10600}$

2. $.823 \overline{) 1.28388}$

3. $5.41 \overline{) 3.50027}$

4. $.798 \overline{) 52.1094}$

5. $.1225 \overline{) 1.057175}$

6. $66.59 \overline{) 30.21854}$

Work these problems on the calculator.

7. $.952 \div 5.6 = \underline{\hspace{2cm}}$

15. $184.7032 \div 5.56 = \underline{\hspace{2cm}}$

8. $94.08 \div 1.12 = \underline{\hspace{2cm}}$

16. $53.9377 \div 54.1 = \underline{\hspace{2cm}}$

9. $31.904 \div 9.97 = \underline{\hspace{2cm}}$

17. $.20522 \div 6.62 = \underline{\hspace{2cm}}$

10. $49.94032 \div 66.41 = \underline{\hspace{2cm}}$

18. $33.75 \div .15 = \underline{\hspace{2cm}}$

11. $.118944 \div 5.664 = \underline{\hspace{2cm}}$

19. $1.4518 \div .017 = \underline{\hspace{2cm}}$

12. $18.4815 \div .555 = \underline{\hspace{2cm}}$

20. $152.49 \div 6.63 = \underline{\hspace{2cm}}$

13. $654.61466 \div 7.42 = \underline{\hspace{2cm}}$

21. $59.51 \div 1.1 = \underline{\hspace{2cm}}$

14. $2192.542 \div 99.661 = \underline{\hspace{2cm}}$

22. $6.660 \div 1.5 = \underline{\hspace{2cm}}$

Practical Application

INVOICE

Phone
FR-2-5121

Jaycee

SUPPLY COMPANY

BEAUTY AND BARBER SUPPLIES

MAIN AT ROOSEVELT

LITTLE ROCK, ARKANSAS

P. O. BOX 144

DATE Dec 30 1965 TERMS Chg.

SOLD TO Hazel Sanders SHOP Hazel's Bty Shop

STREET CITY STATE

CODE	QUAN. ORDERED	QUAN. SHIPPED	DESCRIPTION	unit price	AMOUNT
1010			Custom Snap + Body Waves		15.5
2	2		" " " "		Free
5	5		Custom Sint Perm Waves		9.95
1	1		" " " "		Free
8	8		Body Treat + Hold Waves		29.95
4	4		Control " " "		
6	6		" " " "		free

No Merchandise Accepted For Return After 45 Days From Date of Invoice, Unless Defective.
 Our Responsibility For Delivery and Damage Ceases After Delivery to Carrier. Make All Claims For Losses or Damages with Carrier Immediately.

Total		
Sales Tax		
Ins. & Trans.		XY
NET TOTAL		

- A. Back Ordered Will Ship Soon
- B. To Be Shipped Direct From Factory
- C. Discontinued By The Factory
- D. Delivered By Salesman
- E. Order Not Clear, Our Guess
- F. Out of Stock, Please Reorder
- H. Do Not Stock, Item Cancelled
- J. Reorder, Give Size, Color, Etc.
- M. Substituted, If Not Satisfactory, Return For Credit

DATE SHIPPED	HOW SHIPPED	SELECTED	CHECKED	PACKED	NO. OF CARTONS	SALESMAN
1/5/65	Southwestern	J	BB		2	Bill Jay

TITLE TO THE ABOVE DESCRIBED PROPERTY IS HEREBY RETAINED BY THE SELLER UNTIL PAID FOR IN FULL

CUSTOMER'S COPY

THIS IS YOUR INVOICE—KEEP IT

Find the total, the sales tax, and the net total. Find the price per item on each entry. Do not include free items in figuring the unit price.

CROSS COUNTY HOSPITAL

POST OFFICE DRAWER H

WYNNE, ARKANSAS 72396

Problems in Hospital Laundry

During April 1966 a hospital laundry processed 123,950 lbs. of linen. The total number of hours worked by all laundry employees was 3,040. The total cost for all supplies and salaries was \$7,150.

Question:

1. What was the number of lbs. of laundry processed per employee hour?
2. What was the cost per lb. to process the laundry?

Problem in Medical Records Department

Total salary expense in Medical Records Dept. during April 1966 was \$2,490.32.

Total other expenses in Medical Records Dept. during April 1966 was \$255.85.

Total patients discharged during April 1966 was 1,155.

Question:

1. How much did it cost to process each patient's chart?

SCHOOL SUPPLIES, INC.

SCHOOL SUPPLIES * WHOLESALE AND RETAIL

On the following page you will find an invoice for merchandise ordered from Mallard Pen and Pencil Company, Inc. See if you can answer the following questions in regard to these materials:

1. What was the date of the order? _____
2. What was the shipping date? _____
3. How was the merchandise shipped? _____
4. Who paid freight on this shipment? _____
5. Was all the merchandise shipped that was ordered? _____
6. What are the terms of the sale and how much does this discount amount to on this order? _____
7. How many pencils in a gross? _____
8. How many dozen in a gross? _____
9. How many cases in this shipment? _____
10. What was the total weight of the shipment? _____
11. If the "Humdinger" pencils sold for \$2.16 per gross, what would the per cent of mark-up be? _____
12. What is the cost price per compass? _____
13. What is the cost price of compasses per dozen? _____
14. What is the cost price per ruler? _____
15. Write a check to pay the bill.

Maillard PEN & PENCIL CO., INC.

PENCILS OF QUALITY • GEORGETOWN, KENTUCKY

INVOICE

No. 8470

SOLD TO

SHIP TO

SAME

TERMS: 2% EOM NET 60

CUSTOMER ORDER NO.	DATE OF ORDER	SALESMAN	TO BE SHIPPED ASAP		
	10-24-71	THORNTON			
INVOICE DATE	SHIPPING DATE	SHIPPED VIA	NO. OF CASES		
10-29-71	10-29-71	TRUCK PREPAID	4		
QUANTITY ORDERED	BACK ORDER	DESCRIPTION	QUANTITY SHIPPED	UNIT PRICE	VALUE
75	0	HUNDINGER	75	1.62	121.50
2	0	RULERS	2	6.48	12.96
1	0	ERASERS	2	3.60	7.20
1	0	COMPASS	1	14.40	14.40
1	0	PRECISION	1	4.40	4.40
					<u>160.46</u>

Paid 11-10-71 \$63.34

NO GOODS CAN BE RETURNED WITHOUT OUR PERMISSION. NO FREIGHT ALLOWANCE ON LESS THAN LBS. ALL PRODUCTS OF THIS COMPANY ARE MANUFACTURED IN COMPLIANCE WITH THE FAIR LABOR STANDARDS ACT OF 1938 AS AMENDED. 6% INTEREST CHARGED ON PAST DUE ACCOUNTS.

I. Renaming Rational Numbers

Exercises

1. a. $1 = \frac{\square}{1}$

b. $\frac{5}{5} = \square$

c. $1 = \frac{7}{\square}$

d. $1 = \frac{8}{\square}$

e. $\frac{9}{9} = \square$

2. a. $\frac{12}{15} = \frac{\square}{\square} \cdot \frac{4}{5}$

b. $\frac{2}{3} \cdot \frac{\square}{\square} = \frac{14}{21}$

c. $\frac{\square}{\square} \cdot \frac{7}{8} = \frac{28}{32}$

d. $\frac{8}{36} = \frac{2}{9} \cdot \frac{\square}{\square}$

e. $\frac{1}{7} \cdot \frac{\square}{\square} = \frac{3}{21}$

3. a. $8 = \frac{8}{\square}$

b. $\frac{3}{4} + \frac{3}{5} = \frac{\square}{20} + \frac{\square}{20}$

c. $6 = \frac{\square}{1}$

d. $\frac{1}{2} + \frac{2}{3} = \frac{\square}{6} + \frac{\square}{6}$

e. $\frac{2}{3} + \frac{1}{6} = \frac{4}{\square} + \frac{1}{\square}$

4. a. $5 \frac{2}{3} = 5 + \square$

b. $4 \frac{1}{4} = \frac{\square}{4} + \frac{\square}{4}$

c. $9 \frac{1}{6} = \square + \frac{1}{6}$

d. $3 \frac{4}{7} = \frac{21}{\square} + \frac{4}{\square}$

5. Change fractions to decimals or vice versa:

a. $\frac{2}{5} = \square$

b. $\frac{7}{8} = \square$

c. $\frac{6}{5} = \square$

6. Write the numeral represented by the following:

a. $2^2 = \square$

b. $3^3 = \square$

c. $4^2 = \square$

7. Write in exponent form:

a. $49 = \square$

b. $25 = \square$

c. $81 = \square$

8. Fill in the blanks:

a. 15 minutes = _____ hrs.

b. 2 pounds = _____ ounces

c. _____ inches = $2\frac{1}{2}$ feet

d. 2 quarters = _____ dimes

e. _____ yards = 72 inches

9. (Optional)

a. $82_{\text{ten}} = \square_{\text{eight}}$

b. $122_{\text{three}} = \square_{\text{ten}}$

NUMBERS DIVISIBLE BY THREE

Any number is divisible by 3 if the sum of the digits is divisible by 3. For example, 129 is divisible by 3 since $1 + 2 + 9 = 12$ and 12 is divisible by 3. Checking, we see that 129 divided by 3 is 43.

Is 8217 divisible by 3?

When is a number divisible by 2?

When is a number divisible by 5?

When is a number divisible by 10?

J. Finding the Least Common Multiple

Exercises

1. R is the set of the multiples of 5.

$$R = \{ \quad \quad \quad \}$$

2. Q is the set of the multiples of 6.

$$Q = \{ \quad \quad \quad \}$$

a. Is the set of multiples of 5 finite or infinite? _____

b. Is the set of multiples of 6 finite or infinite? _____

3. The members common to both sets R and Q form a new set.

$$E = \{ \quad \quad \quad \}$$

This is the set of common multiples of 5 and 6.

4. What is the least element in set E? _____

This is called the Least Common Multiple of 5 and 6.

5. Now what about the numbers 8 and 12?

$$\text{Multiples of 8} = \{ \quad \quad \quad \}$$

$$\text{Multiples of 12} = \{ \quad \quad \quad \}$$

$$\text{Common multiples of 8 and 12} = \{ \quad \quad \quad \}$$

Least common multiple of 8 and 12 is

6. By forming sets of multiples, find the Least Common Multiple of:

a. 12 and 15

$$\begin{array}{l} \text{multiples of 12} = \{ \quad \quad \quad \} \\ \text{multiples of 15} = \{ \quad \quad \quad \} \\ \text{common multiples of 12 and 15} = \\ \text{LCM is } \{ \quad \quad \quad \} \end{array}$$

b. Multiples of 6 = {
 Multiples of 8 = {
 Multiples of 9 = {
 Common multiples of 6, 8, 9 = {
 LCM is

c. 8, 9, 12

7. Find the LCM of the denominators in the following problems.

a. $\frac{2}{5} + \frac{1}{2} + \frac{2}{3}$ LCM =

b. $\frac{4}{5} + \frac{8}{9} + \frac{1}{5}$ LCM =

c. $\frac{9}{10} + \frac{4}{5} + \frac{14}{15}$ LCM =

d. $\frac{4}{7} + 5 + \frac{9}{2}$ LCM =

e. $\frac{2}{3} + \frac{1}{27} + \frac{4}{9}$ LCM =

f. $\frac{4}{16} + 3 + \frac{6}{7}$ LCM =

g. $\frac{4}{13} + \frac{1}{2} + \frac{3}{2}$ LCM =

h. $\frac{7}{18} + \frac{3}{13} + \frac{5}{6}$ LCM =

i. $\frac{9}{10} + \frac{10}{9} + \frac{10}{21}$ LCM =

j. $\frac{3}{4} + \frac{4}{3} + \frac{1}{5}$ LCM =

k. $\frac{4}{45} + \frac{1}{15} + \frac{42}{45}$ LCM =

l. $\frac{24}{29} + \frac{13}{39} + \frac{128}{13}$ LCM =

K. Changing Mixed Numerals to Improper Fractions

Exercises

1. $6 \frac{1}{3} =$

2. $2 \frac{1}{3} =$

3. $3 \frac{1}{3} =$

4. $3 \frac{1}{2} =$

5. $4 \frac{1}{2} =$

6. $5 \frac{1}{2} =$

7. $5 \frac{1}{4} =$

8. $5 \frac{2}{4} =$

9. $7 \frac{2}{4} =$

10. $53 \frac{3}{21} =$

11. $3 \frac{5}{41} =$

12. $3 \frac{5}{6} =$

13. $11 \frac{5}{9} =$

14. $9 \frac{2}{3} =$

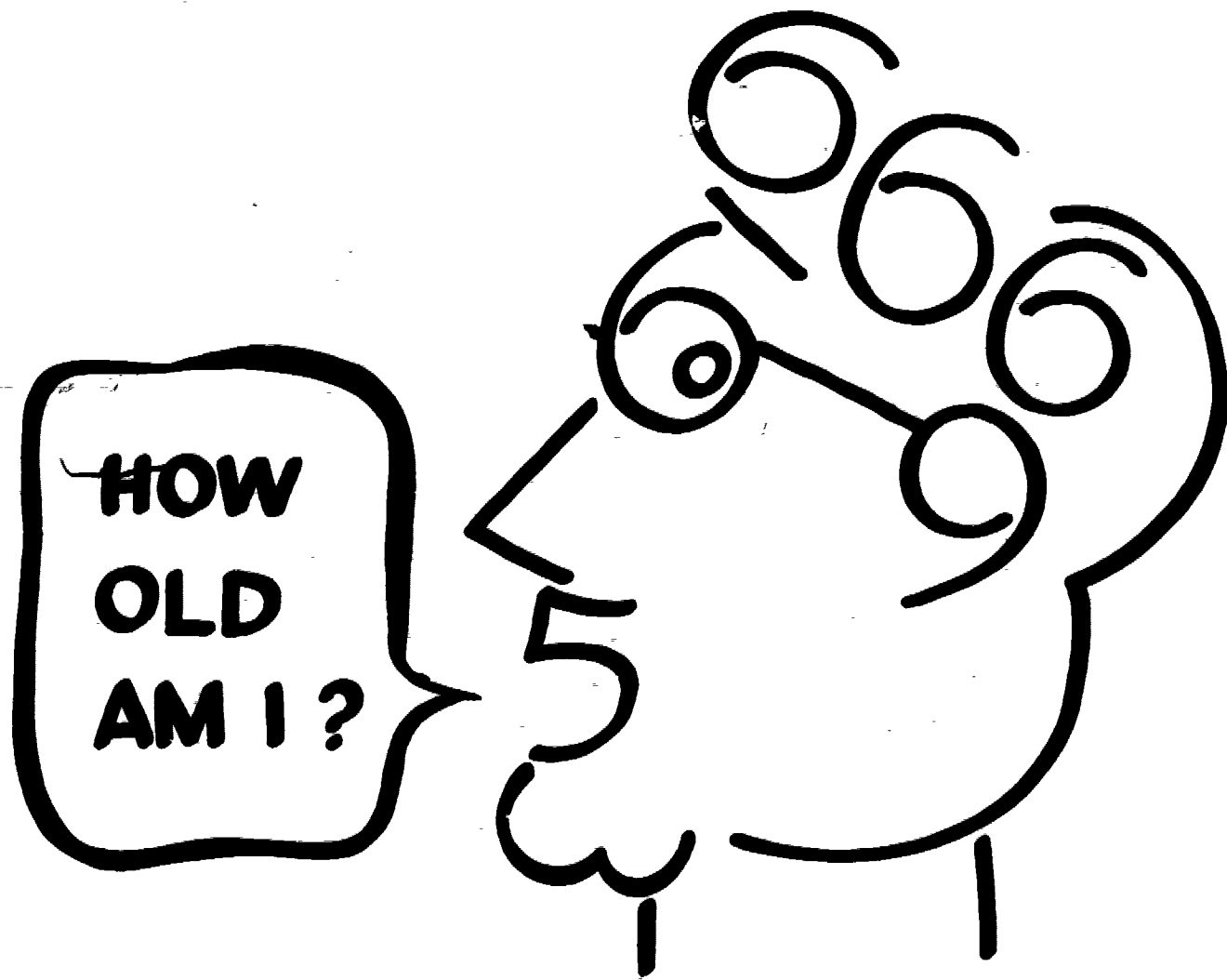
15. $53 \frac{1}{6} =$

16. $2 \frac{3}{4} =$

17. $9 \frac{3}{7} =$

18. $3 \frac{1}{10} =$

Grandfather Time



L. Addition of Fractions

Example:

$$\frac{3}{4} + \frac{4}{5} = \left(\frac{3}{4} \cdot \frac{5}{5}\right) + \left(\frac{4}{5} \cdot \frac{4}{4}\right) = \frac{15}{20} + \frac{16}{20} = \frac{31}{20}$$

Exercises

1. $\frac{1}{3} + \frac{1}{3} =$

2. $\frac{5}{7} + \frac{1}{7} =$

3. $\frac{6}{13} + \frac{2}{13} + \frac{3}{13} =$

4. $\frac{3}{4} + \frac{3}{8} =$

5. $\frac{5}{12} + \frac{1}{3} =$

6. $\frac{1}{2} + 4 =$

7. $\frac{1}{3} + \frac{1}{4} =$

8. $\frac{5}{4} + \frac{9}{8} =$

9. In the above problems is each answer a rational number? _____
10. Are the rational numbers closed under addition? _____

Trick Numbers

1. Write twelve thousand twelve hundred and twelve.
2. Write one hundred using only the nine digits and the signs of arithmetic.
3. Write nineteen using only four 9's.

Exercises

Work each of the following problems and place the answers in the appropriate box in chart. After you have completed the chart find the sum of each row and column.

1. $\frac{1}{5} + \frac{2}{10}$

2. $\frac{4}{9} + \frac{4}{18}$

3. $\frac{1}{3} + \frac{5}{6}$

4. $\frac{3}{5} + \frac{4}{5}$

5. $\frac{5}{10} + \frac{4}{10}$

6. $\frac{7}{13} + \frac{12}{26}$

7. $\frac{18}{20} + \frac{3}{10}$

8. $\frac{9}{12} + \frac{1}{4}$

9. $\frac{5}{6} + \frac{9}{12}$

10. $\frac{7}{21} + \frac{2}{3}$

11. $\frac{4}{30} + \frac{4}{5}$

12. $1\frac{1}{3} + \frac{1}{2}$

13. $\frac{9}{16} + \frac{7}{16}$

14. $\frac{7}{12} + \frac{5}{6}$

15. $1\frac{1}{3} + \frac{2}{6}$

16. $\frac{6}{18} + \frac{2}{3}$

1	2	3	4
5	6	7	8
9	10	11	12
13	14	15	16

M. Addition Properties of Rational Numbers

Exercises

1. a. $\frac{1}{6} + \frac{4}{6} = \square + \frac{1}{6}$

b. $\frac{3}{5} + \square = \frac{4}{5} + \frac{3}{5}$

c. $\frac{2}{5} + \frac{3}{10} = \square + \frac{2}{5}$

d. $\frac{2}{3} + \frac{7}{9} = \frac{7}{9} + \square$

You used the _____ property to complete the above problem. Check your answers in the boxes by comparing the sum of the fractions on each side of the equal sign.

2. a. $\left(\frac{1}{5} + \frac{2}{5}\right) + \frac{4}{5} =$

As problem a is written, what two fractions would you combine first? Then what fraction would you add to this sum? What is your answer?

b. $\frac{1}{5} + \left(\frac{2}{5} + \frac{4}{5}\right) =$

As problem b is written, what two fractions would you combine first? Then what fraction would you add to this sum? How does your final answer compare with a?

c. $\left(\frac{3}{4} + \frac{2}{3}\right) = \frac{4}{5}$

As problem c is written, what two fractions would you combine first? What do you have to do before combining them? What fraction would you add to this sum? Do you have to do the same as above before you can combine them? What is your answer?

d. Rewrite problem c to indicate combining $\frac{3}{4}$ to the sum of $\frac{2}{3}$ and $\frac{4}{5}$. What answer do you get?

Problems a, b, c, and d illustrate the _____ property.

3. a. $2/3 + \underline{\hspace{1cm}} = 2/3$ b. $1/10 + 0 = \underline{\hspace{1cm}}$ c. $0 + 5/6 = \underline{\hspace{1cm}}$

How does the result of each of these problems compare with the given fraction? Can we assume that there exists an identity element for addition of fractions? If so, what is the identity element?

4. a. $1/5 + \underline{-1/5} = \underline{\hspace{1cm}}$ b. $4/5 + \underline{\hspace{1cm}} = 0$ c. $\underline{\hspace{1cm}} + -2/3 = 0$
d. $\underline{-7/8} + 7/8 = \underline{\hspace{1cm}}$ e. $\underline{-9/7} + \underline{\hspace{1cm}} = 0$ f. $\underline{\hspace{1cm}} + 5/9 = 0$





What is true about the addends of each example above?


Compare the results of the above examples.

The result in all these problems is the element for addition.

Therefore, each addend is the of the other addend.

5. Complete the Fraction-o-Grams

			
a. $3 \frac{1}{2}$	b. $5 \frac{4}{5}$	c. $1 \frac{1}{8}$	d. $2 \frac{3}{4}$
e. $7/8$	f. $5/6$	g. $2/3$	h. $7/9$
i. $1/4$	j. $3/4$	k. $5/4$	l. $1/7$
m. $9/10$	n. $1/16$	o. $3/5$	p. $5/7$

 + $\left(\begin{array}{c} \text{triangle} \\ + \\ \text{square} \end{array} \right)$	$\left(\begin{array}{c} \text{circle} \\ + \\ \text{square} \end{array} \right)$ + triangle
a. $2 \frac{3}{4} + (3 \frac{1}{2} + 5 \frac{4}{5}) =$	e. $(1 \frac{1}{8} + 5 \frac{4}{5}) + 3 \frac{1}{2} =$
b.	f.
c.	g.
d.	h.

N. Comparing Fractions

Exercises

1. Circle the larger fraction of each pair.

$1/3$ or $1/4$

$3/5$ or $8/10$

$1/2$ or $3/5$

$1/7$ or $3/14$

$1/4$ or $5/8$

$7/9$ or $13/18$

2. Cross out the incorrect word in the parentheses.

(a) For a particular fraction as the denominator decreases
the value of the fraction (increases, decreases).

(b) For a particular fraction as the numerator increases
the value of the fraction (increases, decreases).

3. Arrange these fractions from least to the greatest.

$3/4$

$7/8$

$5/6$

$11/12$

$23/24$

_____, _____, _____, _____, _____.

4. Arrange these fractions from the greatest to the least.

$3/8$

$5/6$

$3/4$

$5/12$

$7/10$

_____, _____, _____, _____, _____.

0. Addition of Decimals

Example:

$$\begin{array}{r} \text{Add: } 14.32 \\ \quad 5.678 \\ \hline \end{array}$$

In order to keep the decimal point in correct position, we must place zeros as placeholders. Then the problem rewritten would be:

$$\begin{array}{r} 14.320 \\ \quad 5.678 \\ \hline 19.998 \end{array}$$

Zeros are placed to give the same numbers of digits to the right of the decimal point.

Exercises

1. $146.59 + 11.687 =$
2. $1,156.834 + 998.62 + 6.9 =$
3. $742.544 + -69.3194 + 7.13 =$
4. $9,645.7853 + 573.478 + 69.72 + 17.9 =$
5. $\begin{array}{r} 456.6 \\ \quad 68.58 \\ \hline 79.474 \end{array}$
6. $\begin{array}{r} 4,456.93 \\ -579.643 \\ \hline 62.1455 \end{array}$
7. $77.77 + 5.555 + 333.3 =$
8. $107.9 + 10.06 + 3.293 =$
9. $\$104.93 + \$87.45 + \$6.57$
10. $\boxed{} + -709.15 = 57.567$

*
Practical Applications
JUNIOR ACHIEVEMENT

Company Profits Tax Computation For Operating Year 19 -19

UNIRAC	South 31st & Tulsa	Fort Smith
Name of Company	Business Center Address	City

All tax receipts are retained in the local area for the benefit of achievers.

GROSS INCOME

1.	From sale of products or services	\$911.50
2.	Other income	<u>16.84</u>
3.	Total income	<u> </u>

DEDUCTIONS

4.	Cost of goods sold:	
	a. Raw materials	\$380.26
	b. Direct labor	54.60
5.	Rent	<u>8.67</u>
6.	Shop supply	48.84
7.	Office supply	<u>56.60</u>
8.	Depreciation	20.23
9.	Salaries and other compensation	<u> </u>
10.	Commissions	<u> </u>
11.	Other expenses	<u> </u>
	a. Advertising and promotion	<u> </u>
	b. Annual Report	<u> </u>
	c. Contributions	<u> </u>
	d. Bad debts	<u> </u>
	e. Other	24.25
12.	Total deductions	\$646.92
13.	Net income before taxes	<u>\$646.92</u>

No expenses on the following items: annual report, advertising and promotion, contributions, bad debts, and depreciation.

Compute total income, rent, and net income before taxes and write the results in the appropriate blanks.



NO ORDERS
 CHANGE
 C.O.D.

NO CUSTOMER NO.
 NEW CUSTOMER
 NAME/ADDRESS CHANGE

STRATTON WARREN
 Hardware Company

PAGE 1 OF 1
 DATE 11-10-71

Inst. No.	SLS No.	Quot. Order No.	Sold To	Ship to - Credit
			Graham Hardware	
Ship Via	PWP/COL	Address	City & State	Zip Code
7-12-71		Union Ave.		72396
When Ship	Discount	City & State	Address	City & State
8-10-71				
Terms: 2% 10 net 60	Tax	Sub	Bo	Peck
				Slip
				Attention:
				Special Instructions

Item/Stock Number/Size/Color/Description	Index - Serial No.	Quantity	Filling Unit	Price Group	Price	Ext	Extension
3 Rolls - 48' 2x4 Welder Wire	()	3	Rolls	-	2465R		
12 Ea. - 84-103 1/2 Stop + Drain	()	12	ea.	-	137ea		
6 " - 84-105 3/4 " + "	()	6	ea.	-	167 "		
6 " - 79-323 1/2 Gate Valves	()	6	"	-	105 "		
6 " - 79-325 3/4 "	()	6	"	-	185 "		
2 CT - 2 D Flash Lite Butters	()	2	CT	-	278CT		
24 Ea. - 1/2 Cable Clamps	()	24	C	-	1965 C		
12 " - 3/8 Cable Clamps	()	12	C	-	256 C		
12 " - 3/4 " "	()	12	C	-	364 C		
2 " - 1 1/2" TAD Sledge W/1/4"	()	2	ea.	-	490ea.		
50 Ea. # D Screw Eyes	()	50	C	-	650 C		
50 " # 2 " "	()	50	C	-	430 C		
} Find Extensions - C means Per Hundred }							
					7079L		

HOME OF BETTER VALUES



A GOOD PLACE TO TRADE

ASSOCIATE STORE

HOME OF BETTER VALUES



A D-8 GOOD PLACE TO TRADE

ASSOCIATE STORE

WINNIE, ARKANSAS

SALESMAN

YOUR ORDER NO.

DATE 6-27-71

SOLD TO

24C Dalton & Fowler

ADDRESS

208 S. Cottonwood

CITY

Wynona STATE Ark.

QUAN.	DESCRIPTION OF ARTICLES	PRICE	TOTAL
1	Super Photo frame	2.49	
1	Fiberglass Muller pen	5.98	
1	O.P. Fib. for Muller pen	1.79	
1	HC 245 Battery	1.95	
1	Smart Dr. B. B. 1	4.3	
1	3M Training Address	.98	
1	300 Bolt	1.09	
4	White Walle	.25	
2	Tail Pipe Extension	.98	
1	Trusty 4 Jet	.89	
1	TK 157 MV Tuning Kit	1.59	
10	Ac 44 Plug	.79	
	Total		
	Net Total		

TERMS: NET - NO DISCOUNT
Pub-Printed, Inc., Wynona, Arkansas 72095-8

Find the total price for each item, the Arkansas sales tax for each purchase slip, and the total amount purchased on each date.

WINNIE, ARKANSAS

SALESMAN

YOUR ORDER NO.

DATE 5-24-71

SOLD TO

24C Dalton & Fowler

ADDRESS

208 S. Cottonwood

CITY

Wynona STATE Ark.

QUAN.	DESCRIPTION OF ARTICLES	PRICE	TOTAL
1	Red Wagon	3.98	
1	Red 4x4	.97	
1	Cam spray paint	.99	
1	Cam spray paint	1.19	
2	Grease & Soap	.99	
1	Range Arch. Bolt	4.49	
	Bike advertisement	6.26	
	Total		
	Net Total		

TERMS: NET - NO DISCOUNT
Pub-Printed, Inc., Wynona, Arkansas 72095-8

P. Subtraction of Rationals

To subtract two fractions, use the identity for multiplication to get common denominators. Then subtract numerators from numerators and denominators from denominators.

Example:

$$2/3 - 3/5 = (2/3 \times 5/5) - (3/5 \times 3/3) = 10/15 - 9/15 = 1/15$$

Exercises

1. $\frac{4}{7} - \frac{2}{7} =$

2. $\frac{8}{15} - \frac{2}{15} =$

3. $\frac{4}{5} - \frac{1}{10} =$

4. $\frac{7}{8} - \frac{2}{5} =$

5. $1\frac{2}{9} - \frac{7}{8} =$

6. $1\frac{1}{4} - 1\frac{5}{6} =$

7. Is the answer to 6 a rational number?

8. $5\frac{1}{3} - 3\frac{2}{3} =$

9. $8 - 1\frac{7}{16} =$

10. $4\frac{3}{8} - 2\frac{1}{4} =$

11. $14\frac{1}{4} - 5\frac{2}{3} =$

12. $2\frac{3}{4} - 1\frac{1}{3} =$

13. $24\frac{1}{5} - 12\frac{2}{3} =$

14. $3\frac{7}{16} - 1\frac{3}{4} =$

15. $5\frac{4}{45} - 1\frac{1}{3} =$

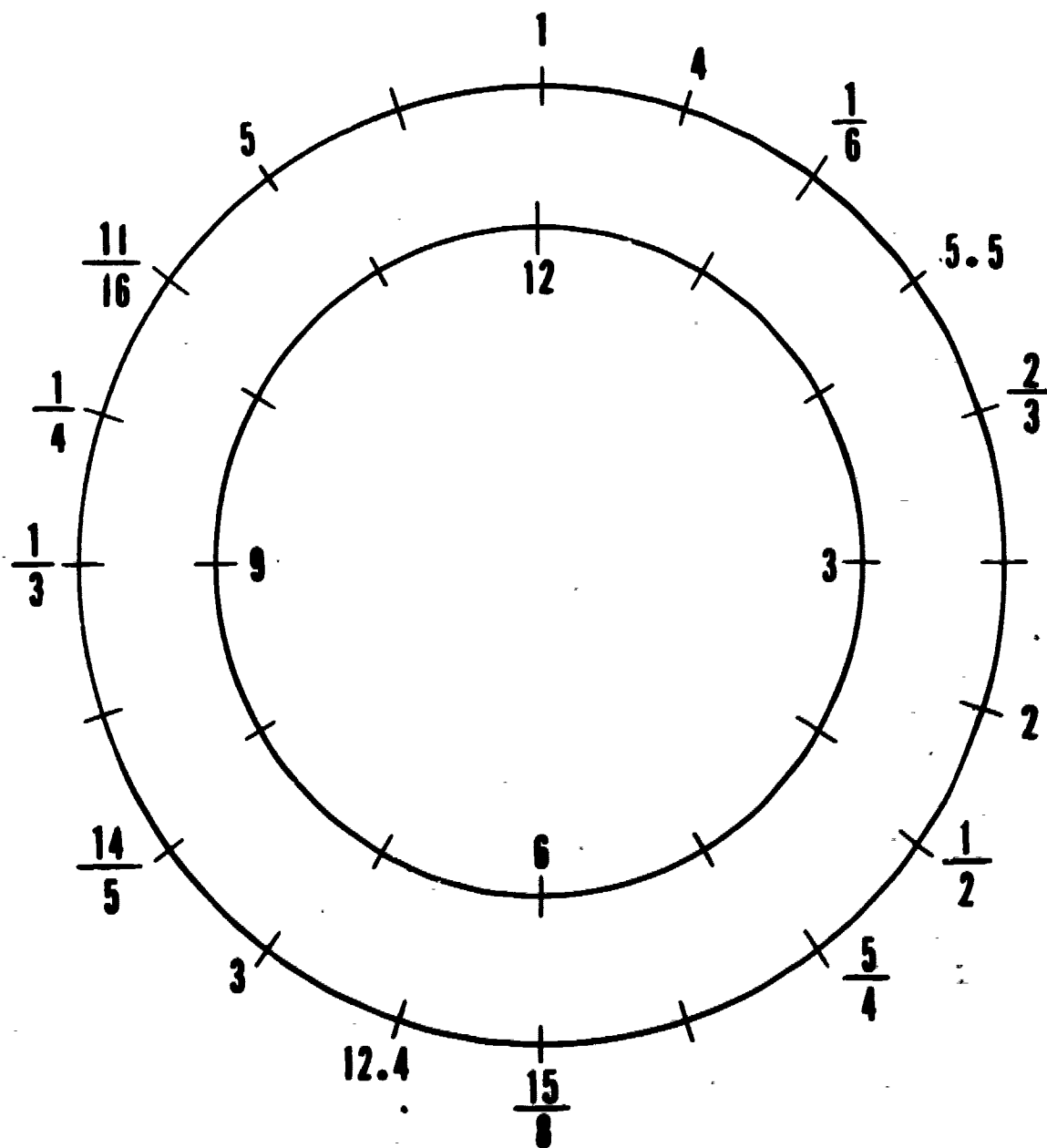
WHAT TIME IS IT?

Each problem consists of two parts. The answer to each part will be found on the outer circle. What time does each problem represent? (clock on page 109)

<u>MINUTE HAND</u>	<u>HOUR HAND</u>	<u>TIME</u>
Example: $\frac{3}{4} + \frac{1}{2} = \frac{5}{4}$	$3.08 + 2.42 = 5.5$	2:24 2:25
1. $\frac{3}{6} - \frac{1}{3} =$	$2.08 - 1.08 =$	_____
2. $\frac{3}{6} \times \frac{2}{3} =$	$1\frac{1}{4} \times 1\frac{2}{4} =$	_____
3. $\frac{5}{16} \times \frac{4}{5} =$	$3.6 \div 1.2 =$	_____
4. $\frac{16}{7} \div \frac{8}{7} =$	$2.01 + 1.89 + 1.10 =$	_____
5. $\frac{14}{7} \div \frac{5}{7} =$	$1 \div \frac{3}{2} =$	_____
6. $1.28 + 2.72 =$	$\frac{5}{16} - \frac{3}{16} + \frac{6}{16} =$	_____
7. $1.32 + 11.08 =$	$\frac{7}{16} + \frac{2}{8} - \frac{4}{4} + 1 =$	_____

Suggestion: Use toothpicks for hands on clocks to save erasing.

WHAT TIME IS IT?



Way Out Problem

	0	1	2	3	4	5	6	7	8	9
0
1
2
3
4
5
6
7
8
9

Let the horizontal numbers represent the numerator and vertical numbers represent the denominator of a rational number.

Example: The dot circled is $\frac{7}{2}$. Join the dots representing the answers in the A and B part of each problem below.

By working the problems in order, circle the problem number at which you are able to determine the design.

1. a. $\frac{7}{1} - \frac{4}{1} = \frac{3}{1}$

b. $\frac{7}{3} - \frac{4}{3} = \frac{3}{3}$

2. a. $\frac{9}{4} - \frac{3}{4} =$

b. $\frac{12}{6} - \frac{6}{6} =$

3. a. $\frac{1}{5} - \frac{1}{5} = \frac{5}{5}$

b. $1 - \frac{3}{5} =$

4. a. $1 + \frac{1}{2} =$

b. $1 + \frac{2}{5} =$

5. a. $1 \times \frac{1}{2} = \square = \frac{\quad}{8}$

b. $\frac{2}{3} \times \frac{2}{3} =$

6. a. $\frac{1}{3} = \frac{\quad}{6}$

b. Same as 3 (a).

7. a. $\frac{4}{8} = \frac{1}{\square} = \frac{\square}{6}$

b. $\frac{11}{12} - \frac{1}{12} = \square = \frac{\square}{6}$

8. a. $1\frac{3}{4} =$

b. $\frac{2}{5} \cdot 4 =$

9. a. $1 = \frac{\square}{5}$ b. Same as 7 (b)
10. a. $\frac{1}{4} - \frac{1}{4} = \frac{\square}{4}$ b. $0 = \frac{\square}{6}$
11. a. $\frac{1}{7} + \frac{1}{3} = \square$ b. $11 (a) + \frac{1}{7} =$
12. a. $\frac{5}{12} \cdot \frac{12}{1} = \square = \frac{\square}{1}$ b. $\frac{4}{3} + \frac{8}{10} = \square = \frac{5}{\square}$
13. a. $2 \frac{1}{2} - 1 \frac{3}{4}$ b. Same as 7 (a)
14. a. Same as 10 (a) b. $\frac{1}{2} = \frac{2}{\square}$
15. a. Same as 13 (a) b. $\frac{7}{8} + \frac{3}{8} = \square = \frac{\square}{4}$
16. a. Same as 15 (b) b. Same as 9 (a)
17. a. Same as 2 (b) b. $\frac{3}{2} - \frac{1}{3} = \square$
18. a. Same as 17 (b) b. Same as 8 (b)
19. a. $1 - \frac{2}{7} = \square$ b. Same as 11 (b)
20. a. Same as 14 (b) b. Same as 3 (b)
21. a. Same as 2 (a) b. Same as 8 (a)
22. a. Same as 11 (b) b. Same as 5 (a)

R. Subtraction of Decimal Numerals

Exercises

In the subtraction of decimals, zeros must also be placed to the right of the decimal point as placeholders.

1. $97.453 - 7.54 =$
2. $\square + 98.976 = 244.476$
3. $56.873 + \square = 113.746$
4. $1465.3 - 976.25 =$
5. $783.768 - 13.656 =$
6. $.3869 - .0789 =$
7. $.97654 - .00423 =$
8. $.13 - .0078 =$
9. $145 - 2.593 =$
10. $\square + 991.55 = 1157$
11. $\$863.57 - \$79.41 =$
12. $\$75.76 + \square = \$1,145$

Count Down

Can you write from 10 to 1 backwards?
Time yourself. How many seconds did it take?

Calculator Practice

Subtract:

$$\begin{array}{r} 1. \quad 3,425.56 \quad 34,567.987 \quad 345.789 \\ \quad \underline{2,976.43} \quad \underline{27,659.654} \quad \underline{4.987} \end{array}$$

$$\begin{array}{r} 2. \quad 6,789 \quad 6,785 \quad 4,567 \quad 2,345 \quad 654 \\ \quad \underline{2,345} \quad \underline{3,456} \quad \underline{2,345} \quad \underline{345} \quad \underline{345} \end{array}$$

$$\begin{array}{r} 3. \quad 987,634 \quad 8,765,432 \quad 7,658,646 \\ \quad \underline{34,567} \quad \underline{456,745} \quad \underline{654,765} \end{array}$$

$$\begin{array}{r} 4. \quad 847,563.87 \quad 746,575.7856 \\ \quad \underline{36,585.75} \quad \underline{25,346.7563} \end{array}$$

$$\begin{array}{r} 5. \quad 384,757,665.76 \quad 85,756,393.89 \\ \quad \underline{87,659,475.86} \quad \underline{6,547,896.76} \end{array}$$

$$\begin{array}{r} 6. \quad 8,475.8578 \quad 958,674.9789 \quad 56.76 \\ \quad \underline{3,456.7658} \quad \underline{654,354.9876} \quad \underline{76.98} \end{array}$$

$$\begin{array}{r} 7. \quad 958,746,353.756 \quad 35,643,654.987 \\ \quad \underline{8,765,547.307} \quad \underline{67,898,765.876} \end{array}$$

S. Comparing Decimal Numerals

Exercises

1. Arrange these numbers from the least to the greatest.

.9 .5683 .77
.88 .34778 .06

2. Arrange these numbers from the greatest to the least.

1.77 1.70 1.8
1.08 1.50
1.35 1.009

3. Arrange these numbers from the least to greatest.

2.975 11.663 .8875
5.1 6.005 70.466
14.50998

4. Which has the least value? Circle answer

- a. Seven tenths or seven hundredths
- b. Nine hundredths or nine thousandths
- c. Two and five tenths or two and five thousandths

PERFECT NUMBERS

A number is perfect if it is the sum of its divisors. For example, 6 has divisors 1, 2, 3 (we exclude the number itself) and $1 + 2 + 3 = 6$. There is only one other perfect number between 6 and 50. Can you find that number?

T. Order of Operations

Exercises

1. Place parentheses which show the operation(s) you would perform first.

a. $4 \cdot 3 - 5$

b. $8 + 7 \cdot 2$

c. $8 - 4 \div 4$

d. $6 \cdot 3 - 2 \cdot 4$

e. $12 + 3 \cdot 5$

2. Find the value of each.

a. $3 + 6 \cdot 5 =$

b. $\frac{12}{3} - \frac{10}{5} =$

c. $7 \cdot 3 + 4 \cdot 8 =$

d. $2 \cdot 3 + 4 =$

e. $3(5 + 6) =$

f. $9 - 3 - 2 =$

g. $9 - (3 - 2) =$

h. $7(5 - 2) =$

i. $9 - \frac{12}{3} + 6 \cdot \frac{8}{2} =$

j. $5 \cdot 6 - 3 \cdot 2 + 8 \cdot 3 =$

3. Find the value of each.

a. $12 + 13 - 2(3 - 1) =$

b. $8 - 12 \div 6 + (7 - 1) - 5 =$

c. $5 + (6 + \overline{3 - 2} + 4) =$

d. $20 + 11 - 4 + \overline{7 - 2} + 1 + 4 - 15 =$

e. $8 \left[\overline{2 + 7 + (6 - \overline{4 - 8 \div 4})} + 2 \cdot 4 - \overline{1} \right] =$

f. $43 - 2 + 19 + 4 + \overline{16 - 4} + 9 - 5 - 13 + 2 =$

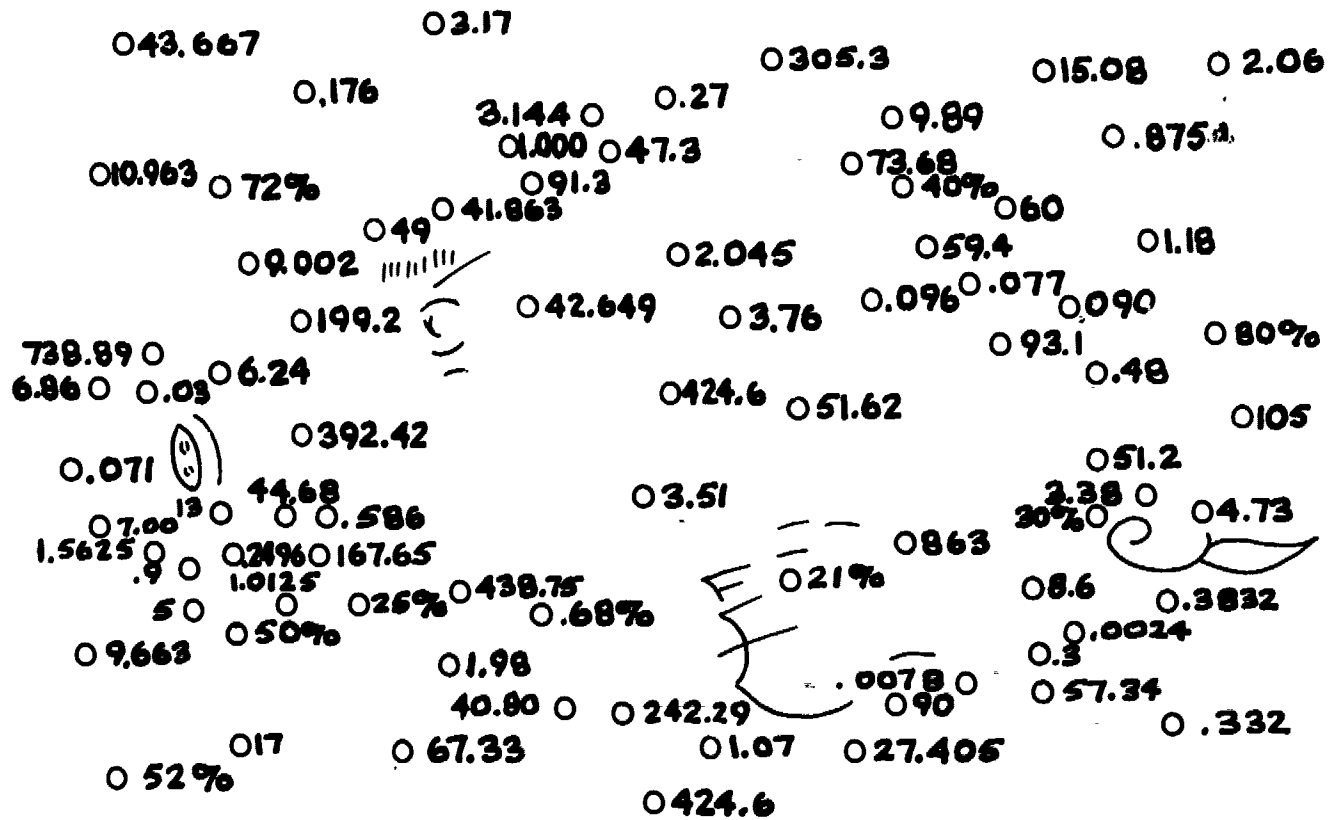
g. $3 - 2 + (8 - 2 + \overline{5 + 3 - 4 \cdot 2}) - 3 =$

h. $23 + 6 + 3 - (7 + 4) - 8 =$

Exercises

1. $2 + \boxed{3} - 2 \cdot 3 \div \boxed{6} - 1 =$
2. $20 - \boxed{8} + 3 \cdot \boxed{2} + 4 =$
3. $\boxed{30} \div (5 \cdot \boxed{2}) - 3 =$
4. $\boxed{(27 \div 9) + (27 + 9) \div 3} =$
5. $\boxed{(14 \cdot 2) + 5} \div 11 =$
6. $(3 \cdot 9) + \boxed{9 \cdot 3} + \boxed{2} =$
7. $11 + 2(6 + 4) - 3(1 + 3) =$
8. $16 - \{10 \div 2 + (6 - 4) - 5\} =$
9. $18 - (9 + \overline{4 - 3} + 2) =$
10. $9 + \{20 - \boxed{5} + \overline{3 - 1} + \boxed{8} + 3\} - 8 =$
11. $14 - 5 + \boxed{3 \cdot 18 \div 2 - (18 + 2 - 10) - 5 - 3} - 11 =$
12. $45 \cdot \overline{8 - 5} + \overline{3 \cdot 17} \div \overline{59 - 8} =$
13. $941 \cdot \boxed{14 \div 2 + 10 - 17} + 8 =$

Dot to Dot

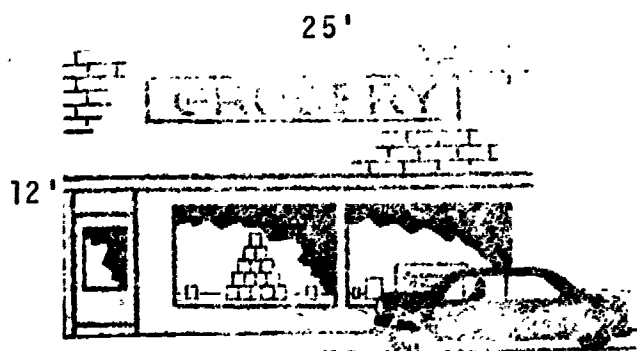


Complete the drawing by starting at the given answer and connecting in order the correct answers to the problems.

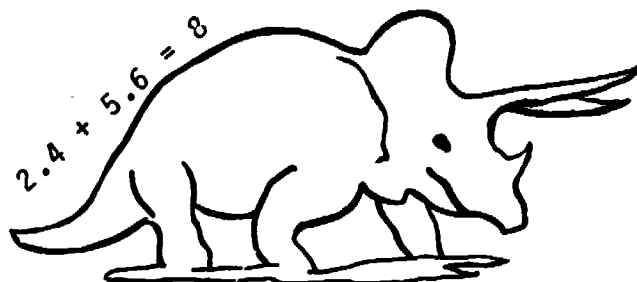
- | | | | |
|----|---------------------|----|--|
| 1 | $4:7 + .03 = 4.73$ | 24 | $3.25 \div .25 =$ |
| 2 | $5.78 - 2.4 =$ | 25 | $42.6 + 2.08 =$ |
| 3 | $6.4 \times 8 =$ | 26 | $71.42 = 321 =$ |
| 4 | $3.34 \div 3 =$ | 27 | $.68 - .094 =$ |
| 5 | $.084 + .006 =$ | 28 | $47.9 \times 3.5 =$ |
| 6 | $36 \div .6 =$ | 29 | $.52 \times .48 =$ |
| 7 | $7.82 + 2.07 =$ | 30 | $.81 \div .9 =$ |
| 8 | $67.3 + 238 =$ | 31 | $4\% \text{ of } 125 =$ |
| 9 | $9 \times .03 =$ | 32 | $32 \text{ is } \underline{\hspace{1cm}} \% \text{ of } 64$ |
| 10 | $112 - 64.7 =$ | 33 | $1\frac{1}{2}\% \text{ of } 67.50 =$ |
| 11 | $78.6 \times .04 =$ | 34 | $\underline{\hspace{1cm}} \% \text{ of } 84 \text{ is } 21$ |
| 12 | $2374 \div 26 =$ | 35 | $6\frac{1}{2}\% \text{ of } \$6,750 =$ |
| 13 | $.667 + .333 =$ | 36 | $\$3.40 \text{ is } \underline{\hspace{1cm}} \% \text{ of } \500 |
| 14 | $38.96 + 2.903 =$ | 37 | $\$680 \text{ } 6\% =$ |
| 15 | $784 \div 16 =$ | 38 | $238 + 4.29 =$ |
| 16 | $83 \times 2.4 =$ | 39 | $4.28 \div 4 =$ |
| 17 | $9.84 - 3.6 =$ | 40 | $6.09 \times 4.5 =$ |
| 18 | $2.97 \div 99 =$ | 41 | $72 \div .8 =$ |
| 19 | $6.49 + 732.4 =$ | 42 | $.007 + .0008 =$ |
| 20 | $7.83 - .97 =$ | 43 | $60.4 - 3.06 =$ |
| 21 | $.38 - .309 =$ | 44 | $.006 \div .02 =$ |
| 22 | $5.75 + 1.25 =$ | 45 | $.6 \times .004 =$ |
| 23 | $12.5 \div 8 =$ | 46 | $43 \times .2 =$ |
| | | 47 | $45 = \underline{\hspace{1cm}} \% \text{ of } 150$ |

For Fun

There are ten mathematical errors on this page. Find them.



300 sq. ft.



3 tons = 5000 lbs.

$$5/4 \cdot 1/12 = 15/4$$



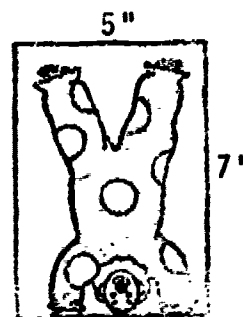
$$C = 2\pi R$$

$$1 \text{ ft. } 5 \text{ in.} = 17 \text{ in.}$$

$$3 \times 3 = 10$$



Length of bow = 2'



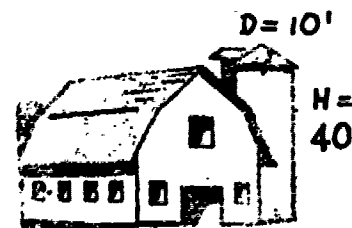
$$P = 2l + 2w$$

$$P = 25"$$

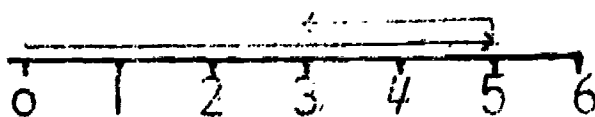
$$1/4 \div 1/3 = 1/12$$



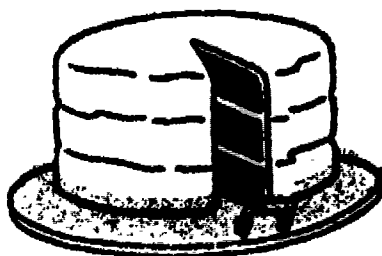
$$1 \text{ ft.} = 1/3 \text{ yd.}$$



Surface Area of Silo:
 $A = \pi R h$
 $R = 3.6 \times 10' \times 40$



$$5 - 2 =$$



$$1 - 1/8 = 7/8$$

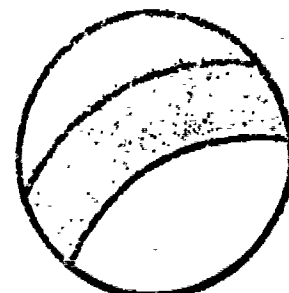
$$36.7$$

$$5.50$$

$$.784$$

$$\underline{6320}$$

$$7.526$$

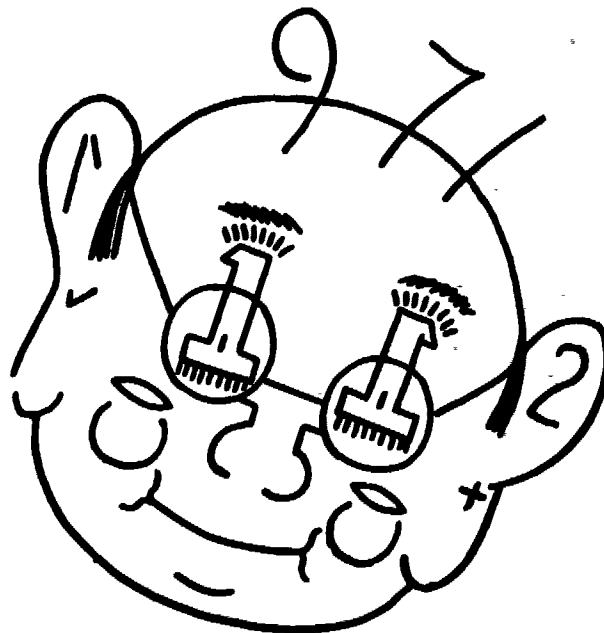


Area of Circle
 diameter = 8"
 $A = 50.24"$

The Pizza Party

1

2 Set had a party at the home of her parents, the 3 . When everyone arrived, she 4 them with math 5 . She didn't have a date for the party because she was batting 6 with her boy friend that week so she called him 7 . For dinner they had 8 ribs since it was a pizza party. All the glasses of Root Beer were full of Pepsi. The 9 party was bound to be a big success! The difference between the boys and girls could be determined by the 10 numbers and their 11 and everyone knew their 12 value, since there were only a few chairs.



The arrival of our instructor's wife, Eve Ann, with the professor himself, Mr. 13 , caused a moment of silence. Soon they were their old selves and the party went on. The professor and Eve Ann didn't 14 with any of the students because they were so involved

with the 15 _____ at the serving table. The 16 _____ of the front door allowed only a 17 _____ of the noise to escape to the adjacent 18 _____. Miss 19 _____ made her entrance with a musical 20 _____. She has had much experience because her parents are 21 _____ of snow business, but they are now divided.

End

Fill the blanks with words from this list. For instance, No. 4 blank would be filled with the word "renamed." Words may be used only once or not at all.

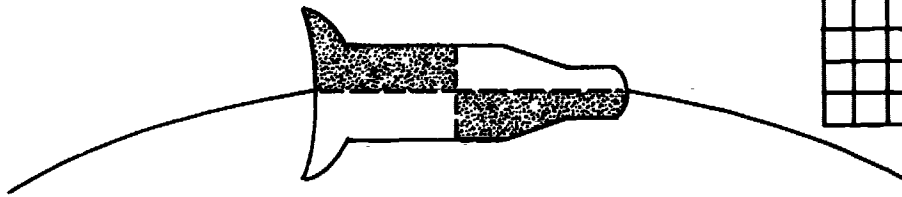
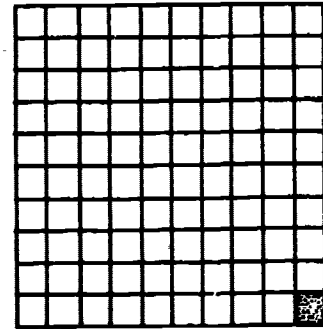
associate	counting	added	closure
distributive	fraction	end	integer
operations	identity	null	prime
opposites	divided	odd	start
products	renamed	place	square
property	symbols	sets	whole
		number	zero

UNIT VII

PERCENTAGE

%

is



A. Student Investigation

Approximately what per cent of the nose cone is shaded? Another way of asking the same question would be: If the nose cone is mentally separated into 100 equal parts, how many of these parts are shaded? One of these 100 parts is $1/100$ of the nose cone, or one per cent of it.

The symbol used for one per cent is %.

$1/100$ is the same as 1%

In the problem above, 100 equal parts would be hard to see! But it does appear that $1/2$ of the nose cone is shaded.

Since $1/2 = 1/2 \times 1 = 1/2 \times 50/50 = 50/100$ or $50 \times 1/100$, if 1% is substituted for $1/100$ the answer is 50%.

Examples:

Change the following to %:

1. $3/4 = 3/4 \times 1 = 3/4 \times 25/25 = 75/100 = 75 \times 1/100 = .75$

$.75 = 75/100 = 75 \times 1/100 = 75\%$

2. $.025 = 2.5 \times 1/100 = 2 \frac{1}{2}$ percent.

$$3. \quad \frac{1}{8} = .125 = \frac{125}{1000} = \frac{125}{10} \cdot \frac{1}{100} = 12.5 \times \frac{1}{100}$$

Therefore, $\frac{1}{8} = 12\frac{1}{2}$ per cent

Exercises

1. $\frac{1}{5} =$

2. $\frac{1}{2} =$

3. $.83 =$

4. $\frac{6}{10} =$

5. $.6 =$

6. $\frac{1}{20} =$

7. $.04 =$

8. $.004 =$

9. $\frac{1}{50} =$

10. $.75 =$

11. $.075 =$

12. $\frac{1}{12} =$

13. $\frac{17}{25} =$

14. $\frac{8}{20} =$

15. $.008 =$

Change these per cents to decimals and then to fractions.

16. 40% _____, _____

17. 75% _____, _____

18. 12.5% _____, _____

19. 9.8% _____, _____

20. .1% _____, _____

21. 5% _____, _____

Exercises

Find the per cent of each number.

1. 82% of 350 = _____
2. 6% of \$39 = _____
3. 75% of 2000 = _____
4. 50% of 366 = _____
5. 4.5% of 800 = _____
6. 180% of 350 = _____
7. 0.5% of 650 = _____
8. $12\frac{1}{2}\%$ of 1000 = _____
9. $33\frac{1}{3}\%$ of 99 = _____
10. $\frac{1}{4}\%$ of 100 = _____

Find the rate of per cent.

1. 16 is _____% of 24
2. \$.48 is _____% of \$3.20
3. 25 is _____% of 75
4. 9 is _____% of 4
5. 5 is _____% of 2
6. 50 is _____% of 200
7. 36 is _____% of 100
8. 2 is _____% of 1
9. 27 is _____% of 99
10. 0.54 is _____% of 9

Find the missing numbers.

1. 28% of _____ = 7
2. 9% of _____ = 72
3. 54 is 3.6% of _____
4. $2\frac{1}{4}\%$ of _____ = 81
5. 60% of _____ = 46.8
6. 26.3% of _____ = 18.41
7. 0.25% of _____ = 2.5
8. $\frac{1}{4}\%$ of _____ = 6.25
9. 0.25% of _____ = 6.25
10. 100% of _____ = 100

Exercises

Matching

<u> </u>	1. 25% of 95	a. 253.08	l. 12.215
<u> </u>	2. 37% of 147	b. 4195.8	m. 26308
<u> </u>	3. 82% of 1,125	c. 253.18	n. 543.9
<u> </u>	4. 74% of 342	d. 623.96	o. 23.75
<u> </u>	5. 44% of 749	e. 6239.6	p. 90.72
<u> </u>	6. 19% of 3,284	f. 2375	q. .9072
<u> </u>	7. 55% of 975	g. 922.50	r. 122.15
<u> </u>	8. 63% of 666	h. 54.39	s. 32956
<u> </u>	9. .7% of 1745	i. 92250	t. 536.25
<u> </u>	10. .09% of 1008	j. 53625	u. 329.56
		k. 419.58	v. 9.072

Find the per cents and totals

1. 9% of 658 =

2. 21% of 658 =

3. 58% of 658 =

4. 7% of 658 =

5. 5% of 658 =

Total

Total

Exercises

1. $181.47 =$ % of 789

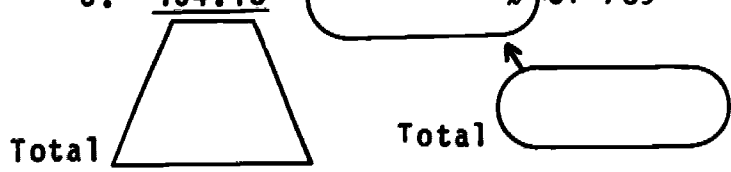
2. $47.34 =$ % of 789

3. $197.25 =$ % of 789

4. $86.79 =$ % of 789

5. $42.02 =$ % of 789

6. $\frac{134.13}{\text{trapezoid}} =$ % of 789



If 25% of 999 is 249.75, then 75% of 999 is 3(249.75) or 749.25.

Using this easy method, work these problems:

1. 33% of 100 is , thus 66% of 100 is

2. 56% of 88 is , thus 28% of 88 is

3. 40% of 95 is , thus 10% of 95 is

4. .6% of 125 is , thus 2.4% of 125 is

The Big Game

(Home) _____ has the ball on the 50 yd. line heading toward (visiting) _____'s goal.

You are the score keeper.

Here are your instructions:

- a. The answer to each problem tells you the yardage made each play. If answer is positive, yards gained; if answer is negative, yards lost.
- b. If answer is zero, there is a fumble and the other team recovers the ball.
- c. A team has four downs to make 10 yards.
- d. When a team makes enough yardage to reach the goal, they score. The other team gets the ball on the 50 yd. line.
- e. No extra points are scored.
- f. Use the chart on page 128 to keep up with the game.

1. $10626.0 \div 885.5 =$

2. $4427 \div -233 =$

3. $\frac{11}{4} \div \frac{22}{88} =$

4. 30% of 10 =

5. $7,956 - (15912 \times .5) =$

6. 20% of 25 =

7. $96714.7 \div 5689.1 =$

8. $\frac{5}{4} + \frac{7}{12} + 1 + \frac{1}{6} =$

9. $\frac{7}{16} - \frac{1}{2} + \frac{33}{16} =$

10. $119794.65 \div 7986.31 =$

11. $-7989.64 + 7969.64 =$

$$12. \frac{1}{3} \times \frac{1}{4} - \left(\frac{1}{6} + \frac{11}{12} \right) =$$

$$13. \left(\frac{117}{15} \div \frac{9}{25} \right) - \frac{80}{3} =$$

$$14. (28 \times .25) \times 5 =$$

$$15. \frac{23}{3} + \frac{68}{6} =$$

$$16. 4^2 =$$

$$17. .05 \times 700 =$$

$$18. 11 \times \boxed{} = 121$$

$$19. (50 \times 2) - (100 \div 4) + -70 =$$

$$20. \frac{1}{7} + \frac{1}{4} + \frac{-1}{14} + \frac{-1}{2} + \frac{33}{28} =$$

$$21. \frac{2}{12} + \frac{-12}{72} + -2 =$$

$$22. 100 = \boxed{}^2$$

$$23. 49 = 7 \times \boxed{}$$

$$24. 144 = 2 \times 2 \times 2 \times 2 \times 3 \times \boxed{}$$

$$25. 75 = 5 \times 3 \times \boxed{}$$

$$26. 50\% \text{ of } 4 =$$

$$27. (5\% \text{ of } 40) - (.5 \times 4) =$$

$$28. 34335444775 \div 512469325 =$$

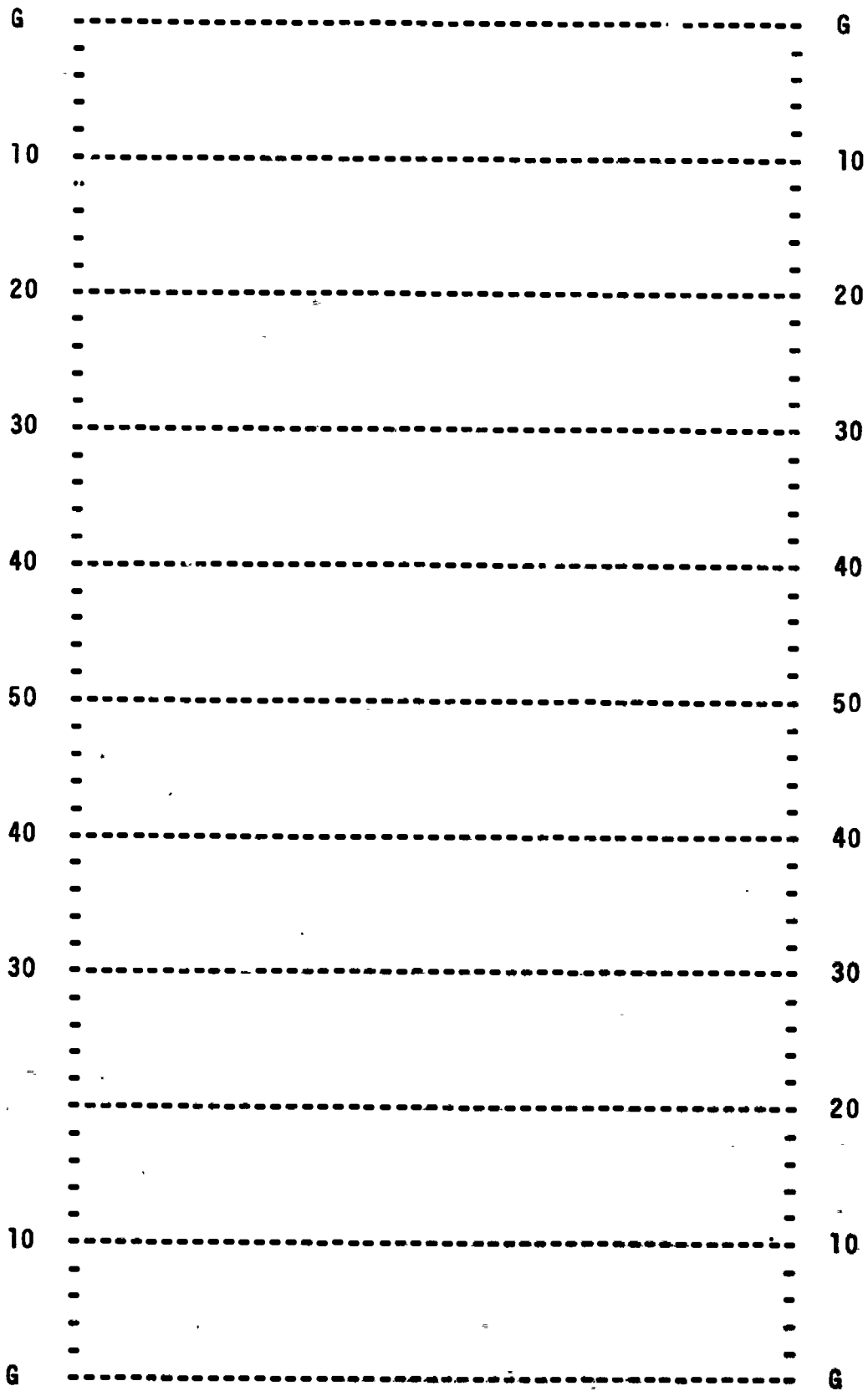
$$29. 2^4 =$$

What is the final score?

What is the total yardage gained by the home team? _____
by the visiting team? _____

What is the total yardage lost by the home team? _____
by the visiting team? _____

Home Team Goal



Visitors' Goal

B. Interest

$$I = P \times R \times T$$

^

Interest = Principal x Rate X Time

$$\frac{\text{Interest}}{\text{Principal} \times \text{time}} = \text{Rate}$$

$$\frac{\text{Interest}}{\text{Rate} \times \text{Principal}} = \text{Time}$$

$$\frac{\text{Interest}}{\text{Rate} \times \text{Time}} = \text{Principal}$$

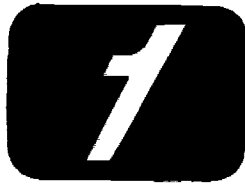
Note: Time in the formula $I = P \times R \times T$ is in years.

Exercises

Complete the picture on the following page by connecting the points which correspond to the answers of the problems below.

	Interest	Principal	Rate	Time
1.	\$ _____	\$25,000	5%	1 yr.
2.	_____	10,000	8%	2 yrs.
3.	_____	575	6%	5 yrs.
4.	_____	425	7%	90 days
5.	_____	750	5%	60 days
6.	_____	25,000	4½%	3 yrs.
7.	1218.56	3,808	____%	4 yrs.
8.	96.00	800	____%	2 yrs.
9.	126.00	600	____%	3 yrs.
10.	15.00	1,500	____%	45 days
11.	52.25	1,900	____%	180 days
12.	3.33	500	____%	30 days
13.	48.00	600	8%	____yr.
14.	360.00	2,000	6%	____yr.
15.	20.80	520	2%	____yr.
16.	8.00	400	8%	____days
17.	14.70	2,352	5%	____days
18.	38.25	7,650	6%	____days
19.	163.80	\$ _____	3%	3 yrs.
20.	12.00	_____	2%	2 yrs.
21.	19.80	_____	10%	1 yr.
22.	199.80	_____	5%	2 yrs.
23.	335.20	_____	8%	5 yrs.
24.	20.00	_____	4%	180 days

066 0789
 05.25 091
 01312 0500 0564
 03451 06 05000
 07 08
 03387 088 044.5
 08 03375
 0607 07.4 076
 05½ 055 06.25 011
 04151 010.101 08 07.44 091
 07911 01 0900 0172.50 01350
 0659 03 01600 0555
 04.994 044
 02 01250
 090 01000 0449
 031.99 0339
 045 0300 0938 0229
 01820 0192 0119
 02425 01998
 030 01998
 02324



SIMMONS FIRST NATIONAL BANK

Pine Bluff, Arkansas

In the following problems:
Use 360 days to find daily interest.
Find annual interest-rate.
Divide annual interest by 360 days
to find daily factor.
Daily factor should be carried to
thousandths.

For example:

$$\$10,000 \text{ at } 6\% = \$600$$

$$\$600 \div 360 = \$1.667 \text{ per day.}$$

1. LOAN OF \$15,000 at 6%.
 - a. WHAT IS AMOUNT OF ANNUAL INTEREST? _____
 - b. WHAT IS DAILY FACTOR? _____
 - c. WHAT IS AMOUNT OF INTEREST FOR 66 DAYS? _____
 - d. LOAN MADE JULY 1, 1971 DUE WHEN? _____

2. LOAN OF \$200,000 AT 5 3/4% FOR 90 DAYS.
 - a. WHAT IS AMOUNT OF ANNUAL INTEREST? _____
 - b. WHAT IS DAILY FACTOR? _____
 - c. WHAT IS THE AMOUNT OF INTEREST FOR 90 DAYS? _____
 - d. INTEREST WOULD BE _____ IF LOAN WAS \$200. _____
 - e. LOAN MADE SEPTEMBER 5, 1971 DUE WHEN? _____

C Commission

$$\text{Commission} = \text{Base} \times \text{Rate}$$



Example: John's paper route:

Papers sold = 65

Price of each paper = 15¢

Rate of commission = 30%

John's commission =

Exercises

1. Mr. Graves, insurance salesman:

Amount of Insurance sold: \$2500

Rate of Commission: 15%

Mr. Graves' Commission:

2. Don Jackson, appliance salesman in large department store:

Sold \$6,120 worth of appliances in one month:

Rate of Commission: 6%

Don's commission for that month:

3. John Greene: car salesman

Amount of sales - 1st week: \$2400

Amount of sales - 2nd week: \$ 900

Amount of sales - 3rd week: \$2550

Amount of sales - 4th week: \$2625

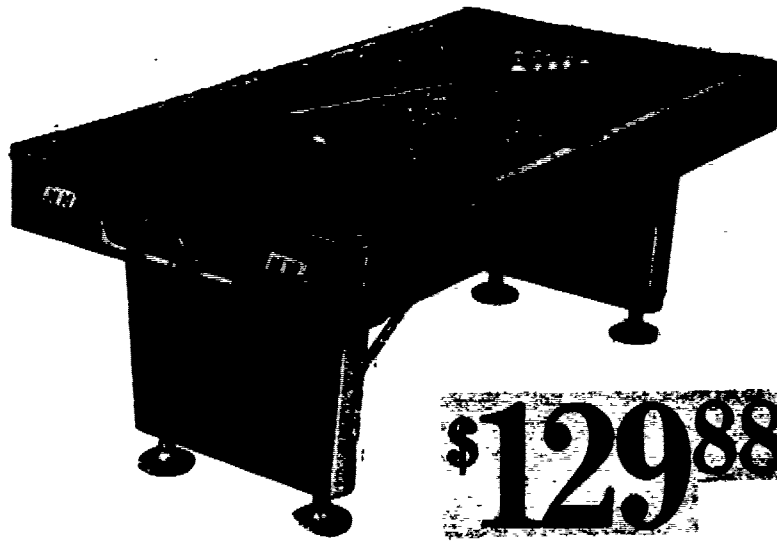
Rate of commission: 4%

Total sales:

Total amount of commission:

Practical Application

DEAR ANN LANDERS: I am a salesman in a large department store. Like most salesmen of major items (furniture, rugs, jewelry, refrigerators, stoves, etc.) I work on commission. Last week I spent the better part of two days with three couples. They asked dozens of questions, which I was happy to answer. That's what I'm here for. I gave them my card and said if they decided to buy I'd be happy to help them. At the end of the week I followed up by telephoning these couples and all three told me they had been in the store and bought the item from someone who just happened to be standing there. They all added, "You aren't on commission are you?"



\$439.88

This man worked for a 5% commission. If the three couples bought these three items, how much commission did he lose on each sale? What would have been his earnings if he had made the sales? Note: Each couple purchased only one item.

D. Discount

$$\text{Discount} = \text{Selling price} \times \text{Rate}$$

Example: Judy buys a sweater:

$$\text{Selling price} = \$8.95$$

$$\text{Rate of discount} = 20\%$$

$$\text{Amount of discount} = \boxed{\$1.79}$$

$$\text{Judy's Price} = \boxed{\$7.16}$$

Exercises

1. Phillip buys a 12 hp. boat motor:

$$\text{Selling price} = \$380.25$$

$$\text{Rate of discount} = 10\%$$

$$\text{Amount of discount} = \boxed{\$}$$

$$\text{Phillip's price} = \boxed{\$}$$

2. Jim is buying a new Plymouth V.I.P.

$$\text{Selling price} = \$4250$$

$$\text{Rate of discount} = 15\%$$

$$\text{Amount of discount} = \boxed{\$}$$

$$\text{Jim's price} = \boxed{\$}$$

3. Phyllis is buying ten 33 1/3 rpm stereo records.

$$\text{Selling price} = \$5.98 \text{ each}$$

$$\text{Rate of discount} = 30\%$$

$$\text{Amount of discount} = \boxed{\$}$$

$$\text{Phyllis' price} = \boxed{\$}$$

Exercises

	<u>Retail</u> <u>Price</u>	<u>Rate of</u> <u>Discount</u>	<u>Amount</u> <u>Discount</u>	<u>Sale</u> <u>Price</u>
1.	\$ 2,400	_____	_____	<u>\$1,920</u>
2.	\$ 18.75	_____	_____	<u>18.00</u>
3.	\$ 15.00	_____	_____	<u>11.25</u>
4.	\$100.00	_____	_____	<u>95.50</u>
5.	\$800.00	_____	_____	<u>768.00</u>
6.	\$ 1.44	_____	_____	<u>.84</u>
7.	\$ 16.00	_____	_____	<u>15.00</u>
8.	\$ 75.00	_____	_____	<u>70.00</u>
9.	\$ 32.00	_____	_____	<u>28.00</u>
10.	\$ 80.00	_____	_____	<u>68.00</u>
11.	\$175.00	_____	_____	<u>140.00</u>
12.	\$ 4.50	_____	_____	<u>4.00</u>

Exercises

	Retail Price	Rate of Discount	Amount of Discount	Sale Price
1.	\$.50	25%	_____	_____
2.	\$900.00	33%	_____	_____
3.	\$ 8.59	40%	_____	_____
4.	\$ 50.55	75%	_____	_____
5.	\$ 19.00	24%	_____	_____
6.	\$ 23.98	66%	_____	_____
7.	\$ 34.88	10%	_____	_____
8.	\$146.10	20%	_____	_____
9.	\$ 6.90	1/3 off	_____	_____
10.	\$198.88	30%	_____	_____
11.	\$ 12.95	1/4 off	_____	_____
12.	\$ 11.75	15%	_____	_____

Northside High School Athletic Department

North 23rd and B Streets

Fort Smith, Arkansas



COST OF SUITINGS:

	list price	team price
1 pair shoulder pads	\$24.50	\$16.95
1 helmet	33.50	24.95
1 pair football shoes	30.00	24.95
1 pair football pants	28.50	20.95
1 jersey	18.50	13.95
1 pair Grizzly Bear emblems	1.25	0.95
Total	_____	_____

Using list price and team price, figure the rate of discount and the amount of discount.

	Amount of Disc.		% of Discount
A.	_____	on shoulder pads	_____
B.	_____	helmet	_____
C.	_____	shoes	_____
D.	_____	pants	_____
E.	_____	jersey	_____
F.	_____	emblems	_____

Each year 32 boys are fitted with new equipment. Figure the cost at list price then at team price.

	List Price		Team Price
Shoulder Pads	_____	_____
Helmets	_____	_____
Shoes	_____	_____
Pants	_____	_____
Jerseys	_____	_____
Emblems	_____	_____

STERLING STORES COMPANY, INC

1. Fourth of July Sale

beach towels (were \$1.98) 40% off
stereo LP records (were \$3.89) 1/3 off
candy (was .79 per lb.) 25% off

Nancy bought	sale price	total price
2 beach towels	_____	_____
4 stereo LP records	_____	_____
3 lb. candy	_____	_____
	total	_____
	3% tax	_____
	total	_____

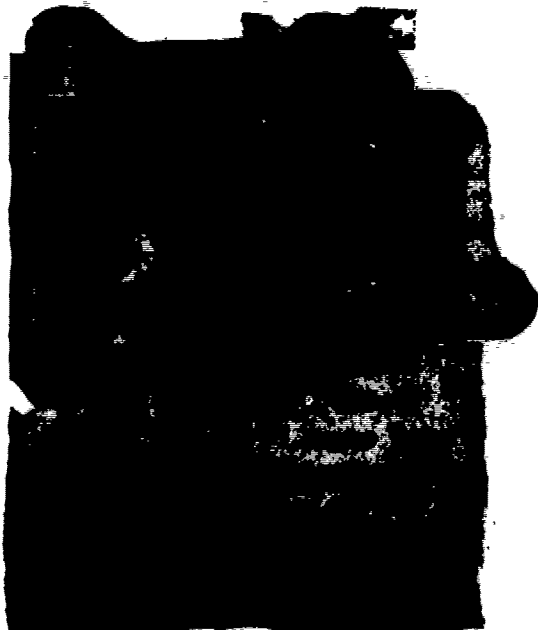
How much did Nancy save? _____

2. Joe Payne's Dance Contest

First Prize - Stereo Tape Cartridge
Player

How much was saved? _____

What was the rate of discount? _____



Exercises

1. List Price	Discounts	Net Price
a. \$75.00	20%, 12½%	_____
b. \$75.00	20% + 12½%	_____

Did you get the same result for both methods?

Note: In successive discounts the discount rates must not be added together.

2. List Price	Discounts	Net Price
a. \$18.50	10%, 5%	_____
b. \$923.00	30%, 25%, 15%	_____
c. \$40.16	50%, 20%, 10%	_____
d. \$27.60	33 1/3%, 25%	_____
e. \$117.00	20%, 15%, 5%	_____

3. A store offers a motor bike for \$450 less discounts of 20% and 10%. Another store offers the same bike at \$475 less 25% and 10% discounts.

Which one would you buy?

4. Which would you rather buy, a stereo priced at \$225.00 with discounts of 25%, 20%, 12½%, or the same stereo with a single discount of 50%?

Practical Application

DUE DATE

REMITTANCE ADVICE

25-10-2

DISCOUNT AMOUNT

Barton Lumber Company

CORNER HUNTINGTON & UNION • TELEPHONE WEBSTER 2-6675

Jonesboro, Arkansas

DATE	REFERENCE	CHARGES	CREDITS	BALANCE
	104 gal. BPS Housepaint	\$8.72/gal.	40¢/gal promotional discount	
	50 squares roofing	\$11.98/sq.	none	
	15 pc. 12' metal molding	44¢/lin. ft.	none	

Use the name of any building contractor in your town as the buyer. Assume you are the bookkeeper for the contractor. Find the balance after successive discounts for each item. What is the total amount of the order before sales tax is added?

E. Taxes

Exercises

1. Sales Tax - Arkansas 3%

Schedules: .00 - .14 no tax .15 - .44 1¢
 .45 - .74 2¢ .75 - 1.14 3¢

Purchase	Sales Tax
a. \$ 17.74	_____
b. \$ 33.95	_____
c. \$295.00	_____
d. \$ 8.98	_____
e. \$ 0.50	_____
f. \$ 0.88	_____
g. \$1487.98	_____
h. \$ 2.39	_____

2. School Millage (rate varies by school districts)

e.g. Jonesboro 49 mills Hope 40 mills
 Lepanto 45 mills Ft. Smith 49 mills
 Wynne 49 mills Little Rock 51 mills

49 mills = \$4.90 tax per \$100. assessed evaluation
 Arkansas Law: assessed value = 20% real value.

Assessed Evaluation	Millage	School Tax
a. \$650.	49	_____
b. \$85.	45	_____
c. \$1175.	40	_____
d. \$1720.	51	_____
e. \$210.	49.5	_____

3. Gas Tax-Federal: 4¢ gallon State: 7 1/2¢ gallon
 (Taxes included in pump price. No sales tax extra)

Purchase	Pump Price	Total	Federal Tax	State Tax
a. 14.3 gal.	30.9	_____	_____	_____
b. 5.0 gal.	32.9	_____	_____	_____
c. 19.7 gal.	32.9	_____	_____	_____
d. 11.4 gal.	34.9	_____	_____	_____
e. 16.5 gal.	31.9	_____	_____	_____

4. Cigarette Tax: Federal - 4¢ per pack
 Arkansas - 17 3/4¢ per pack

Carton Price: \$4.25 How much of this is tax? _____
 What is the price per pack? _____

5. Telephone Tax: Federal 10% State 3%
 (No state tax on out-of-state long distance calls)

a. Monthly rental (single line)	\$5.80
Long distance call to Little Rock	1.90
Long distance call to Memphis	.85
Long distance call to St. Louis	2.20
Long distance call to Dallas	4.65
Long distance call to Fayetteville	2.63

Sub Total _____
 Federal Tax _____
 State Tax _____
 Total _____

b. What would be the amount of the statement if no long distance calls were made?

6. Personal Property and Real Property Tax.

	Mills on assessed value	
School Tax	49	}
County Tax	5	
County Library Tax	1	
County Road Tax	3	
County Hospital Tax	4.2	
Courthouse Bonds	.8	}
City Tax	5	
Firemen's Pension	.25	
Police	1	}

Arkansas Law: assessed value = 20% real value

Jim owns:	a. In city:		b. Outside city:
	Home	\$11,500 Value	40 acre farm
	Furniture	5,000 Value	
	Car	2,225 Value	\$8,500 Value
	Total	_____	Assessed
	Assessed Value	_____	Value _____

- c. What is the total assessed value? _____
- d. What is the city tax rate? _____
- e. What is the farm tax rate? _____
- f. What is the total city taxes? _____
- g. What is the total farm taxes? _____
- h. What were the total taxes paid? _____
- i. How much did Jim pay in school taxes? _____
- j. How much did Jim pay to support the county library? _____
- k. How much did he pay to support the city administration? _____

Practical Application

Cooksey's Flower Shop

FOR FINER FLOWERS
1006 FLOWERLAND DR P. O. DRAWER 1387 PH 932-6973
JONESBORO, ARKANSAS 72401



Date _____ 19 ____

Sold To _____

A. M.	P. M.	CHARGE	C. O. D.	CASH	TEL. DEL.
DESCRIPTION					

Card _____

Deliver to _____

4090

Rec'd by _____

MASTER PRINTING COMPANY, JONESBORO, ARK

0-60884-8

Mrs. A. A. Rudd bought a container for \$5.98, 6 chiffon roses at 65 cents each, 3 pineapple blossoms at 65 cents each, and 1 can of spray paint for \$1.15. What was her total bill including tax? Write the sales ticket.

F. Mark-Up

$$\text{Mark-Up} = \text{Selling Price} - \text{Cost}$$

$$\% \text{ Mark-up (Based on cost)} = \frac{\text{Amount of mark-up}}{\text{Cost}} \quad \text{Change to \%}$$

$$\% \text{ Mark-up (Based on selling price)} = \frac{\text{Amount of mark-up}}{\text{Selling Price}} \quad \text{Change to \%}$$

Example: Pork & Beans:

$$\text{Selling Price} = 15\text{¢}$$

$$\text{Cost per can} = 11\text{¢}$$

$$\text{Mark-up} = 4\text{¢}$$

$$\% \text{ mark-up on selling price} = 26.7\%$$

$$\% \text{ mark-up on cost} = 36.4\%$$

Exercises

1. A grocer buys butter at 62¢ a pound and sells it at 73¢ a pound.
 - a. Find the mark-up.
 - b. What percent of cost is the mark-up?
 - c. What percent of the selling price is the mark-up?
2. Copy and complete the table, then find the percent of mark-up on the selling price and cost.

	Cost	Selling Price	Mark-up (Margin)	%mark-up on Selling Price	%mark-up on Cost
a.	\$.45	\$.60	_____	_____	_____
b.	\$.84	\$ 1.05	_____	_____	_____
c.	\$ 2.50	\$ 2.75	_____	_____	_____
d.	\$ 3.75	\$ 4.50	_____	_____	_____
e.	\$20.00	\$23.00	_____	_____	_____

G. Per Cent Increase or Decrease

Exercises

$$\% \text{ of Increase} = \frac{\text{Amount of Increase}}{\text{Original}}$$

Change answers to per cents:

1. Mrs. Riddle buys an air conditioner this year:

Price last year = \$300

Price this year = \$400

Amount of increase =

Per cent of increase =

$$\% \text{ of Decrease} = \frac{\text{Amount of Decrease}}{\text{Original}}$$

2. Mary goes to buy gasoline:

Original price 41.9¢ per gallon

Present price 32.9¢ per gallon

Amount of decrease =

Per cent of decrease =

3. Color TV

Price last year =
Price this year = \$475
Amount of decrease = \$145
Per cent of decrease =

4. Belinda Adams: Secretary

Salary last year = \$3,400
Salary this year = \$3,900
Amount of increase =
Per cent of increase =

5. Short Cut Check

Checking multiplication by casting out 9's
Check problems "b" and "c" as "a" is checked.

$$\begin{array}{r} \text{a. } 235 \\ \quad 66 \\ \hline 1410 \\ \quad 1410 \\ \hline 15510 \end{array} \quad \begin{array}{l} 1 \\ \times 3 \\ \hline 3 \end{array}$$

$$\begin{array}{r} \text{b. } 621 \\ \quad 237 \\ \hline \end{array}$$

$$\begin{array}{r} \text{c. } 725 \\ \quad 527 \\ \hline \end{array}$$

(Please Print)

RETAIL INSTALLMENT CONTRACT

ADDRESS Name _____
 OF Address _____
 BUYER City _____ State _____ Zip _____
 Tel. No. _____
 Tel. No. _____
 Home _____
 Bus. _____
 Account No. _____

Undersigned Seller sells and undersigned Buyer (if more than one, jointly and severally) purchases, subject to the terms and conditions as set forth on both sides hereof the Merchandise described below, to be kept at the above address. Buyer acknowledges that Seller has offered to sell the below described Merchandise for the cash sale price indicated but Buyer has elected to purchase on the terms and upon the conditions of this agreement. Seller hereby acquires a purchase money security interest in the Merchandise sold hereunder in accordance with the Uniform Commercial Code to secure the Buyer's payment of the Total of Payments and other charges if applicable, pursuant to this agreement.

Buyer agrees to pay the Total of Payments in _____ consecutive monthly installments beginning one month from the date of execution hereof unless a different first payment date is inserted at this point.

Each installment shall be in the amount of \$ _____ EXCEPT the final installment which shall be \$ _____

payments to be made at the place designated by Seller or his assignee.

FINANCE CHARGE begins to accrue upon the date of this agreement or upon a later date if such date is inserted hereafter.

Merchandise in which Security Interest is provided	New or Used	Model	Serial No.	Price
GE Air Conditioner	N	423	TJ 012066	389.95
			Tax	
			Total	

1. Cash Price _____
 Cash Down Payment _____
 Trade-in (Described below) _____
 2. Total Down Payment _____
 3. Unpaid Balance of Cash Price _____
 4. Other Charges _____
 a. Insurance (For term of this contract) _____
 *Life _____
 *Acc. And Health _____
 Property _____
 b. Official Fees/ Filing Ins. Premium \$ 2.00
 Total Other Charges _____
 5. Amount Financed (3 plus 4) _____
 6. FINANCE CHARGE _____
 7. Total of Payments (5 plus 6) _____
 8. Deferred Payment Price (Sum of 1, 4 & 8) _____
 ANNUAL PERCENTAGE RATE 10 %

*Name of Buyer Proposed for Insurance _____

Complete only if such person is less than age 65 on date of this contract and a charge for life insurance and accident and health insurance is included. If Buyer is a corporation, no charge for any insurance should be included. See Notice of Proposed Group Insurance on the reverse side hereof.

Buyer acknowledges and confirms, with respect to ANY insurance purchased hereunder and for which the cost thereof is set forth under item 4a above, that, at the purchase of such insurance is voluntary and not required by the Seller in the extension of credit; b) Buyer's decision to purchase such insurance was made after disclosure to him of the costs thereof, which are Life \$ _____, Accident and Health \$ _____, and c) Buyer was provided with the opportunity to obtain property insurance from or through another person of his own choice other than the Seller.

Signature of Buyer _____

Date _____

Time is of the essence hereof. In addition to the regular installment, Buyer agrees to pay as a delinquency and collection charge on each installment in default for 10 days or more, 5% of each such installment or \$5 whichever is less. Buyer also agrees, if this contract is referred to an attorney to effect collection, to pay court costs plus reasonable attorneys' fees incurred.

Should balance be prepaid in full prior to maturity date, a refund of the unearned portion of the FINANCE CHARGE will be calculated using the Rule of 78 after deduction of a \$25 acquisition charge, except in Arkansas where no such charge is permitted.

Accepted: The foregoing contract is hereby assigned under the terms of the assignment on the reverse side.

Receipt of an executed copy of this RETAIL INSTALLMENT CONTRACT is hereby acknowledged.

DEALER SIGN HERE _____ LANDERS' APPLIANCE CENTER (SELLER) (L.S.) Date _____
 BUYER SIGN HERE _____ Signed _____ (BUYER) (L.S.) Date _____
 By _____ (AUTHORIZED REPRESENTATIVE - TITLE) Date _____
 Seller's Address _____
 Witness _____

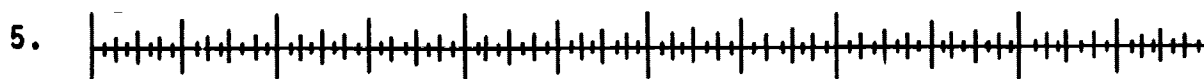
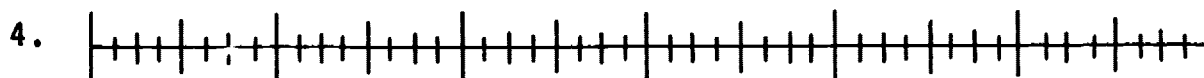
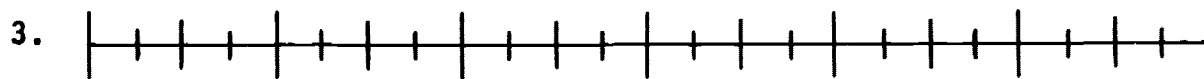
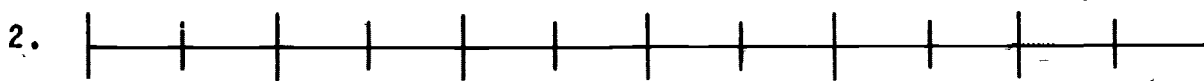
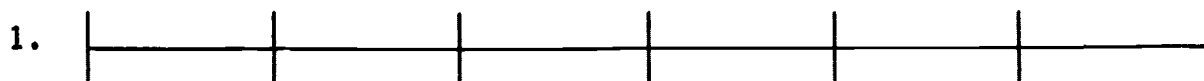
Judy, will you complete this contract for me. He has no trade-in and wants to pay \$51.65 down and the balance in 30 months. I have already figured insurance and finance charges from the charts.

UNIT VIII
MEASUREMENT

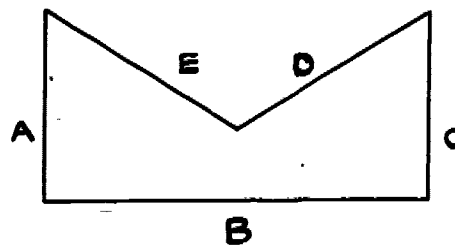
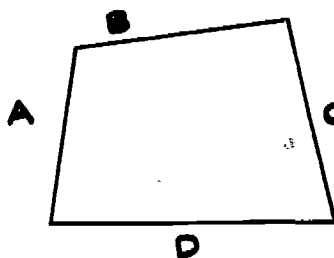
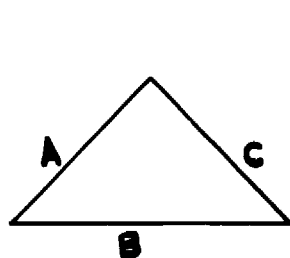
A. Linear Measurement

Exercises

Label the points on these rulers:



6. Find the length of each side and the total distance around each figure.



Exercises

1. How many $\frac{1}{2}$ inches are in:

a. 1" _____ b. 2" _____

2. How many $\frac{1}{8}$ inches are in:

a. 1" _____ b. $\frac{1}{2}$ " _____

3. How many $\frac{1}{16}$ inches are in:

a. $\frac{1}{8}$ " _____ b. $\frac{1}{4}$ " _____

c. $\frac{1}{2}$ " _____ d. 1" _____

4. How many $\frac{1}{4}$ inches are in:

a. 2" _____ b. $\frac{3}{4}$ " _____

c. 1" _____ d. $\frac{1}{2}$ " _____

5. Locate the following points on ruler.

a. $2\frac{1}{2}$ " b. $4\frac{1}{16}$ " c. $2\frac{3}{4}$ "

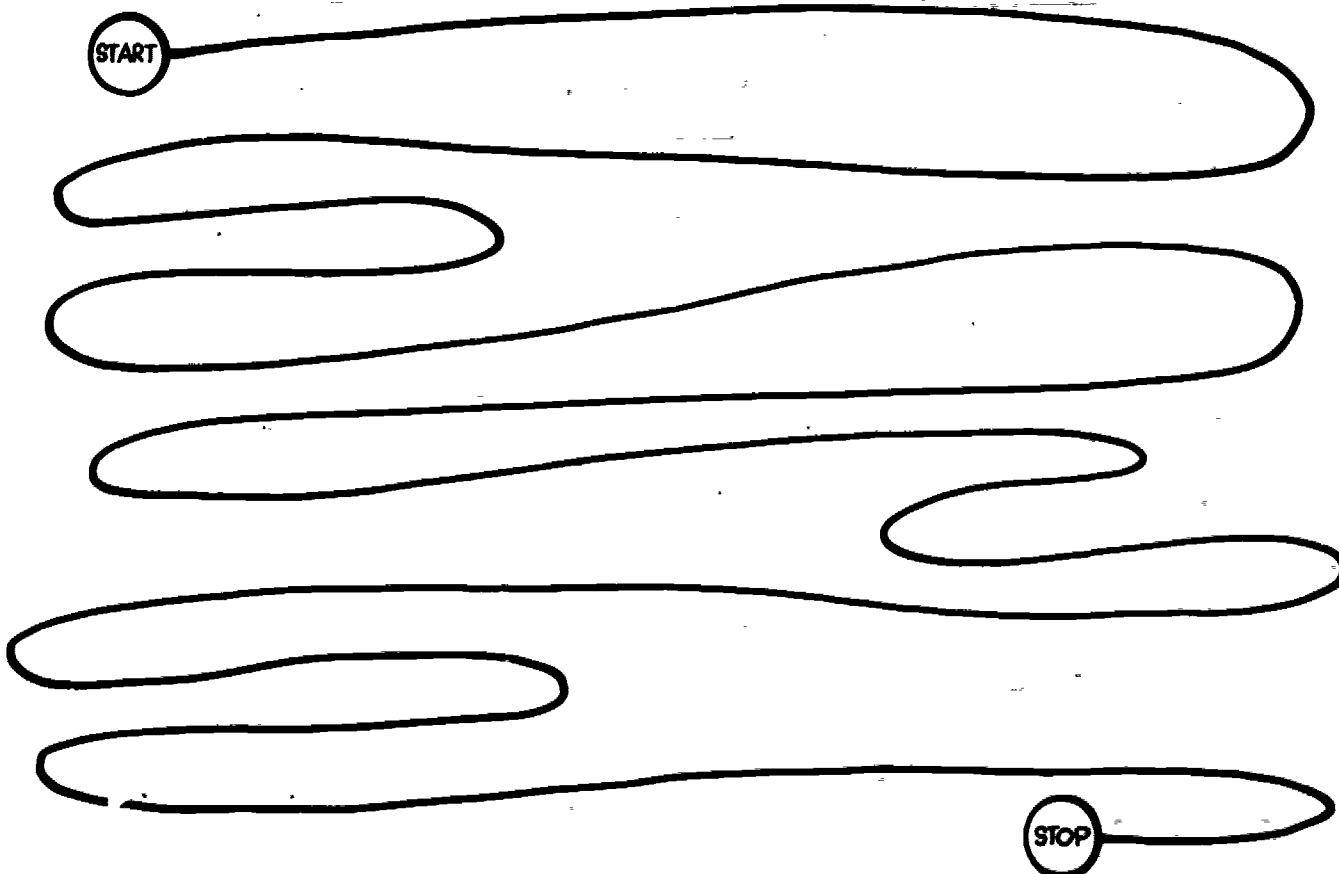
d. $3\frac{9}{16}$ " e. $3\frac{3}{8}$ " f. $5\frac{7}{16}$ "

g. $5\frac{3}{4}$ " h. $\frac{7}{8}$ " i. $4\frac{15}{16}$ "

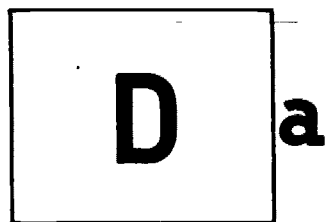
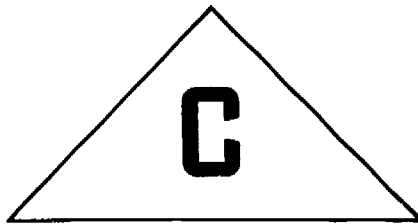
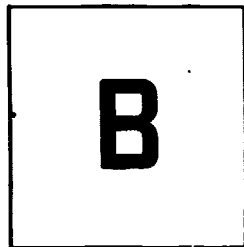
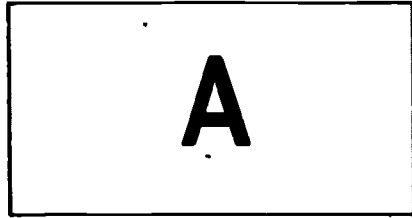
STERLING STORES COMPANY, INC.

1. One of the most common problems in this store is figuring fractions when a product is measured in yards.
 - a. A customer buys $1 \frac{3}{4}$ yds. of lace at 29¢ a yard. Find the price. _____
 - b. Another problem is that in our candy department a customer will ask for 25¢ worth of candy that sells for 80¢ per pound. How many ounces will the customer get? _____
2.
 - a. Make a guess in inches. The length from start to stop is _____.
 - b. Now measure in inches! The length from start to stop is _____.
 - c. What is the amount of error? _____

$$\text{per cent of error} = \frac{\text{amount of error}}{\text{distance measured}}$$



Exercises



1. Figure A is a swimming pool:
Width: 40'
Length: 90'
If you swim around the pool,
how far do you swim? _____
2. Figure B is a _____.
Describe it. Measure the sides.
The perimeter of a figure like
B is 144 ft. Each side has a
length of _____.
3. Figure C is a _____.
Describe it. Measure its sides.
The perimeter of a figure like C
is 135 ft. The length of the
sides could be _____.
4. Figure D is a _____. How
would you describe it? Measure
all four sides. The perimeter of
a like figure is 140 ft. Side a
is 20 ft. long. Can you find the
lengths of the other three sides?

Exercises

1.	<u>C</u>		<u>D</u>		<u>π (approx.)</u>
	31.4 in.	-----	10 in.	-----	3.14
	131.88 in.	-----	<input type="text"/>	-----	3.14
	<input type="text"/>	-----	28 ft.	-----	<input type="text"/>

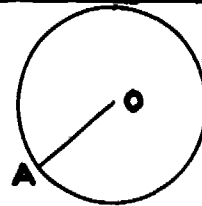
2. What is another way of finding the circumference of a circle other than measuring? Explain. Using c to represent circumference, D for diameter and 3.14 for π write the rule for the circumference of a circle.

Rule 1.

3. Use this rule to find the circumference of each circle with the given diameter.

- | | | | |
|----|----------|--------------|-------|
| a. | Diameter | 8 inches | _____ |
| b. | Diameter | 63 miles | _____ |
| c. | Diameter | 8 3/4 inches | _____ |
| d. | Diameter | 2.5 yards | _____ |

4. a. Measure diameter in inches. _____
 b. Measure A to O . _____
 c. How does this last length compare to the length of the diameter? _____
 d. What is the length from O to A called? _____
 e. Restate the rule above using R for the length of OA .



Rule 2.

5. Use Rule 2 to find the circumference of each circle with the radius given.

- | | | | |
|----|--------|-----------------|-------|
| a. | Radius | 9 feet | _____ |
| b. | Radius | 14 inches | _____ |
| c. | Radius | 3.75 miles | _____ |
| d. | Radius | 2 1/3 yards | _____ |
| e. | Radius | 2 feet 4 inches | _____ |

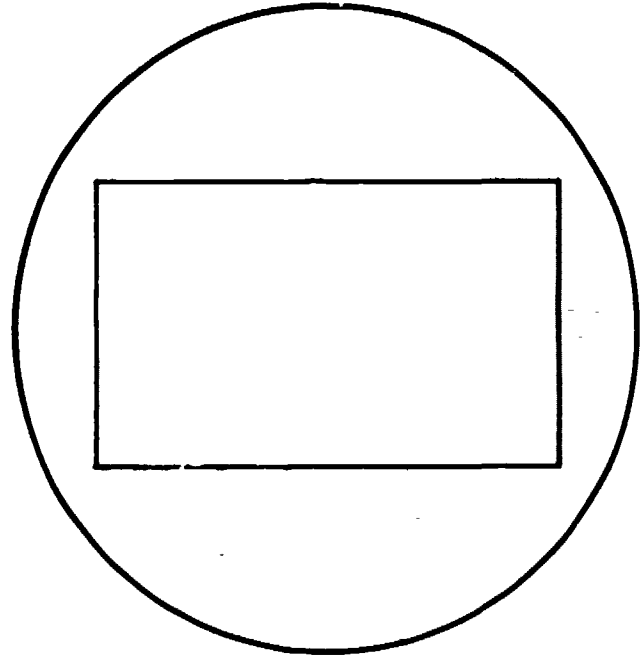
6. What distance in feet does the tip of a propeller travel in one revolution if its length (diameter) is 7 feet? _____

7. The circumference of a tree is 5 feet 6 inches. What is the diameter of the tree? _____

Azalea



————— Practical Application —————



A beautification committee wants to build a circular flower bed with a frog pond in the middle of the bed. The circular bed is to have a 10' radius. The rectangular pond is to be 3' by 5'. They will plant azaleas on the circle 1' apart and around the pond they will plant sedum every 8". What will be the cost of the plants?

Optional:

How much would it cost to plant grass in the space between the two flower beds?

One bag of sprigs cost \$2.25 and plants 300 Sq. ft. with rows 12" apart and sprigs 6" apart in the row.

SEDUM



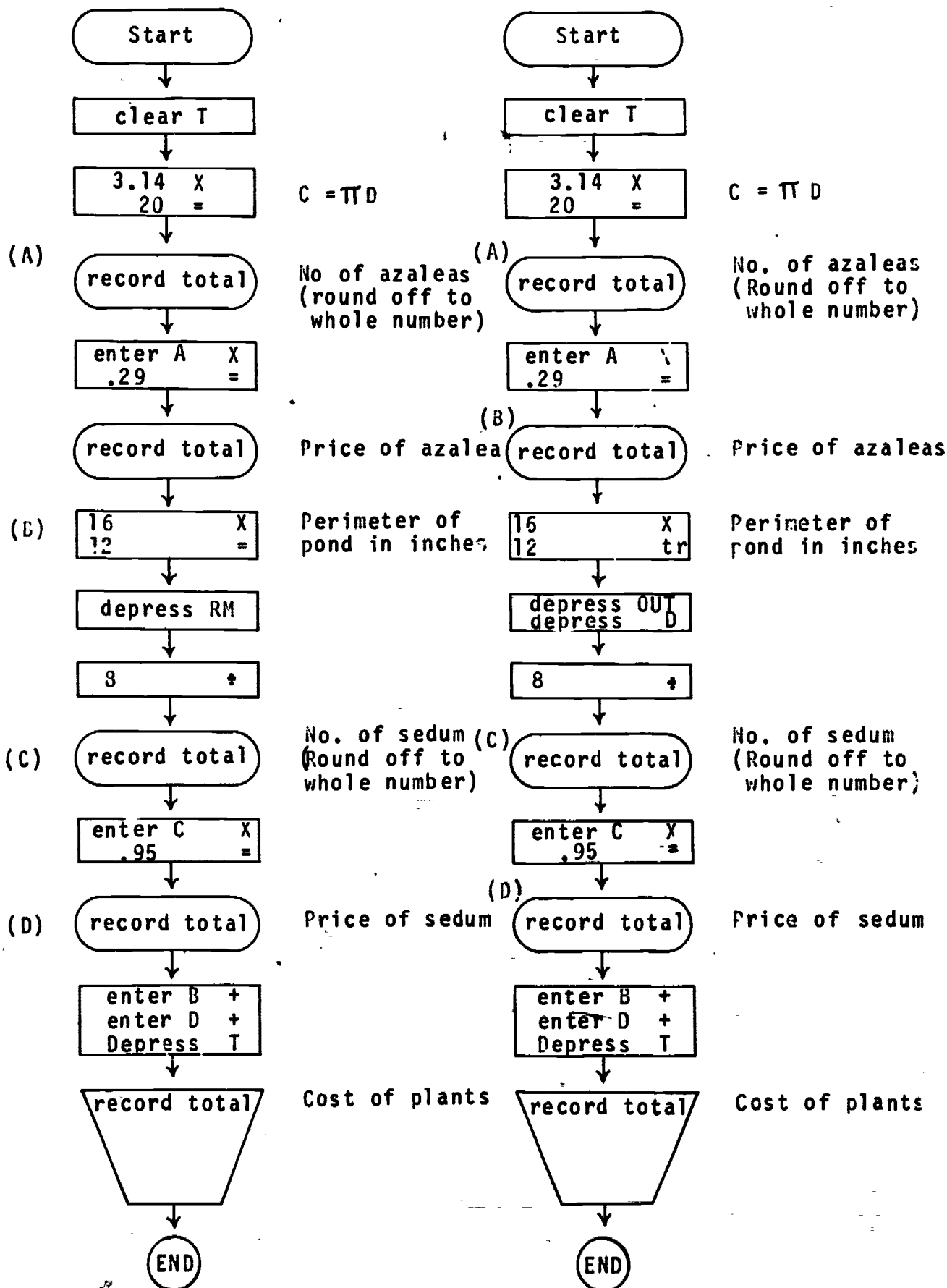
Sedum, Autumn Joy, above

Select Plants, Each 95c,

FLOW CHARTS FOR AZALEAS

(For Totalia Calculator)

(For Olivetti Calculator)



SUNRAY D. X. OIL CO.

Example: What size sheave should be placed on a motor which runs @225 R.P.M. in order to drive a 24" sheave @160 R.P.M.?

$$\text{P.D. of Eng. Sheave} = \frac{\text{Sheave Dia} \times \text{RPM}}{\text{Engine RPM}} = \frac{24 \times 160}{225}$$

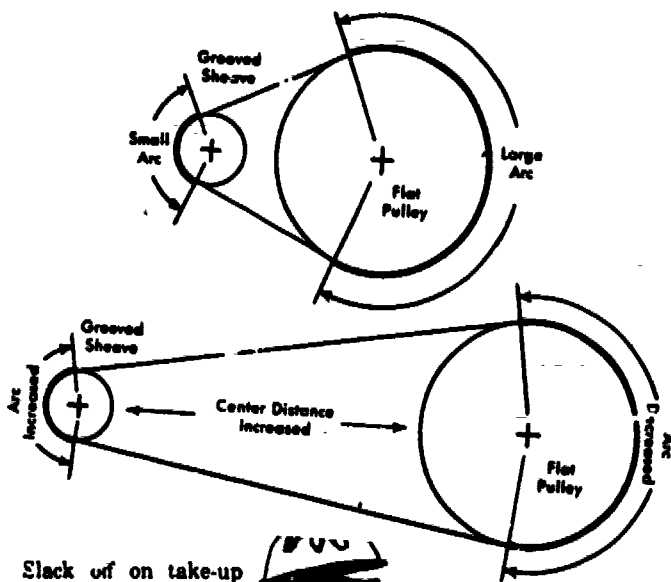
$$\frac{3840}{225} = 17"$$

Problem: What size sheave should be placed on a motor which runs @325 R.P.M. in order to drive a 24" sheave @180 R.P.M.?

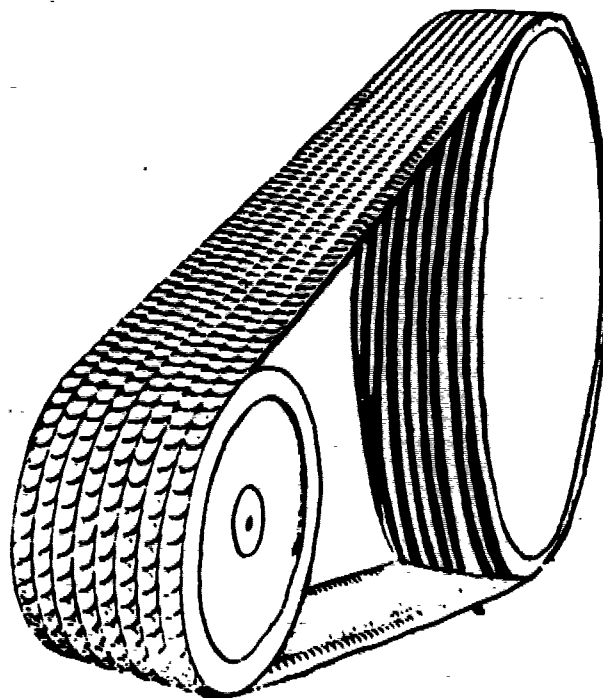
Example: Find approximate belt length needed where the diameter of the big sheave is 40", the diameter of a small sheave is 15", and the center distance between sheaves is 72".

$$BL = (D + d) \times 1.57 + 2C = 55 \times 1.57 + 2(72") = 230.35"$$

Problem: Find approximate belt length needed where diameter of big sheave is 60", diameter of small sheave is 20", and center distance between sheaves is 84".



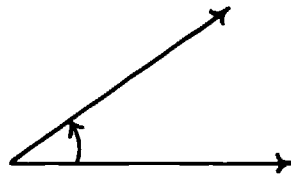
Slack off on take-up until belts can be placed in grooves without forcing.



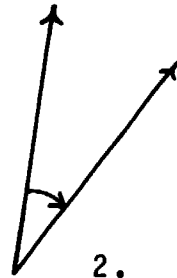
8. Angle Measurement

Exercises

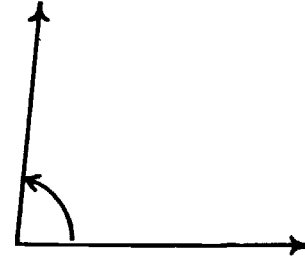
Use your protractor to measure these angles.



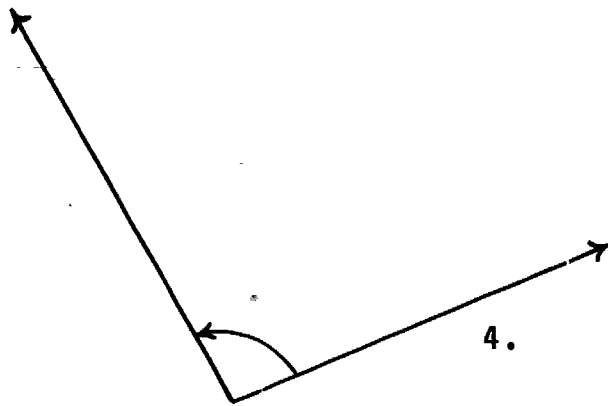
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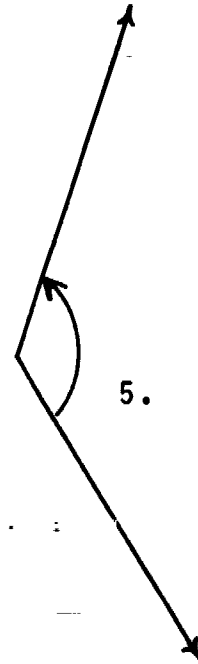
2.



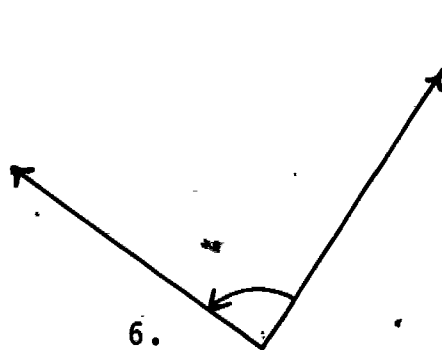
3.



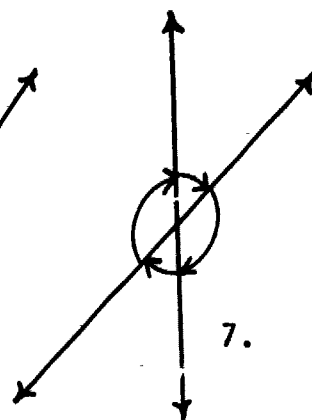
4.



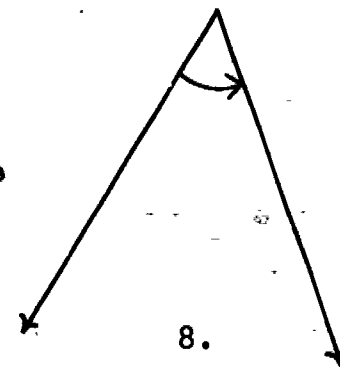
5.



6.



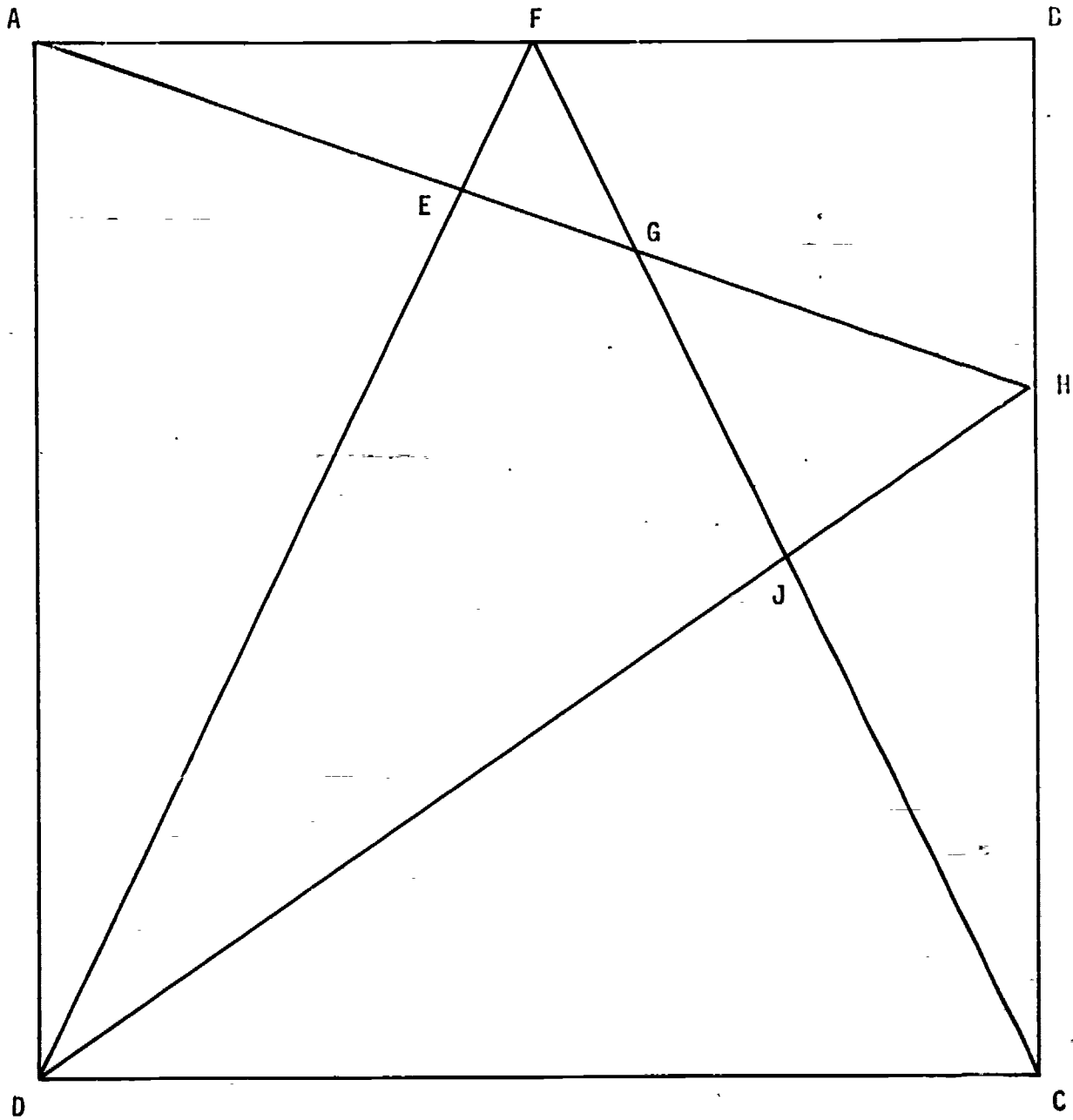
7.



8.

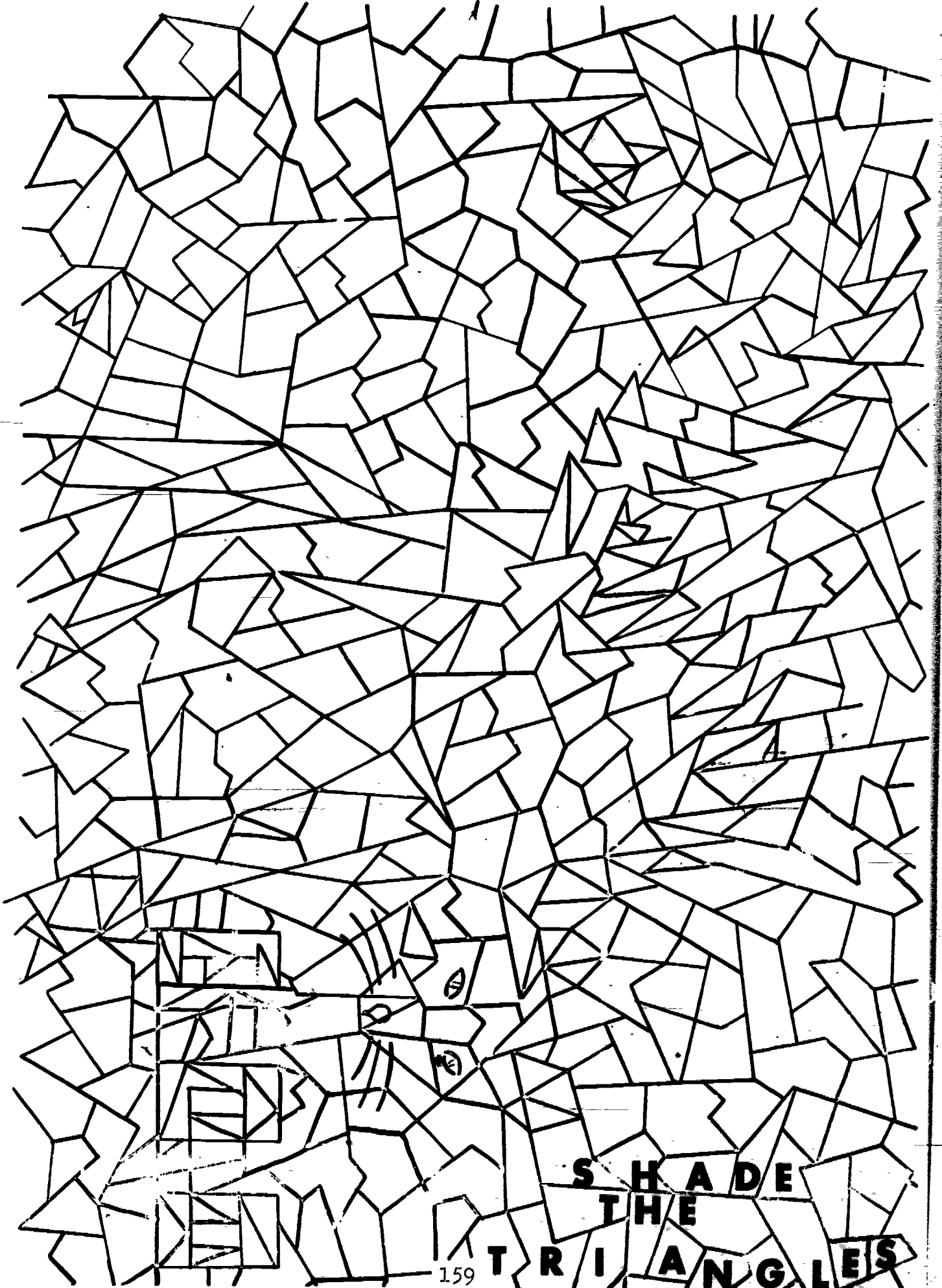
9. What is the sum of the angles in problem 7?

A Square Filled With Triangles



1. List the triangles in this figure. _____
2. The perimeter of triangle DFC is
3. The perimeter of triangle EFG is

The Mad Cat



SHADE
THE
TRIANGLES

C. Ratio:

Exercises

1. Compare the following quantities by division. Be sure the numbers are in the same units.

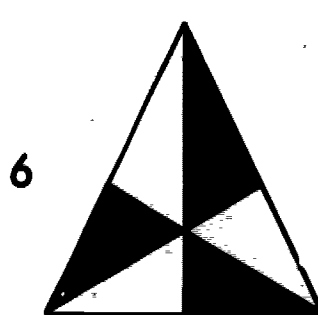
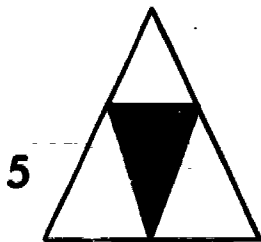
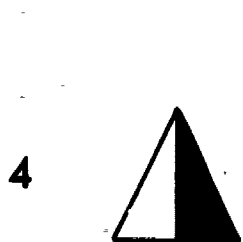
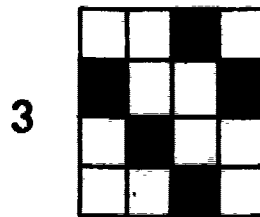
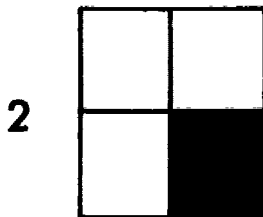
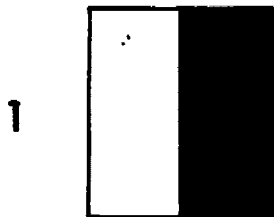
- | | |
|------------------------|------------------------|
| a. 5 inches, 30 inches | b. 54 apples, 3 apples |
| c. 18 feet, 12 feet | d. 10 cars, 90 cars |
| e. 4 minutes, 4 hours | f. 3 days, 3 weeks |
| g. 9 inches, 9 feet | h. 600 lb., 2 tons |
| i. 220 ft., 1 mile | j. 4 weeks, 1 year |

2. Find the quotient of the vertical pairs of numbers in each table. Can you complete each table?

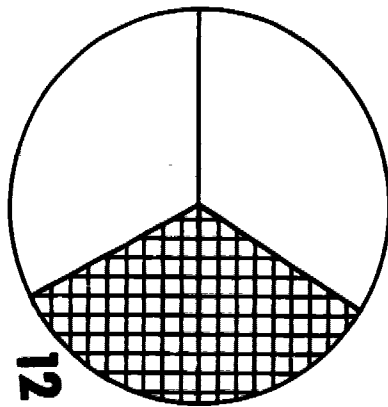
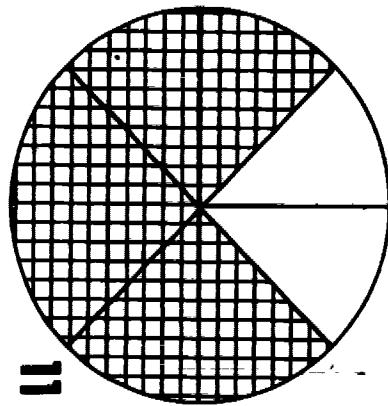
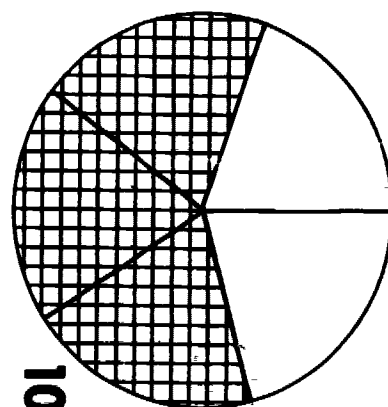
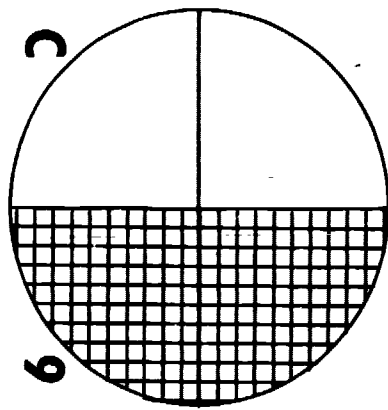
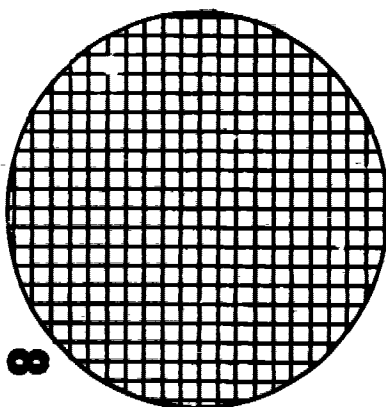
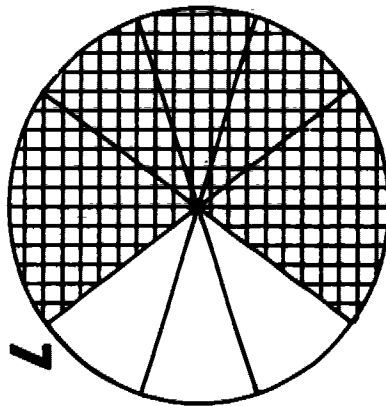
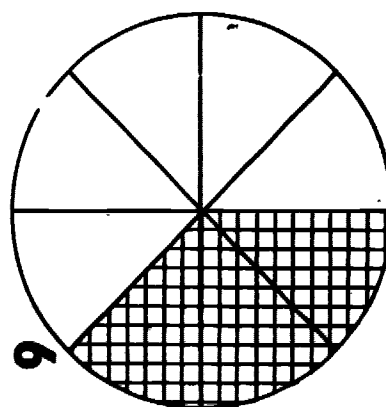
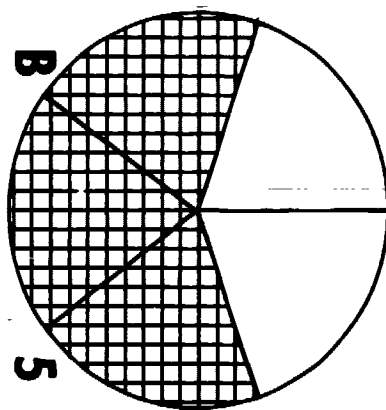
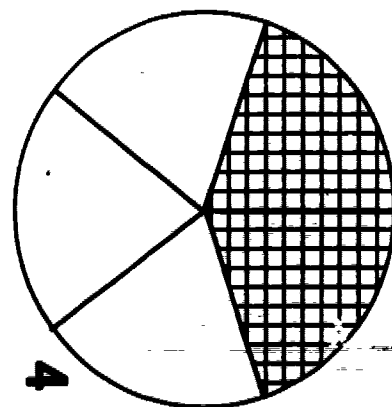
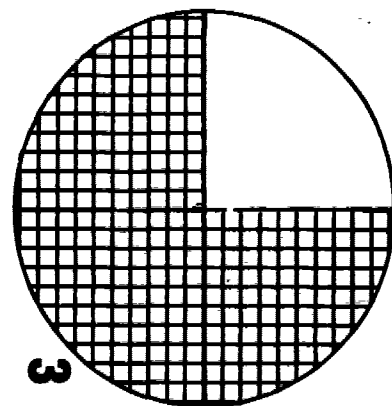
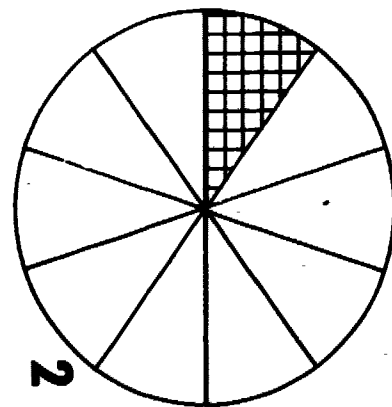
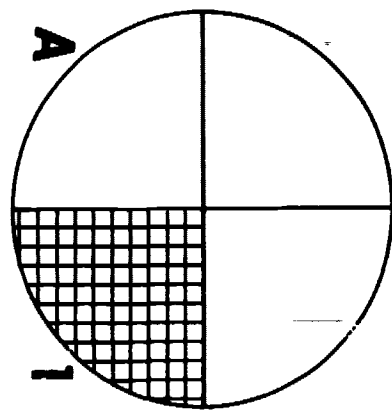
9	27	42	66		99
3	9	14		25	

12	30	48	72		132
10	25	40		85	

3. A bag contained 6 red marbles, 7 white marbles and 10 green marbles.
- Compare the number of red marbles to the green marbles.
 - Compare the number of green marbles to the white marbles.
 - Compare the number of white marbles with the contents of the bag.
 - What part of the bag's contents are not red?
 - Compare the number of marbles that are not red to those that are red.
4. For each figure compare by division:
- Number of shaded parts to unshaded.
 - Number of unshaded parts to shaded.
 - Number of shaded parts to total number of parts.
 - Number of unshaded parts to total number.



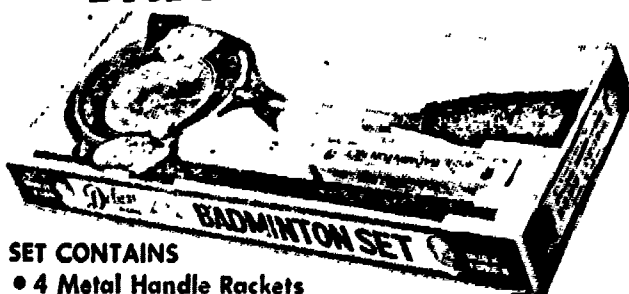
Ratio Practice



Practical Application

4 PLAYER

BADMINTON SET



SET CONTAINS

- 4 Metal Handle Rackets
- 4 SHUTTLE COCKS
- 1 NET
- 1 METAL POLE SET
- 1 RULE BOOK

REG.
\$6.88

NOW
ONLY!

\$4⁸⁸

THERMOTOTE

INSULATED BAG

PERFECT FOR PICNICS AND OTHER
OUTINGS

4 1/4" x 6" x 9"

REG. \$1.29

NOW ONLY!



88^c

1. Find the ratio of the sale price to the regular price.
2. Find the ratio of the savings to the regular price. What is the per cent of discount?
3. How much is saved if you buy one of each article on this page?
4. What is the best buy on this page?

D. Proportions

1. Complete these proportions:

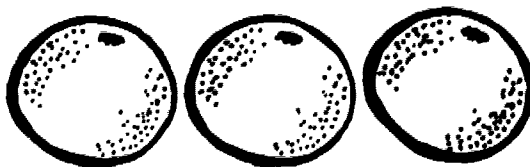
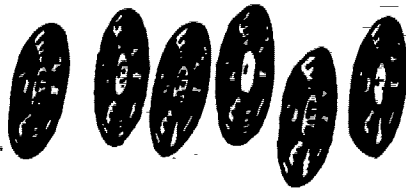
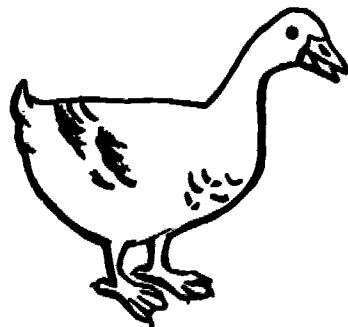
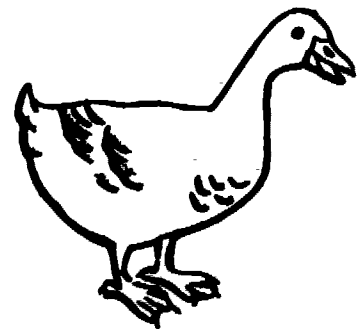
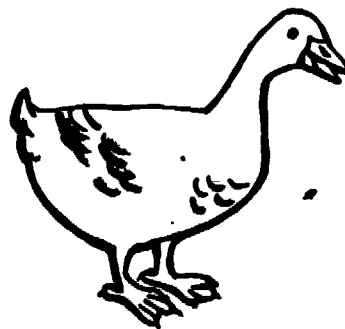
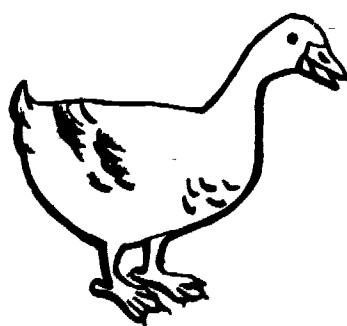
a. $\frac{3}{4} = \frac{9}{\quad}$

d. $\frac{\quad}{3} = \frac{15}{9}$

b. $4:\quad = 8:14$

e. $\frac{8}{\quad} = \frac{24}{15}$

c. $5:6 = \quad:42$



2. Farmer Jones bought:

3 - 10# ducks that cost \$2.82. Batman bought (at the same price) 1 - 10# duck. How much did Batman's duck cost?

3. One apiarist harvested:

1000# honey from 25 hives. Jon harvested (at the same rate) 18 bee hives. How much honey did Jon harvest?

4. Student Council buys:

Records at the rate of 6 for \$1.00. Mary Smith buys (at the same price) 25 records. How much do Mary's records cost?

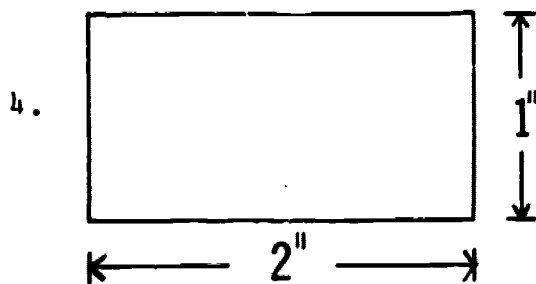
5. Grapefruit

$\frac{3}{4}$ for 10¢ for ? _____ (at the same price)

E. Scale Drawings

Exercises

1. Given scale $\frac{1}{4}$, how long a line will represent a distance of 4 inches? 12 inches? 24 inches? 2 feet? 2 yards?
2. Given scale $\frac{1}{3}$, what distance will be represented by a line 1 inch long? 3 inches? $1\frac{1}{2}$ inches? 1 foot?
3. ~~Make~~ a scale drawing of a swimming pool which is 50 ft. long and 24 ft. wide. Set up your own scale. Express your scale as a ratio.



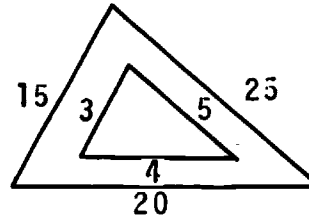
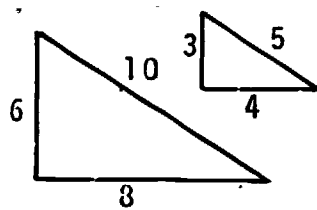
The scale drawing at the left is of a farmer's field. If our scale is $\frac{1}{4}$ in. = 50 rods, find the perimeter of the field.

5. Make a scale drawing of our basketball court, using the scale $1'' = 10'$.

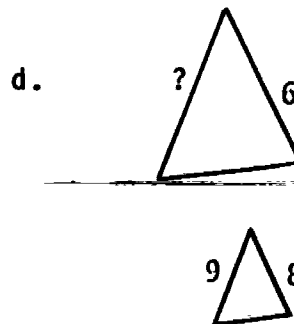
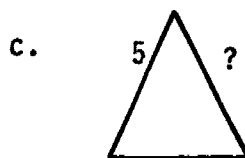
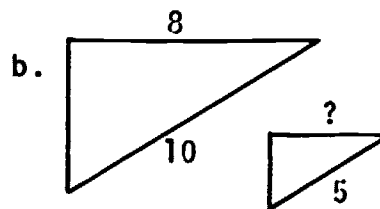
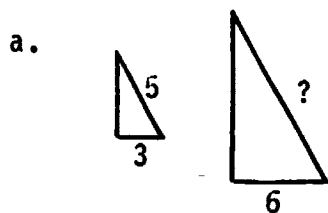
F. Similar Triangles

Exercises

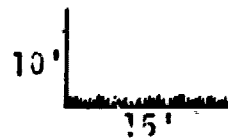
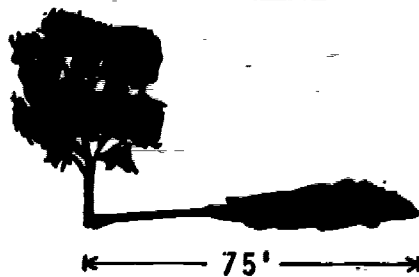
1. These are similar triangles. What characteristics can you find?



2. Similar triangles. Find the length of the missing side.

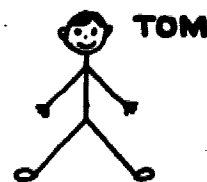
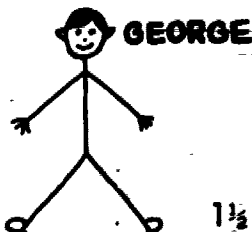


3.



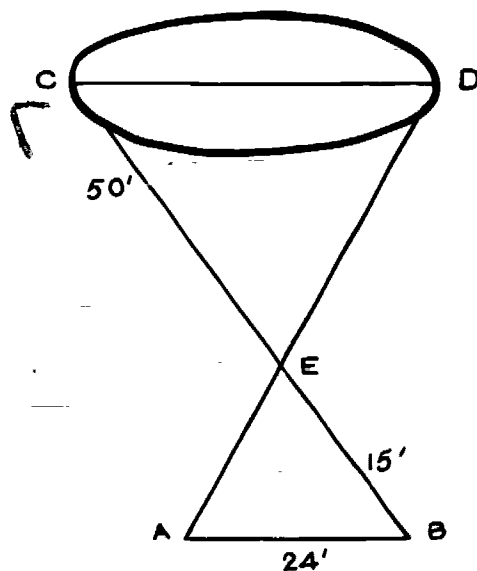
- a. If we drew a line from top of a tree to end of shadow, what kind of triangle will be formed?
- b. What is the height of the tree?
4. How tall is George?

George _____ . Tom is 4' tall.

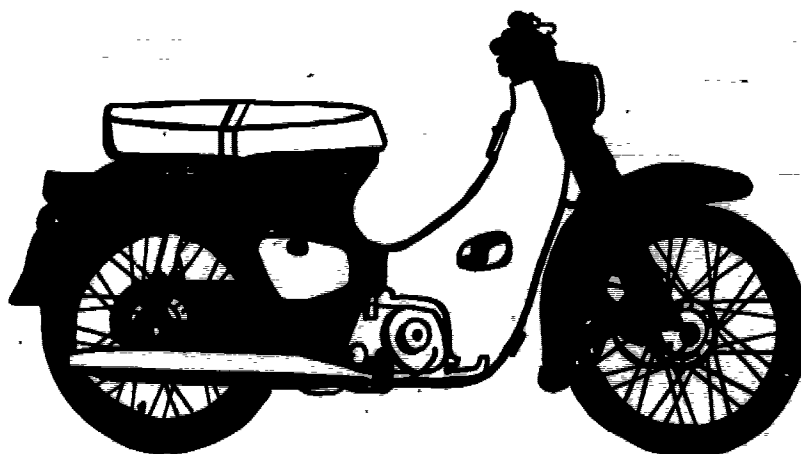


5. A tower casts a shadow 21' long at the same time a 6' man casts a shadow 3' long. How tall is the tower? Draw a diagram.

6. How long is the pond?



7.



Honda 50 Cost \$239.

This is $\frac{1}{2}$ the cost of a calculator.

What is the cost of a calculator?

3. Pythagorean Theorem

Exercises

Given two sides of a right triangle, find the other side.

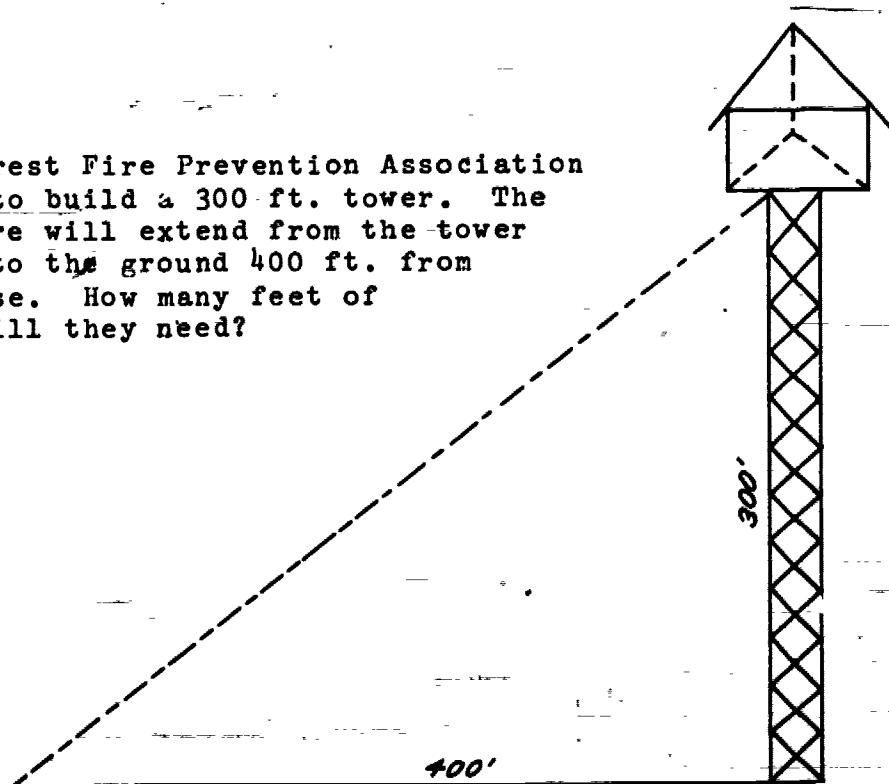
	Side A	Side B	Hypotenuse
1.	8	6	?
2.	?	12	15
3.	15	?	25
4.	5	12	?

5. How did you find the third side of the triangle? Explain your method or represent it in a short form.
6. The television companies measure the screen of a set by using a line which divides the screen into two right triangles. When they say a 21" screen they mean this line is 21" long.

If I bought a 20" screen that was 12" wide, how long would the screen be?

7.

The Forest Fire Prevention Association plans to build a 300 ft. tower. The guy wire will extend from the tower floor to the ground 400 ft. from the base. How many feet of wire will they need?



H. Area of Plane Geometric Figures:

Exercises

1. Find the cost of cementing a sidewalk 25 ft. X 8 ft. at \$.65 per sq. ft.
2. Find the cost of sodding a lawn 12 ft. by 9 ft. at \$.08 per sq. ft.
3. How many square feet of floor space remain uncovered if an 8 ft. by 10 ft. rug is placed on a floor 15 ft. long and 12 ft. wide?
4. How many square feet of tarpaulin are needed to cover the infield of a baseball diamond if the space between the bases is 90 feet?
5. The official United States flag is 4 ft. wide and 7.6 ft. long. What is the area of the flag?

Floorcraft

PHONE JE 5-5200 625 MAIN ST.

PINE BLUFF, ARKANSAS

1. Mr. Anthony West
Faucett Rd.

Living room 14'3" x 12' _____ sq. yds. Carpet @5.95
sq. yd. Pad 1.00 sq. yd. and labor @1.00 sq. yd.

Complete _____

2. Mr. Paul Greene
1605 W. 27th

Living room 12'6" x 15' _____ sq. yds. Carpet @4.50
sq. yd. Pad 1.00 sq. yd. and labor @1.00 sq. yd.

Complete _____

3. Mr. J. H. Jones
1419 Cherry St.

Living room 12' x 15' _____ sq. yds. Carpet @6.95 sq.
yd. Pad 1.00 sq. yd. and labor @1.00 sq. yd.

Complete _____

4. The cost of flooring a room 13' x 15' with space to be
omitted (6' x 3') with 9 x 9 tile costing 15¢ each and
selling @23¢. What is the cost and the profit?

Exercises

1. A farmer's field is divided into two triangles. He wants to know the areas in order to buy fertilizer.

The two parts of the field have these dimensions:

- a. base: 440 yards: 220 yards altitude
 b. base: 605 yards: 496 yards altitude

Find the total area of the farmer's field in square yards. in acres. (4840 sq. yd. = 1 acre)

Find the cost of fertilizer if 300 lbs. will cover 1 acre and fertilizer is \$3.10 per 100 lbs.

2. Find area. Put answers in appropriate place in square. The sum of row i should equal the sum of column i , etc.

- a. Rectangle: $l = 20$; $w = 22$
 b. Triangle: $h = 100$; $b = 45$
 c. Parallelogram: $b = 20$; $h = 17$
 d. Triangle: $b = 50$; $h = 10$
 e. Rectangle: $l = 31$; $w = 30$
 f. Triangle: $b = 45$; $h = 8$
 g. Parallelogram: $b = 118$; $h = 35$
 h. Triangle: $b = 38$; $h = 20$
 i. Rectangle: $l = 61$; $w = 20$
 j. Parallelogram: $b = 122$; $h = 20$
 k. Triangle: $b = 20$; $h = 17$
 l. Rectangle: $l = 35$; $w = 26$
 m. Triangle: $b = 23$; $h = 60$
 n. Rectangle: $l = 30$; $w = 25$
 o. Square: $s = 10$
 p. Parallelogram: $b = 20$; $h = 100$

a	b	c	d
e	f	g	h
i	j	k	l
m	n	o	p

3. A challenge:

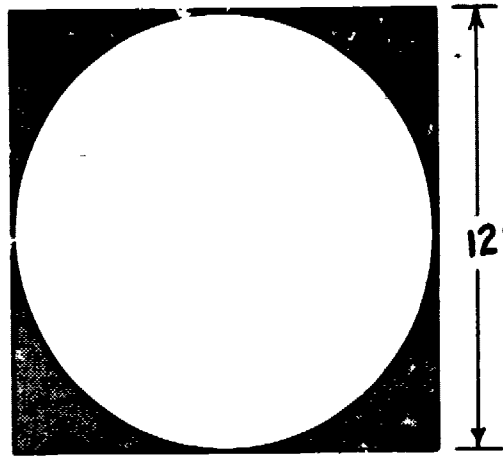
Area of Figure	Dimensions	What type figure?
a. 175 sq. in.	10 in. 35 in.	_____
b. 322 sq. in.	23 in. 14 in.	_____
c. 306 sq. in.	17 in. 36 in.	_____
d. 251 sq. in.	11 in. 23 in.	_____



Exercises

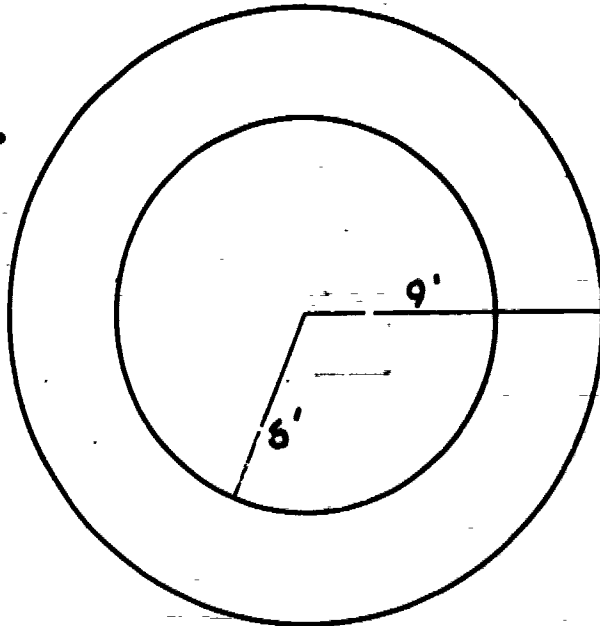
Finding The Areas of Circles:

1.



What is the area of the square?
What is the area of the circle?
What is the area of the shaded portion?

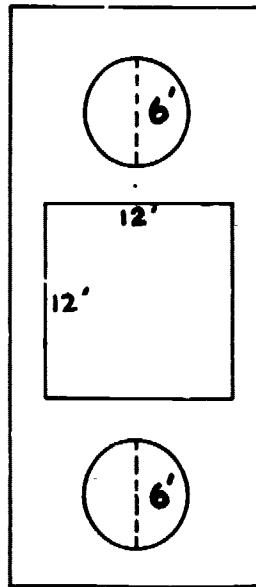
2.



At the left is a diagram of a circular swimming pool surrounded by a circular patio. The owner wished to paint the patio. He must find the area of the larger circle and subtract the area of the smaller circle.

A quart of paint costs \$2.49 and will cover 10 sq. ft. Find the cost of the paint.

3.



A park is 15 feet wide and 45 feet long. The park contains 2 circular flower gardens and 1 square flower garden. The rest of the park is covered with grass. What is the area of the part that is grass covered?

4. Go to the basketball court and find the area of the following using 100-foot tape. (This is a good place to discuss error.)

a. The court has _____ sq. ft.

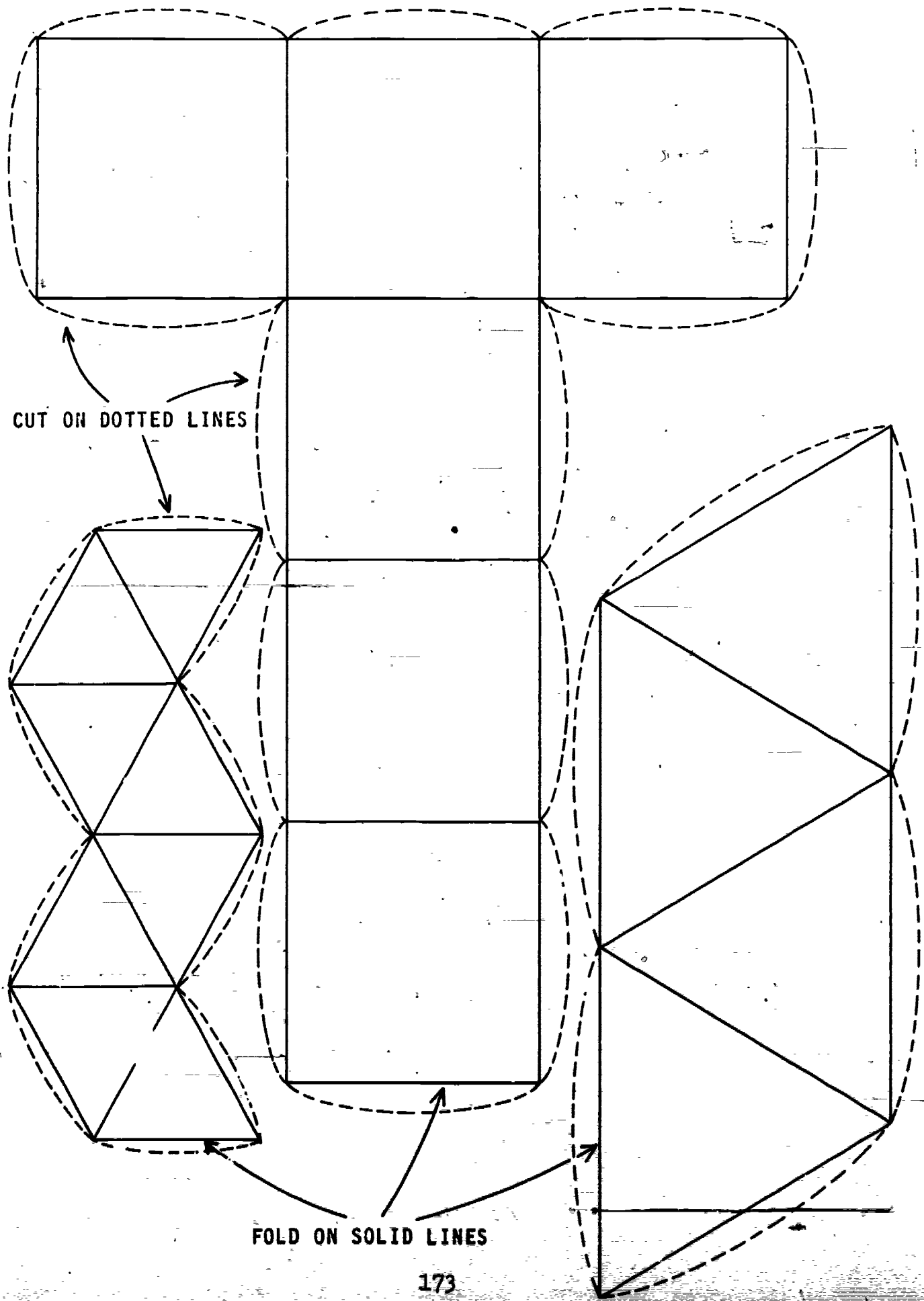
b. The center circle has _____ sq. ft.

c. The free throw circles have _____ sq. ft.

_____ The Repetitious Number _____

Write down any 3 digits; repeat the digits a second time making it a six digit number. Divide your number by 7; divide this quotient by 11; divide this next quotient by 13. Your answer? _____

Cut Out - Fold It - Name It



CUT ON DOTTED LINES

FOLD ON SOLID LINES

I. Surface area of cubes

Exercises

1. Cut a 1" square from paper.
2. How many one inch squares would you need to cover a 1 inch cube?
3. Let's make a cube:
 - a. First draw a pattern to make the cube.
 - b. Then construct the cube.
 - c. In building a house people have different patterns.
 - d. Could we make different patterns to use in making a cube?
 - e. Can we make a one piece pattern?
 - f. How many different one piece patterns can we design?
4. Talk about the cube.
 - a. What is the shape of one side?
 - b. What is the shape of the top? bottom?
 - c. Could the top become a side by changing the position of the cube?
 - d. Is there a name that could be used for both top and sides?
 - e. What is the area of one face?
 - f. Are the faces the same size?
 - g. How many faces?
 - h. What is the total area of the cube?

J. Surface area of a Rectangular Solid

Exercises

1. Make a rectangular box.
 - a. Measure all the faces.
 - b. Did you find any the same size?
 - c. Can you find the total area of the box?
2. Joe bought a new transistor radio.
 - a. The length is 10 inches.
 - b. The width is 6 inches.
 - c. The depth is 2 inches.

Can you find the total area of the radio?

3. The diagram in Figure A represents a closed wooden box.
 - a. Find the number of square feet of lumber required to make four sides, the top, and the bottom of the box.
 - b. What is the cost if lumber is 12¢ per sq. ft.?

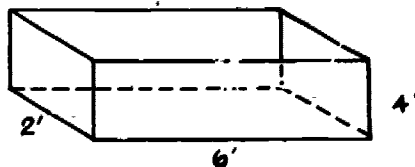


FIGURE A

"Time Killer"

Draw a circle around all the names for 8.

$$2 \quad 64 \quad 9-1 \quad 10-3 \quad 5+3$$

$$(2 \times 3) + 2 \quad 15 \div 3 \quad \text{VIII}$$

$$\text{eight} \quad 12 - 5 \quad 8 + 0$$

$$6 + 2 \quad 8.0 \quad 6/3 \times 2 \quad \frac{16}{2}$$

$$4 + 1 + 1 + 2$$

K. Surface area of a cylinder

Exercises

1. Cut a rectangular piece of paper.
 - a. Measure the length of the paper.
 - b. Measure the width of the paper.
 - c. Find the area of the piece of paper.
 - d. Tape the widths of the paper together to form a cylinder.
 - e. Do you know the circumference of the top of this cylinder without measuring?
 - f. Can you find the diameter?
 - g. How can you find the area of the top of this cylinder?
 - h. Do you know the area of the bottom of this cylinder without measuring?
 - i. How can you find the total area of the cylinder?

2.
 - a. Can you find the total surface area of a cylinder which has a diameter of 5 inches and a height of 6 inches?
 - b. Now if you had a diameter of 6 inches and a height of 8 inches, could you find the total area of a cylinder?
 - c. A grocery store had a game going:

If you tell the total surface area of a cola can, you are given a case of colas.

The diameter is 2-1/2 inches.

The height is 5 inches.

Will you be able to get a free case of colas?

L. Volume of a Cube

Exercises

1. What dimensions would a wooden cube have if its volume has 27 cubic inches? 64 cu. in? 8 cu. in?
2. If a wooden cube 5 in. x 5 in. x 5 in. was submerged in a can full of water, how much water would it force out of the can?
3. If a lb. of green beans occupied 48 cu. in., how many lbs. could be packed in a cubic box with 36 in. sides?
4. How many 1 in. cubic blocks could be made from a rectangular solid 12 in. x 14 in. x 15 in.?
5. A swimming pool is 25 ft. long, 10 ft. wide and 12 ft. deep. How long would it take to fill the pool, if water flows into the pool at the rate of 50 gallons per half hour? A cubic foot of water is equal to 7.5 gallons.
6.
 - a. Produce truck bed is 4 ft. x 15 ft. x 9 ft. How many pounds of strawberries will the truck carry if it would hold 5.5 lbs. per cu. ft.?
 - b. If one bushel weighs 65 pounds, how many bushels could the truck carry?

Special Project

If you have a ten inch cube with top and one side painted red and any two other adjacent sides green, how many one inch cubes can be made from this cube?

Consider these 1 inch cubes:

Number of sides		Number of 1 in. cubes
Red	Green	
0	0	_____
0	1	_____
0	2	_____
0	3	_____
0	4	_____
1	0	_____
1	1	_____
1	2	_____
1	3	_____
2	0	_____
2	1	_____
2	2	_____
3	0	_____
3	1	_____
4	0	_____

Northside High School Athletic Department

North 23rd and B Streets



Fort Smith, Arkansas

Athletic Expenses

1. Adhesive tape for the athletic department is delivered in containers packed in boxes which are 6 containers long, 4 containers wide, and 1 container deep.
 - a. _____ How many containers are in each box?
 - b. _____ How many containers are in 100 boxes?
 - c. _____ How many rolls of tape are in 100 boxes if each container holds 4 rolls?
 - d. _____ Each roll of tape is 10 yards long. How many yards of tape are in 100 boxes?
 - e. _____ How many feet of tape are in the 100 boxes?
 - f. _____ Each container of tape costs \$2.00. How much will each box of tape cost?
 - g. _____ How much will 100 boxes of tape cost?
 - h. _____ How much does each roll of tape cost?

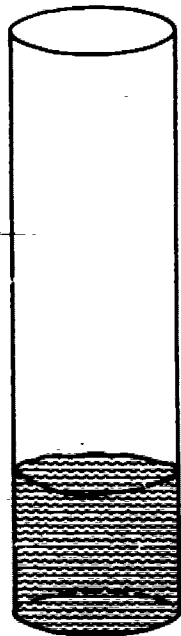
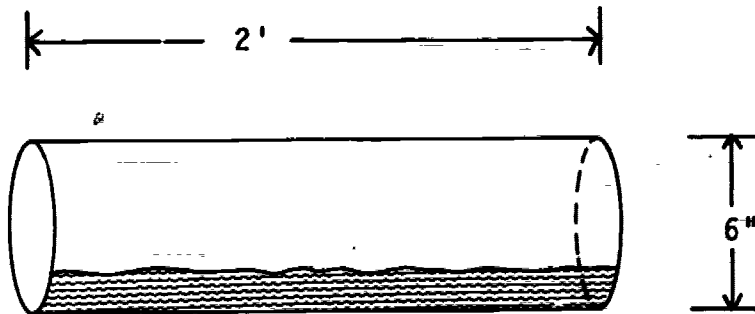
2. If the tape in 100 boxes was joined end to end and placed on a road from your city, what is the farthest city or town the tape would reach?

M. Volume of a Cylinder

Exercises

1. Suppose you went to a gas station with a can for gas and the attendant said he would fill it free if you could tell him how many cubic inches were in the can. If the can is 15" tall and 12" in diameter, could you get your gas free?
2. The tank on an oil truck is 7 ft. in diameter and 35 ft. tall (or long). If 1 cubic foot is approximately $7\frac{1}{2}$ gallons, how many gallons of oil will the truck hold?
3. How many cubic yards of dirt must be removed in digging a well 5 ft. in diameter and 54 ft. deep?

Make A Guess



The tanks are the same size.

The water level in each tank is $\frac{1}{3}$ the height of the tank.

What do you think about the amount of water in the vertical tank compared to the horizontal tank?

Circle one: More, same, less



SOLID STEEL-WALL REDI-POOL WITH ATTACHED VINYL LINER

. . . just unroll into a circle and add water

. . . . BIG 8 FEET DIAMETER 20 INCHES DEEP



1. Find the surface area of the Splasher Pool. How many gallons of water would it take to fill the pool?
2. Find the total surface area of the file cabinet.

II. Comparing Units of Measure

Measurements You Need To Know

16 fluid ounces = 1 pint

16 ounces = 1 pound)

2 measuring cups = 1 pint

2000 pounds = 1 ton

2 pints = 1 quart

12 units = 1 dozen

4 quarts = 1 gallon

8 quarts = 1 peck

3 teaspoons = 1 tablespoon

4 pecks = 1 bushel

Exercises

Place the letter to the correct answer in the blank. There are more answers than problems.

- | | | |
|---------------------------|---------------------------|-------------------------|
| _____ 1. 4 pecks | a. 3 pecks, 4 qts. | k. 4 dozen |
| _____ 2. 12 tablespoons | b. 100 lbs. | l. 144 units |
| _____ 3. 1600 ounces | c. 36 teaspoons | m. 4 pints |
| _____ 4. 12 quarts | d. 3 gallons | n. 146 un.ts |
| _____ 5. 32 pints | e. 9 tons,
1200 pounds | o. 17 measuring
cups |
| _____ 6. 16 gallons | | |
| _____ 7. 12 dozen | f. 23 tablespoons | p. 2 pints |
| _____ 8. 19,200 pounds | g. 32 quarts | q. 19 tons |
| _____ 9. 2 measuring cups | h. 3 pints | r. 64 quarts |
| _____ 10. 32 fluid ounces | i. 15 pecks | s. 16 fl. oz. |
| _____ 11. 6 pints | j. 6 tablespoons | t. 16 quarts |
| _____ 12. 48 units | | u. 12 measuring
cups |
| _____ 13. 48 fluid ounces | | |
| _____ 14. 28 quarts | | |
| _____ 15. 18 tons | | |

0. Denominate Numbers

Exercises

Add each set of denominate numbers. Include the units in your answer.

Length

$$\begin{array}{r} 1. \quad 3' \ 5'' \\ \quad 7' \ 7'' \\ \quad 4' \ 11'' \\ \hline \quad 2' \ 4'' \end{array}$$

$$\begin{array}{r} 2. \quad 2 \text{ yds. } 1 \text{ ft. } 5 \text{ in.} \\ \quad 3 \text{ yds. } 2 \text{ ft. } 8 \text{ in.} \\ \hline \quad 1 \text{ yd. } \quad 11 \text{ in.} \end{array}$$

Weight

$$\begin{array}{r} 3. \quad 7 \text{ lb. } \quad 3 \text{ oz.} \\ \quad 2 \text{ lb. } \quad 9 \text{ oz.} \\ \quad 4 \text{ lb. } \quad 5 \text{ oz.} \\ \hline \quad 1 \text{ lb. } 10 \text{ oz.} \end{array}$$

$$\begin{array}{r} 4. \quad 2 \text{ tons } \quad 450 \text{ lbs.} \\ \quad 1 \text{ ton } \quad 800 \text{ lbs.} \\ \quad 3 \text{ tons } 1400 \text{ lbs.} \\ \hline \quad 5 \text{ tons } \quad 975 \text{ lbs.} \end{array}$$

Dry Measure

$$\begin{array}{r} 5. \quad 2 \text{ tablespoons } 2 \text{ teaspoons} \\ \quad 4 \text{ tablespoons } 1 \text{ teaspoon} \\ \quad 3 \text{ tablespoons } 1 \text{ teaspoon} \\ \hline \quad 5 \text{ tablespoons } 2 \text{ teaspoons} \end{array}$$

$$\begin{array}{r} 6. \quad 3 \text{ bu. } 1 \text{ peck} \\ \quad 2 \text{ bu. } 2 \text{ pecks} \\ \quad 5 \text{ bu. } 3 \text{ pecks} \\ \hline \quad 1 \text{ bu. } 3 \text{ pecks} \end{array}$$

$$\begin{array}{r} 7. \quad 1 \text{ bu. } 2 \text{ pecks } 3 \text{ qts.} \\ \quad \quad 6 \text{ pecks } 5 \text{ qts.} \\ \quad 4 \text{ bu. } 3 \text{ pecks } 4 \text{ qts.} \\ \hline \quad 2 \text{ bu. } 2 \text{ pecks } 1 \text{ qt.} \end{array}$$

Liquid Measure

8. 2 gal. 3 qt. 1 pt.
 1 gal. 1 qt. 3 pt.
 4 gal. 2 qt. 2 pt.
 5 gal. 3 qt. 1 pt.

9. 3 qt. 1 pt. 1 cup
 3 pt. 5 cup
 2 qt. 1 cup

Angle Measurement

10. 37⁰ 15' 47"
 123⁰ 41' 5"
 21⁰ 33' 29"
 87⁰ 59' 13"

11. 23⁰ 17' 57"
 202⁰ 48'
 69⁰ 17"
 50' 42"

12. 13⁰ 6' 9"
 108⁰ 59' 43"
 42⁰ 43' 31"

Exercises

Subtract the second denominate number from the first and include the units in your answer.

LENGTH

$$\begin{array}{r} 1. \quad 17 \text{ ft.} \quad 2 \text{ in.} \\ - \quad 8 \text{ ft.} \quad 7 \text{ in.} \\ \hline \end{array}$$

$$\begin{array}{r} 2. \quad 5 \text{ yd.} \quad 7 \text{ in.} \\ - \quad 2 \text{ yd.} \quad 1 \text{ ft.} \quad 10 \text{ in.} \\ \hline \end{array}$$

$$\begin{array}{r} 3. \quad 5 \text{ mi.} \quad 700 \text{ yd.} \\ - \quad 1 \text{ mi.} \quad 880 \text{ yd.} \\ \hline \end{array}$$

WEIGHT

$$\begin{array}{r} 4. \quad 6 \text{ lb.} \quad 10 \text{ oz.} \\ - \quad 2 \text{ lb.} \quad 13 \text{ oz.} \\ \hline \end{array}$$

$$\begin{array}{r} 5. \quad 18 \text{ lb.} \\ - \quad 5 \text{ lb.} \quad 3 \text{ oz.} \\ \hline \end{array}$$

$$\begin{array}{r} 6. \quad 6 \text{ T.} \quad 1300 \text{ lb.} \\ - \quad 3 \text{ T.} \quad 1575 \text{ lb.} \\ \hline \end{array}$$

DRY MEASURE

$$\begin{array}{r} 7. \quad 7 \text{ tbsp.} \quad 1 \text{ tsp.} \\ - \quad 2 \text{ tbsp.} \quad 2 \text{ tsp.} \\ \hline \end{array}$$

$$\begin{array}{r} 8. \quad 12 \text{ bu.} \quad 1 \text{ pk.} \\ - \quad 5 \text{ bu.} \quad 3 \text{ pk.} \\ \hline \end{array}$$

$$\begin{array}{r} 9. \quad 8 \text{ bu.} \quad 1 \text{ pk.} \quad 5 \text{ qt.} \\ - \quad 7 \text{ bu.} \quad 3 \text{ pk.} \quad 7 \text{ qt.} \\ \hline \end{array}$$

LIQUID MEASURE

$$\begin{array}{r} 10. \quad 17 \text{ gal.} \quad 2 \text{ qt.} \quad 1 \text{ pt.} \\ - \quad 4 \text{ gal.} \quad 3 \text{ qt.} \quad 3 \text{ pt.} \\ \hline \end{array}$$

$$\begin{array}{r} 11. \quad 9 \text{ qt.} \quad 1 \text{ pt.} \quad 1 \text{ cup} \\ - \quad 2 \text{ qt.} \quad 3 \text{ pt.} \quad 2 \text{ cup} \\ \hline \end{array}$$

ANGULAR MEASURE

$$\begin{array}{r} 12. \quad 63^{\circ} \quad 17' \quad 42'' \\ - \quad 27^{\circ} \quad 38' \quad 59'' \\ \hline \end{array}$$

$$\begin{array}{r} 13. \quad 121^{\circ} \quad 18'' \\ - \quad 69^{\circ} \quad 19' \quad 31'' \\ \hline \end{array}$$

Exercises

Multiply each pair of denominate numbers and include the units in your answer.

Length

1. $\begin{array}{r} 6 \text{ ft. } 5 \text{ in.} \\ \times 4 \\ \hline \end{array}$ 2. $\begin{array}{r} 7 \text{ yd. } 2 \text{ ft. } 5 \text{ in.} \\ \times 7 \\ \hline \end{array}$ 3. $\begin{array}{r} 4 \text{ mi. } 623 \text{ yd.} \\ \times 3 \\ \hline \end{array}$

Weight

4. $\begin{array}{r} 14 \text{ lb. } 7 \text{ oz.} \\ \times 3 \\ \hline \end{array}$ 5. $\begin{array}{r} 9 \text{ lb. } 2 \text{ oz.} \\ \times 9 \\ \hline \end{array}$ 6. $\begin{array}{r} 8 \text{ T. } 869 \text{ lb.} \\ \times 3 \\ \hline \end{array}$

Dry Measure

7. $\begin{array}{r} 11 \text{ tbsp. } 2 \text{ tsp.} \\ \times 7 \\ \hline \end{array}$ 8. $\begin{array}{r} 16 \text{ bu } 3 \text{ pk.} \\ \times 6 \\ \hline \end{array}$ 9. $\begin{array}{r} 4 \text{ bu. } 2 \text{ pk. } 7 \text{ qt.} \\ \times 5 \\ \hline \end{array}$

Liquid Measure

10. $\begin{array}{r} 7 \text{ gal. } 3 \text{ qt. } 1 \text{ pt.} \\ \times 7 \\ \hline \end{array}$ 11. $\begin{array}{r} 5 \text{ qt. } 1 \text{ pt. } 1 \text{ cup} \\ \times 4 \\ \hline \end{array}$

Angular Measure

12. $\begin{array}{r} 70^{\circ} 0' 51'' \\ \times 9 \\ \hline \end{array}$ 13. $\begin{array}{r} 27^{\circ} 32' 45'' \\ \times 8 \\ \hline \end{array}$

Exercises

Length

1. $3 \overline{) 6 \text{ ft. } 9 \text{ in.}}$

2. $2 \overline{) 3 \text{ mi. } 40 \text{ yd.}}$

3. $4 \overline{) 3 \text{ yd. } 2 \text{ ft. } 4 \text{ in.}}$

Weight

4. $9 \overline{) 10 \text{ lb. } 2 \text{ oz.}}$

5. $5 \overline{) 4 \text{ lb. } 11 \text{ oz.}}$

6. $8 \overline{) 3 \text{ T. } 1200 \text{ lb.}}$

Dry Measure

7. $4 \overline{) 6 \text{ tbsp. } 2 \text{ tsp.}}$

8. $5 \overline{) 3 \text{ bu. } 3 \text{ pk.}}$

9. $9 \overline{) 5 \text{ bu. } 2 \text{ pk. } 4 \text{ oz.}}$

Liquid Measure

10. $3 \overline{) 5 \text{ gal. } 2 \text{ qt. } 1 \text{ pt.}}$

11. $3 \overline{) 6 \text{ qt. } 1 \text{ pt. } 1 \text{ cup}}$

Angular Measure

12. $7 \overline{) 113^{\circ} 40' 6''}$

13. $4 \overline{) 57^{\circ} 12''}$

P. Measuring Time:

Exercises

1. Tom started on his homework at 4:30 p.m., and worked until 7:15 p.m. How long did he study?
2. From the time the first bell rings in the morning to the time the last period ends, how long are you in school?
3. We get out of school December 16 and start back on January 2. How many days are we out for Christmas?
4. School started September 5. We are out 2 days for Thanksgiving, 2 days for AEA, 10 days for Christmas, 2 days for spring holiday and school closes on May 26. How many days are we in school?
5. Find the date of maturity of each of the following notes.
 - a. 30 day note dated April 9
 - b. 4 month note dated March 17
 - c. 60 day note dated November 30
 - d. 45 day note dated August 14

6. Add:

a.
6 yr. 2 mo.
3 yr. 7 mo.
4 yr. 1 mo.

b.
4 wks. 5 da.
1 wk. 3 da.
2 wk. 6 da.

c.
3 hr. 43 min. 28 sec.
7 hr. 19 min. 53 sec.
5 hr. 52 min. 49 sec.

7. Subtract:

a.
3 day 9 hr.
18 hr.

b.
35 min. 18 sec.
19 min. 50 sec.

c.
3 hr. 42 min. 25 sec.
1 hr. 48 min. 39 sec.

8. Multiply:

a.
5 da. 2 hr.
9

b.
4 hr. 21 min. 34 sec.
5

9. Divide:

a. $5 \overline{) 15 \text{ yr. } 10 \text{ mo.}}$

b. $3 \overline{) 21 \text{ min. } 45 \text{ sec.}}$

Exercises

Computing wages:

1. Mr. Fox is paid \$3.10 per hour. (a) How much is he paid for an 8-hour day? (b) a 40-hour week?
2. Miss Williams is paid \$2.25 an hour. She receives time and a half for any hours worked over 40 per week. Find her pay for a 44-hour week.
3. Barbara, as a baby sitter, received \$1.00 an hour before midnight and \$1.25 an hour after midnight. If she got a job from 8:00 p.m. to 1:30 a.m. the next day, how much would she earn?
4. Given a time card: Compute the number of hours each day, to the nearest 15 minutes, and the total time for the week. Then find the amount of wages due if the rate was \$1.80 per hour.

	In	Out	In	Out	No. of hours
Mon.	8:59	12:10	12:59	5:02	_____
Tues.	8:56	12:00	12:57	5:00	_____
Wed.	9:00	12:02	12:58	4:30	_____
Thurs.	8:59	12:00	12:57	5:00	_____
Fri.	8:58	12:03	1:00	5:03	_____

5. Use Time Cards
Make out the time cards and compute the week's wages for your week's work if your schedule was as follows:

	In	Out
Monday	7:53	4:40
Tuesday	7:56	4:38
Wednesday	8:05	4:35
Thursday	8:00	6:00
Friday	7:50	6:30

Rate per hour: \$2.75

Normal work day begins at 8:00 a.m. and ends at 4:30 p.m.

Unpaid lunch period of 1/2 hour.

Time and a half to be paid for all time to the nearest 1/2 hour in excess of 8 hours per day if time out is circled.

Pay is docked 1/4 hour for each 15 minute period or part of a 15 minute period that the employee is late.

BI-MONTHLY TIME CARD, WYNNE PUBLIC SCHOOL

From _____ To _____

Hours Worked Date	Time Started A.M.	Time Stopped	Time Started P.M.	Time Stopped	TOTAL HOURS

Signed _____ Total Hours Worked This Period _____

BI-MONTHLY TIME CARD, WYNNE PUBLIC SCHOOL

From _____ To _____

Hours Worked Date	Time Started A.M.	Time Stopped	Time Started P.M.	Time Stopped	TOTAL HOURS

Signed _____ Total Hours Worked This Period _____

Exercises

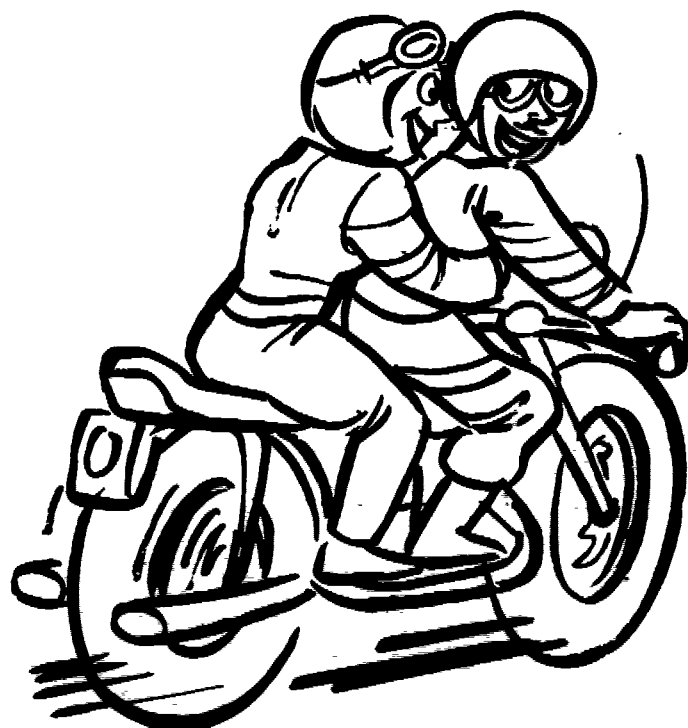
Computing time in days, months and years:

1. How much older is Amy than Ann if they were born the same year and Amy's birthday is January 24 and Ann's is June 3?
2. Find the number of days between the following dates.
 - a. May 28 and Sept. 2.
 - b. Nov. 28 and Dec. 25.
 - c. Sept. 6 and May 28.
 - d. May 31 and March 1.
 - e. June 13 and July 22.
 - f. Dec. 25 and March 22.
3. How many days from:
 - a. Feb 2 to June 15?
 - b. April 5 to November 15?
 - c. August 4, 1966 to April 15, 1968?
 - d. Jan. 10 to May 1?
4. What day is the 133rd day of the year?
5. What was the date of 43 days ago?
6. If you are 14 years, 3 mo. and 2 days old, when were you born?
7. If you went on a 26 day vacation which began June 16, when would you be due back at work?
8. Find days between Sept. 5, 1956 and July 31, 1958.
9. How old is Nancy if she was born August 3, 1955?
10. Find the maturity date of the following notes:
 - a. 45 day note from Jan. 14.
 - b. 174 day note from July 4.

LITTLE JOE

Joe was a general 1 _____ student who bought a Honda with some extras, including handlebars set at a sharp 2 _____. He found that there were still some things to work on. He started by 3 _____ the air pressure of the tires after an 4 _____ of the amount in each. He found that the tires were 5 _____ in air pressure. The tail light was shaped like a 6 _____ (a member of the 7 _____ family) and the headlight was in the shape of a 8 _____. The motor of his Honda was "missing" so he decided to 9 _____ the spark plug and buy a new 10 _____ of points. Since the 11 _____ of the gas tank was six 12 _____ across he figured the 13 _____ and found it was 1 gallon. After counting his change, he filled her up and was ready to blast off.

He really wouldn't have bought this particular Honda but after much 14 _____ Joe decided upon the motor with the lowest price and the biggest 15 _____ he could get. This machine had the lowest gear 16 _____. After adding the 17 _____ on to the regular price, Joe decided to make a 18 _____ 19 _____ and



"IT'S SUCH A BEAUTIFUL DAY, LET'S ROAR UP 101, BLAST ACROSS 33 TO 99 AND BURN IT BACK TO L.A."

buy it on what is called an 20 _____ plan. Even though he has already had to 21 _____ the spark plug and a set of 22 _____, he still feels he bought the best.

The license number was a 23 _____ 24 _____ and the license plate was a three-sided figure called a 25 _____.

Joe also liked to eat a large piece of 26 _____ and strum a few 27 _____ on his brother's guitar. Since Joe and his brothers were little boys the grocery bill has 28 _____ to a steady 29 _____. The 30 _____ of increase gives his father a headache.

In school Joe disliked using a 31 _____ to measure lines but enjoyed using the 32 _____ and 33 _____ to draw circles. His 34 _____ grade is good, but could be better if he wouldn't spend so much time with a certain blonde who has many 35 _____ and is quite short in 36 _____.

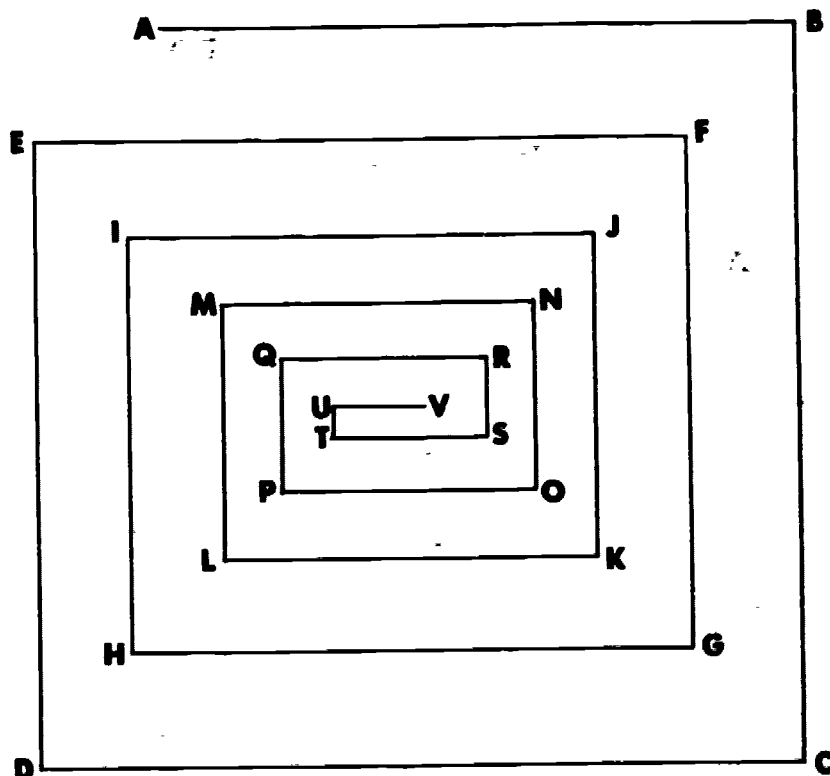
Fill blanks with words from this list. Use each word only once or not at all.

angle
average
area
calculation
chords
circle
compass
counting
commutative
curves

diameter
difference
discount
down
estimate
height
inches
increase
increased
installment

mathematics
measuring
number
payment
per cent
pi
points
protractor
quadrilateral
quantity

rate
ratio
rational
replace
ruler
set
square
sum
tax
triangular
unequal
volume



Name the line segments.

Measure them.

Find their sum.

PERMUTATIONS

The letters A and B can be rearranged as AB and BA. The letters A, B, and C can be rearranged as ABC, ACB, BCA, BAC, CAB, and CBA. Two letters were rearranged two ways, three letters were rearranged six ways. How many ways can you rearrange the four letters A, B, C, and D? Can you find a rule so that if you were given the letters A, B, C, D, and E to rearrange you could tell how many ways this can be done without writing them down?

Q. Board Feet:

Exercises

How many board feet in each?

- | | | | |
|-----|----------------|-----|----------------|
| 1. | 1" x 12" x 10' | 14. | 1" x 10" x 16' |
| 2. | 2" x 6" x 12' | 15. | 1" x 8" x 12' |
| 3. | 2" x 4" x 12' | 16. | 1" x 2" x 6' |
| 4. | 1" x 4" x 12' | 17. | 4" x 8" x 16' |
| 5. | 1" x 6" x 8' | 18. | 2" x 4" x 8' |
| 6. | 2" x 8" x 16' | 19. | 2" x 2" x 8' |
| 7. | 4" x 4" x 10' | 20. | 8" x 8" x 16' |
| 8. | 2" x 6" x 16' | 21. | 4" x 6" x 12' |
| 9. | 1" x 2" x 12' | 22. | 6" x 8" x 6' |
| 10. | 2" x 12" x 12' | 23. | 1" x 12" x 8' |
| 11. | 2" x 2" x 10' | 24. | 1" x 8" x 8' |
| 12. | 1" x 4" x 8' | 25. | 2" x 4" x 10' |
| 13. | 1" x 10" x 10' | | |

R. Order Relations

Exercises

Fill in each circle with the correct symbol.

Choose from these: $=$, $>$, $<$

1. The number of girls in our class the number of boys.
2. 1 ft. 8 inches 19 inches.
3. 1 lb. 17 ounces.
4. 1 mile 5283 ft.
5. Number of pounds you weigh 200 lbs.
6. Your height 5 ft. 8 in.
7. Number of grains of sand in a quart jar number of grains of sand in a pint jar.
8. Number of ounces in a lb. number of ounces in a pint.
9. Number of days in April number of days in May.
10. Number of days in week number of days in school week.
11. Price of new Cadillac price of new Mustang.
12. Distance from your home to Memphis distance from your home to Little Rock.

Fun

Add me to myself.
Multiply by 4.
When you divide by 8
You'll have me once more.
Who Am I?

— Exercises —

Fill in the circles with the correct symbols: ($>$, $<$, or $=$).

1. $-5 \bigcirc -2$

2. $7 \bigcirc 3$

3. $-1 \bigcirc 3$

4. $3 \bigcirc 5$

5. $4 \bigcirc -3$

6. $-6 \bigcirc -8$

7. $-3 \bigcirc 3$

8. $-7 \bigcirc 0$

9. $\frac{11}{4} \bigcirc \frac{9}{6}$

10. $\frac{-5}{6} \bigcirc \frac{-7}{8}$

11. $\frac{3}{8} \bigcirc \frac{1}{4}$

12. $\frac{-19}{7} \bigcirc -2$

13. $-2 \bigcirc -3$ but $\bigcirc -1$

14. $4 \bigcirc 6$ but $\bigcirc 3$

15. $0 \bigcirc 1$ but $\bigcirc -3$

16. $4 \bigcirc 4$ but $\bigcirc 10$

LOST WORDS

The beginnings or endings of the words listed below were lost. With the help of the given clues, can you find the missing letters?

- | | | |
|----|-------------------|--------------------------------|
| 1. | _ _ _ end | Number added |
| | _ _ _ _ _ end | Number divided |
| | _ _ _ _ _ _ _ end | Number subtracted |
| 2. | _ ven | Number divisible by 2 |
| | _ _ ven | Lucky number |
| | _ _ _ ven | Prime number |
| 3. | _ int | Unit of liquid measure |
| | _ _ int | A location |
| | _ _ _ _ _ int | Center of a segment |
| 4. | _ ine | Unending straight mark |
| | _ _ ine | Number |
| | _ _ _ _ _ ine | To find a solution |
| 5. | _ ear | Unit of time |
| | _ _ ear | Understandable problem |
| | _ _ _ ear | Type of measure such as a foot |
| | _ _ _ _ _ ear | Three or more points in a line |
| 6. | rat_ | Acceleration |
| | rat_ _ | Comparison of two things |
| | rat_ _ _ | Rank |
| | rat_ _ _ _ _ | Fractional number |

- | | | |
|-----|-----------|--|
| 7. | _ector | Directional arrow |
| | __ector | Divides into two equal parts |
| | ___ector | Divides equally into three parts |
| | ____ector | Line meeting another line |
| 8. | _____ent | Part of a line |
| | _____ent | A member of a set |
| | _____ent | Line touching a circle only once |
| | _____ent | Beside or next to |
| | _____ent | Coinciding or equal |
| | _____ent | Equal or same as |
| | _____ent | At same time or place |
| | _____ent | One of two angles whose sum is 90 |
| 9. | __ter | Basic unit of measure |
| | ___ter | Part of a circle |
| | ___ter | Method of identifying members of a set |
| | ___ter | More than |
| | ___ter | Point where angle bisectors meet |
| | ___ter | Distance around something |
| | ___ter | Line in circle |
| | ___ter | Approx. 2/5 inch |
| 10. | _ight | Number |
| | _ight | Angle of 90° |
| | __ight | Mass |
| | __ight | Altitude |
| | ___ight | Not crooked |

F	L	O	W	C	H	A	R	T	S	S	P	A	C	E	N	X	E
R	B	G	C	O	D	D	A	N	G	L	E	T	M	T	N	A	S
A	L	G	E	B	R	A	S	U	V	A	N	D	R	N	E	F	R
C	H	L	Y	J	B	R	D	M	A	M	T	B	O	I	S	U	E
T	R	Z	C	I	R	C	L	E	W	I	A	X	T	O	Q	R	V
I	I	T	H	N	E	P	N	R	L	C	G	R	A	P	H	J	N
O	H	T	A	V	D	I	V	I	D	E	O	L	R	A	D	I	I
N	E	H	R	E	U	N	Z	C	J	D	N	P	E	F	E	N	W
D	T	U	T	R	C	O	M	A	T	H	P	S	M	T	H	O	M
F	I	N	I	T	E	I	N	L	D	L	L	L	U	N	O	E	R
D	M	A	L	E	M	N	O	P	R	E	W	S	N	A	L	Q	A
A	E	C	G	X	F	G	I	N	Q	W	Y	Z	C	B	B	D	R
P	S	X	A	R	B	F	C	E	N	T	E	R	O	Y	R	E	C
E	U	M	R	R	A	Y	J	I	M	O	R	R	I	S	Y	O	P
A	M	C	L	N	Q	M	R	E	D	X	P	I	D	A	V	I	D

Find as many of the following mathematical terms as possible. Draw a line through each word found.

- | | | | |
|-------------|---------------|-----------------|------------|
| 1. decimals | 11. math | 21. subtraction | 31. pi |
| 2. invert | 12. reduce | 22. arithmetic | 32. center |
| 3. fraction | 13. angle | 23. flowchart | 33. null |
| 4. set | 14. problem | 24. integer | 34. odd |
| 5. add | 15. numerical | 25. answer | 35. arc |
| 6. times | 16. algebra | 26. divide | 36. ray |
| 7. finite | 17. pentagon | 27. circle | 37. radii |
| 8. space | 18. rational | 28. square | 38. point |
| 9. equal | 19. diagram | 29. inverse | 39. sum |
| 10. graph | 20. numerator | 30. vertex | 40. chart |

Unit IX

FINANCE

A. Time Budget

Exercises

1. Give the time for one 24 hour day which you spent on things listed below and others not listed, which you feel should be listed.

	hrs.	%
a. T.V.	_____	_____
b. Study	_____	_____
c. Sports	_____	_____
d. School	_____	_____
e. Sleeping	_____	_____
f. Work at home	_____	_____
g. Recreation	_____	_____
h. Job away from home	_____	_____

2. If you do not have a job, budget your time so you can have a job away from home.

OR

If you have a job, budget your time so you can have a second job away from home or work longer hours, if possible.

ACTIVITY	TIME SPENT
a. _____	_____
b. _____	_____
c. _____	_____
d. _____	_____
e. _____	_____
f. _____	_____
g. _____	_____

3. Name one item you would like to buy. _____

Deductions

Exercises

1. Compute the following based on the fact that a job pays \$2.83 per hour and the work week is 40 hours.

GROSS PAY	_____
Deductions (Single-1 exemption)	
State Income Tax	<u>\$1.63</u>
Federal Income Tax	<u>\$17.10</u>
Social Security	<u>\$4.75</u>
TOTAL DEDUCTIONS	_____
NET PAY	_____

**TOOL AND
DIE MAKER**

IMMEDIATE OPENING RATE OF PAY COMPARES WITH NATIONAL SCALE. EXCELLENT WORKING CONDITIONS AND LIBERAL EMPLOYEE BENEFITS CALL US COLLECT AT ME 6-1206 ROGERS, ARKANSAS. AND ASK FOR H. L. BRYLES

2. Compute the following for a 46 hour week. The man earns \$2.83 per hour and is paid time and a half over-time for over 40 hours.

$\$2.83 \times 40 =$ _____
 $1\frac{1}{2} \times \$2.83 \times \underline{\hspace{1cm}} =$ _____

DAISY MFG. CO.
ROGERS, ARK.

GROSS PAY	_____
Deductions (Single-1 exemption)	
State Income Tax	<u>\$1.72</u>
Federal Income Tax	<u>\$21.10</u>
Social Security	<u>\$5.82</u>
TOTAL DEDUCTIONS	_____
NET PAY	_____

3. In problems 1 and 2
State Income Tax is what percent of salary?

(1) _____ (2) _____

Federal Income Tax is what percent of salary?

(1) _____ (2) _____

Social Security is what percent of your salary?

(1) _____ (2) _____

HOW TO FIND YOUR PARCEL POST ZONE FROM MEMPHIS USING YOUR POST OFFICE ZIP CODE NUMBER

Look for the first three numbers of your ZIP CODE on the following chart to determine parcel post zone from Memphis. For example: If you live in Amite, Louisiana and your ZIP CODE number is 70422, the first three (3) numbers 704 indicates your parcel post zone from Memphis is Zone 3.

ALABAMA	Parcel Post Zone	MISSISSIPPI	Parcel Post Zone
ZIP CODE NUMBERS beginning with: 350, 351, 354, 355, 356, 367, 369 are:	3	ZIP CODE NUMBERS beginning with: 386, 387, 388, 389 are:	1 & 2
ZIP CODE NUMBERS beginning with: 364, 365 are:	4	ZIP CODE NUMBERS beginning with: 390, 391, 392, 393, 394, 396, 397 are:	3
		ZIP CODE NUMBERS beginning with: 395 are:	4
ARKANSAS	Parcel Post Zone	MISSOURI	Parcel Post Zone
ZIP CODE NUMBERS beginning with: 716, 720, 721, 722, 723, 724, 725 are:	1 & 2	ZIP CODE NUMBERS beginning with: 637, 638, 639 are:	1 & 2
ZIP CODE NUMBERS beginning with: 717, 718, 719, 726, 728, 729 are:	3	ZIP CODE NUMBERS beginning with: 636, 654, 655, 656, 657 are:	3
KENTUCKY	Parcel Post Zone	TENNESSEE	Parcel Post Zone
ZIP CODE NUMBERS beginning with: 420 are:	1 & 2	ZIP CODE NUMBERS beginning with: 381 are:	Local
ZIP CODE NUMBERS beginning with: 421, 422, 424, 427 are:	3	ZIP CODE NUMBERS beginning with: 380, 382, 383 are:	1 & 2
ZIP CODE NUMBERS beginning with: 400 are:	4	ZIP CODE NUMBERS beginning with: 370, 371, 372, 373, 384, 385 are:	3
LOUISIANA	Parcel Post Zone		
ZIP CODE NUMBERS beginning with: 704, 710, 712, 713, 714 are:	3		
ZIP CODE NUMBERS beginning with: 700, 701, 703, 707, 708 are:	4		

PARCEL POST RATE TABLE

SHIPPING WEIGHT (16-oz. equal 1 lb.)	Local Zone	ZONE 1 and 2	ZONE 3	ZONE 4	ZONE 5	SHIPPING WEIGHT (16-oz. equal 1 lb.)	Local Zone	ZONE 1 and 2	ZONE 3	ZONE 4	ZONE 5	
Up to but not including 16 oz.		6c for the first 2 ounces and 2c for each additional ounce.					18 lbs. 1 oz. to 19 lbs.	\$1.05	\$1.70	\$2.00	\$2.30	\$2.55
16 oz. to 2 lbs.	60c	65c	70c	75c	80c	19 lbs. 1 oz. to 20 lbs.	1.05	1.75	2.05	2.40	2.95	
2 lbs. 1 oz. to 3 lbs.	60c	75c	80c	85c	95c	20 lbs. 1 oz. to 21 lbs.	1.10	1.85	2.10	2.45	3.05	
3 lbs. 1 oz. to 4 lbs.	65c	80c	85c	95c	\$1.10	21 lbs. 1 oz. to 22 lbs.	1.15	1.90	2.15	2.55	3.15	
4 lbs. 1 oz. to 5 lbs.	70c	85c	90c	\$1.05	1.20	22 lbs. 1 oz. to 23 lbs.	1.15	1.95	2.20	2.60	3.25	
5 lbs. 1 oz. to 6 lbs.	70c	95c	\$1.00	1.15	1.35	23 lbs. 1 oz. to 24 lbs.	1.20	2.00	2.25	2.65	3.35	
6 lbs. 1 oz. to 7 lbs.	75c	\$1.05	1.10	1.25	1.50	24 lbs. 1 oz. to 25 lbs.	1.20	2.05	2.30	2.75	3.45	
7 lbs. 1 oz. to 8 lbs.	75c	1.10	1.15	1.35	1.60	25 lbs. 1 oz. to 26 lbs.	1.20	2.10	2.35	2.85	3.55	
8 lbs. 1 oz. to 9 lbs.	80c	1.15	1.20	1.45	1.75	26 lbs. 1 oz. to 27 lbs.	1.25	2.15	2.40	2.90	3.70	
9 lbs. 1 oz. to 10 lbs.	80c	1.20	1.30	1.55	1.90	27 lbs. 1 oz. to 28 lbs.	1.25	2.20	2.45	2.95	3.80	
10 lbs. 1 oz. to 11 lbs.	80c	1.25	1.35	1.60	2.00	28 lbs. 1 oz. to 29 lbs.	1.30	2.25	2.50	3.05	3.90	
11 lbs. 1 oz. to 12 lbs.	85c	1.30	1.45	1.70	2.10	29 lbs. 1 oz. to 30 lbs.	1.30	2.30	2.55	3.10	4.00	
12 lbs. 1 oz. to 13 lbs.	85c	1.35	1.55	1.80	2.20	35 lbs.	1.45	2.55	2.85	3.45	4.50	
13 lbs. 1 oz. to 14 lbs.	90c	1.40	1.60	1.90	2.35	40 lbs.	1.55	2.80	3.15	3.85	5.00	
14 lbs. 1 oz. to 15 lbs.	90c	1.45	1.65	2.00	2.45	45 lbs.	1.70	3.05	3.40	4.20	5.55	
15 lbs. 1 oz. to 16 lbs.	95c	1.55	1.75	2.05	2.55	50 lbs.	1.80	3.25	3.70	4.60	6.05	
16 lbs. 1 oz. to 17 lbs.	\$1.00	1.60	1.80	2.15	2.65	55 lbs.	1.95	3.45	4.00	4.95	6.55	
17 lbs. 1 oz. to 18 lbs.	1.00	1.65	1.90	2.20	2.75	60 lbs.	2.05	3.65	4.30	5.35	7.00	
						65 lbs.	2.20	3.85	4.60	5.70	7.45	
						70 lbs.	2.30	4.05	4.85	6.05	7.85	

POSTAL MONEY ORDER, AMERICAN EXPRESS AND PARCEL POST C.O.D. FEES

C.O.D. FEES	POSTAL MONEY ORDER FEES	AMERICAN EXPRESS MONEY ORDER FEES
Up to \$10.00..... 70c	Up to \$10.00..... 25c	Up to \$200.00..... 35c*
\$10.01 to \$25.00..... 80c	\$10.01 to \$50.00..... 35c	*Exception 30c or 40c in some areas.
\$25.01 to \$50.00..... 90c	\$50.01 to \$100.00..... 40c	Check your local American Express Agency.
\$50.01 to \$100.00..... \$1.00		
\$100.01 to \$200.00..... 1.10		

For amounts over \$100, purchase additional money orders at above rates. American Express money orders can be purchased at any American Express Agency. Postal money orders can be purchased at any post office or through your carrier on rural routes. On C.O.D. orders we bill you for C.O.D. collection fees and money order fees which we must pay the post office.

Complete the order blank on the following page. Use your own name and address and the current date.

- Find the total price of each item.
- Find the total for goods.
- What is the tax on the order?
- How do you want the order shipped?
- What is the weight of the order in pounds and ounces?
- What is total weight in pounds?
- What is your zip code?
- What is your total cash price?
- What is the amount of the money order?
- How much is the money order fee?
- What postage do you put on the letter?
- How much cash does it take to pay the money order clerk, including your stamp for letter?
- What square do you mark in the lower left hand corner if this is a cash order?
- Would it be cheaper to send a Money Order or Check?
- What does C.O.D. mean?
- Which is cheaper, cash or C.O.D.? Why?

Exercises

Send Mail Orders to:
SEARS, ROEBUCK AND CO.
 495 N. Watkins
 Memphis, Tennessee 38102

OR, use this handy form when you place your order by phone or in person at Sears Catalog Sales Office, Sears Retail Catalog Dept. or Sears Authorized Catalog Sales Merchant.



Date _____ 19____

PLEASE BE SURE TO INCLUDE ZIP CODE IN YOUR ADDRESS

PLEASE DO NOT WRITE IN THIS SPACE

%2-0- _____

NO. ORDERS _____ BATCH NO. _____

%3-0- - - -5- - & _____

OP. OR. NO. TP. MTH. ADJ. NO. NO. LN. SL. SHP. CASH

ACCT. NO. _____ TERMS _____ CONT. LIFE _____ DEF. CODE _____

#E - - - -

Brch CODE _____ SHP CHGE. _____ TAX % _____ ZONE _____

All members of the same household should order under one name

PLEASE PRINT PLAINLY ONE LETTER IN EACH SQUARE

MY SEARS CREDIT ACCOUNT NUMBER IS: _____ PLEASE DO NOT WRITE IN THIS SPACE

NAME _____

Mailing Address _____

Post Office _____ State _____

Telephone No. _____ Zip Code _____

PLEASE DO NOT WRITE IN THIS SPACE

SHIP TO ANOTHER ADDRESS? If you want this order shipped to another person or to a different address, freight or express station, give address here:

Name _____

Mailing Address _____

Post Office _____ State _____ Zip Code _____

IF YOUR ADDRESS HAS CHANGED since last order, please give your old mailing address here:

Mailing Address _____

Post Office _____ State _____ Zip Code _____

STATE COLOR OR PATTERN CHOICE BY NUMBER WHERE REQUESTED

CATALOG NUMBER	HOW MANY	NAME OF ITEM	COLOR NO. Pattern, Finish, Etc.	SIZE Measure to be used	PRICE Ea., Yd., Pr., Etc.	TOTAL PRICE Dollars Cents	SHPG. Lbs. Oz.	WT. Oz.
1 \$7R7211	- 1	AM radio	Blue		17 59		1 4	
2 119R8307	- 1	Swim trunks	Green	34	7 08			15
3 6 F 2448	- 1	Football			8 67		1 10	
6F 5057C	- 2	Bike tires	Black		1 89		6 0	
5	-							
6	-							
7	-							
8	-							
9	-							
10	-							
11	-							

ARKANSAS, LOUISIANA, MISSOURI or TENNESSEE customers add 3c tax for each dollar of goods. LOUISIANA and TENNESSEE customers also add local tax if required by your city, county or parish.

ALABAMA customers add 4c tax for each dollar of goods.

KENTUCKY or MISSISSIPPI customers add 5c for each dollar of goods.

Tax rates based on information available at printing and subject to change.

HOW SHALL WE SHIP? Parcel Post Express Freight (Rail or Truck)

Add this to my

- SEARS REVOLVING CHARGE ACCOUNT,
- SEARS EASY PAYMENT PLAN or
- MODERNIZING CREDIT PLAN RETAIL INSTALLMENT CONTRACT AND SECURITY AGREEMENT, which is incorporated herein by reference.

ENTER ACCOUNT NUMBER IN THE SPACE PROVIDED ABOVE.
 AT WHICH SEARS STORE IS YOUR ACCOUNT CARRIED?
(DO NOT SEND IDENTIFICATION CARD OR PLATE)

Signature of the Head of Household

(WRITE—DO NOT PRINT)

TOTAL FOR GOODS

AMOUNT FOR TAX

If credit order, we will figure and bill this in for you

POSTAGE

Amount I owe Sears on previous order

TOTAL CASH PRICE

AMOUNT ENCLOSED

Sears Checks
 Money Order or Check

Total Pounds Total Ounces

Total Weight in Pounds

Enter Parcel Post Zone No.

See yellow pages for shipping information

E
 Sears 665

Practical Application

Send Mail Orders to:
SEARS, ROEBUCK AND CO.
 495 N. Watkins
 Memphis, Tennessee 38102

Or, use this handy form when you place your order by phone or in person at Sears Catalog Sales Office, Sears Retail Catalog Dept. or Sears Authorized Catalog Sales Merchant.



Date _____ 19__

PLEASE BE SURE TO INCLUDE
 ZIP CODE IN YOUR ADDRESS

PLEASE DO NOT
 WRITE IN THIS SPACE

%2-0- - - - - - **C**
 NO. ORDERS BATCH NO. **R**

%3-0- - - - - - **C**
 OP. OR. NO. TP. MTH. ADJ. **R**
 NO. NO. LN. SL. SHP. CASH

ACCT. NO. **TERMS** **CONT. DEF.** **CODE** **C**
IF - - - - - **R**
 Brch SHP TAX ZONE **C**
 CODE CHGE. %

All members of the same household should order under one name

PLEASE PRINT PLAINLY ONE LETTER IN EACH SQUARE

MY SEARS CREDIT ACCOUNT NUMBER IS:

PLEASE DO NOT WRITE IN THIS SPACE

NAME _____

Mailing Address _____

Post Office _____ State _____

Telephone No. _____ Zip Code _____ **C**

PLEASE DO NOT WRITE IN THIS SPACE

SHIP TO ANOTHER ADDRESS? If you want this order shipped to another person or to a different address, freight or express station, give address here:

Name _____

Mailing Address _____

Post Office _____ State _____ Zip Code _____

IF YOUR ADDRESS HAS CHANGED since last order, please give your old mailing address here:

Mailing Address _____

Post Office _____ State _____ Zip Code _____

STATE COLOR OR PATTERN CHOICE BY NUMBER WHERE REQUESTED

CATALOG NUMBER	HOW MANY	NAME OF ITEM	COLOR NO. Pattern, Finish, Etc.	SIZE Measure in size	PRICE		TOTAL PRICE Dollars	PRICE Cents	SHPG. Lbs.	WT. Oz.
					Ea., Yd., Ft., Etc.					
1	-		-							
2	-		-							
3	-		-							
4	-		-							
5	-		-							
6	-		-							
7	-		-							
8	-		-							
9	-		-							
10	-		-							

LOUISIANA customers add 2c tax for each dollar of goods.
 LOUISIANA customers also add local tax if required by your city or parish.
 ARKANSAS, MISSOURI or TENNESSEE customers add 3c tax for each dollar of goods.
 TENNESSEE customers also add 1c or 1½c county tax if applicable.
 ALABAMA customers add 4c tax for each dollar of goods.
 MISSISSIPPI or KENTUCKY customers add 5c for each dollar of goods.
 Tax rates based on information available at printing and subject to change.

HOW SHALL WE SHIP? Parcel Post Express Freight (Rail or Truck)

Add this order to my REVOLVING CHARGE ACCOUNT
 EASY PAYMENT PLAN ACCOUNT Do not send identification card or plate
 MODERNIZING CREDIT PLAN ACCOUNT

ENTER ACCOUNT NUMBER IN THE SPACE PROVIDED ABOVE,
 AT WHICH SEARS STORE IS YOUR ACCOUNT CARRIED? _____

Signature of the Head of Household _____

(WRITE—DO NOT PRINT)

TOTAL FOR GOODS		Total Pounds	Total Ounces
← AMOUNT FOR TAX		Total Weight in Pounds	
If credit order, we will figure and bill this in for you	POSTAGE	Enter Postal Post Zone No.	
Amount I owe Sears on previous order		See other side for shipping information	
TOTAL CASH PRICE			
AMOUNT ENCLOSED	Sears Checks		
	Money Order or Check		

EP883 5-79
 Printed in U.S.A.

D. Banking

Exercises

Assume your bank balance on the 1st of the month was \$328.78. Using pages 207, 208, 209, write the checks, fill out the deposit slips, and check register for the following: Make checks to whomever you please. Be sure to state the reason each check was written.

<u>Month</u>	<u>Day</u>	<u>Check or Deposit</u>
_____	2	Deposited \$50.70
_____	3	Checks for \$5.06, \$10.50, \$15.00
_____	7	Deposited \$210.15, Checks \$25.00 and \$6.79
_____	10	Checks \$71.95 and \$38.76
_____	15	Check \$19.95, Deposited \$17.64 and \$95.00
_____	20	Deposited \$17.50, Check for \$225.00
_____	29	Deposited \$62.50

What is your bank balance at the end of the month?

How Much Money?

When Bill bought his lunch at school, it cost him half the money that he had brought from home. After school he bought a candy bar for 10 cents, and also had a snack at a diner. The snack cost half the money he had left. He left a five-cent tip at the diner.

Then Bill spent seven-eighths of his remaining money on a magazine. When he reached home, he had a nickel in his pocket.

How much money did Bill have when he started out?

LITTLE RIVER Bank

No. _____

LEPANTO, ARKANSAS, _____ 19 _____

81-622
841

PAY TO THE ORDER OF _____ \$ _____

_____ DOLLARS

FOR _____

⑆0841⑆0622⑆

LITTLE RIVER Bank

No. _____

LEPANTO, ARKANSAS, _____ 19 _____

81-622
841

PAY TO THE ORDER OF _____ \$ _____

_____ DOLLARS

FOR _____

⑆0841⑆0622⑆

LITTLE RIVER Bank

No. _____

LEPANTO, ARKANSAS, _____ 19 _____

81-622
841

PAY TO THE ORDER OF _____ \$ _____

_____ DOLLARS

FOR _____

⑆0841⑆0622⑆

Exercises

STATEMENT OF ACCOUNT

U. R. Teck
711 West Ave. D
Hope, Ark. 71801

Checks	Deposits	Date	Balance
Balance brought forward	\$ 395.45	11-1-71	
\$ 23.49-		11-2-71	
7.83- 2.93-		11-5-71	
121.23-	101.01+	11-8-71	
40.00-		11-11-71	
12.49- 7.85-		11-15-71	
79.38-	240.38+	11-18-71	
32.45- 16.34-		11-19-71	
11.23-		11-20-71	
236.70-		11-23-71	
78.34-		11-24-71	
4.46-		11-26-71	
38.39- 2.98-		11-28-71	
	240.38+	11-30-71	

FIND THE BALANCE AT THE END OF EACH DAY

CITIZENS NATIONAL
Bank
HOPE, ARKANSAS

Exercises

\$25 Bond - Maturity Value of Bonds Bought After June 1, 1970

<u>PERIOD HELD</u>	<u>REDEMPTION VALUE</u>
First 1/2 year	\$18.75
1/2 to 1 year	19.05
1 year to 1 1/2 year	19.51
1 1/2 year to 2 years	19.95
2 years to 2 1/2 years	20.40
2 1/2 years to 3 years	20.88
3 years to 3 1/2 years	21.39
3 1/2 years to 4 years	21.93
4 years to 4 1/2 years	22.53
4 1/2 years to 5 years	23.16
5 years to 5 1/2 years	23.82
5 1/2 years to 5 years 10 months	24.51
5 years 10 months from issue date.	25.73

Note: "E" Bonds have a 1/2% bonus rate added if held to maturity, raising the yield to 5 1/2% from issue date to maturity.

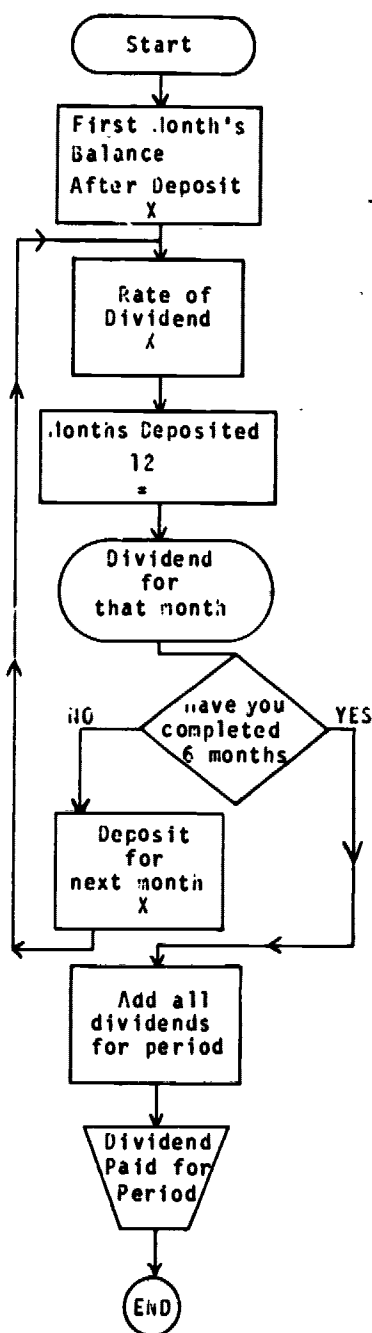
You are saving \$6.25 per month on a payroll savings plan.

- How many months until you can buy a \$25 savings bond?
- In 2 years how much would you have saved?
- If you started on January 1, 1971, when will you buy your first bond?
- (a) Find the number of years and months from time bought to January 1, 1973 for each bond bought.
 (b) Find the accumulated value of each of these bonds you have bought using the redemption value table.

<u>Date Bought</u>	<u>Years and Months to Jan. 1, 1973</u>	<u>Accumulated Value</u>
March 1, 1971	_____	_____
June 1, 1971	_____	_____
September 1, 1971	_____	_____
December 1, 1971	_____	_____
March 1, 1972	_____	_____
June 1, 1972	_____	_____
September 1, 1972	_____	_____
December 1, 1972	_____	_____

- How much interest has been earned?

Exercises



You put \$6.25 into a savings account on the first of each month for 2 years starting January 1, 1971

How dividends are computed:

$$6.25 \times .0475 \times \frac{6}{12} = .148437 \quad 6.25 \times .0475 \times \frac{3}{12} = .074218$$

$$6.25 \times .0475 \times \frac{5}{12} = .123697 \quad 6.25 \times .0475 \times \frac{2}{12} = .049479$$

$$6.25 \times .0475 \times \frac{4}{12} = .098958 \quad 6.25 \times .0475 \times \frac{1}{12} = .024739$$

.519528

Do not round off dividends until after you add.

1. What is the rate of dividend?
2. Amount of dividend earned for March deposit?
3. Total dividends first six mo.

Continue finding dividends on deposits through December 31, 1972 and record on next page.

4. Second six months
5. Third six months.
6. Fourth six months

What is "first month's balance after deposit" for:

7. July, 1971
8. January, 1972
9. July, 1972
10. What is my balance after dividend for: December, 1972
11. What was total earnings on savings account?
12. Which earned more--savings account or savings bond?
13. How much more?

Date	Memo.	Earnings Dividend	Withdrawals	Savings Added	Balance
1 Jan. 1, 71				\$6.25	6.25
2 Feb. 1, 71				6.25	12.50
3 Mar. 1, 71				6.25	18.75
4 April 1, 71				6.25	25.00
5 May 1, 71				6.25	31.25
6 June 1, 71				6.25	37.50
7 June 30, 71	Dividend 4 3/4%	\$.52			38.02
8 July 1, 71				6.25	44.27
9 Aug. 1, 71					
10 Sept. 1, 71					
11 Oct. 1, 71					
12 Nov. 1, 71					
13 Dec. 1, 71					
14 Dec. 31, 71	Dividend 4 3/4%				
15 Jan. 1, 72					
16 Feb. 1, 72					
17 Mar. 1, 72					
18 April 1, 72					
19 May 1, 72					
20 June 1, 72					
21 June 30, 72	Dividend 4 3/4%				
22 July 1, 72					
23 Aug. 1, 72					
24 Sept. 1, 72					
25 Oct. 1, 72					
26 Nov. 1, 72					
27 Dec. 1, 72					
28 Dec. 31, 72	Dividend 4 3/4%				



**FIRST
NATIONAL**
Trust and
Savings Bank

E. Car Expenses

Expenses

Cost of Operating a Second Hand Car

Don Jones:
1967 Buick Wildcat
11825 miles

Expenses:

947 gal. gas	at	\$.339	_____
43 qts. oil	at	.55	_____
9 lube jobs	at	1.50	_____
2 oil filters	at	2.85	_____
1 air filter	at	3.65	_____
2 head lamps	at	.88	_____
1 muffler	at	9.88	_____
1 tail pipe	at	5.25	_____
8 spark plugs	at	1.03	_____
2 sets points	at	1.05	_____
2 tires	at	21.45	_____
1 battery	at	18.95	_____
2 battery cables	at	1.00	_____
4 spinner hubcaps	at	7.95	_____
2 rear view mirrors	at	3.25	_____
License - State	\$19.00	} Sub Total	_____
City	5.00		
Driver's	2.00		
Depreciation	\$450.00	-----	_____
Interest on bank loan			_____
\$1000 at 5.5%	\$55.00		_____
Insurance - Comprehensive (5-10-5)	\$208.00		_____
Repair--minor wreck	\$98.47		_____
Seven flats at \$1.25			_____
Total			_____
Average cost per mile			_____

Practical Application



LINCOLN-MERCURY
DIVISION OF

Ford Marketing Corporation

	SUGGESTED RETAIL PRICE	
MONTEREY CUSTOM 4DR PIL/HT	4030 00	U
INCLUDES AT NO EXTRA COST		
400 CID ENGINE, PWR STEERING	NC	
SELECT-SHIFT TRANSMISSION	NC	
POWER FRONT DISC BRAKES	NC	
PROTECTIVE BODY MOLDINGS	NC	
DELUXE WHEEL COVERS	NC	
DELUXE STEERING WHEEL	NC	
POWER VENTILATION SYSTEM	NC	
DARK GREEN METALLIC		
DELUXE ALL VINYL INTERIOR	NC	
DARK GREEN VINYL ROOF	119 20	U
WSP G-78X15 BELTED TIRES	32 40	
FRONT BUMPER GUARDS	9 10	
FENDER SKIRTS	36 30	
WHISPER-AIRE CONDITIONER	441 70	
AM RADIO	66 10	
REMOTE CTL LEFT HAND MIRROR	13 00	
TINTED GLASS - COMPLETE	51 90	
	<u>168 00</u>	U
D & D SCHEDULE B	4967 70	
TOTAL		

D & D SCHEDULE B
TOTAL

168 00
4967 70

SOLD TO

HOPE AUTO CO
220 WEST 2ND ST
HOPE

AR 71801

ALL MERCHANDISE COVERED BY THIS INVOICE IS ACCEPTED FOR TRANSPORTATION BY THE CARRIER AND IS IMMEDIATELY SUBJECT TO THE TERMS OF THE BILL OF LADING, CUSTOMARILY USED BY THE PARTIES FOR SIMILAR SHIPMENTS.

SHIP TO (IF OTHER THAN ABOVE)

SHIP THROUGH

VEHICLE IDENTIFICATION NO.

FINAL ASSEMBLY POINT

METHOD OF TRANSP.

DEALER NO.

12545618650

ST LOUIS

RAIL

26F 277 RC37

THIS INVOICE TO BE USED FOR THE BILLING & SHIPPING OF VEHICLES ONLY

TRANSPORTATION CO. COPY

Use the Dealer Statement of Transaction blank to complete the papers for the purchase of a car based on the following facts.

- Down payment \$550
- Trade in \$1450 - (68 Mustang)
- Comprehensive insurance \$335
- Finance charges and credit life is 5.8% of the principal amount financed
- 3% sales tax and \$19.00 license

ACCOUNT NO. **ARKANSAS AUTOMOBILE RETAIL INSTALMENT CONTRACT** DATE _____

Buyer (and Co-Buyer) - Name and Address (include - County and Zip Code)

Seller - Name and Address

Buyer (which means the undersigned Buyers and Co-Buyers, jointly and severally) having been quoted both a time sale price and a lesser cash price hereby purchases from Seller on a time price basis, upon the terms and conditions set forth on the face and reverse sides hereof, the following property (hereinafter called the "Property") delivery and acceptance of which in good order hereby are acknowledged by Buyer.

New or Used	Year and Make	Series	Body Style	No. Cyl.	If Truck Ton Capacity	Manufacturer's Serial Number	Use For Which Purchased
							<input type="checkbox"/> Personal <input type="checkbox"/> Agriculture <input type="checkbox"/> Business

INCLUDING:

- Radio
 Air Conditioner
 Automatic Transmission
 Power Steering
 Power Brakes
 Power Seats
 Power Windows

DESCRIPTION OF TRADE IN

_____ \$ _____ (Gross Allowance)
 (Year and Make)

_____ \$ _____ (Amount Owing)
 (Serial Number)

OPTIONAL INSURANCE

Buyer authorizes Seller to obtain the following insurance coverages:

(a) Automobile Physical Damage Insurance: Coverages checked below for a term of _____ months (or for such shorter term as the insurer to whom Seller shall apply therefor will provide for the amount included herein) from the date hereof, payable to Buyer or Seller as interests may appear:

- Comprehensive
 Fire-Theft & Combined Additional Coverage } \$ _____ (a)
- \$ _____ Deductible Collision
 Towing & Labor Costs (\$25.00 Limit) }

(b) Credit Life Insurance on the life of _____ (Insured Person)

- Provided under Ford Life Insurance Company's Group Policy No. 2200 in accordance with the "Credit Life Insurance Eligibility" section below. } \$ _____ (b)
- Provided by _____ in accordance with the separate Application, Notice, Certificate or Policy delivered to Buyer this date.

(c) Credit Accident and Health Insurance provided by _____

in accordance with the separate Application, Notice, Certificate or Policy delivered to Buyer this date \$ _____ (c)

(d) Other Optional Insurance \$ _____ (d)

Total Cost of Optional Insurance \$ _____

NOTICE TO BUYER: (1) You are not required to obtain the Credit Life and/or Credit Accident and Health Insurance for which a charge is indicated above and such is not a factor in the Seller's approval of this credit. (2) You have the right to choose the person through whom the Automobile Physical Damage Insurance required under this contract is to be obtained. **ACKNOWLEDGING** the foregoing, BUYER requests and authorizes SELLER to obtain each insurance coverage for which an amount is included above.

_____ Date
 (Cost of Insurance to be included only if signed and dated by Buyer)

DETAILS OF TRANSACTION

- (1) Cash Price \$ _____ (1)
 Cash Down Payment \$ _____
 Trade In (See Opposite) \$ _____
- (2) Total Down Payment \$ _____ (2)
- (3) Unpaid Balance of Cash Price (Difference between Items 1 & 2) \$ _____ (3)
- (4) Other Charges
- Optional Insurance (See Opposite) \$ _____
 Official Fees \$ _____
 Taxes (Not included in Cash Price) \$ _____
 License, Title & Registration Fees \$ _____
 Total Other Charges \$ _____ (4)
- (5) Unpaid Balance - Amount Financed \$ _____ (5)
- (6) FINANCE CHARGE \$ _____ (6)
- (7) ANNUAL PERCENTAGE RATE _____ % (7)
- (8) Total of Payments (Sum of Items 5 & 6) \$ _____ (8)
- (9) Payment Schedule: Buyer hereby agrees to pay to Seller the Total Payments (Item 8 above) in _____ monthly instalments of \$ _____ each and one final instalment of \$ _____ on the like day of each month commencing _____ 19____, or, if no date is specified, one month after the date of this contract.



Exercises

Computing the cost of operating a new car

Name: Sam Bennett

Kind of Car: Plymouth Duster

Miles driven: 18,725

Expenses		Total
1440 gallons gas	at \$.339	_____
36 quarts oil	at .75	_____
9 lube jobs	at 1.50	_____
2 oil filters	at 2.70	_____
1 air filter	at 4.10	_____
License--State	\$19.00	_____
Sales tax	\$75.00	_____
Driver's license	2.00	_____
Depreciation	\$850.00	_____
Interest on bank loan \$2500 at 5.8%		_____
Insurance--comprehensive 10-20-5 (male--under 25)	\$233.40	_____
	Total	_____
	Average cost per mile:	_____

WELCH'S GRAPE JUICE

**SPARE-TIME FROZEN
MEAT PIES**
8 6-oz. For **\$1**

3 1 PT. 8-OZ. BTLs. **\$1.**

**SHARPNE ORANGE
JUICE**
6 6-oz. For **\$1**

WHOLE KERNEL NIBLETS CORN..... 4 12-OZ. CANS 89¢

**CUT CORN OR CUT
OKRA**
6 10-oz. For **\$1**

EXERCISES

- How many items are advertised on this page? _____
- What is the price of 1 meat pie? _____
- What is the price of 1 can of corn? _____
- What is the price of 1 can of vienna sausage? _____
- What is the price of 1 bottle of grape juice? _____
- What is the price per ounce of Treet? _____
- What is the price per ounce of okra? _____
- What is the price per ounce of peanut butter? _____

Peanut Butter
Peter Pan Smooth or Crunchy 12-Oz. Jar **39¢**

One item is shown at two prices. At which price would it cost less per item?

Sausage Armour Vienna **4** 5-Oz. Cans **89¢**

Orange Juice
Kroger Frozen Fresh from Florida **3** 6-Oz. Cans **49**

TREET Armour's All Purpose Luncheon Meat 12-Oz. Can **49¢**

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Exercises

Quantity and size	Item	Cost	Retail Cost Per Unit	Mark up Per Unit	% of Mark up
10/5#	C & H Sugar	\$ 6.01	.59	_____	_____
6/10#	C & H Sugar	5.90	1.19	_____	_____
48/tall	Pet Milk	7.80	3/.53	_____	_____
10/qt.	Soap Powder	6.60	.71	_____	_____
24/1#	Folgers Coffee	18.80	.79	_____	_____
24/8oz.	Pillsbury Biscuits	1.72	3/.25	_____	_____
1-1/2 gal.	Foremost Milk		.51	_____	_____
24/4oz.	Gerber Baby Food	3.20	5/.59	_____	_____
10/5#	Pillsbury Flour	5.90	.67	_____	_____
24/2oz.	Martha White Corn Bread Mix	1.92	.10	_____	_____
4/6ct.	Can Coca Cola	2.40	.73	_____	_____
4/6ct.	One Way Pepsi	1.80	.55	_____	_____





SAFEGWAY

Exercises

Circle the better buys.

- | | | | |
|----|-------------------------|-----------------|----------|
| 1. | "Cokes" | 16 oz. | 53¢ ctn. |
| | | 10 oz. | 43¢ ctn. |
| | | 6 oz. | 37¢ ctn. |
| 2. | Lucerne Milk | 1/2 gal. ctn. | 53¢ |
| | | 1 gal. ctn. | 99¢ |
| 3. | Folger's Inst. Coffee | 10 oz. | \$1.79 |
| | | 6 oz. | .99 |
| | | 2 oz. | .49 |
| 4. | Town House Orange Juice | 18 oz. | 5/1.00 |
| | | 1 qt. 14 oz. | .39 |
| 5. | Morrell Canned Ham | 5 lb. | \$5.49 |
| | | 3 lb. | 3.39 |
| 6. | Domino Sugar | 5 lb. | .65 |
| | | 10 lb. | 1.19 |
| 7. | Hiway Peaches | 1 lb. can | 4/1.00 |
| | | 1 lb 13 oz. can | 3/1.00 |



- | | | | |
|-----|---------------------------|--------------|--------|
| 8. | Mrs. Wright's Biscuits | 8 oz. can | 3/25¢ |
| | | 4 oz. can | 2/15¢ |
| 9. | Nabisco Crackers | 1/2 lb. box | 27¢ |
| | | 1 lb. box | 35¢ |
| | | 2 lb. box | 67¢ |
| 10. | Hormel Weiners | 12 oz. pkg. | 59¢ |
| | | 1 lb. pkg. | 69¢ |
| 11. | Campbell's Pork and Beans | 1 lb. | 6/1.00 |
| | | 1 lb. 12 oz. | 3/1.00 |
| 12. | Pride of Illinois Corn | 15 oz. | 2/45¢ |
| | Highway Cream Corn | 15. oz. | 5/1.00 |
| 13. | Mrs. Wright's Bread | 20 oz. | 3/73¢ |
| | Holsum Bread | 1 lb. | 31¢ |
| 14. | Bel Air Frozen Corn | 2 lbs. | 59¢ |
| | Hills-of-Home Frozen Corn | 1-1/2 lbs. | 39¢ |
| 15. | Wrigley's Gum | | 5/19¢ |
| | Dentyne Gum | | 6/23¢ |

Exercises

Cost of Feeding a Family

1. This table shows the cost of feeding a family in the South for one week. Using the table and the adjustments, find the cost of feeding your family.

		SOUTH		
		LOW COST	MEDIUM COST	HIGH COST
CHILDREN	UNDER 1 YEAR	2.80	3.50	3.90
	1 - 3 years . . .	3.40	4.20	4.90
	4 - 6 years . . .	3.90	5.10	6.20
	7 - 9 years . . .	4.70	6.10	7.10
	10 -12 years . . .	5.40	7.30	8.50
GIRLS	13 -15 years . . .	5.70	7.70	9.00
	16 -19 years . . .	5.80	7.70	9.10
BOYS	13 -15 years . . .	6.20	8.40	9.80
	16 -19 years . . .	7.20	9.80	11.30
WOMEN	20 -34 years . . .	4.80	6.70	7.90
	35 -54 years . . .	4.70	6.50	7.70
	55 -74 years . . .	4.40	6.20	7.30
	75 & over	4.30	5.80	6.80
MEN	20 -34 years . . .	6.30	8.50	9.90
	35 -54 years . . .	5.90	8.00	9.10
	55 -74 years . . .	5.60	7.60	8.70
	75 & over	5.40	7.30	8.40

- IF YOU ARE USING A FAMILY OF 1 ADD 20%
- 2 ADD 10%
- 3 ADD 5%
- 4 USE AS IS
- 5 SUBTRACT 5%
- 6 OR MORE SUBTRACT 10%

2. Using a merchandising list, make up a grocery list for feeding a family of four for one week. Use a family of 4 including a father, mother, teen-ager, and one baby girl. Find the total cost.

3. Using the merchandising list on page 220, determine if it is always, sometimes, or never cheaper to buy the economy size.

Record Party

Time: 8:00p.m.

Limited to 9 couples

Place: Betty's house

Refreshments: cokes and spudnuts

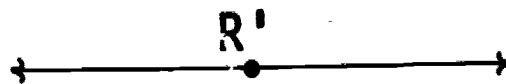
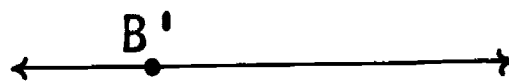
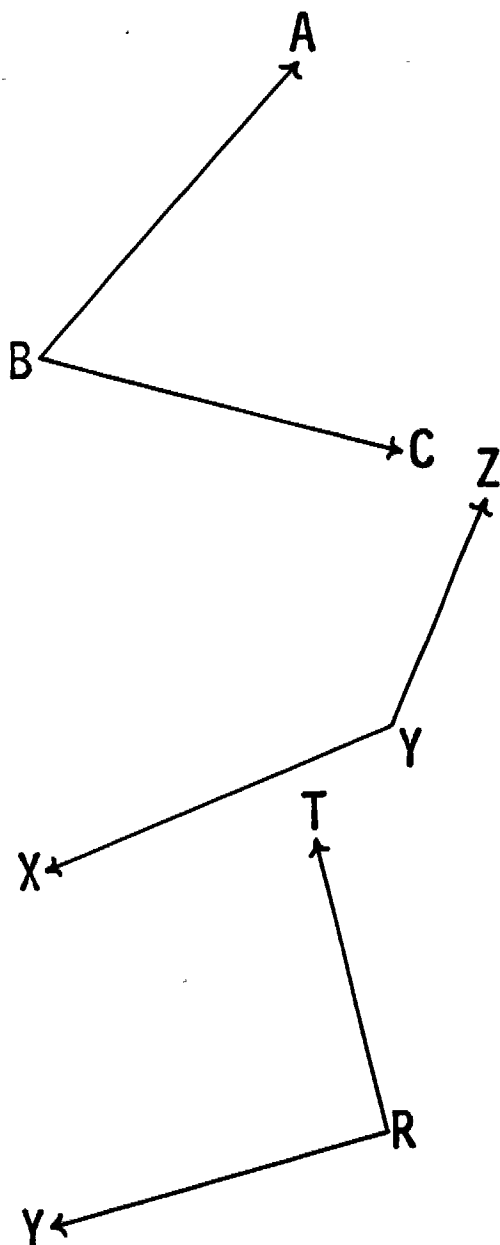
Betty figures 2 cokes and 3 spudnuts per person. If cokes cost \$1.72 per case and spudnuts cost 59¢ a dozen, what is the expected total cost of the party and how much is each person's share of the cost?

UNIT X
CONSTRUCTION

A. Congruent Angles

Exercises

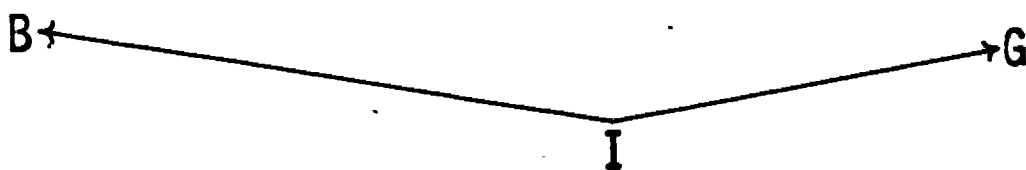
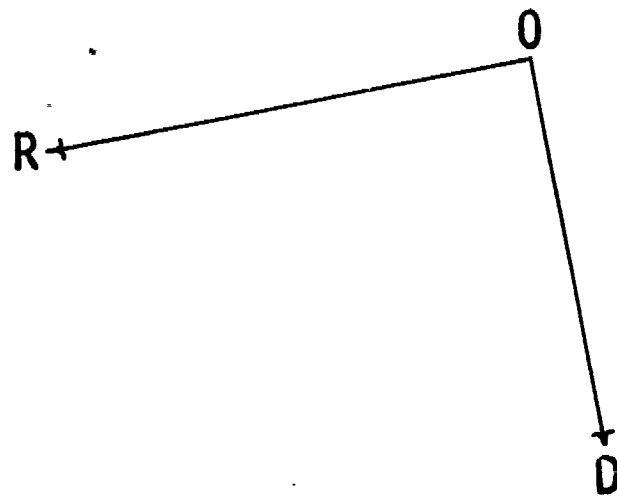
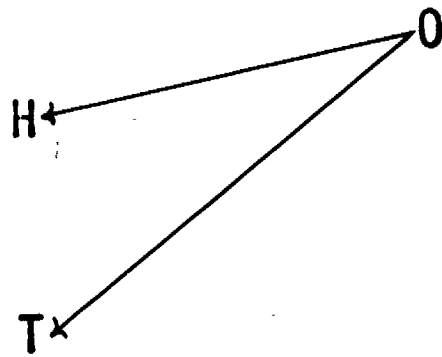
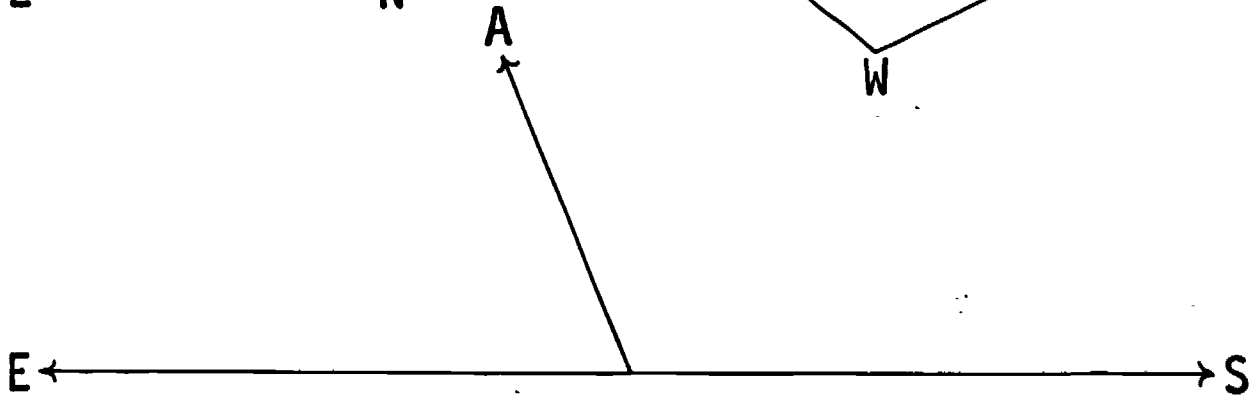
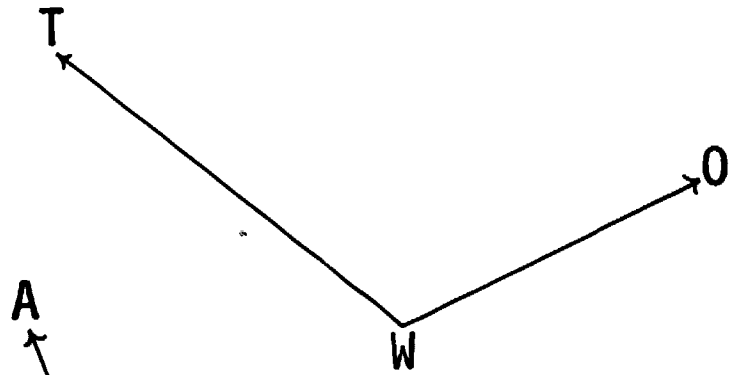
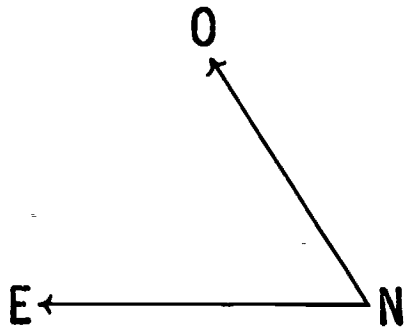
Construct an angle congruent to each given angle.



B. Angle Bisector

Exercises

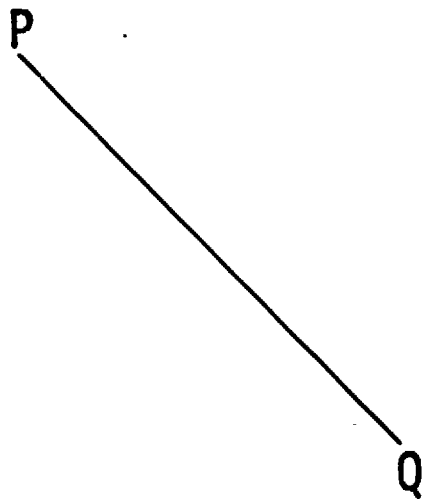
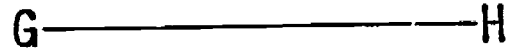
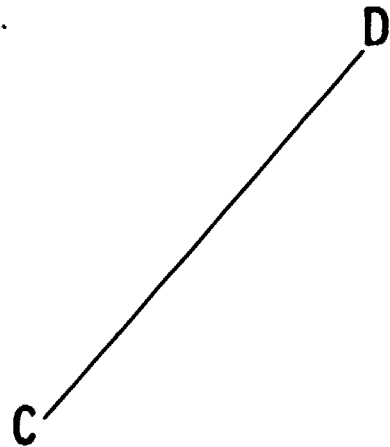
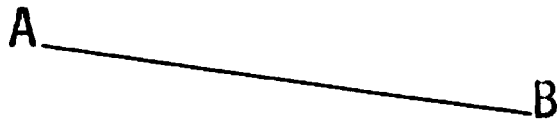
Bisect each given angle



C. Perpendicular Bisector

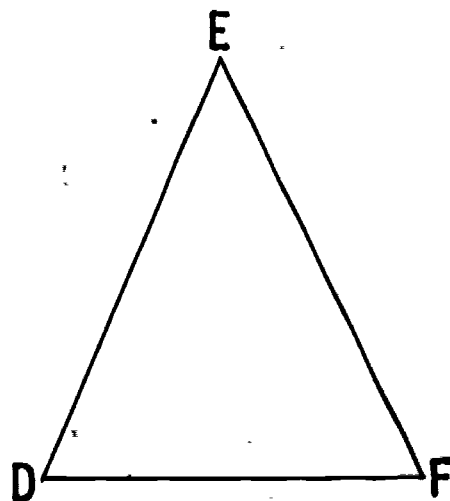
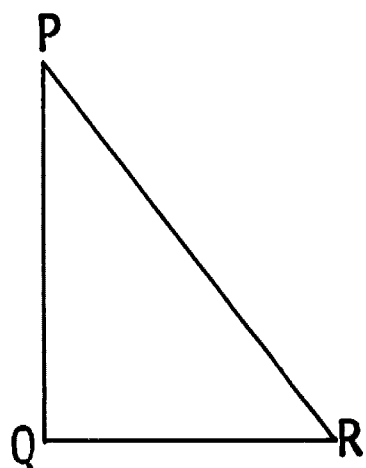
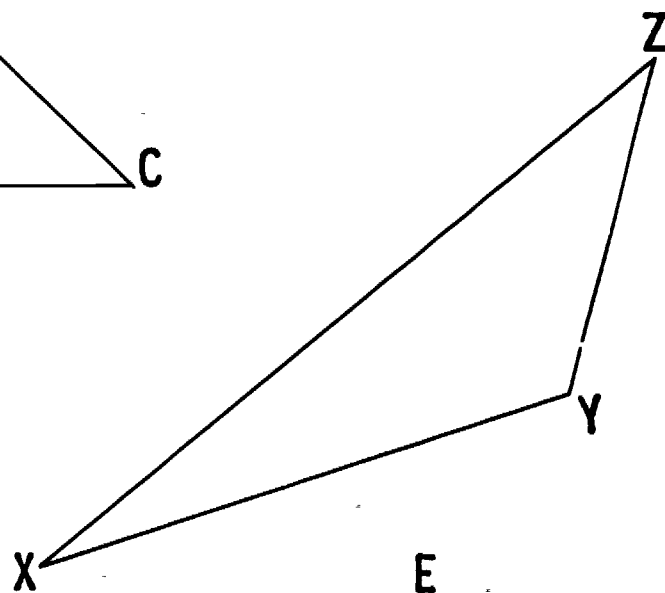
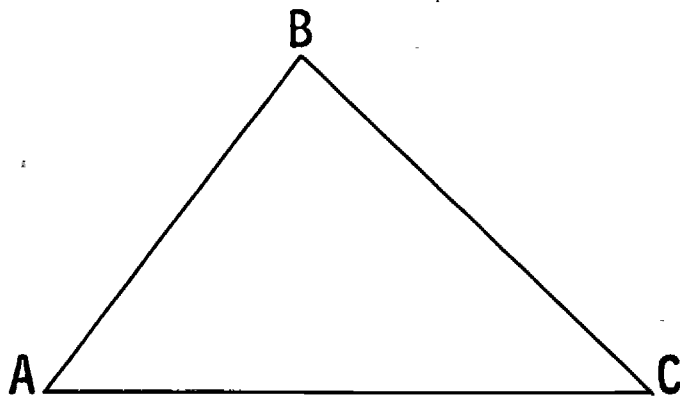
Exercises

Construct a perpendicular bisector of each line segment.



Exercises

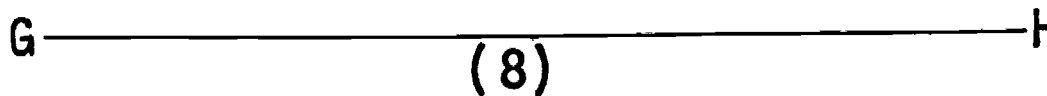
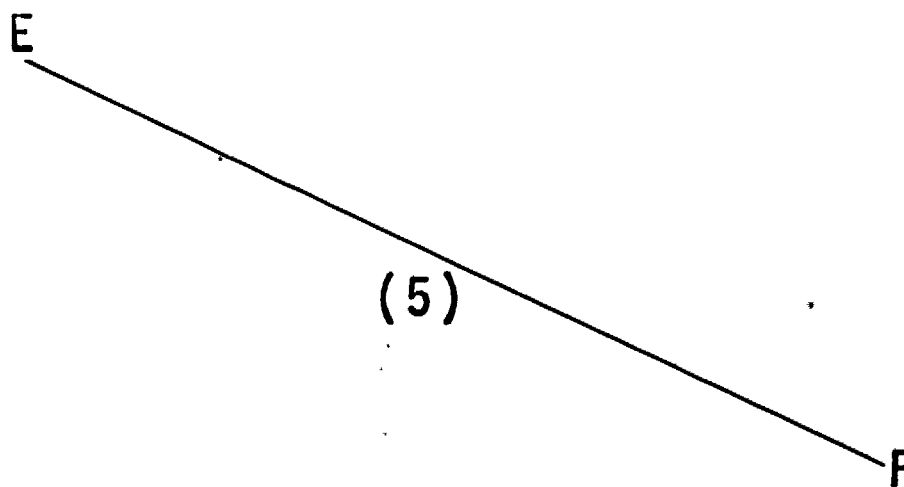
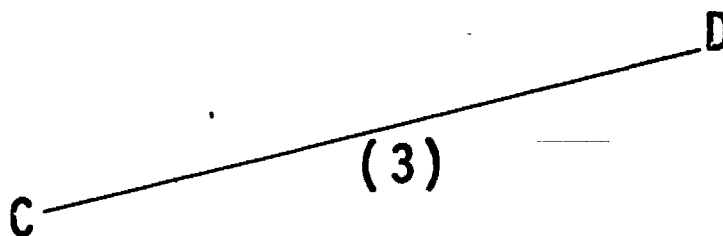
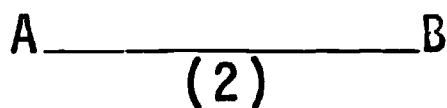
Construct the perpendicular bisectors of all three sides of the triangles. Then use the point of intersection as the center and circumscribe circles about the triangles.



D. Equal Line Segments

C Exercises

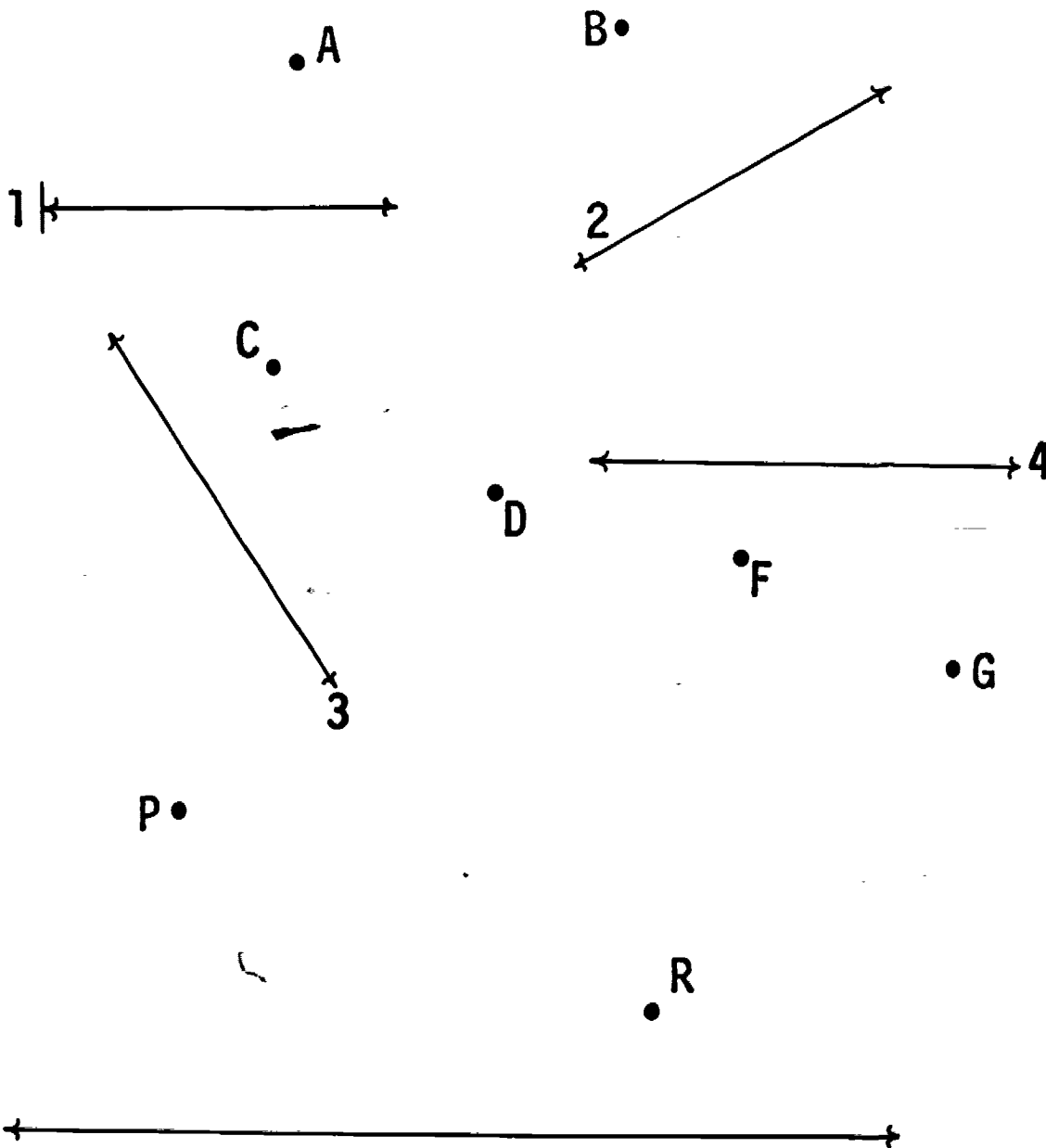
Divide the lines into specified equal segments.



E. Perpendicular Lines

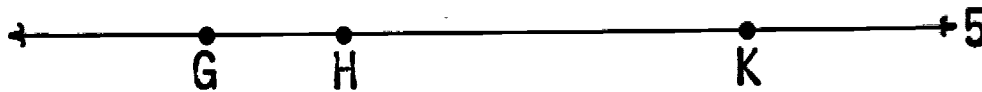
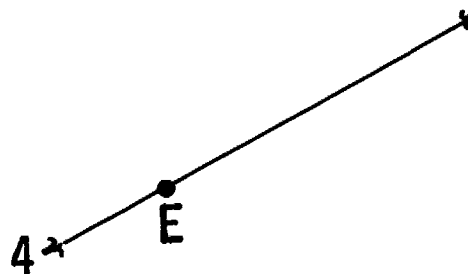
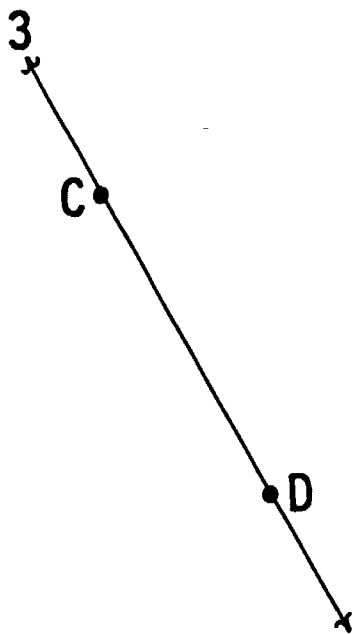
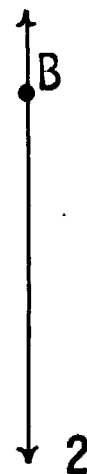
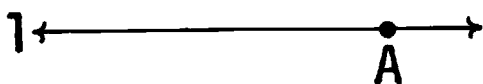
Exercises

Construct a perpendicular line through the given point or points to the given line.



Exercises

Construct lines perpendicular to each given line through the given points.



F. Parallel Lines

EXERCISES

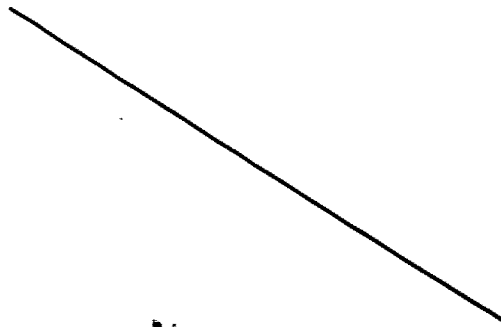
1. Construct a line parallel to the given line by constructing equal alternate interior angles.



2. Construct a line parallel to the given line by constructing equal corresponding angles.



3. Construct a parallel line one inch from the given line by constructing a perpendicular to a perpendicular. (1" apart)



4. By construction, locate the center stripe of Arkansas Highway 1.



Highway 1

UNIT XI
STATISTICS

A. Probability

EXERCISES

1. Drop 4 circular discs on the table (one side red, one side blue).
 - a. List all the different ways they can fall.
 - b. List all the ways you get three red and one blue.
 - c. What is the ratio of b. to a.?
2. What determines the number of possibilities?
3. Can you suggest a rule to go by to determine the expected number of possibilities?
4. Refer back to problem one. Find the probability of the event:
 - a. "Four reds and no blues"
 - b. "Two reds and two blues"
 - c. "One red and three blues"
 - d. "No reds and four blues"
 - e. Compare the chances of events a., b., c., d.
5. A box contains 40 slips of paper. The slips are numbered from 1 through 40. A slip is drawn. What is the probability that the slip drawn will be marked with:
 - a. A number less than 15?
 - b. A number greater than 30?
 - c. An odd number?
 - d. An even number?
 - e. A multiple of 5?
 - f. A multiple of 6?
 - g. A number greater than 20?
 - h. A number less than 5?
 - i. The square of a counting number?
 - j. A number ending in 5?
 - k. A multiple of 18?
 - l. A number which ends in 0?
 - m. A number which is divisible by 12?
 - n. A prime number?

Exercises

1. In a bowl of 12 red and 15 blue marbles, if one marble drawn, replaced, and one marble again selected, what is the probability that:
- Both marbles are blue?
 - Both marbles are red?
 - The two marbles have different colors?
 - The two marbles have the same color?
 - The first marble is blue and the second red?
 - The first marble is red and the second blue?
 - Either marble is red?

2. Your football team is scheduled to play team A & team B. It is estimated that the probability of winning over A is $\frac{1}{3}$ and over B is $\frac{3}{4}$. Which is the stronger opponent?

Who is favored in the game with A? Game with B? What is the probability of your team:

- Losing the second game?
- Losing the 1st game?
- Losing the 1st game and winning the second?
- Winning the 1st game and losing the second?
- Losing both games?
- Winning either game?

3. Basket contains 10 oranges and 6 apples.

- What are the chances of drawing an apple first draw?
- If you drew an apple the 1st draw and ate it, what is the chance of drawing an apple on the second draw?
- What is the probability of drawing an apple the first draw and an orange on the second draw, after replacing the apple? What about the probability of drawing an apple on the first draw and an orange on the second draw after the apple was eaten?

B. Charts and Graphs

Example:

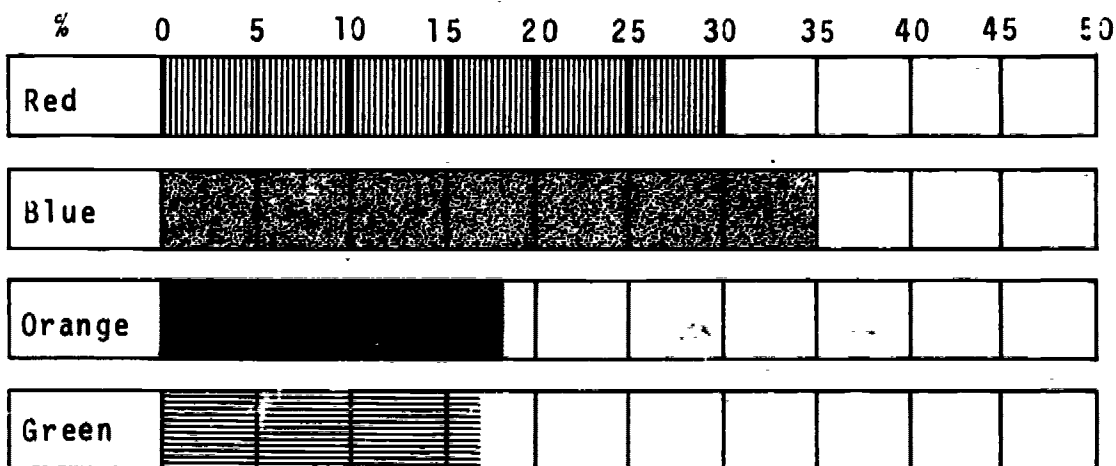
Take 5 cubes where each cube has 2 faces red, 2 faces blue, 1 face green, 1 face orange. Shake the five cubes and let them fall on the table. Record the number of each colored face that appears upward. Repeat your throw 20 times, giving a total of 100 faces recorded. There are several different ways to record this information.

Cube Throwing Chart

Trials	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	Total	%
Red	1	2	3	2	0	1	1	1	0	3	2	1	1	4	2	1	2	0	1	2	30	30%
Blue	4	1	1	2	2	2	1	1	2	1	2	2	3	0	1	4	1	2	1	2	35	35%
Orange	0	2	1	0	2	2	1	0	0	1	0	0	1	1	2	0	2	2	1	0	18	18%
Green	0	0	0	1	1	0	2	3	3	0	1	2	0	0	0	0	0	1	2	1	17	17%

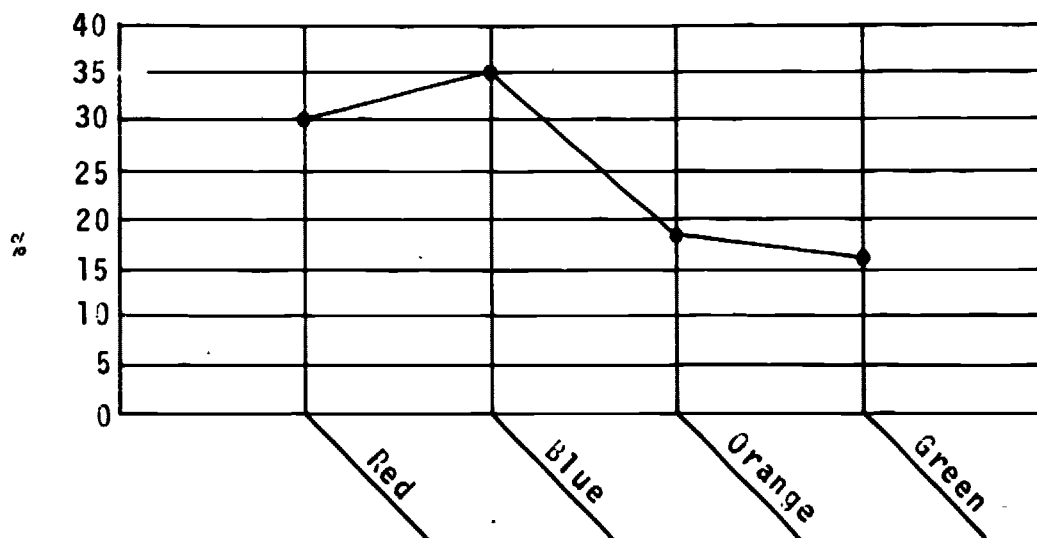
Note: The purpose of the chart is to organize and compare information.

Horizontal Bar Graph

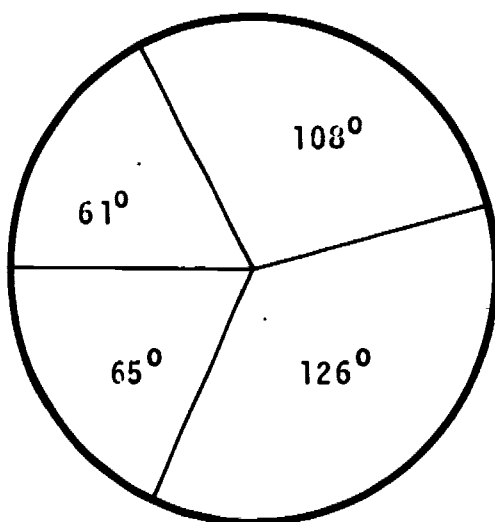


Note: The purpose of a bar graph is to organize the information in picture form so that it may be compared visually.

Line Graph



Circle Graph



$$\text{Red: } \frac{30}{100} \times 360^\circ = 108^\circ$$

$$\text{Blue: } \frac{35}{100} \times 360^\circ = 126^\circ$$

$$\text{Orange: } \frac{18}{100} \times 360^\circ = 65^\circ$$

$$\text{Green: } \frac{17}{100} \times 360^\circ = 61^\circ$$

Exercises

1. Refer to the example problem and make 30 throws instead of 20 throws. Make a chart - compare the per cent of each color to the example. Can you make a bar graph?
2. Make a chart, titled integers 1 to 100, showing how many even numbers, prime numbers, perfect numbers, Fermat primes, numbers evenly divisible by six, and Merseene primes. (Note: For the above numbers we are interested in only how many. Try the library for any of these you do not know.) Make a line graph.
3. Go to a parking lot and count the number of Fords, Chevrolets, Oldsmobiles, and Plymouths.
 - a. Chart the number of each make of car.
 - b. Make a circle graph.

Seating Game

Make a seating chart for your class room.

Name each desk with this symbol ($\square \Delta$) where the number in the position of the square shows the column and the letter in the position of the triangle shows the row.

g.						
f.						
e.						
d.				(5,d)		
c.						
b.	(1,b)					
a.	(1,a)	(2,a)				
	1	2	3	4	5	6
	Front of Room					

Let each desk be represented by a rectangle in the above chart.

1. Write each desk's name in the lower part of the rectangle.
2. Write the student's name in the upper part.
3.
 - a. Who sits in desk (3,d)?
 - b. Who sits in desk (1,a)?
4. Mark an X through desk (4, f).

Practical Application

Reading the Arkansas State Withholding Tax chart, find the rate of state withholding for each of the following:

- | | |
|------------------------|-----------|
| 1. Semi-monthly income | \$ 212.00 |
| 2. Weekly income | 94.75 |
| 3. Monthly income | 510.00 |
| 4. Bi-weekly income | 260.52 |
| 5. Weekly income | 82.74 |
| 6. Bi-weekly income | 700.10 |
| 7. Monthly income | 1500.65 |

FORMULA 4
FORMULA FOR CALCULATING
ARKANSAS STATE WITHHOLDING TAX

<u>Net Taxable Weekly Income</u>			<u>Net Taxable Bi-weekly Income</u>		
From	Thru	Rate %	From	Thru	Rate%
.00	60.32	1.1	.00	130.65	1.1
60.33	71.17	1.2	130.66	142.35	1.2
71.18	82.87	1.3	142.36	165.75	1.3
82.88	95.55	1.4	165.76	191.10	1.4
95.56	117.97	1.5	191.11	235.55	1.5
117.98	127.72	1.6	235.96	255.45	1.6
127.73	137.47	1.7	255.46	274.95	1.7
137.48	147.22	1.8	274.96	294.45	1.8
147.23	161.85	1.9	294.46	323.70	1.9
161.86	178.42	2.0	323.71	356.85	2.0
178.43	192.07	2.1	356.86	384.15	2.1
192.08	212.55	2.2	384.16	425.10	2.2
212.56	226.20	2.3	425.11	452.40	2.3
226.21	239.85	2.4	452.41	479.70	2.4
239.86	253.50	2.5	479.71	507.00	2.5
253.51	263.25	2.6	507.01	526.50	2.6
263.26	273.00	2.7	526.51	546.00	2.7
273.01	292.50	2.8	546.01	585.00	2.8
292.51	312.00	2.9	585.01	624.00	2.9
312.01	331.00	3.0	624.01	662.00	3.0
331.01	350.00	3.1	662.01	700.00	3.1
350.01	375.00	3.2	700.01	750.00	3.2
375.01	400.00	3.3	750.01	800.00	3.3

"FORMULA #5"

FORMULA FOR CALCULATING ARKANSAS STATE WITHHOLDING TAX

Net Taxable Semi-monthly income			Net Taxable Monthly income		
From	Thru	Rate $\frac{\%}{100}$	From	Thru	Rate $\frac{\%}{100}$
.00	130.65	1.0	.00	261.30	1.0
130.66	122.35	1.1	261.31	284.70	1.1
142.36	165.75	1.2	284.71	331.50	1.2
165.76	191.10	1.3	331.51	382.20	1.3
191.11	235.95	1.4	382.21	471.90	1.4
235.96	255.45	1.5	471.91	510.90	1.5
255.46	274.95	1.6	510.91	549.90	1.6
274.96	294.45	1.7	549.91	588.90	1.7
294.46	323.70	1.8	588.91	647.40	1.8
323.71	356.85	1.9	647.41	713.70	1.9
356.86	384.15	2.0	713.71	768.30	2.0
384.16	425.10	2.1	768.31	850.20	2.1
425.11	452.40	2.2	850.21	904.80	2.2
452.41	479.70	2.3	904.81	959.40	2.3
479.71	507.00	2.4	959.41	1014.00	2.4
507.01	526.50	2.5	1014.01	1053.00	2.5
526.51	546.00	2.6	1053.01	1092.00	2.6
546.01	585.00	2.7	1092.01	1170.00	2.7
585.01	624.00	2.8	1170.01	1248.00	2.8
624.01	662.00	2.9	1248.01	1324.00	2.9
662.01	700.00	3.0	1324.01	1400.00	3.0
700.01	750.00	3.1	1400.01	1500.00	3.1
750.01	800.00	3.2	1500.01	1600.01	3.2

Code Messages

Examine the code table and the decoded messages at the right.

0 1 2 3 4 5 6 7 8 9	8 5 7 8 3 6 == 7 4 7 4
a b c d e f g h i j	S P R I N G I S H E R E
k l m n o p q r s t	1 8 2 9 4 7 4 == 4 0 7 8
u v w x y z	V I C T O R Y I S O U R S

Any letter or digit in one of the columns may stand for any other letter or digit in the same column.

To decode a message, list all possible replacements under each numeral, then select those letters that form words. Can you decipher these messages?

1. *7083 = 249
2. 54024 = 507024039
3. WYNOI = PAD

UNIT XII

COMPUTER BASED MATH

A. Base Eight

1. Count from 51 through 100 in base eight. Write the names for these numbers in base eight.
2. The following names for numbers are written in decimal form (base 10). Rename each using base eight notation.
 - a. 37
 - b. 79
 - c. 143
 - d. 465
 - e. 1304
3. Each of the following is a name for a number in a base eight system. Rename each as a decimal number (base 10).
 - a. 174
 - b. 75
 - c. 44
 - d. 203
 - e. 777

Exercises

1. Add the following in base 8 notation.

$$\begin{array}{r} 35 \\ +61 \\ \hline \end{array} \text{ eight} \quad \begin{array}{r} 126 \\ +403 \\ \hline \end{array} \text{ eight} \quad \begin{array}{r} 724 \\ +454 \\ \hline \end{array} \text{ eight} \quad \begin{array}{r} 470 \\ +217 \\ \hline \end{array} \text{ eight} \quad \begin{array}{r} 3203 \\ +346 \\ \hline \end{array} \text{ eight}$$

Check your results using decimals (base ten).

2. Subtract the following in base 8 notation.

$$\begin{array}{r} 76 \\ -34 \\ \hline \end{array} \text{ eight} \quad \begin{array}{r} 53 \\ -27 \\ \hline \end{array} \text{ eight} \quad \begin{array}{r} 204 \\ -65 \\ \hline \end{array} \text{ eight} \quad \begin{array}{r} 620 \\ -256 \\ \hline \end{array} \text{ eight} \quad \begin{array}{r} 712 \\ -305 \\ \hline \end{array} \text{ eight}$$

Weird Operations

Can you work these problems? Study the four examples of each operation.

* operation	Δ operation	□ operation
7 * 4 = 4	2 Δ 3 = 7	14 □ 3 = 1
10 * 16 = 16	5 Δ 8 = 18	40 □ 6 = 8
3 * 1 = 1	15 Δ 2 = 32	26 □ 5 = 3
89 * 72 = 72	0 Δ 5 = 5	64 □ 10 = 12
1. 22 * 0 =	6. 7 Δ 11 =	11. 3 □ 1 =
2. 9 * 51 =	7. 4 Δ = 14	12. 18 □ 4 =
3. 14 * 5 =	8. 12 Δ 1 =	13. 20 □ = 6
4. 6 * 34 =	9. Δ 2 = 20	14. □ 7 = 20
5. 2 * 2 =	10. 1 Δ 1 =	15. 4 □ 1 =

Exercises

The following problems are in base eight notation. Find the product and write your answer in base eight notation.

$$\begin{array}{r} 1. \quad 7 \\ \times 6 \\ \hline \end{array}$$

eight

$$\begin{array}{r} 2. \quad 26 \\ \times 22 \\ \hline \end{array}$$

eight

$$\begin{array}{r} 3. \quad 34 \\ \times 70 \\ \hline \end{array}$$

eight

$$\begin{array}{r} 4. \quad 63 \\ \times 47 \\ \hline \end{array}$$

eight

$$\begin{array}{r} 5. \quad 205 \\ \times 62 \\ \hline \end{array}$$

eight

$$\begin{array}{r} 6. \quad 417 \\ \times 135 \\ \hline \end{array}$$

eight

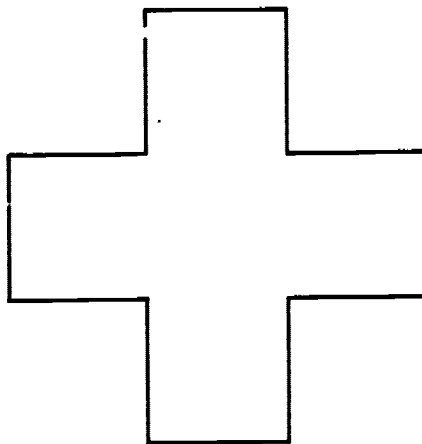
$$\begin{array}{r} 7. \quad 673 \\ \times 55 \\ \hline \end{array}$$

eight

$$\begin{array}{r} 8. \quad 100 \\ \times 100 \\ \hline \end{array}$$

eight

Squaring A Cross



Can you draw four straight lines that divide the cross into five pieces which can be rearranged to form a square?

B. Base Two

EXERCISES

1. Write the names of the numbers from ten to thirty inclusive in binary numerals.
2. What base ten numbers are represented by these binary numerals?

a. 1101 c. 100011 e. 111110 g. 11001 i. 111011
b. 1011 d. 11000 f. 111011 h. 10111 j. 111101

3. Using suggested short cut methods, rename these base ten numbers using binary numerals.

a. 83 b. 104 c. 41 d. 213 e. 59

4. Add:

a.
$$\begin{array}{r} 11011 \\ \underline{1101} \\ \text{two} \end{array}$$
 b.
$$\begin{array}{r} 111111 \\ \underline{1001} \\ \text{two} \end{array}$$
 c.
$$\begin{array}{r} 100011 \\ \underline{11001} \\ \text{two} \end{array}$$
 d.
$$\begin{array}{r} 11100 \\ \underline{1111} \\ \text{two} \end{array}$$

e.
$$\begin{array}{r} 11011 \\ \underline{1001} \\ \text{two} \end{array}$$

Check your accuracy in base ten.

5. Subtract:

a.
$$\begin{array}{r} 11011 \\ \underline{1101} \\ \text{two} \end{array}$$
 b.
$$\begin{array}{r} 111111 \\ \underline{1001} \\ \text{two} \end{array}$$
 c.
$$\begin{array}{r} 100011 \\ \underline{11001} \\ \text{two} \end{array}$$
 d.
$$\begin{array}{r} 11100 \\ \underline{1111} \\ \text{two} \end{array}$$

e.
$$\begin{array}{r} 11011 \\ \underline{1001} \\ \text{two} \end{array}$$

6. Multiply:

a.
$$\begin{array}{r} 111 \\ \underline{11} \\ \text{two} \end{array}$$
 b.
$$\begin{array}{r} 1001 \\ \underline{101} \\ \text{two} \end{array}$$
 c.
$$\begin{array}{r} 1110 \\ \underline{110} \\ \text{two} \end{array}$$
 d.
$$\begin{array}{r} 110111 \\ \underline{1011} \\ \text{two} \end{array}$$

e.
$$\begin{array}{r} 11101 \\ \underline{1101} \\ \text{two} \end{array}$$

C. Base Five

EXERCISES

1. Count from 50 to 100 using base 5 numerals.
2. What decimal numbers are represented by the following base 5 numerals?
 - a. $\begin{array}{r} 31 \\ \text{five} \end{array}$
 - b. $\begin{array}{r} 24 \\ \text{five} \end{array}$
 - c. $\begin{array}{r} 420 \\ \text{five} \end{array}$
 - d. $\begin{array}{r} 12 \\ \text{five} \end{array}$
 - e. $\begin{array}{r} 103 \\ \text{five} \end{array}$
 - f. $\begin{array}{r} 2133 \\ \text{five} \end{array}$

3. Rename the following decimals with base 5 numerals:

- a. 73
- b. 124
- c. 346
- d. 47
- e. 625
- f. 160

4. Add:

$\begin{array}{r} 30 \\ +24 \\ \hline \end{array}$	$\begin{array}{r} 42 \\ +13 \\ \hline \end{array}$	$\begin{array}{r} 123 \\ +422 \\ \hline \end{array}$	$\begin{array}{r} 403 \\ +241 \\ \hline \end{array}$	$\begin{array}{r} 341 \\ +123 \\ \hline \end{array}$
five	five	five	five	five

5. Subtract:

$\begin{array}{r} 32 \\ -23 \\ \hline \end{array}$	$\begin{array}{r} 40 \\ -14 \\ \hline \end{array}$	$\begin{array}{r} 204 \\ -112 \\ \hline \end{array}$	$\begin{array}{r} 341 \\ -123 \\ \hline \end{array}$	$\begin{array}{r} 4024 \\ -1231 \\ \hline \end{array}$
five	five	five	five	five

6. Multiply:

$\begin{array}{r} 40 \\ \times 24 \\ \hline \end{array}$	$\begin{array}{r} 32 \\ \times 14 \\ \hline \end{array}$	$\begin{array}{r} 242 \\ \times 32 \\ \hline \end{array}$	$\begin{array}{r} 312 \\ \times 103 \\ \hline \end{array}$	$\begin{array}{r} 223 \\ \times 341 \\ \hline \end{array}$
five	five	five	five	five

UNIT XIII

REFUELING THE BRAIN

A. Whole numbers and fractions

In each problem show the number of times both the denominator and numerator are exactly divisible by the numbers 2, 3, 5, and 7, and then write the fractions in lowest terms.

1.	<u>Divisible</u>	<u>Lowest Terms</u>
a. $\frac{12}{16}$	_____	_____
b. $\frac{18}{36}$	_____	_____
c. $\frac{24}{42}$	_____	_____
d. $\frac{54}{135}$	_____	_____
e. $\frac{128}{224}$	_____	_____
f. $\frac{70}{245}$	_____	_____

2. Change the following to fractions in lowest terms.

a. $\frac{27}{6}$

c. $\frac{10}{16}$

b. $\frac{14}{35}$

d. $\frac{77}{10}$

3. Solve:

a. $7\frac{2}{3} + 9\frac{3}{4} + 11\frac{1}{2} =$

d. $8 + \frac{7}{4} + \frac{8}{3} + \frac{7}{2} =$

b. $\frac{9}{10} + \frac{7}{12} + \frac{5}{4} + \frac{2}{3} =$

e. $14\frac{3}{4} + 30\frac{1}{2} + 4 =$

c. $12\frac{1}{12} + 24\frac{1}{24} + 36\frac{1}{36} =$

f. $\frac{4}{5} + \frac{5}{6} + \frac{7}{10} =$

4. A golfer drives a ball $180 \frac{3}{4}$ yds., $253 \frac{7}{8}$ yds., $33 \frac{1}{3}$ yds., and then putts $2 \frac{5}{8}$ yds. How many yards was the ball played? _____

5. Find the difference of the sum of $7 \frac{7}{8}$ and $3 \frac{3}{4}$, and the sum of $2 \frac{1}{5}$ and $4 \frac{1}{2}$.
a. sum _____
b. sum _____
c. difference _____

6. A fountain pen and pencil set sells for \$7.50. The pen sells for $\frac{2}{3}$ of the price of the set.

a. What fractional part does the pencil sell for? _____

b. How much does the pencil sell for? _____

7. How much will $55 \frac{1}{2}$ feet of wire cost at $3 \frac{3}{4}$ ¢ per foot? _____

8. Solve each:

a. $6 \times \frac{2}{3} =$ _____ d. $6 \frac{7}{8} \times 22 =$ _____

b. $\frac{5}{8} \times \frac{4}{15} =$ _____ e. $4 \frac{2}{4} \times 5 \frac{1}{4} =$ _____

c. $8 \frac{5}{8} \times \frac{2}{3} =$ _____ f. $\frac{3}{5} \times \frac{2}{3} \times \frac{5}{8} =$ _____

9. A man drove 220 miles in $6 \frac{2}{3}$ hours. What was his average speed per hour? _____

10. Solve:

a. Divide $\frac{7}{8}$ by $\frac{7}{16} =$ _____

b. Divide $4 \frac{1}{16}$ into 15 = _____

c. $4 \frac{1}{2} \div 6 \frac{1}{4} =$ _____

11. A reciprocal of a number is one divided by that number.

Give the reciprocal of:

a. 12 =

c. $\frac{1}{6} =$

e. $3 \frac{1}{3} =$

b. $2 \frac{1}{2} =$

d. $\frac{5}{4} =$

12. Find the difference between $3 \frac{1}{3}$ and its reciprocal.

B. Decimals

Exercise

1. Write in decimal form

a. One hundred fifty-six millionths _____

b. Nineteen ten thousandths _____

c. Forty-five and sixty-five hundredths _____

2. Match the items in Column A with the items in Column B.

	A	B
_____ a.	.1	(1) .875
_____ b.	$3/4$	(2) $5/8$
_____ c.	$7/8$	(3) .4
_____ d.	.625	(4) $1/6$
_____ e.	.125	(5) .833
_____ f.	$5/6$	(6) $1/2$
_____ g.	$.16 \frac{2}{3}$	(7) $1/10$
_____ h.	$2/5$	(8) $1/8$
_____ i.	.50	(9) .75

3. Change each decimal to a fraction. Show your work.

a. $.34 =$ _____

b. $.285 =$ _____

c. $.005 =$ _____

d. $.375 =$ _____

e. $.0013 =$ _____

4. Change each fraction to a decimal and round off the result to thousandths.

a. $4/9 =$

c. $7/12 =$

e. $3/32 =$

b. $7/24 =$

d. $2/15 =$

5. Round off the following:

- a. 35.635 to hundredths _____
- b. 58.063 to tenths _____
- c. .0071 to thousandths _____

6. Solve:

- a. $87 + 362.23 + 23.5 + 316.07 =$ _____
- b. $8.62 + .123 + 7.5 + 75 =$ _____
- c. From 293.3 take 24.61 = _____
- d. Subtract .017 from 1.1654 _____
- e. Take 4.578 from 10.39 _____

7. Multiply:

- a. 545 by 39.06 _____
- b. 57.98 by 56 _____
- c. .054 by 1283 _____
- d. .82 and 39.98 _____

8. Divide: Round off to hundredths

- a. 22 by 26 _____
- b. 83.52 by 116 _____
- c. .72 by .9 _____
- d. 87.5 into 76.32 _____

9. Give the following answer in decimal form:

$$14\frac{1}{5} + 12.5 + 128.675 + 15\frac{7}{8} + .50 = \underline{\hspace{2cm}}$$

C. Number Sequence

Exercises

Find the next two terms in each sequence.

- | | | | | | | | | |
|-------|-----------------|-----------------|-----------------|-----------------|-----------------|---------------|-------|-------|
| 1. a. | 1 | 3 | 5 | 7 | 9 | _____ | _____ | |
| b. | 2 | 4 | 6 | 8 | 10 | _____ | _____ | |
| c. | 45 | 50 | 65 | 70 | 85 | 90 | _____ | _____ |
| d. | 24 | 23 | 22 | 21 | 20 | _____ | _____ | |
| e. | 75 | 72 | 69 | 66 | | _____ | _____ | |
| f. | 1 | 3 | 6 | 10 | 15 | 21 | _____ | _____ |
| g. | $\frac{1}{1}$ | $\frac{1}{2}$ | $\frac{1}{3}$ | $\frac{1}{4}$ | $\frac{1}{5}$ | $\frac{1}{6}$ | _____ | _____ |
| h. | $\frac{11}{12}$ | $\frac{12}{13}$ | $\frac{13}{14}$ | $\frac{14}{15}$ | | | _____ | _____ |
| i. | $\frac{25}{4}$ | $\frac{22}{6}$ | $\frac{19}{8}$ | $\frac{16}{10}$ | | | _____ | _____ |
| j. | $\frac{3}{4}$ | $\frac{6}{7}$ | $\frac{12}{10}$ | $\frac{24}{13}$ | $\frac{48}{16}$ | | _____ | _____ |

2. Find the sum of the first 6 terms of the above sequences:

- | | | |
|----|----|----|
| a. | c. | e. |
| b. | d. | f. |

Note: A sequence in which each term is obtained by adding or subtracting the same number to the previous term is an arithmetic progression.

3. Which of the sequences above are arithmetic progressions?

Exercises

List the next 2 terms of the following "special" progressions.

1. a. 2, 4, 8, 16, 32, 64, ... _____ _____
b. 3, 9, 27, 81, ... _____ _____

2. Find 2 more terms at the beginning and 2 at the end of each "special" progression.

- a. _____, _____, 12, 24, 48, _____, _____
b. _____, _____, $\frac{1}{4}$, 1, 4, _____, _____
c. _____, _____, 5, $\frac{1}{5}$, $\frac{1}{5}$, _____, _____
d. _____, _____, 3, $\frac{3}{2}$, $\frac{3}{4}$, _____, _____

3. Find 2 more terms at the end of each "special" progression.

- a. $\frac{1}{3}$, $\frac{2}{3}$, $\frac{4}{3}$, $\frac{8}{3}$, ... _____ _____
b. $\frac{1}{2}$, $\frac{2}{6}$, $\frac{4}{18}$, $\frac{8}{54}$, ... _____ _____
c. $\frac{2}{3}$, $\frac{4}{9}$, $\frac{8}{27}$, $\frac{16}{81}$, ... _____ _____
d. 3, $\frac{9}{4}$, $\frac{27}{16}$, $\frac{81}{64}$, ... _____ _____

Note: A sequence in which each term is obtained by multiplying the previous term by the same number is a geometric progression.

D. Percentage

Exercises

1. Change the following decimals to per cents.

- | | | | |
|----------|-------|----------|-------|
| a. .03 | _____ | f. .076 | _____ |
| b. .2 | _____ | g. .125 | _____ |
| c. .0025 | _____ | h. .2468 | _____ |
| d. .0825 | _____ | i. .005 | _____ |
| e. .004 | _____ | | |

2. Change the following per cents to fractions.

- | | | | |
|---------------------|-------|---------------------|-------|
| a. $7\frac{1}{2}\%$ | _____ | e. $1/4\%$ | _____ |
| b. 125% | _____ | f. 309% | _____ |
| c. 5% | _____ | g. 20% | _____ |
| d. 8.1% | _____ | h. $7\frac{3}{7}\%$ | _____ |

3. Jack puts $1/4$ of his allowance into savings bonds each week. What % of his allowance does he save? _____

4. Jerry got $4/5$ of his math test correct. John got 85% on his test. a. Which had the higher mark? _____

b. What was Jerry's mark? _____

5. Find:

- | | | | |
|---------------------|-------|--------------------|-------|
| a. 7% of 152 | _____ | f. 200% of \$560 | _____ |
| b. 15% of 90 | _____ | g. 18% of 4.15 | _____ |
| c. 20% of \$65 | _____ | h. 3.2% of 193 | _____ |
| d. 40% of 2.5 | _____ | i. $1/4\%$ of 800 | _____ |
| e. 125% of 1264 ft. | _____ | j. $3/11\%$ of 300 | _____ |

6. Find what per cent one number is of another.

- a. 12 is _____ % of 16.
- b. 32 is _____ % of 48.
- c. 88 is _____ % of 160.
- d. 36 is _____ % of 192.
- e. 13 lbs. is _____ % of 175 lbs.

7. Find the whole number when a per cent is known:

- a. $24 = 33 \frac{1}{3}\%$ of _____ . d. 45 is 50% of _____ .
b. 46 is 10% of _____ . e. 100 is 10% of _____ .
c. 72 is 60% of _____ .

8. Fill in the blanks.

- a. On a test Joe got 12 examples correct out of 15. The percent of examples he got correct was _____ %.
- b. A seaman was told that he was 20% overweight. If he weighs 180 lbs., he must lose _____ lbs. before he is acceptable.
- c. A dealer's commission on an automobile was 27% of its sale price. The dealer earned _____ by selling a car for \$1452.
- d. A salesman earned \$58 a week when working on a commission of 35% of his sales. His total sales were _____ .
- e. A study showed that an important firm was 20% over staffed. If it employed 720 people the firm would have to dismiss _____ employees.
- f. During a recent year a hardware store collected all but $\frac{9}{10}$ of its total sales of 95,000 dollars. _____ amount of money was not collected.
- g. A clerk's weekly salary was raised from \$20 to \$24. This was a _____ percent increase.
- h. Of \$690 collected for charity, $\frac{7}{8}$ was used to pay expenses. _____ was actually used for charity.
- i. A camera priced at \$27.50 was sold for 80% of this price, the camera sold for _____ .
- j. The price of eggs increased from \$.26 per dozen to \$.54 per dozen, which was a _____ percent increase.

9. One of the answers is correct. Put the number which corresponds to the correct answer in space provided at left.

- a. The sugar content of strawberries is equal to 52.7% of their weight. 50 lbs. of strawberries would have a sugar content of: (1) 264% (2) 26.3 1/2% (3) 2.63% (4) 2635% (5) None
- b. During a sale a merchant sold 159 shirts or 75% of the shirts in stock. The number of shirts he had before the sale was: (1) 2.12 (2) 12100 (3) 21.2 (4) 212 (5) None
- c. If 35% of a number is 70, the number is: (1) .200 (2) 200 (3) 2.00 (4) 20 (5) None
- d. It was found that 5 out of each 1000 ships which were convoyed in the Pacific were sunk. The percentage sunk was: (1) .5% (2) 5% (3) .005% (4) 500% (5) None
- e. While at target practice a gunner made 27 hits out of 32 shots. The percentage of hits was: (1) 84 4/9% (2) .84% (3) 8.4% (4) .084% (5) None
- f. In an insurance company which employs 2700 people 165 absentees were reported one day. The percent of absentees reported on that day was: (1) .6 1/9% (2) 6 1/9% (3) .06 1/9% (4) .05 5/9% (5) None
- g. There are 960 pupils in Childress School. 55% can swim. The number that can swim is: (1) 528 (2) .528 (3) 5.28 (4) 52.8 (5) None
- h. The average price of tomatoes last fall was \$3.20 per bushel. This year it is \$2.30 per bushel. The percent of decrease is (1) .028% (2) .28% (3) 28 1/8% (4) 2.8% (5) None
- i. A bank charged .2% to collect a bill of \$1680. The cost of collection was: (1) \$33.60 (2) \$.33 (3) \$37. (4) \$3.36 (5) None
- j. A student practiced shooting fouls in basketball. If he shot 14 out of 24 shots, the percent of his successful shots was: (1) 58 1/3% (2) 33 1/3% (3) 66 2/3% (4) 50 2/3% (5) None

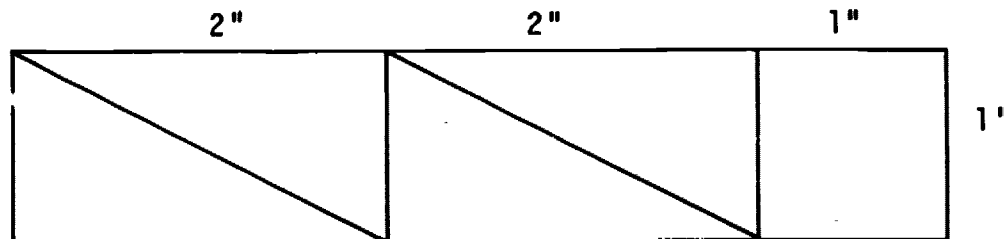
E. Sharpie Section

Exercises

1. Can you plant ten trees in ten rows, each row having three trees and each tree in three different rows?
2. Draw 4 straight lines through 9 dots (as shown) so as to cross out every dot. No dot can be crossed out twice, no line retraced, nor can the pencil be lifted from the paper until all 9 dots have been crossed out.



3. Cut it out then answer the questions.



Can you make a square using all 5 pieces?
 Can you make a square using only 4 pieces?

4. Multiply:

$$\begin{array}{r}
 12345679 \times 9 = \\
 12345679 \times 18 = \\
 12345679 \times 27 = \\
 12345679 \times 36 = \\
 12345679 \times 45 = \\
 12345679 \times 54 = \\
 12345679 \times 63 = \\
 12345679 \times 72 = \\
 12345679 \times 81 =
 \end{array}$$

Is there anything unusual about the answers you get?
 How are they related to the multiplier in each case?

5.

$$\begin{array}{r}
 + 1 + 2 + 1 = 2^2 \\
 1 + 2 + 3 + 2 + 1 = 3^2 \\
 1 + 2 + 3 + 4 + 3 + 2 + 1 = 4^2
 \end{array}$$

Can you continue this pattern until you reach 10^2 ?
 Can you explain the pattern and its relation to the result?

6. $123456789 \times 3 =$
 $123456789 \times 30 =$
 $123456789 \times 57 =$

$123456789 \times 6 =$
 $123456789 \times 33 =$
 $123456789 \times 60 =$

$123456789 \times 12 =$
 $123456789 \times 39 =$
 $123456789 \times 66 =$

$123456789 \times 21 =$
 $123456789 \times 48 =$
 $123456789 \times 75 =$

Multiply these problems.

Is there anything unusual about the answers?

Find the sum of the answers in each group and compare answers to multipliers.

7. Biblical Arithmetic:

- a. Take the number of commandments.
- b. Add the number of letters in the name of the man who received them.
- c. Subtract the number of Jacob's sons.
- d. The result will be the number of patriarchs.

8. Political Arithmetic:

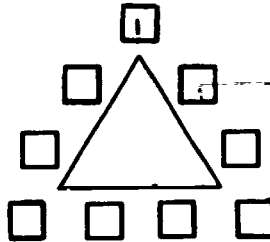
- a. Take the number of states in U.S.
- b. Subtract the number of Senators from each state.
- c. Subtract the number of original colonies.
- d. Produces the number of Presidents of U.S. to date.

9. Sporty Arithmetic:

- a. Take the number of men on a football team.
- b. Add the number of men on a baseball team.
- c. Divide by the number of men on a basketball team.
- d. Add the number of men on an ice hockey team.
- e. Your answers will be the number of men on a softball team.

10. Arrange the following units of measure in order of length from the smallest to the largest: a. inch b. cable
c. fathom d. furlong e. yard f. rod g. hand
h. centimeter i. nautical mile j. cable length.

11. Use all of the elements of the set $\{1, 2, 3, \dots, 9\}$. Arrange them around the triangle so that there is exactly 4 numbers on each side that total 17 in any direction. Do not repeat a number. (Can you find more than one solution?)



12. A farmer wants to plant a tree in a square plot. He wants it planted 30' from one corner, 40' from another corner, and 50' from another corner. How big is the square?

13. Provide the answers to the last three problems based on the pattern shown in the first three.

$$\begin{array}{r} 11 \\ \times 11 \\ \hline 121 \end{array}$$

$$\begin{array}{r} 111 \\ \times 111 \\ \hline 12,321 \end{array}$$

$$\begin{array}{r} 1111 \\ \times 1111 \\ \hline 1,234,321 \end{array}$$

$$\begin{array}{r} 11111 \\ \times 11111 \\ \hline \end{array}$$

$$\begin{array}{r} 11111111 \\ \times 11111111 \\ \hline \end{array}$$

$$\begin{array}{r} 111111111 \\ \times 111111111 \\ \hline \end{array}$$