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The Mathematics Content Authority List for K-6 (abridged) represents an attempt to list in one volume the mathematics concepts and skills currently taught in the elementary schools. The list consists of approximately 300 items involving concepts from number systems and numeration, sets, geometry, measurement of non-geometric quantities, and number patterns and relationships. Definitions, explanations, and examples are provided in an expanded version of this list. This list is used by the Pennsylvania Retrieval of Information for Mathematics Education System (PRIMES) Project to code elementary school mathematics textbooks and textbook activities for storage and retrieval. (RP)

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**Abridged  
Mathematics Content  
Authority List: K-6**

**PRIMES**  
PENNSYLVANIA RETRIEVAL OF INFORMATION FOR MATHEMATICS EDUCATION SYSTEM

SE 006 640

MATHEMATICS CONTENT AUTHORITY  
LIST: K-6 (abridged)

Commonwealth of Pennsylvania  
Department of Public Instruction  
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Bureau of General and  
Academic Education

NOVEMBER, 1968

## PREFACE

The *MATHEMATICS CONTENT AUTHORITY LIST: K-6 (abridged)* represents an attempt to collect in one volume the mathematics concepts and skills currently taught in the elementary schools. The list consists of approximately three hundred items. Definitions, explanations and examples are provided in an expanded version of this list. The numbers in parentheses following selected items are cross-references to other items that may be relevant. This list is used by the Pennsylvania Retrieval of Information for Mathematics Education System (PRIMES) project to code twenty elementary school mathematics series. The numbers along the left margin are code numbers used to access a computer-generated index that lists the relevant lessons in the commercially published series.

The *MATHEMATICS CONTENT AUTHORITY LIST: K-6 (abridged)* is the result of contributions made by many individuals over the last three years. But were it not for the dedication and commitment of *Dr. Joy E. Mahachek*, retired, chairman, mathematics department, Indiana University of Pennsylvania, this publication would not have been possible. The final draft was carefully reviewed by *Dr. Lee Boyer*, retired, professor, mathematics department, Millersville State College, and many of his suggestions were incorporated in the text.

Among the other people who participated in the development of the publication are: *Dr. J. Fred Weaver*, University of Wisconsin; *Dr. Earle F. Myers*, University of Pittsburgh; *Dr. C. Alan Riedesel*, The Pennsylvania State University, who served on a committee to review the main concepts of this publication and to edit an early draft of the content items.

Additional suggestions were made by *Dr. Sara Rhue*, Temple University; *Dr. Michael Montemuro*, West Chester State College, Pennsylvania; *Dr. Willard Hennemann* and *Miss Mildred Reigh*, Indiana University of Pennsylvania; and *Mr. Donald Sapko*, California State College, Pennsylvania.

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MATHEMATICS CONTENT AUTHORITY LIST: K-6  
(abridged)

0002 . . Topic I: Number Systems

0004 . . . A. Whole Numbers

0006 . . . . . 1. Basic concepts

0010 . . . . . a. Definition: set of whole numbers

0019 . . . . . b. Developing cardinal number sense

0020 . . . . . 1) Developing cardinal number zero  
(See 4070, 3050)

0030 . . . . . 2) Developing cardinal numbers one through ten  
(See 3050, 0060)

0035 . . . . . 3) Developing cardinal numbers beyond ten  
(See 3070, 0060)

0040 . . . . . c. Developing ordinal number sense  
(See 0075)

0050 . . . . . d. Associating the idea of number with the number  
line (one-to-one correspondence)  
(See 4010)

0060 . . . . . e. Counting to find cardinal number of set (one-to-  
one correspondence)  
(See 0030, 0035, 4010)

0070 . . . . . f. Ordinal counting

0075 . . . . . g. Sequence of numbers increasing by one  
(See 0040, 7090)

0080 . . . . . h. Skip counting  
(See 7000, 7055, 7090, 0380)

0090 . . . . . i. Other counting: backward, rote, etc.

0100 . . . . . j. Ordering numbers as greater than, less than, equal  
to or not equal to and between; and objects as  
fewer than or more than  
(See 4010, 4030)

- 0102 . . . . . 2. Operations
- 0104 . . . . . a. Addition
- 0106 . . . . . 1) Properties
- 0110 . . . . . a) Addition, a binary operation
- 0120 . . . . . b) Addition developed from union of disjoint sets or joining action  
(See 4093)
- 0130 . . . . . c) Addition developed from number line
- 0140 . . . . . d) Closure, a property of addition
- 0150 . . . . . e) Commutativity, a property of addition
- 0160 . . . . . f) Associativity, a property of addition
- 0170 . . . . . g) Zero, the identity element in addition
- 0180 . . . . . h) Role of one in addition
- 0182 . . . . . 2) Computation
- 0184 . . . . . a) Two addends
- 0190 . . . . . (1) Elementary facts of addition
- 0200 . . . . . (2) Multi-digits used in addition without renaming  
(See 3010)
- 0210 . . . . . (3) Multi-digits used in addition with renaming  
(See 3010)
- 0221 . . . . . b) More than two addends
- 0223 . . . . . (1) Single digits used in addition without renaming

- 0225 . . . . . (2) Single digits used in addition with renaming
- 0227 . . . . . (3) Multi-digits used in addition without renaming  
(See 3010)
- 0229 . . . . . (4) Multi-digits used in addition with renaming  
(See 3010)
- 0232 . . . . . b. Subtraction
- 0234 . . . . . 1) Properties
- 0240 . . . . . a) Subtraction, a binary operation
- 0250 . . . . . b) Subtraction developed in relation to subsets or separating action  
(See 4060)
- 0260 . . . . . c) Subtraction developed from number line
- 0270 . . . . . d) Subtraction, the inverse of addition  
(relationship of addition and subtraction)
- 0280 . . . . . e) Role of zero in subtraction
- 0290 . . . . . f) Nonclosure, noncommutativity, nonassociativity of subtraction of whole numbers
- 0300 . . . . . g) Role of one in subtraction
- 0302 . . . . . 2) Computation
- 0310 . . . . . a) Elementary facts of subtraction
- 0320 . . . . . b) Multi-digits used in subtraction without renaming
- 0330 . . . . . c) Multi-digits used in subtraction with renaming  
(See 3010)



- 0332 . . . . . c. Multiplication
- 0334 . . . . . 1) Properties
- 0340 . . . . . a) Multiplication, a binary operation
- 0350 . . . . . b) Multiplication developed from union of two or more equivalent sets
- 0360 . . . . . c) Multiplication developed from arrays
- 0370 . . . . . d) Multiplication developed from the number line
- 0380 . . . . . e) Multiplication developed as repeated addition  
(See 0080)
- 0390 . . . . . f) Multiplication developed from Cartesian product sets  
(See 4160)
- 0400 . . . . . g) Closure, a property of multiplication
- 0410 . . . . . h) Commutativity, a property of multiplication
- 0420 . . . . . i) Associativity, a property of multiplication
- 0430 . . . . . j) Distributivity, a property of multiplication over addition or subtraction
- 0440 . . . . . k) One, the identity element in multiplication
- 0450 . . . . . l) Property of zero in multiplication
- 0452 . . . . . 2) Computation
- 0454 . . . . . a) Two factors
- 0460 . . . . . (1) Elementary facts of multiplication

- 0470 . . . . . (2) Multi-digits used in multiplication  
without renaming
- 0480 . . . . . (3) Multi-digits used in multiplication  
with renaming
- 0490 . . . . . b) Multiplication with more than two factors  
without renaming
- 0500 . . . . . c) Multiplication with more than two factors  
with renaming
- 0510 . . . . . d) Multiples of ten as a factor
- 0515 . . . . . e) A power of ten as a factor
- 0520 . . . . . f) A number expressed in exponential form as  
a factor  
(See 3120)
- 0522 . . . . . d. Division
- 0524 . . . . . 1) Properties
- 0530 . . . . . a) Division, a binary operation
- 0540 . . . . . b) Division developed from partitioning into  
equivalent sets  
(See 4060)
- 0550 . . . . . c) Division developed as successive subtraction
- 0555 . . . . . d) Division developed from arrays
- 0560 . . . . . e) Division developed from the number line
- 0570 . . . . . f) Division, the inverse of multiplication

- 0575 . . . . . g) Distributivity of division over addition  
or subtraction
- 0580 . . . . . h) Role of one in division
- 0590 . . . . . i) Zero not a divisor
- 0600 . . . . . j) Nonclosure, noncommutativity, nonassociativity  
of division
- 0602 . . . . . 2) Computation
- 0610 . . . . . a) Elementary facts of division
- 0620 . . . . . b) Division - known factor (divisor), less  
than ten, product (dividend) not renamed;  
no remainder
- 0630 . . . . . c) Division -- known factor (divisor), less  
than ten, product (dividend) not renamed;  
remainder
- 0640 . . . . . d) Division - known factor (divisor), less  
than ten, product (dividend) renamed; no  
remainder
- 0650 . . . . . e) Division - known factor (divisor), less  
than ten, product (dividend) renamed;  
remainder
- 0660 . . . . . f) Division by ten or greater numbers
- 0665 . . . . . g) Division by multiples of ten
- 0667 . . . . . h) Division by powers of ten
- 0670 . . . . . i) Division with numbers expressed in  
exponential form  
(See 3120)

0672 . . . . . e. Combined operations (addition, subtraction,  
multiplication, division)

0680 . . . . . 1) Two sequential operations

0690 . . . . . 2) More than two sequential operations

0700 . . . . . f. Raising to powers and finding roots  
(See 3120)

0002 . . Topic I: Number Systems

0992 . . . B. Nonnegative Rational Numbers (fractional numbers)

0994 . . . . . 1. Basic concepts

1000 . . . . . a. Definition: set of nonnegative rationals  
(fractional numbers)

1005 . . . . . b. Developed in terms of basic operations

1010 . . . . . c. Developed from subset of a given set

1020 . . . . . d. Developed as distances on the number line

1030 . . . . . e. Developed from plane and solid regions

1035 . . . . . f. Developed in other ways

1040 . . . . . g. Whole numbers as related to set of nonnegative  
rationals (fractional numbers)  
(See 3040)

1060 . . . . . h. Definition: equality  
(See 3020, 3040)

1080 . . . . . i. Counting

1090 . . . . . j. Ordering: greater than; less than; equal to; not  
equal to; between

1100 . . . . . k. Density

1102 . . . . . 2. Operations

1104 . . . . . a. Addition

1106 . . . . . 1) Properties

- 1110 . . . . . a) Addition, a binary operation
- 1120 . . . . . b) Addition developed from union of disjoint sets
- 1130 . . . . . c) Addition developed from the number line
- 1140 . . . . . d) Addition developed from plane or solid regions
- 1150 . . . . . e) Closure, a property of addition
- 1160 . . . . . f) Commutativity, a property of addition
- 1170 . . . . . g) Associativity, a property of addition
- 1180 . . . . . h) Zero, the identity element in addition
- 1182 . . . . . 2) Computation
- 1190 . . . . . a) Addition with common fraction notation, equal denominators (like fractions)
- 1200 . . . . . b) Addition with common fraction notation, unequal denominators (unlike fractions) (See 7060)
- 1210 . . . . . c) Addition with exact decimal fraction notation
- 1212 . . . . . b. Subtraction
- 1214 . . . . . 1) Properties
- 1220 . . . . . a) Subtraction, a binary operation
- 1230 . . . . . b) Subtraction developed in relation to subsets

- 1240 . . . . . c) Subtraction developed from the number line
- 1250 . . . . . d) Subtraction developed from plane or solid regions
- 1260 . . . . . e) Subtraction, the inverse of addition
- 1270 . . . . . f) Role of zero in subtraction
- 1280 . . . . . g) Nonclosure, noncommutativity, nonassociativity in subtraction
- 1282 . . . . . 2) Computation
- 1290 . . . . . a) Subtraction with common fraction notation, equal denominators (like fractions)
- 1300 . . . . . b) Subtraction with common fraction notation, unequal denominators (unlike fractions) (See 7060)
- 1310 . . . . . c) Subtraction with decimal fraction notation
- 1312 . . . . . c. Multiplication
- 1314 . . . . . 1) Properties
- 1320 . . . . . a) Multiplication, a binary operation
- 1330 . . . . . b) Multiplication developed from addition of two or more equal fractions
- 1340 . . . . . c) Multiplication developed from arrays or sets
- 1345 . . . . . d) Multiplication developed from the number line
- 1350 . . . . . e) Multiplication developed from plane and solid regions

- 1360 . . . . . f) Closure, a property of multiplication
- 1370 . . . . . g) Commutativity, a property of multiplication
- 1380 . . . . . h) Associativity, a property of multiplication
- 1390 . . . . . i) Distributivity, a property of multiplication  
over addition or subtraction
- 1400 . . . . . j) One, the identity element in multiplication
- 1410 . . . . . k) Role of zero in multiplication
- 1420 . . . . . l) Multiplicative inverse (reciprocal) for any  
fractional number greater than zero
- 1422 . . . . . 2) Computation
- 1430 . . . . . a) Multiplication with common fraction notation
- 1440 . . . . . b) Multiplication with decimal fraction notation
- 1441 . . . . . c) Multiplication by powers or multiples of ten
- 1442 . . . . . d. Division
- 1444 . . . . . 1) Properties
- 1450 . . . . . a) Division, a binary operation
- 1460 . . . . . b) Division developed from successive subtraction  
of two or more equal fractional numbers
- 1470 . . . . . c) Division developed from the number line
- 1480 . . . . . d) Division developed from plane and solid  
regions



- 1490 . . . . . e) Division, the inverse of multiplication with fractional numbers
- 1500 . . . . . f) Closure, a property of division
- 1510 . . . . . g) Role of one in division
- 1520 . . . . . h) Zero not a divisor
- 1530 . . . . . i) Noncommutativity, nonassociativity of division
- 1532 . . . . . 2) Computation
- 1540 . . . . . a) Division with common fraction notation
- 1550 . . . . . b) Division with decimal fraction notation
- 1555 . . . . . c) Division by powers or multiples of ten
- 1560 . . . . . e. Sequential operations

- 0002 . . Topic I: Number Systems
  
- 1992 . . . C. Integers
  
- 1994 . . . . . 1. Basic concepts
  
- 2000 . . . . . a. Definition: set of integers
  
- 2010 . . . . . b. Developed from the number line
  
- 2020 . . . . . c. Developed from physical world situations
  
- 2030 . . . . . d. Ordering: greater than; less than; equal to or  
not equal to; between
  
- 2040 . . . . . e. Directed numbers: absolute value
  
- 2042 . . . . . 2. Operations
  
- 2044 . . . . . a. Addition
  
- 2046 . . . . . 1) Properties
  
- 2050 . . . . . a) Addition, a binary operation
  
- 2053 . . . . . b) Addition developed from number line
  
- 2055 . . . . . c) Addition developed from physical world  
situations
  
- 2060 . . . . . d) Closure, a property of addition
  
- 2070 . . . . . e) Commutativity, a property of addition
  
- 2080 . . . . . f) Associativity, a property of addition

- 2090 . . . . . g) Zero, the identity element in addition
- 2100 . . . . . h) Additive inverse for addition
- 2110 . . . . . 2) Addition computation
- 2112 . . . . . b. Subtraction
- 2114 . . . . . 1) Properties
- 2120 . . . . . a) Subtraction, a binary operation
- 2123 . . . . . b) Subtraction developed from number line
- 2125 . . . . . c) Subtraction developed from physical world situations
- 2130 . . . . . d) Subtraction, the inverse of addition
- 2140 . . . . . e) Role of zero in subtraction
- 2150 . . . . . f) Closure, a property of subtraction
- 2160 . . . . . g) Noncommutativity, nonassociativity of subtraction
- 2170 . . . . . 2) Subtraction computation
- 2172 . . . . . c. Multiplication
- 2174 . . . . . 1) Properties
- 2180 . . . . . a) Multiplication, a binary operation
- 2183 . . . . . b) Multiplication developed from number line

- 2185 . . . . . c) Multiplication developed from physical world situations
- 2190 . . . . . d) Closure, a property of multiplication
- 2200 . . . . . e) Commutativity, a property of multiplication
- 2210 . . . . . f) Associativity, a property of multiplication
- 2220 . . . . . g) One, the identity element in multiplication
- 2230 . . . . . 2) Multiplication computation
- 2232 . . . . . d. Division
- 2234 . . . . . 1) Properties
- 2240 . . . . . a) Division, a binary operation
- 2243 . . . . . b) Division developed from number line
- 2245 . . . . . c) Division developed from physical world situations
- 2250 . . . . . d) Division, the inverse of multiplication
- 2255 . . . . . e) Role of one in division
- 2260 . . . . . f) Nonclosure, noncommutativity, nonassociativity of division
- 2270 . . . . . 2) Division computation

0002 . . Topic I: Number Systems

2500 . . . D. Negative rationals (fractional numbers)

2510 . . . . . 1. Basic concepts

2520 . . . . . a. Definition for a set of negative rationals

2530 . . . . . b. Developed from number line

2600 . . . . . 2. Computation

0002 . . Topic I: Number Systems

2700 . . . E. Natural numbers (counting numbers)

2710 . . . . . 1. Basic concepts

2720 . . . . . a. Definition for a set of natural numbers

2730 . . . . . b. Relation to set of whole numbers, nonnegative  
rationals, integers, negative rationals

2992 . . . Topic II: Numeration and Notation

3000 . . . A. Difference between number and numeral

3002 . . . B. Difference numerals for the same number

3010 . . . . . 1. Expanded notation for whole numbers  
(See 0200, 0210, 0227, 0229, 0330, 3070, 3080)

3015 . . . . . 2. Expanded notation for nonnegative rationals (fractions)

3020 . . . . . 3. Equivalent common fraction notation  
(See 1060)

3025 . . . . . 4. Equivalent mixed numeral notation

3030 . . . . . 5. Equivalent decimal fraction notation with terminating  
decimals

3033 . . . . . 6. Equivalent decimal notation with repeating decimals

3035 . . . . . 7. Equivalent percent notation  
(See 8004)

3040 . . . . . 8. Other names for a number  
(See 1040, 1060)

3042 . . . C. Place value in base ten

3050 . . . . . 1. Reading and/or writing words or numerals for the ten  
basic symbols (0-9)  
(See 0020, 0030)

3070 . . . . . 2. Units, tens (10-99)  
(See 0035, 3010)

3080 . . . . . 3. Beyond tens  
(See 3010)

3090 . . . . . 4. Commas to separate into periods

3100 . . . . . 5. Rounding numbers  
(See 8150)

- 3110 . . . . . 6. Decimal fractions
- . 3120 . . . . . 7. Exponential notation  
(See 0520, 0670, 0700)
- . 3130 . . . . . 8. Scientific notation
  
- 3140 . . . D. Historical development of number concepts
  
- 3150 . . . E. Historical systems of notation (nonplace or place value)  
(See 3160)
  
- 3160 . . . F. Working with nondecimal place value systems (other number bases)  
(See 3150)



3992 . . Topic III: Sets: physical and abstract

3994 . . . A. Description of sets

4000 . . . B. Set members or elements

4004 . . . C. Kinds of sets

4010 . . . . . 1. Equivalent (one-to-one correspondence)  
(See 0050, 0060, 0100)

4030 . . . . . 2. Non-equivalent (general)  
(See 0100)

4035 . . . . . 3. Non-equivalent (one-to-many correspondence)

4037 . . . . . 4. Equal (identical)

4040 . . . . . 5. Unequal

4060 . . . . . 6. Subsets  
(See 0250, 0540)

4070 . . . . . 7. The empty set  
(See 0020)

4090 . . . . . 8. Disjoint

4093 . . . . . 9. Union of sets  
(See 0120)

4095 . . . . . 10. Intersection of sets

4097 . . . . . 11. Venn diagrams

4100 . . . . . 12. Finite

4110 . . . . . 13. Infinite

4120 . . . . . 14. Universal and complement

4125 . . . . . 15. Solution sets  
(See 8170)

4160 . . . . . 16. Cartesian product sets (cross products)  
(See 0390)

4992 . . . Topic IV: Geometry

5000 . . . A. Intuitive concepts of geometric figures and ideas

5010 . . . . . 1. Geometric figures in environment

5020 . . . . . 2. Geometric designs or patterns (sequences)

5030 . . . . . 3. Spatial relations without measurement (size, position)

5040 . . . . . 4. Two dimensional figures (plane)

5050 . . . . . 5. Three dimensional figures (solid)

5060 . . . . . 6. Curves: simple, closed, open

5070 . . . . . 7. Regions: interior, exterior

5080 . . . . . 8. Representations of point, line, plane, space

5082 . . . B. Concepts of geometric figures and ideas explored in depth

5090 . . . . . 1. Point

5100 . . . . . 2. Line

5101 . . . . . 3. Line segment

5103 . . . . . 4. Ray

5105 . . . . . 5. Related lines: intersecting, parallel, skew, oblique, ...

- 5115 . . . . . 6. Angles
- 5125 . . . . . 7. Kinds of angles
- 5140 . . . . . 8. Regions: interior, exterior
- 5143 . . . . . 9. Planes: two dimensional figures
- 5145 . . . . . 10. Polygons (plane figures)
  - 5150 . . . . . a. Triangles
  - 5160 . . . . . b. Quadrilaterals
  - 5170 . . . . . c. Other polygons
- 5172 . . . . . 11. Curves
  - 5174 . . . . . a. Simple, closed, open
  - 5176 . . . . . b. Convex, concave
- 5180 . . . . . 12. Circles
- 5183 . . . . . 13. Space: three dimensional figures
- 5185 . . . . . 14. Space figures: three dimensional figures
  - 5186 . . . . . a. Pyramid
  - 5188 . . . . . b. Prism
  - 5191 . . . . . c. Cylinder

- 5192 . . . . . d. Cone
- 5194 . . . . . e. Sphere
- 5195 . . . . . 15. Conic sections other than circles; the ellipse, parabola,  
and hyperbola
- 5202 . . . C. Construction
- 5210 . . . . . 1. Line constructions (one dimensional figures)
- 5220 . . . . . 2. Two dimensional figures (plane figures)
- 5230 . . . . . 3. Three dimensional figures (figures in space)
- 5232 . . . D. Metric geometry
- 5234 . . . . . 1. Comparing sizes, shapes, distances (including latitude,  
longitude)
- 5240 . . . . . a. Congruency
- 5245 . . . . . b. Symmetry
- 5250 . . . . . c. Similarity
- 5255 . . . . . d. Similarity: scale drawing  
(See 8000)
- 5258 . . . . . 2. Measurement of geometric quantities
- 5260 . . . . . a. Line segments with ruler and/or compass or other  
measuring device  
(See 6030, 6032, 6060, 6065)
- 5270 . . . . . b. Angles with protractor and/or compass or other  
measuring device

- 5280 . . . . . c. Perimeter or circumference of simple closed curves  
(See 6030, 6032)
- 5290 . . . . . d. Area of plane figures  
(See 6034, 6035)
- 5300 . . . . . e. Volume of solids  
(See 6036, 6037)
- 5400 . . . E. Operations with geometric figures
- 5410 . . . . . 1. Union
- 5420 . . . . . 2. Intersection
- 5500 . . . F. Other topics
- 5510 . . . . . 1. Separation of sets of points
- 5520 . . . . . 2. Locus of points



- 5992 . . . Topic V: Measurement of Nongeometric Quantities
- 6000 . . . A. Meaning of measurement (direct, indirect)
- 6001 . . . . . 1. Approximate nature of measurement
- 6003 . . . . . 2. Precision
- 6005 . . . . . 3. The greatest possible error
- 6007 . . . B. Units of Measure
- 6008 . . . . . 1. Historical development of units of measure
- 6009 . . . . . . . . . . a. Non-standard units such as foot, cubit, furlong  
leading to the standardized English system
- 6010 . . . . . . . . . . b. Metric units
- 6025 . . . . . 2. Linear units of measure
- 6028 . . . . . . . . . . a. Non-standard
- 6030 . . . . . . . . . . b. English units for yards or less  
(See 5260, 5280)
- 6032 . . . . . . . . . . c. Metric units for meters or less  
(See 5260, 5280)
- 6034 . . . . . 3. Square units of measure in the English system of measures  
(See 5290)
- 6035 . . . . . 4. Square units of measure in the metric system of measures  
(See 5290)
- 6036 . . . . . 5. Cubic units of measure in the English system  
(See 5300)
- 6037 . . . . . 6. Cubic units of measure in the metric system  
(See 5300)

- 6038 . . . C. Need for modern units of measure
- 6040 . . . D. Money
- 6050 . . . E. Time
- 6060 . . . F<sub>1</sub>. Distance in English units for lengths longer than a yard  
(See 5260)
- 6065 . . . F<sub>2</sub>. Distance in metric units for lengths longer than a meter  
(See 5260)
- 6070 . . . G<sub>1</sub>. Liquids in English units
- 6075 . . . G<sub>2</sub>. Liquids in metric units
- 6080 . . . H. Temperature: Fahrenheit and centigrade
- 6090 . . . I<sub>1</sub>. Weight in English units
- 6095 . . . I<sub>2</sub>. Weight in metric units
- 6100 . . . J. Dry measures
- 6110 . . . K. Quantity (dozen, gross, etc.)
- 6120 . . . L. Operations related to denominate numbers
- 6130 . . . M. Conversion to other standard units measuring several kinds  
of nongeometric quantities



6992 . . . Topic VI: Number Patterns and Relationships

6994 . . . . A. Elementary number theory

7000 . . . . . 1. Odd and even numbers  
(See 0080)

7010 . . . . . 2. Factors and primes

7020 . . . . . 3. General composite numbers

7030 . . . . . 4. Special composite numbers

7050 . . . . . 5. Greatest common factor

7055 . . . . . 6. Multiples  
(See 0080)

7060 . . . . . 7. Least common multiple  
(See 1200, 1300)

7070 . . . . . 8. Unique factorization (prime factorization)

7080 . . . . . 9. Rules for divisibility

7082 . . . . B. General number sequences and patterns

7088 . . . . C. Special number sequences

7090 . . . . . 1. Arithmetic progressions  
(See 0075, 0080)

7100 . . . . . 2. Geometric progressions

7110 . . . . . 3. Triangular numbers

7120 . . . . . 4. Square numbers

7130 . . . . . 5. Factorial numbers

7140 . . . . . 6. Grid

7150 . . . . . 7. Fibonacci numbers

7160 . . . . D. Special patterns (including short cuts)

7992 . . Topic VII: Other Topics

8000 . . . . A. Ratio and proportion  
(See 5255)

8002 . . . . . 1. Rate pairs

8003 . . . . B. Percent

8004 . . . . . 1. Meaning and vocabulary  
(See 3035)

8005 . . . . . 2. Developed through use of ratios

8006 . . . . . 3. Developed through use of equations

8007 . . . . . 4. Developed through use of the formula  $P = b \times r$   
(percentage equals base times rate)

8008 . . . . . 5. Computation related to percent

8012 . . . . C. Graphs

8020 . . . . . 1. Solution sets of equalities and inequalities on the  
number line

8030 . . . . . 2. Ordered pairs on a coordinate plane

8040 . . . . . 3. Solution sets of equalities and inequalities on a  
coordinate plane

8044 . . . . D. Descriptive statistics

8050 . . . . . 1. Frequency tables, charts, graphs (bar, line, circle,  
dot, picture, etc.)

8060 . . . . . 2. Measures of central tendency: average, mean, mode, median

- 8070 . . . . . 3. Measures of variability: range, quartiles, percentiles,  
average deviation, standard deviation
  
- 8080 . . . . . E. Probability
  
- 8084 . . . . . F. Finite mathematical systems
  
- 8100 . . . . . 1. Modular arithmetic (clock arithmetic)
  
- 8110 . . . . . 2. Without numbers
  
- 8120 . . . . . 3. Other
  
- 8130 . . . . . G. Logic
  
- 8140 . . . . . H. Functions and relations
  
- 8150 . . . . . I. Estimation  
(See 3100)
  
- 8160 . . . . . J. Relations (properties of)
  
- 8170 . . . . . K. Mathematical sentences (equations)  
(See 4125)

8992 . . . Topic VIII: Summaries

• 9000 . . . . A. General review

• 9010 . . . . B. Test

9020 . . . . C. Review properties of and basic operations with whole numbers

9030 . . . . D. Review properties of and basic operations with fractional numbers

9040 . . . . E. Review properties of and basic operations with integers

9050 . . . . F. Review of numeration

9060 . . . . G. Review of sets

9070 . . . . H. Review of geometry

9080 . . . . I. Review of measurement

9090 . . . . J. Review of number patterns and relationships

9100 . . . . K. Review of other topics

9101 . . . . . 1. Ratio and proportion

9102 . . . . . 2. Percent

9103 . . . . . 3. Graphs

9104 . . . . . 4. Statistics

9105 . . . . . 5. Probability

9106 . . . . . 6. Finite mathematical systems

- 9107 . . . . . 7. Logic
- 9108 . . . . . 8. Functions and relations
- 9109 . . . . . 9. Estimation
- 9110 . . . . . 10. Relations, properties
- 9111 . . . . . 11. Mathematical sentences (equations)